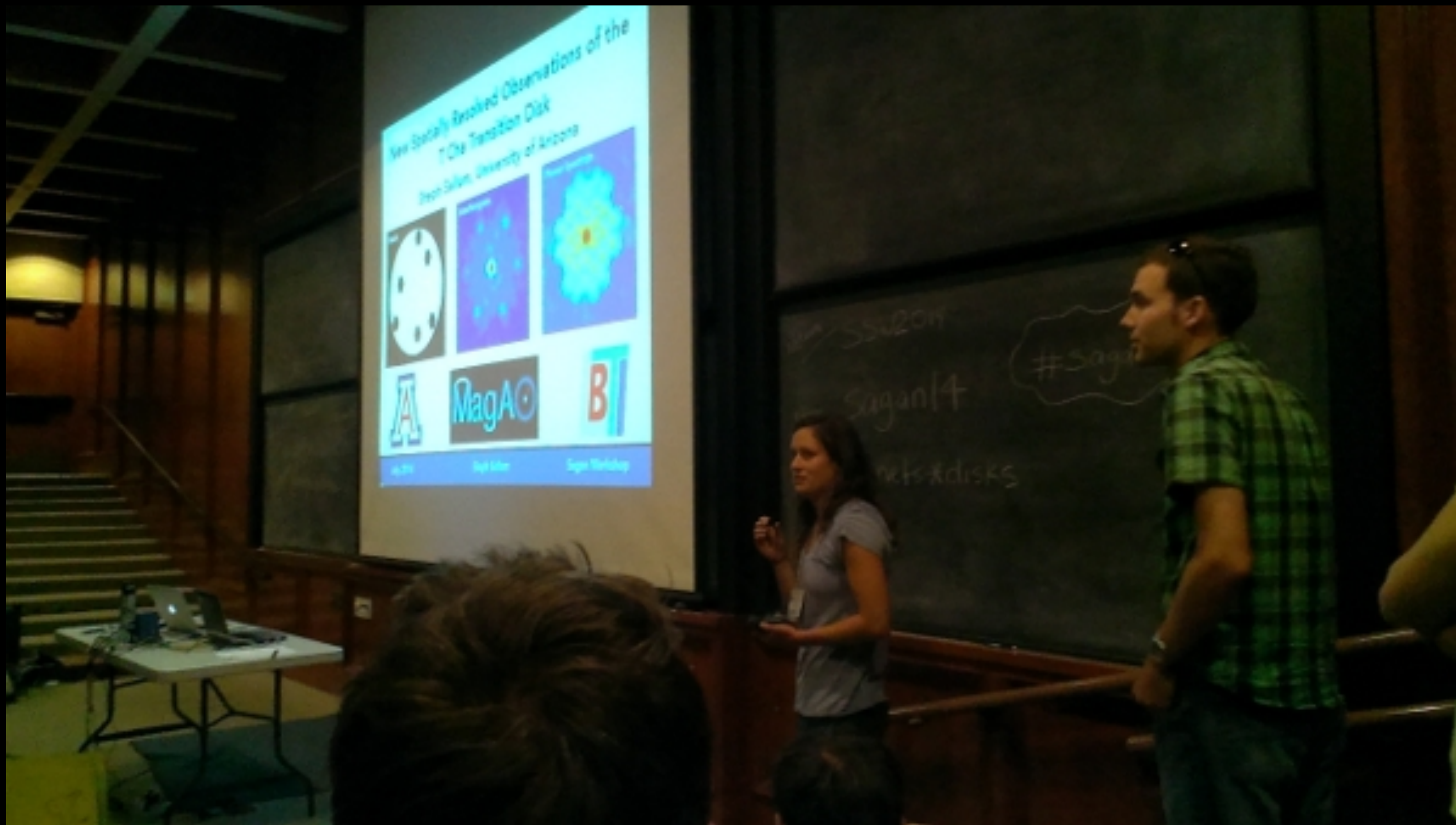


Aperture Masking Interferometry in Astronomy

Steph Sallum
Sagan Summer Workshop
July 26, 2024

10 years ago at the Sagan Workshop...



“Her slides were very patriotic.”

<https://xwcl.science/magao-c/sagan-2014-imaging-planets-and-disks/>

Some (Very) Quick Motivation

Direct imaging observations suffer from uncorrected phase errors.

Observing (and post processing) strategies that can remove these phase errors would allow us to access small angular separations, benefiting a wide variety of science cases!

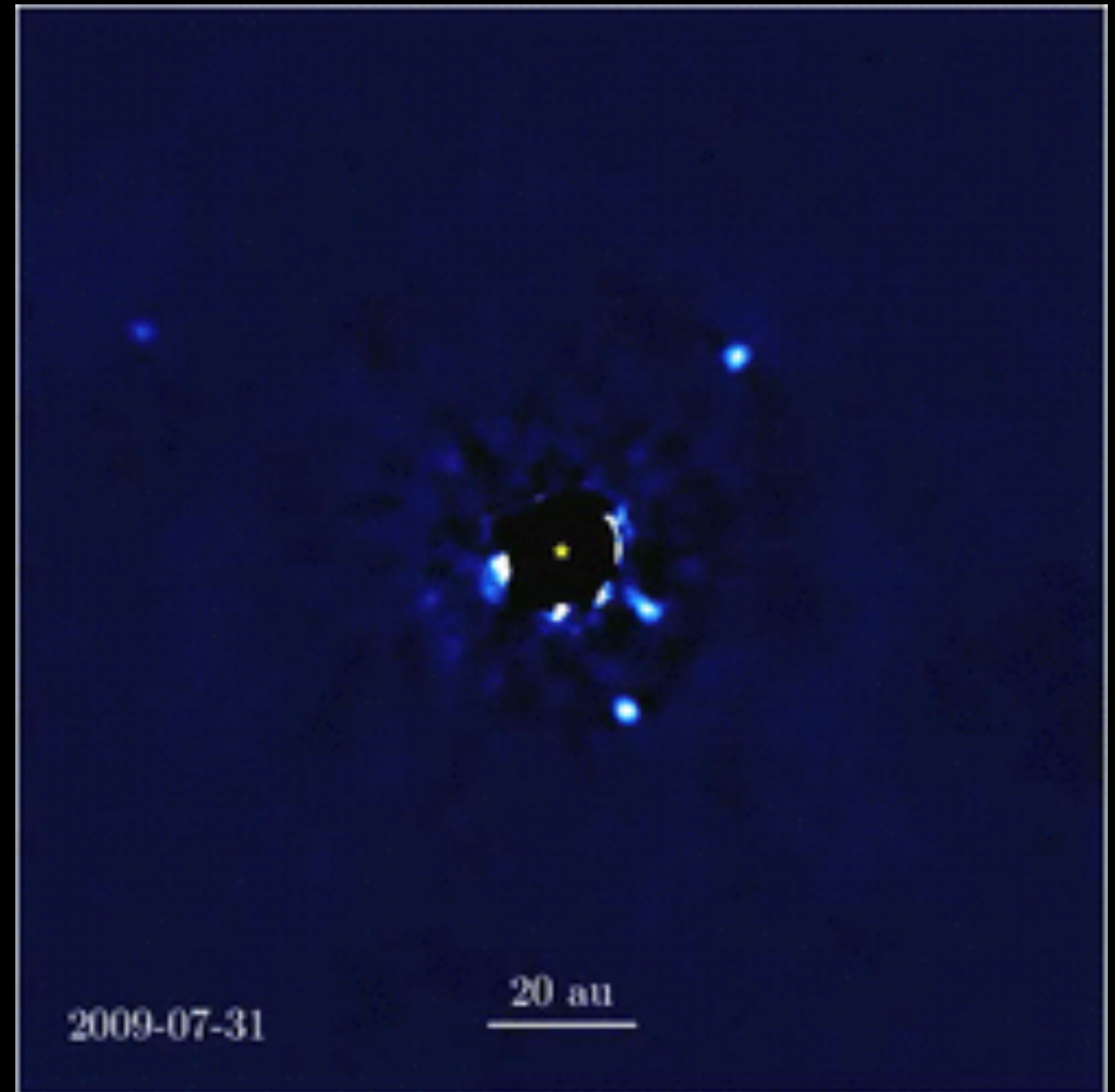


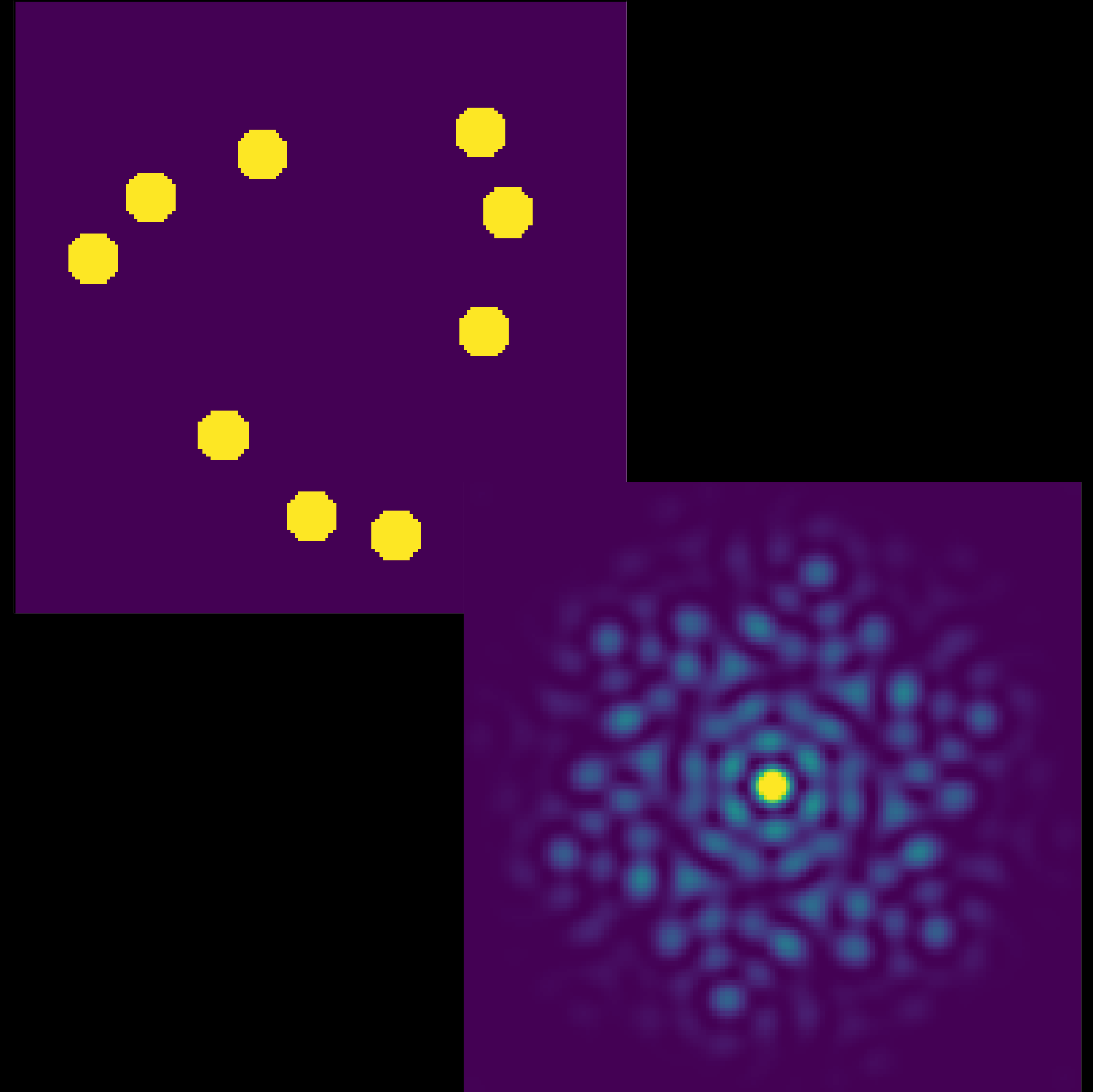
Image credit: Jason Wang (Northwestern)/William Thompson (UVic)/
Christian Marois (NRC Herzberg)/Quinn Konopacky (UCSD)

Aperture Masking Interferometry

Transforming a filled aperture into an interferometric array via a pupil-plane mask.



Image credit: Peter Tuthill

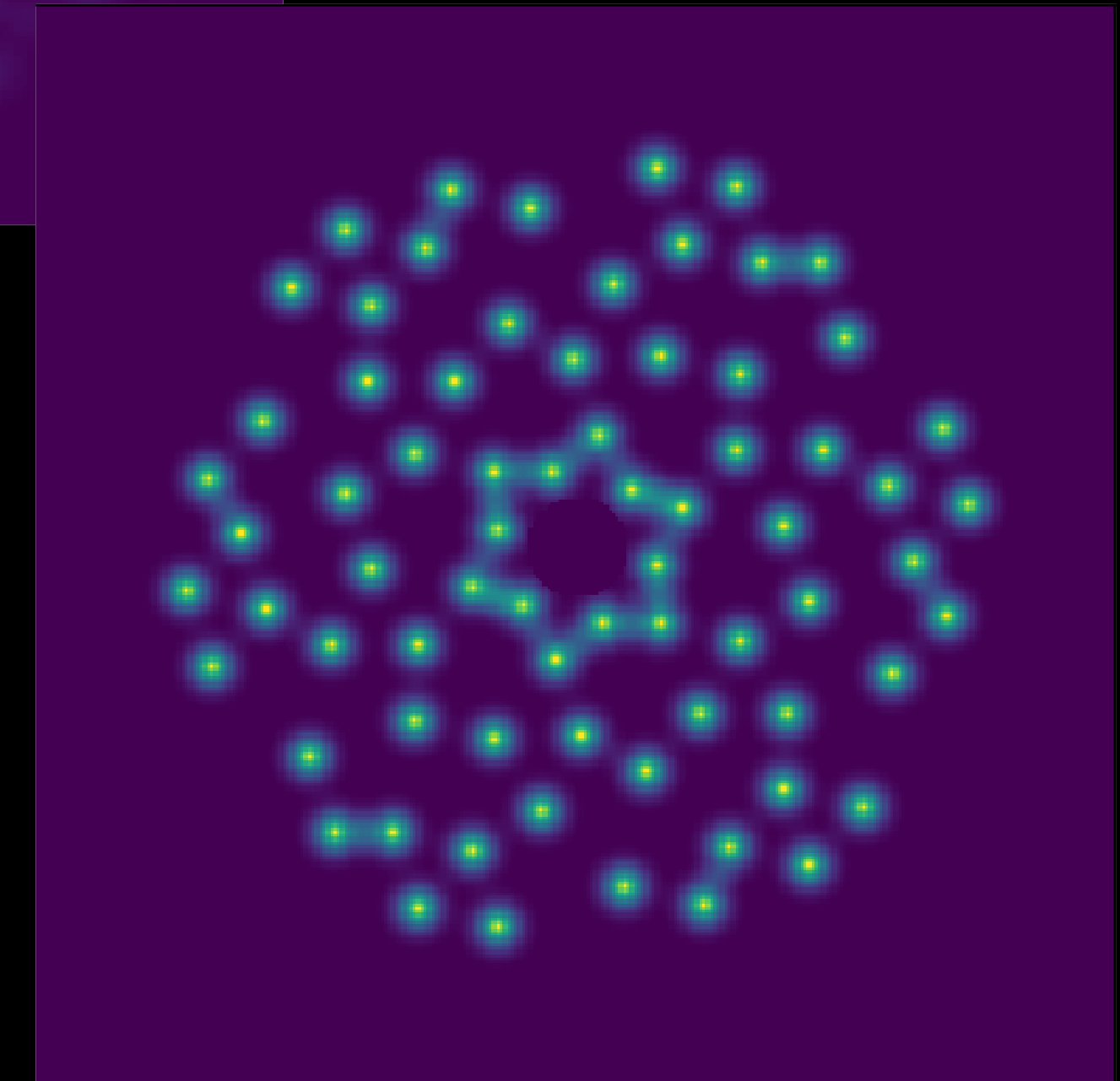
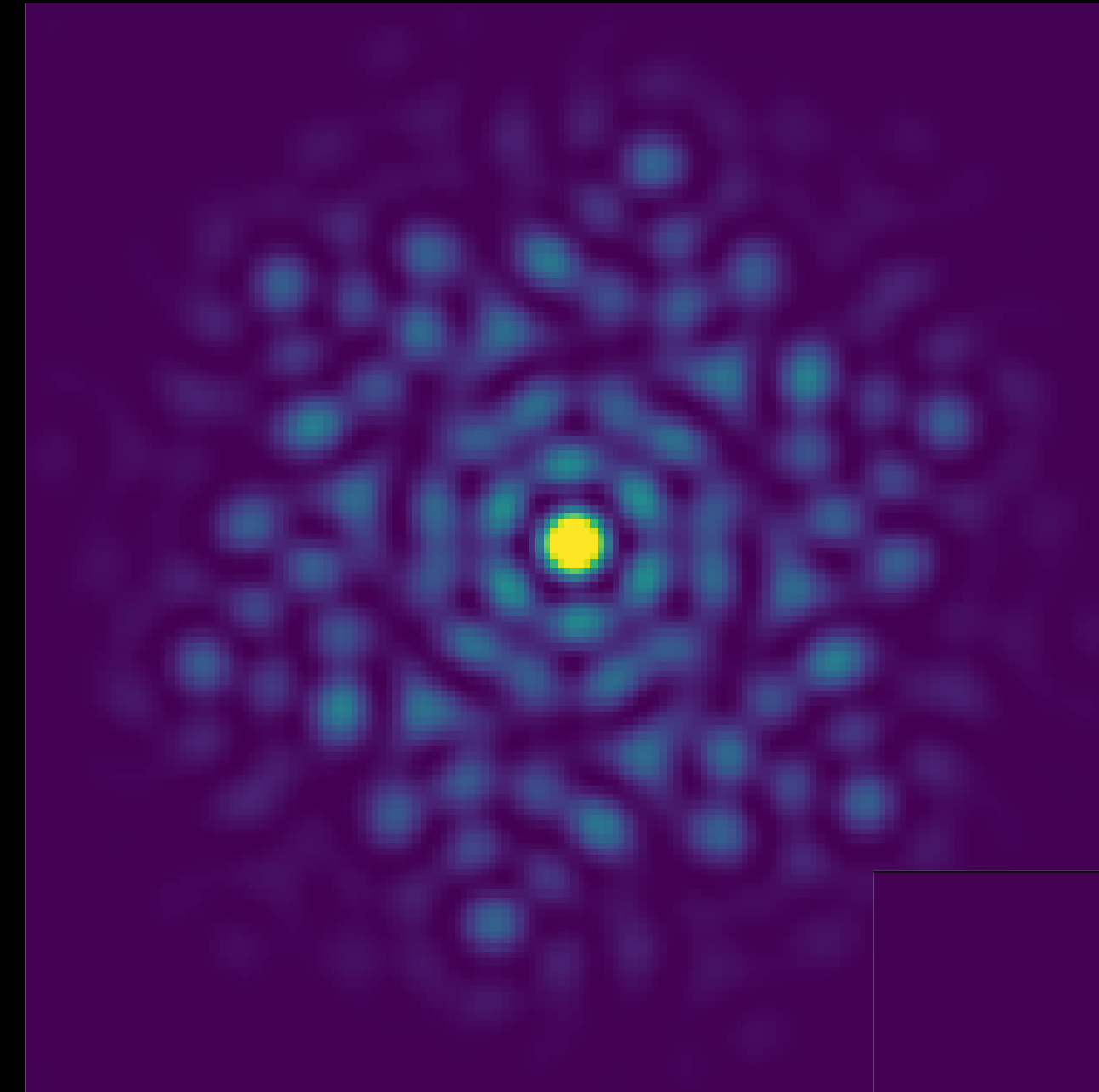


Aperture Masking Interferometry

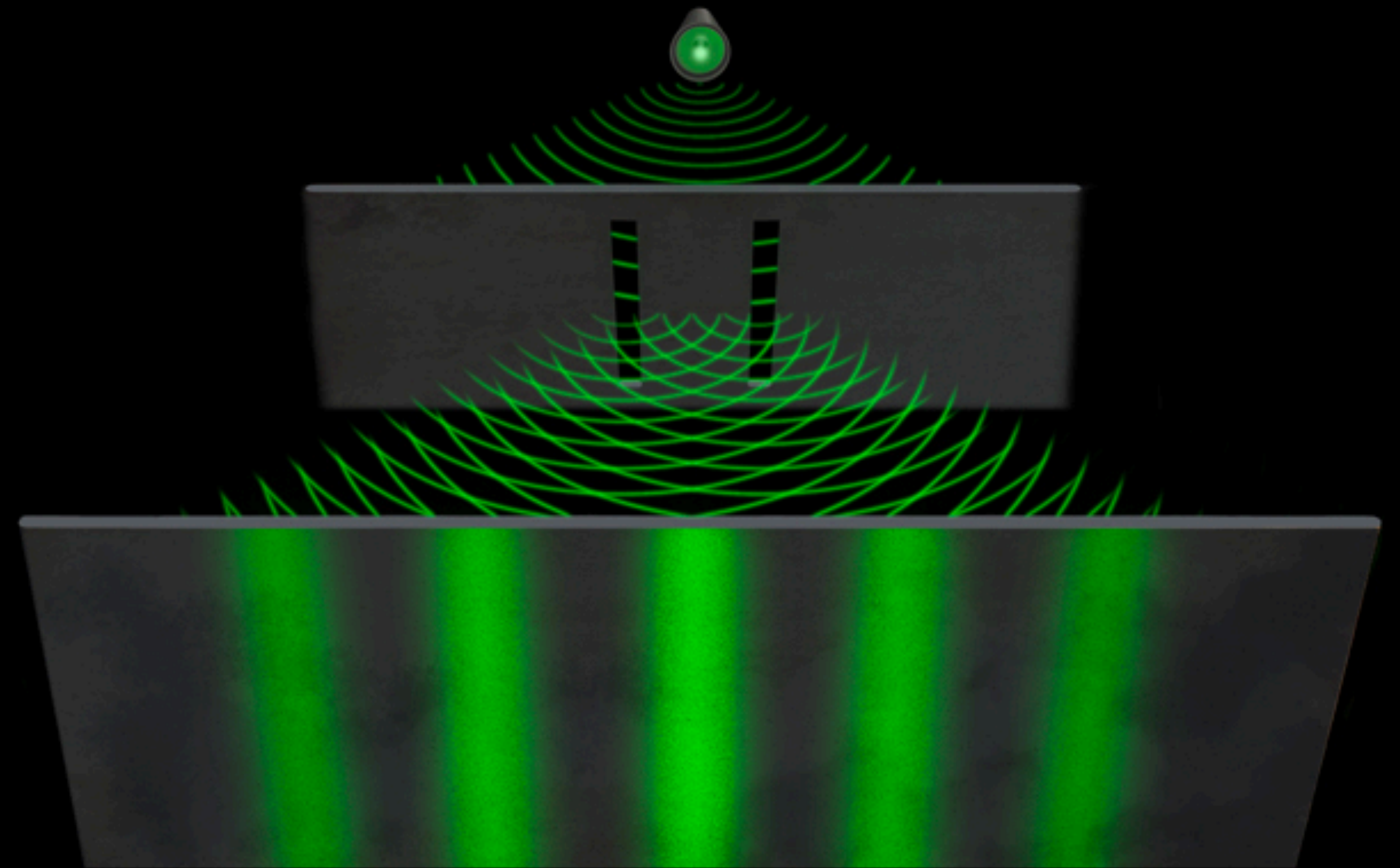
Transforming a filled aperture into an interferometric array via a pupil-plane mask.



Image credit: Peter Tuthill



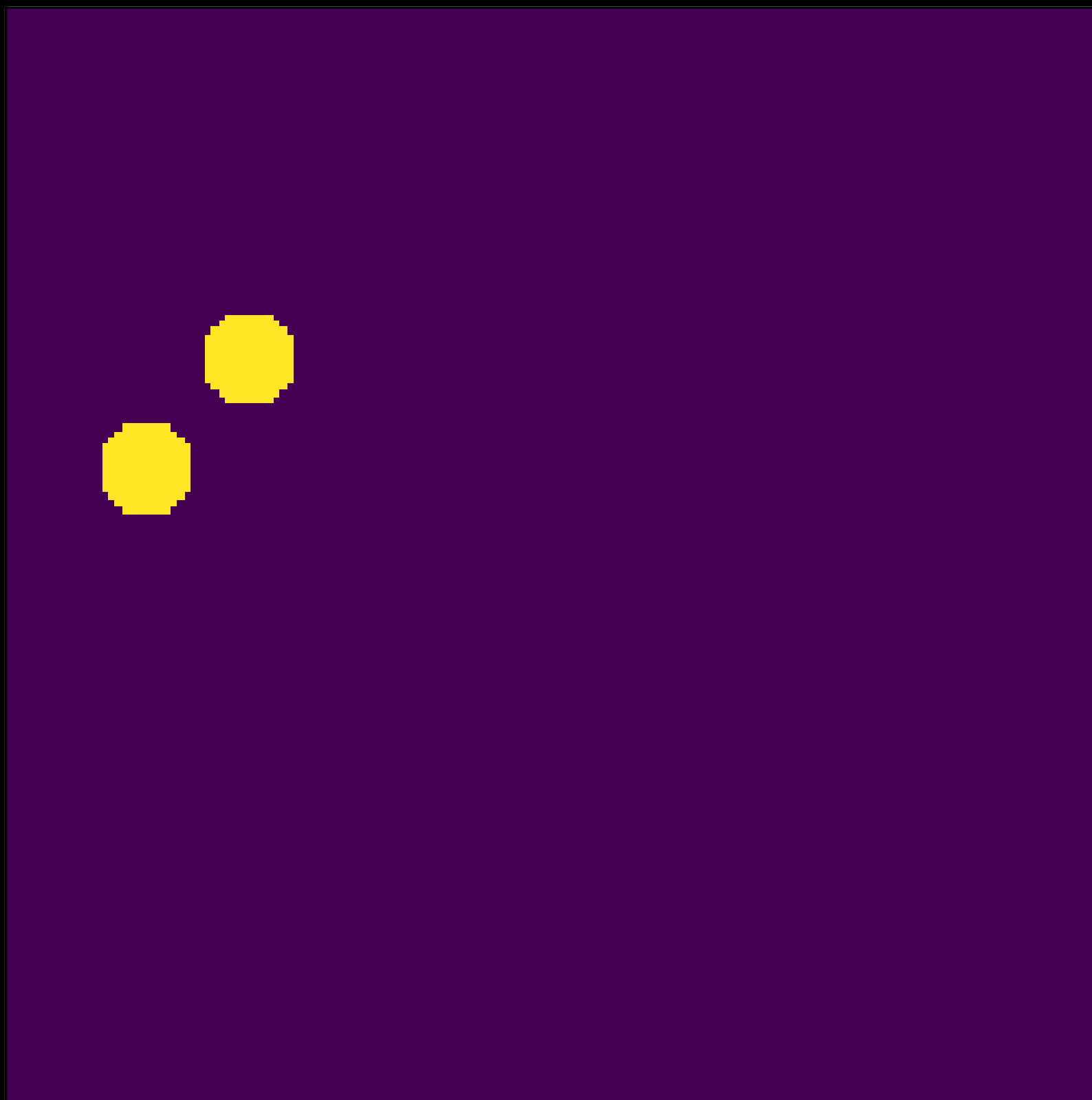
Young's Double Slit Experiment (1801)



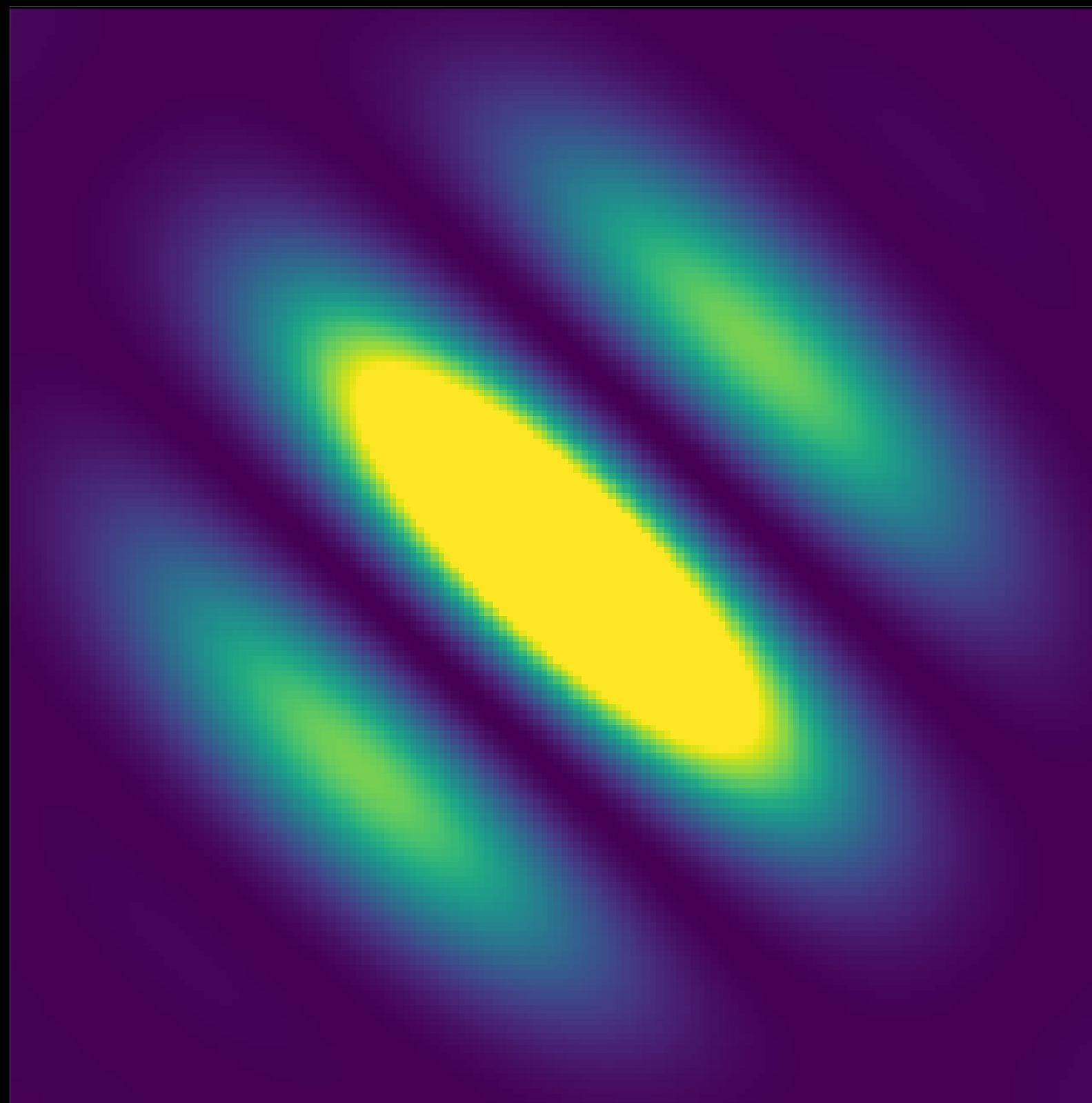
**Fringe spacing depends on slit separation,
modulation depends on slit size!**

Non-Redundant Masking

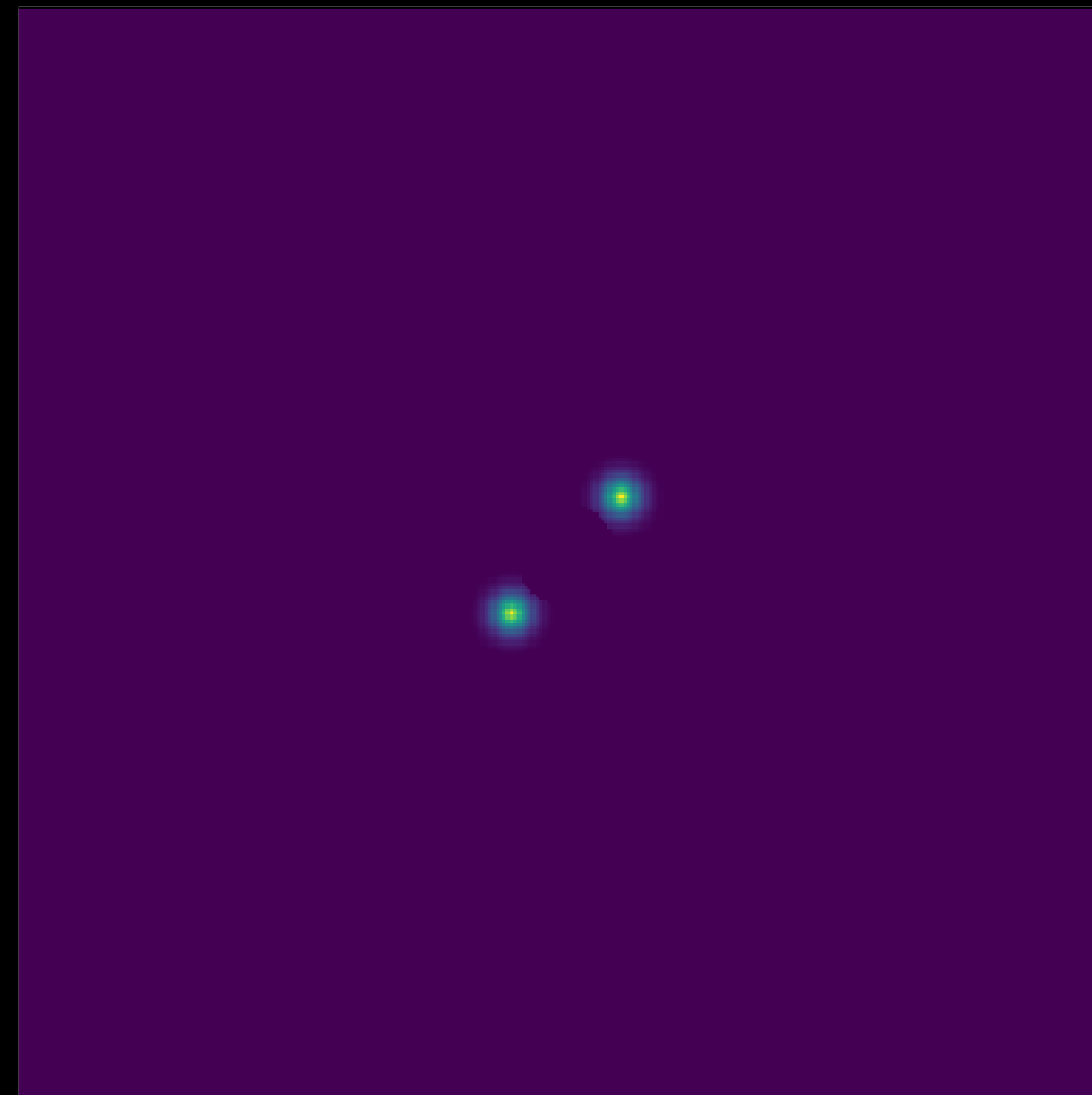
Pupil



Image

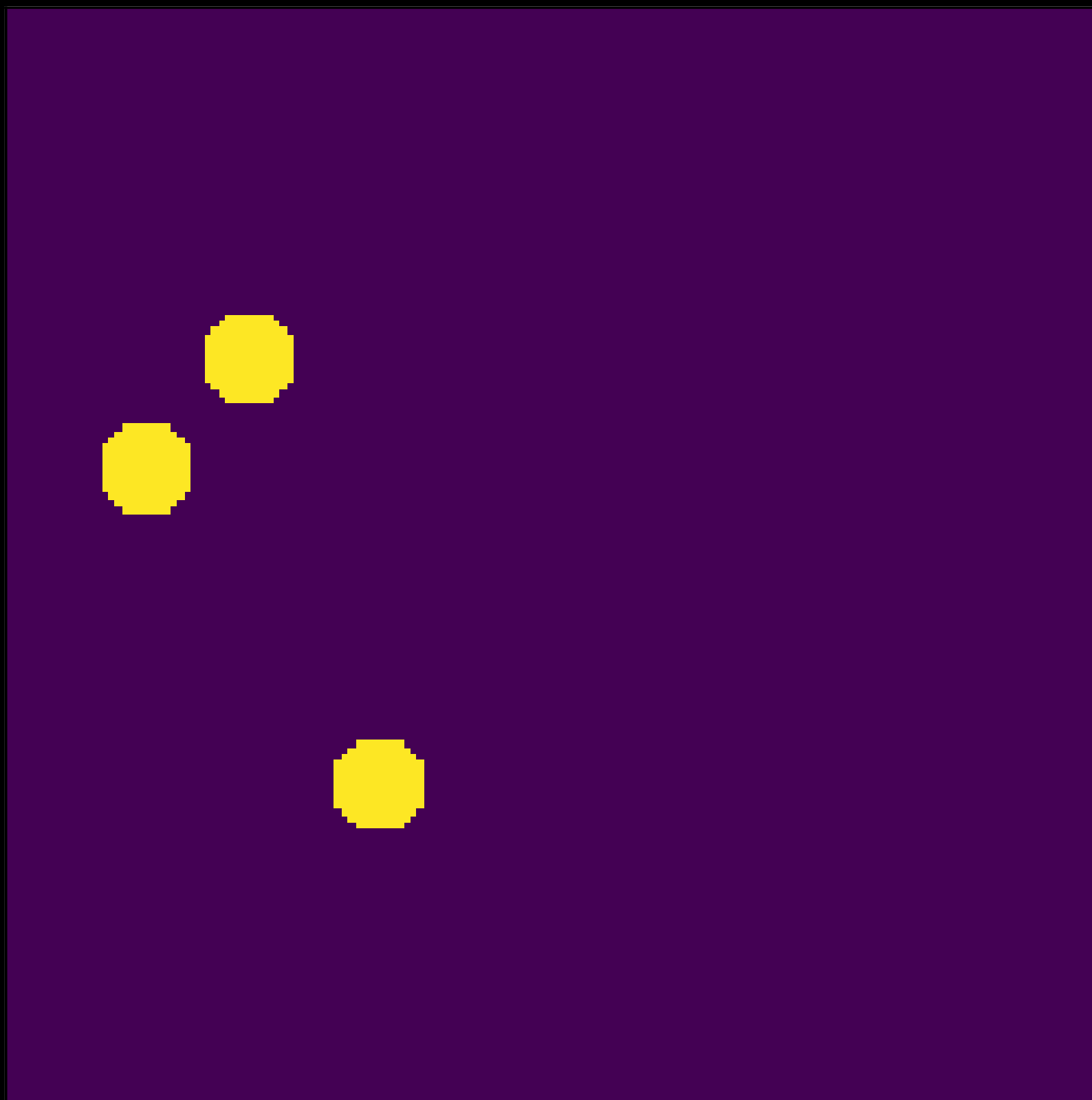


Complex Visibilities

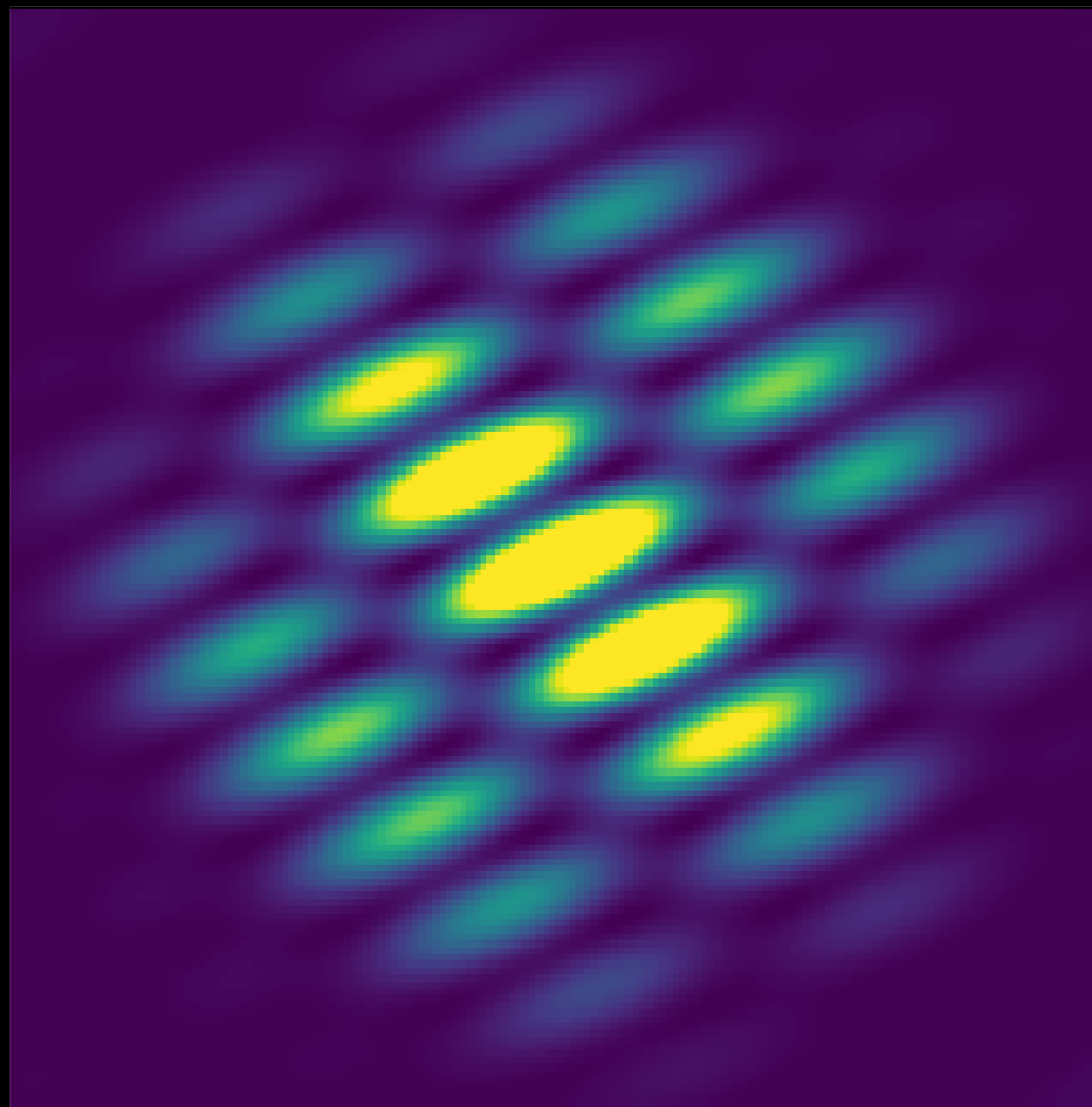


Non-Redundant Masking

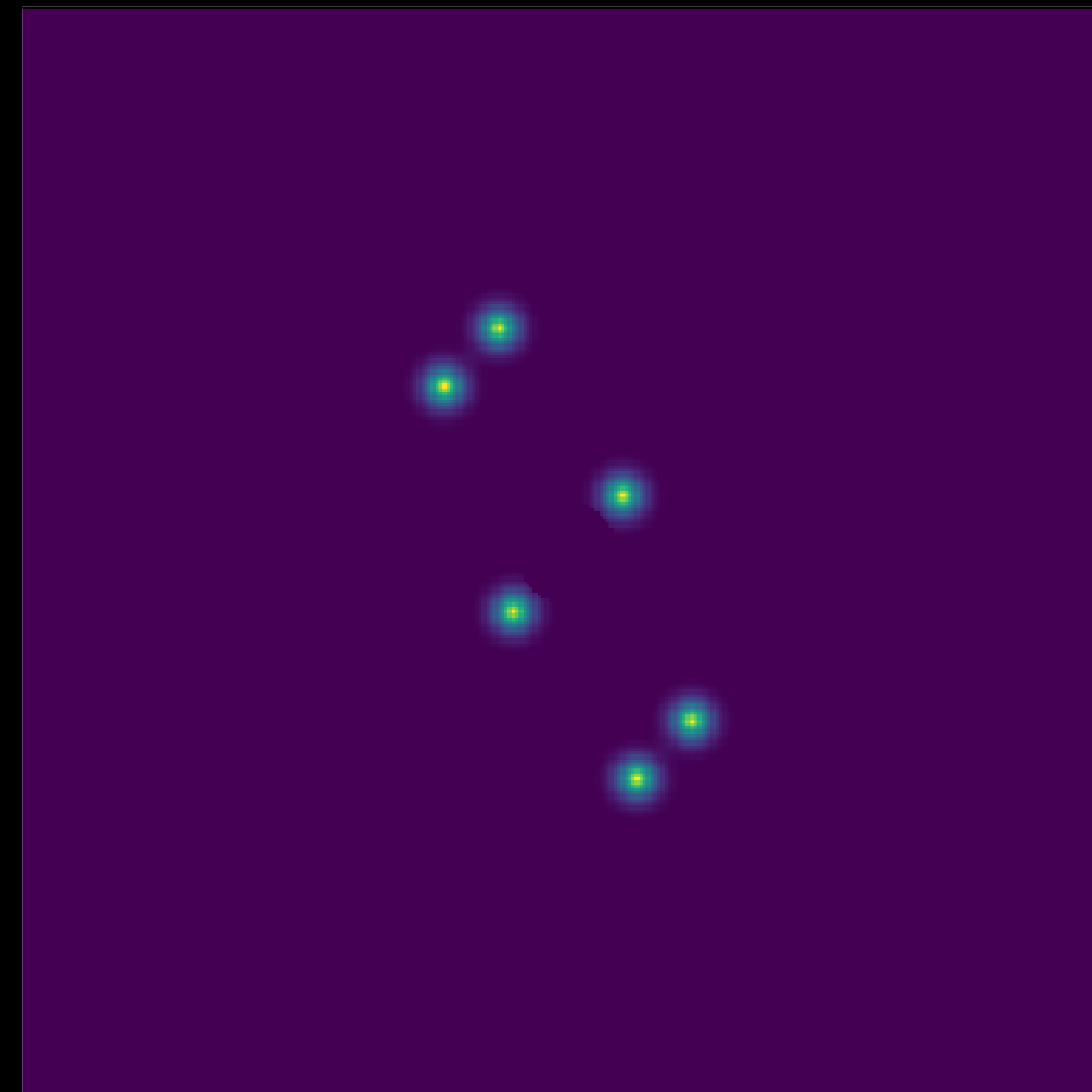
Pupil



Image

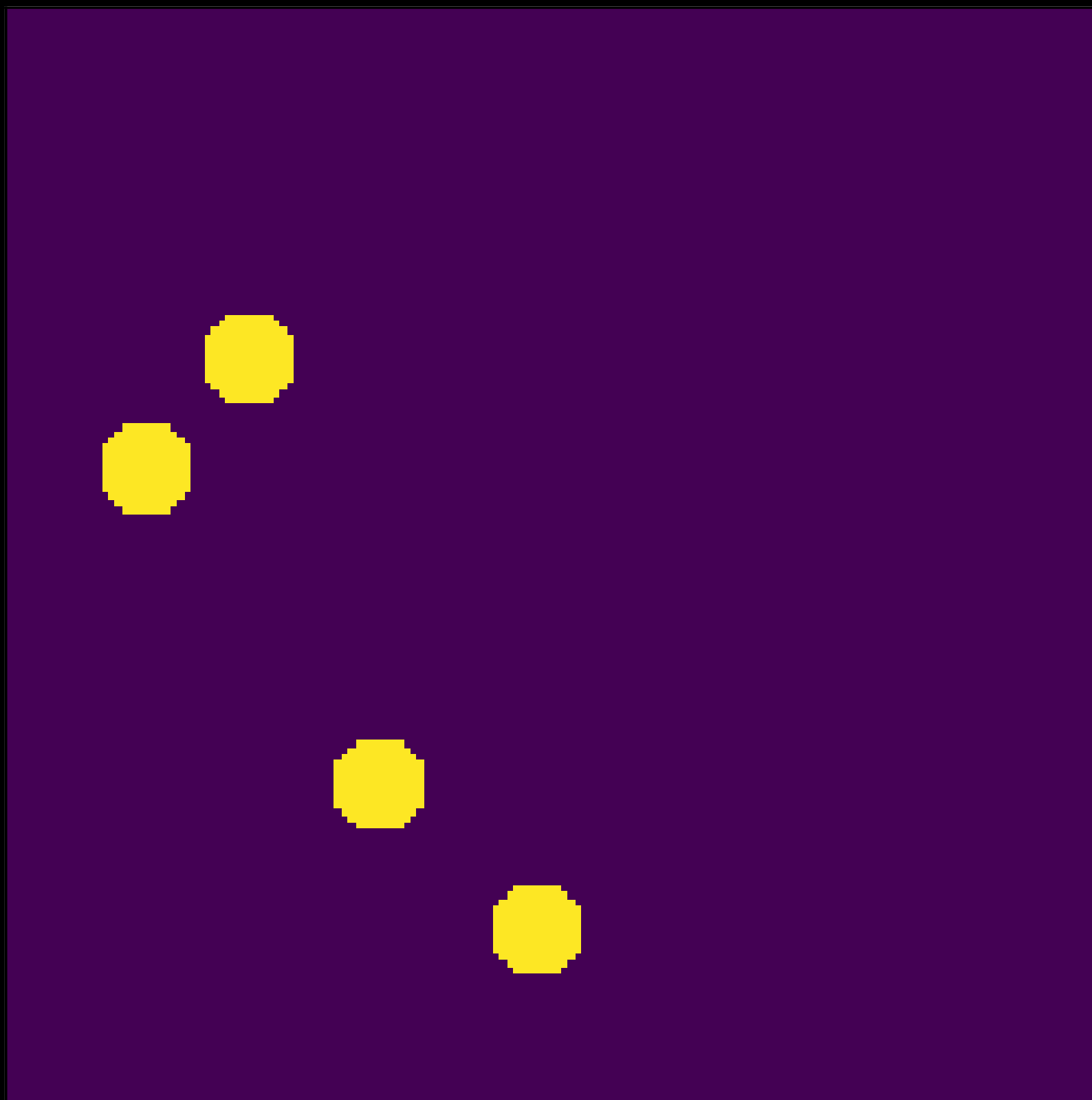


Complex Visibilities

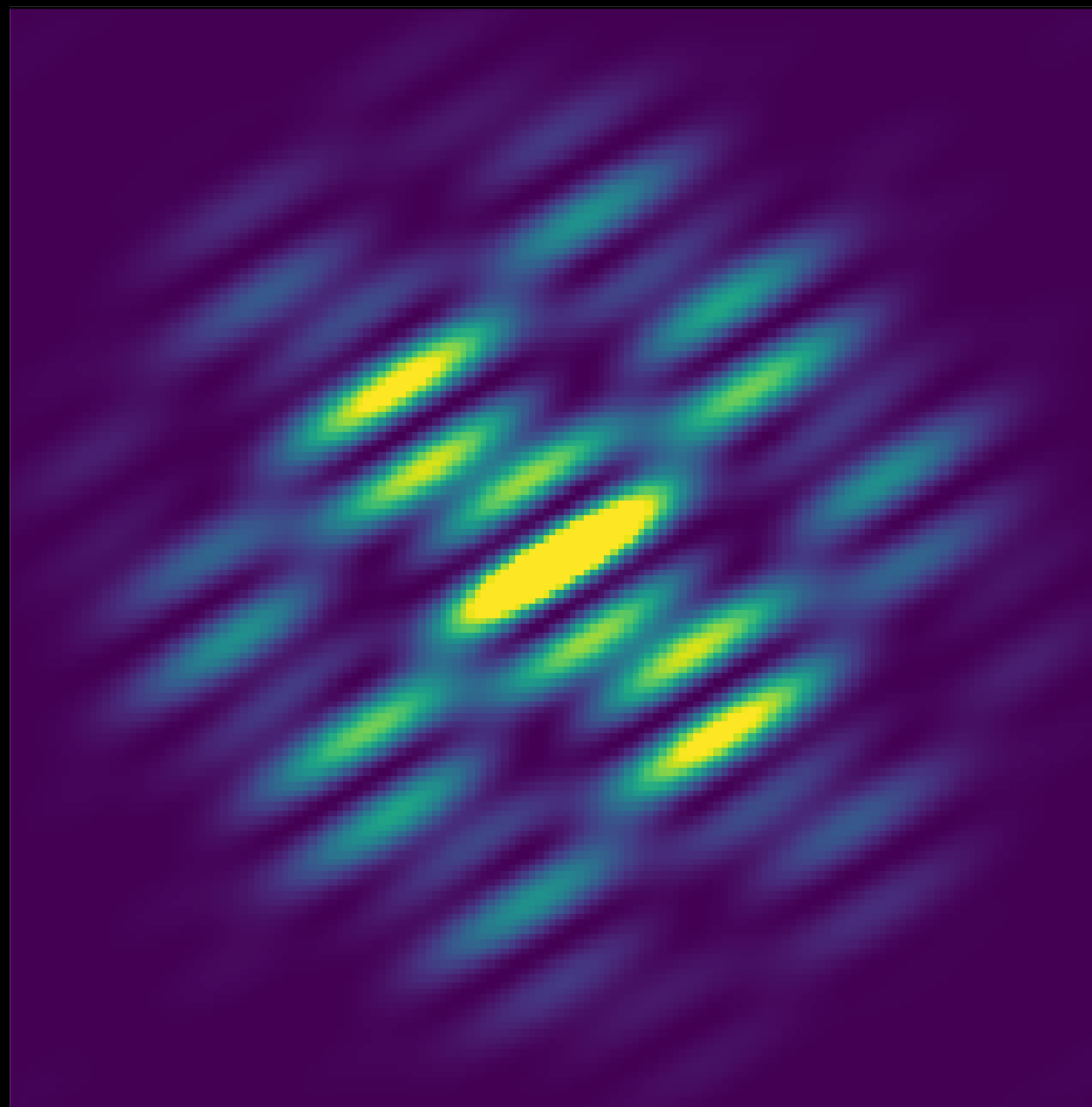


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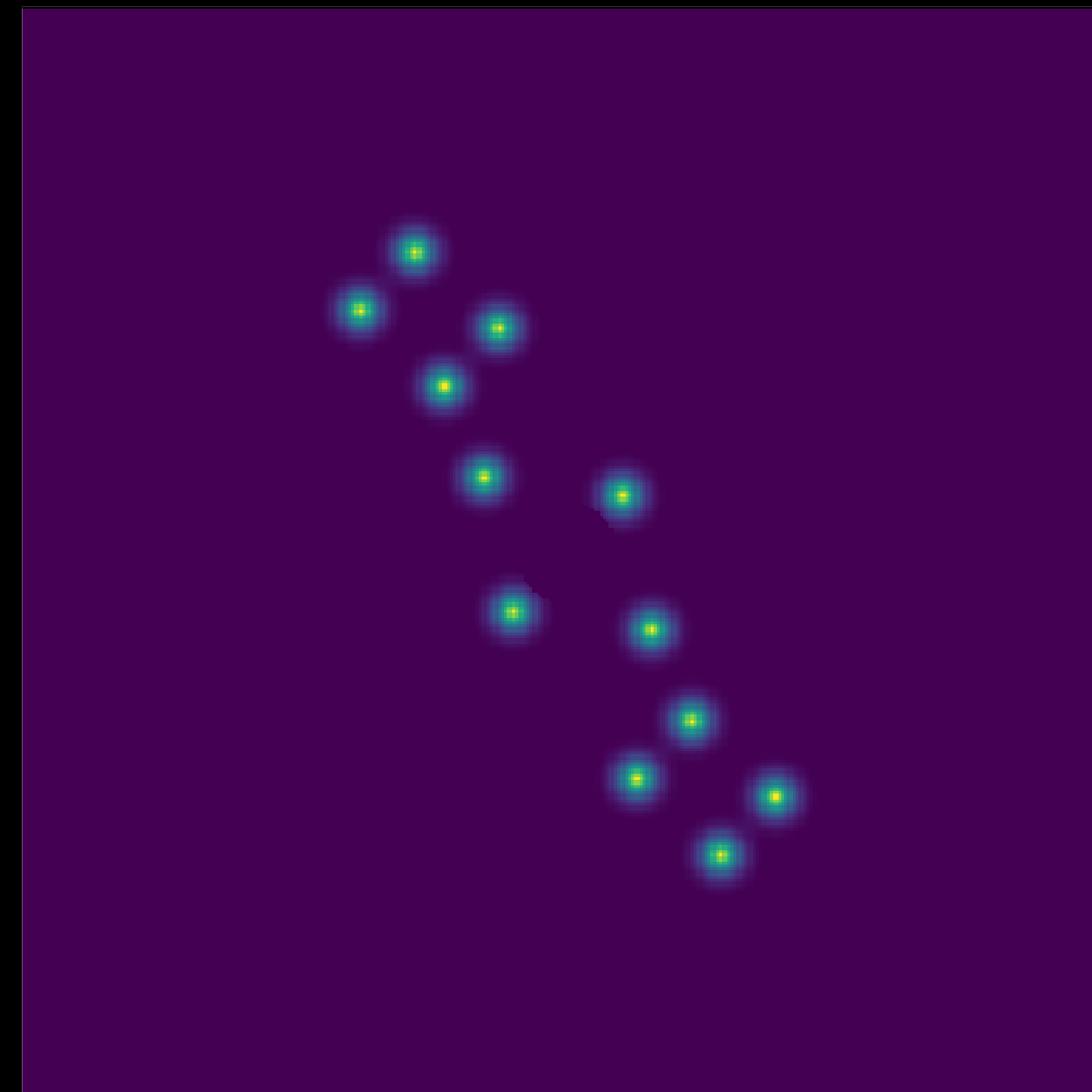
Pupil



Image

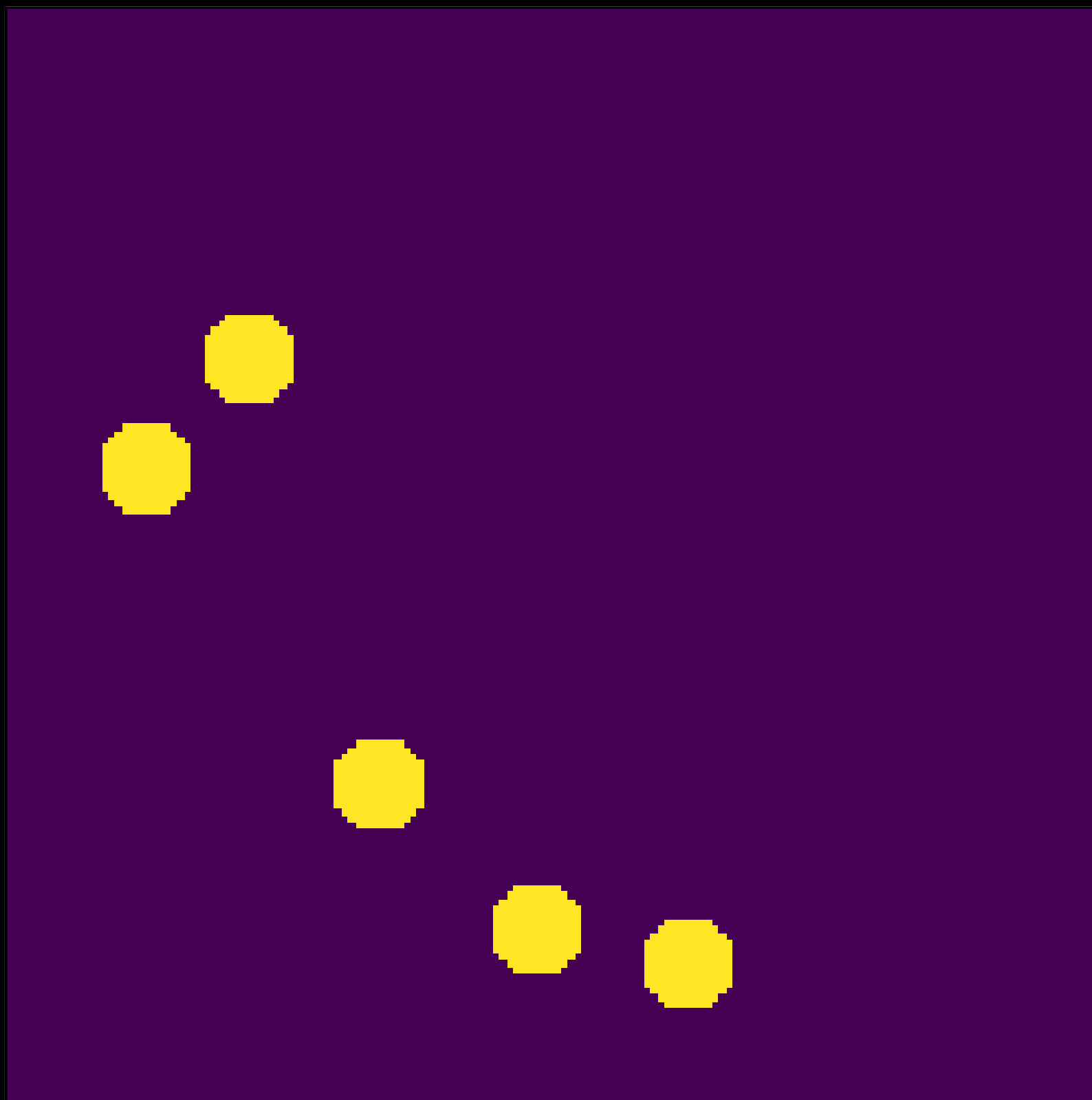


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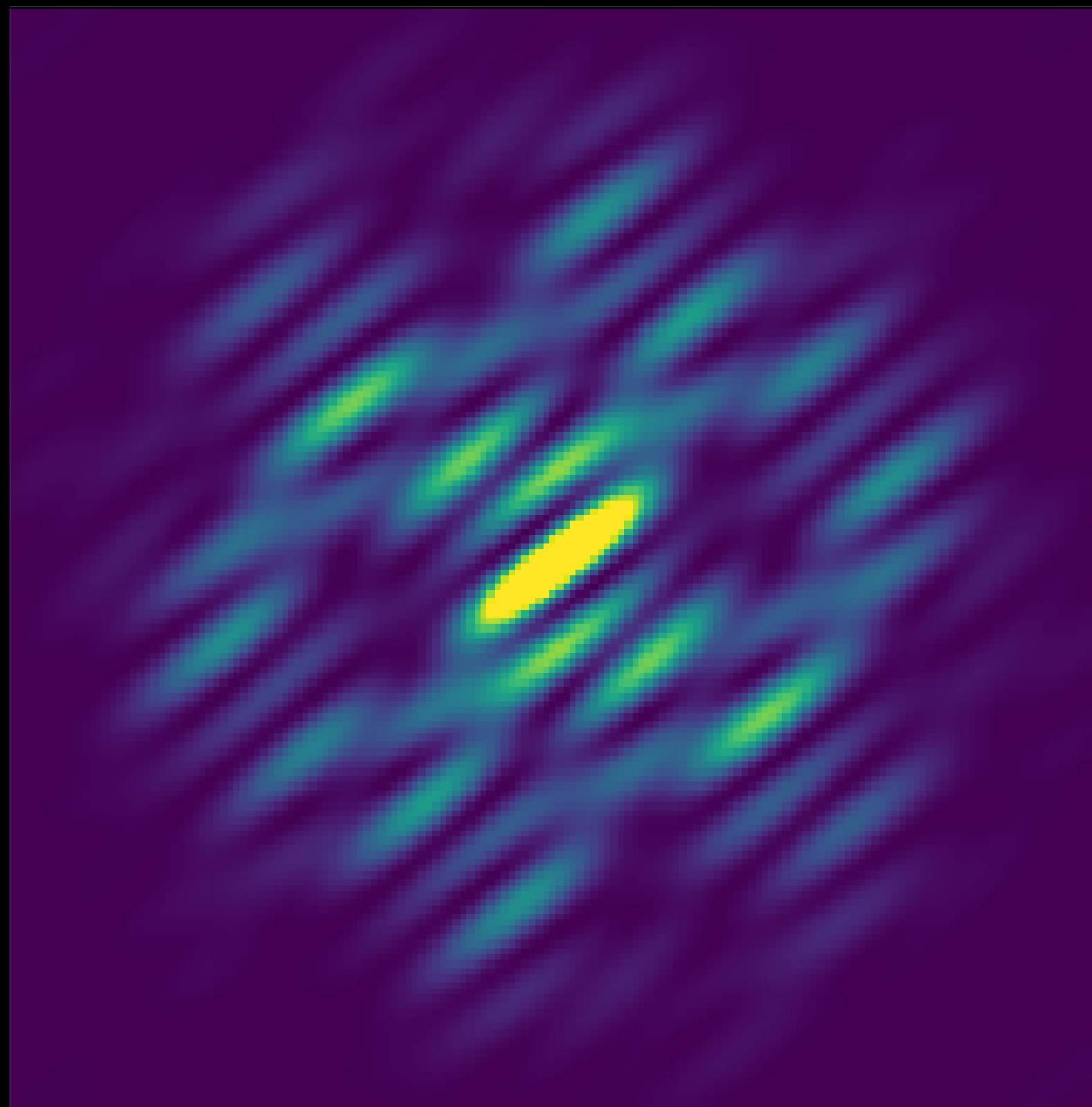


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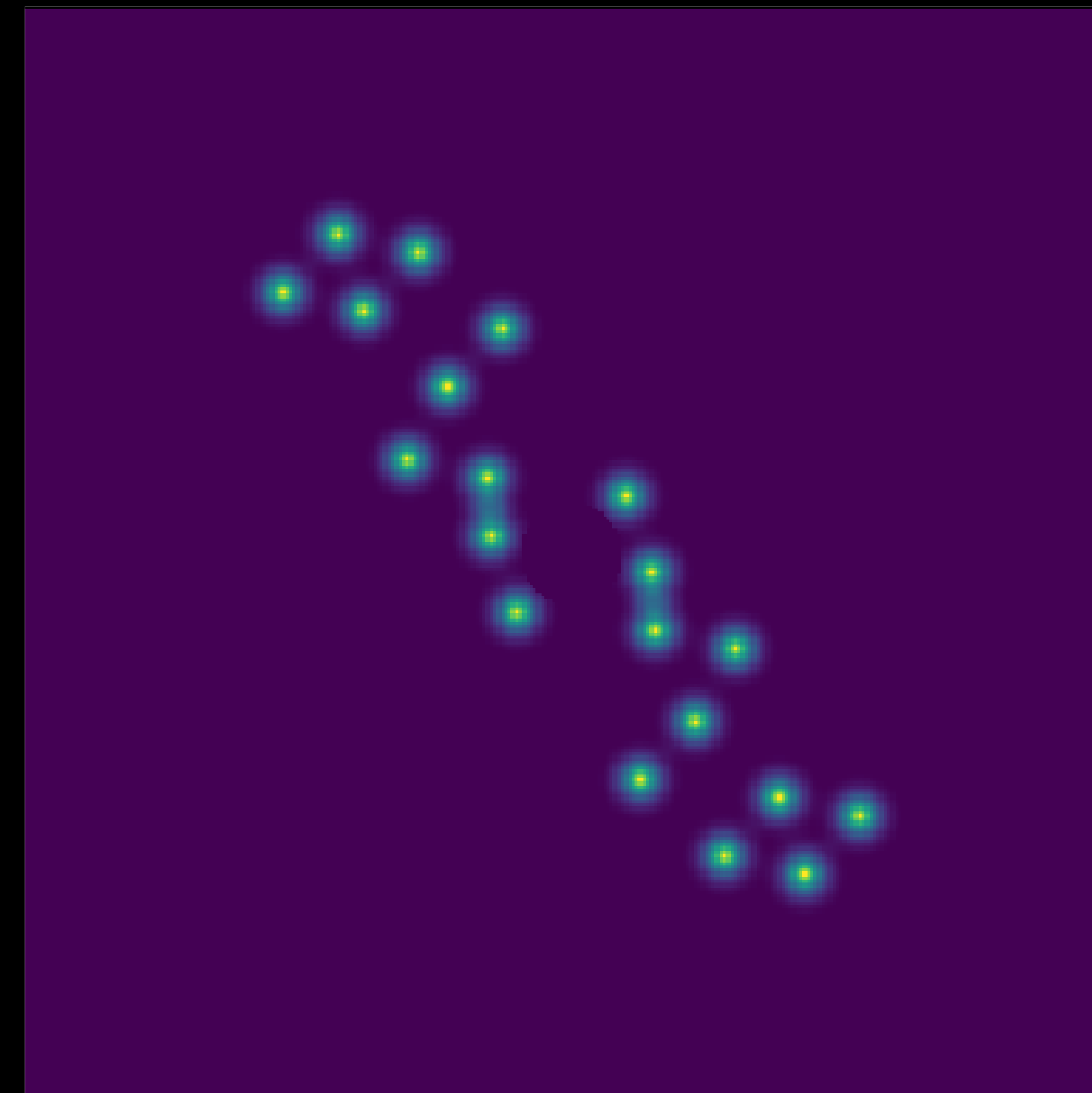
Pupil



Image

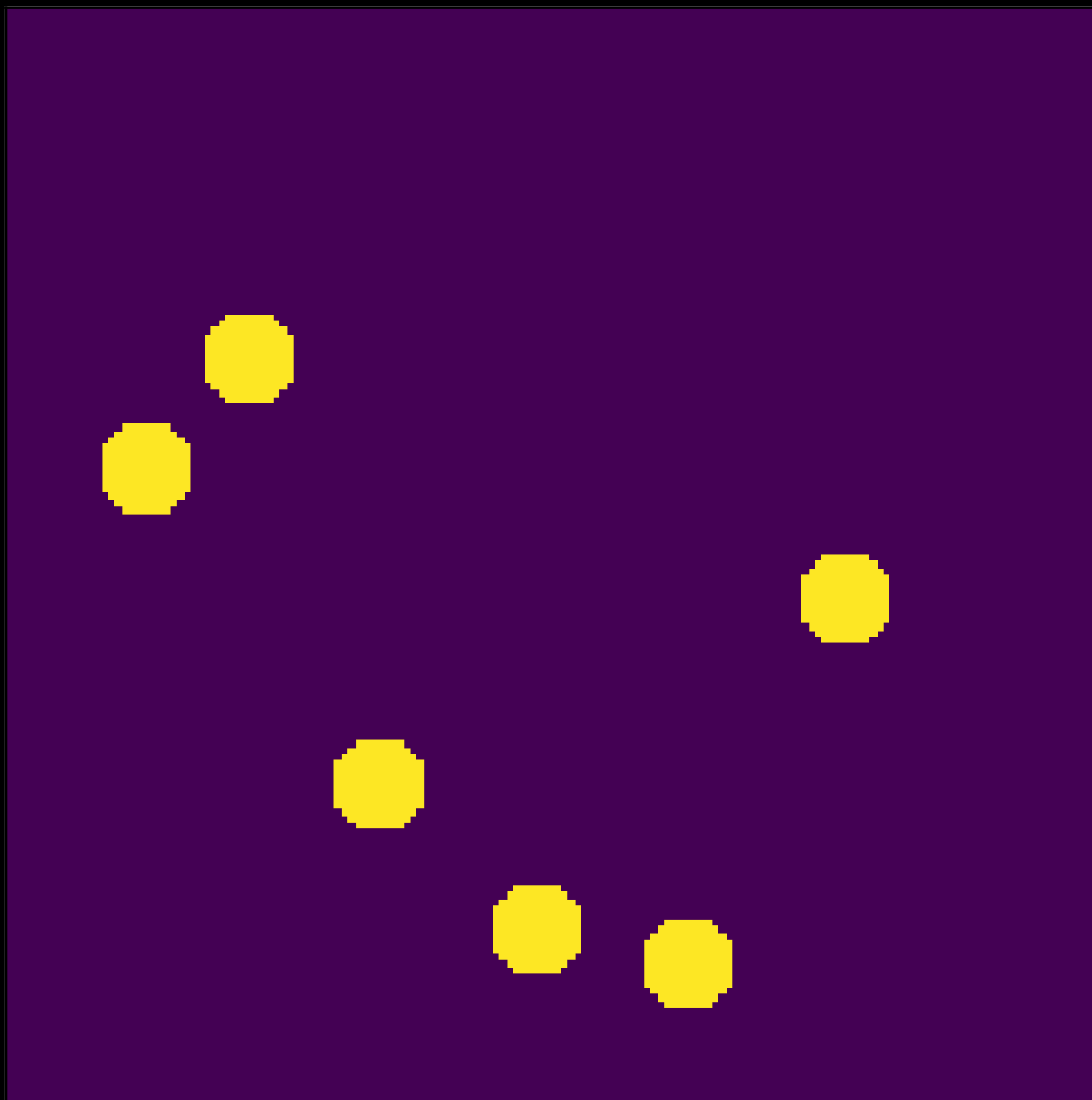


Complex Visibilities

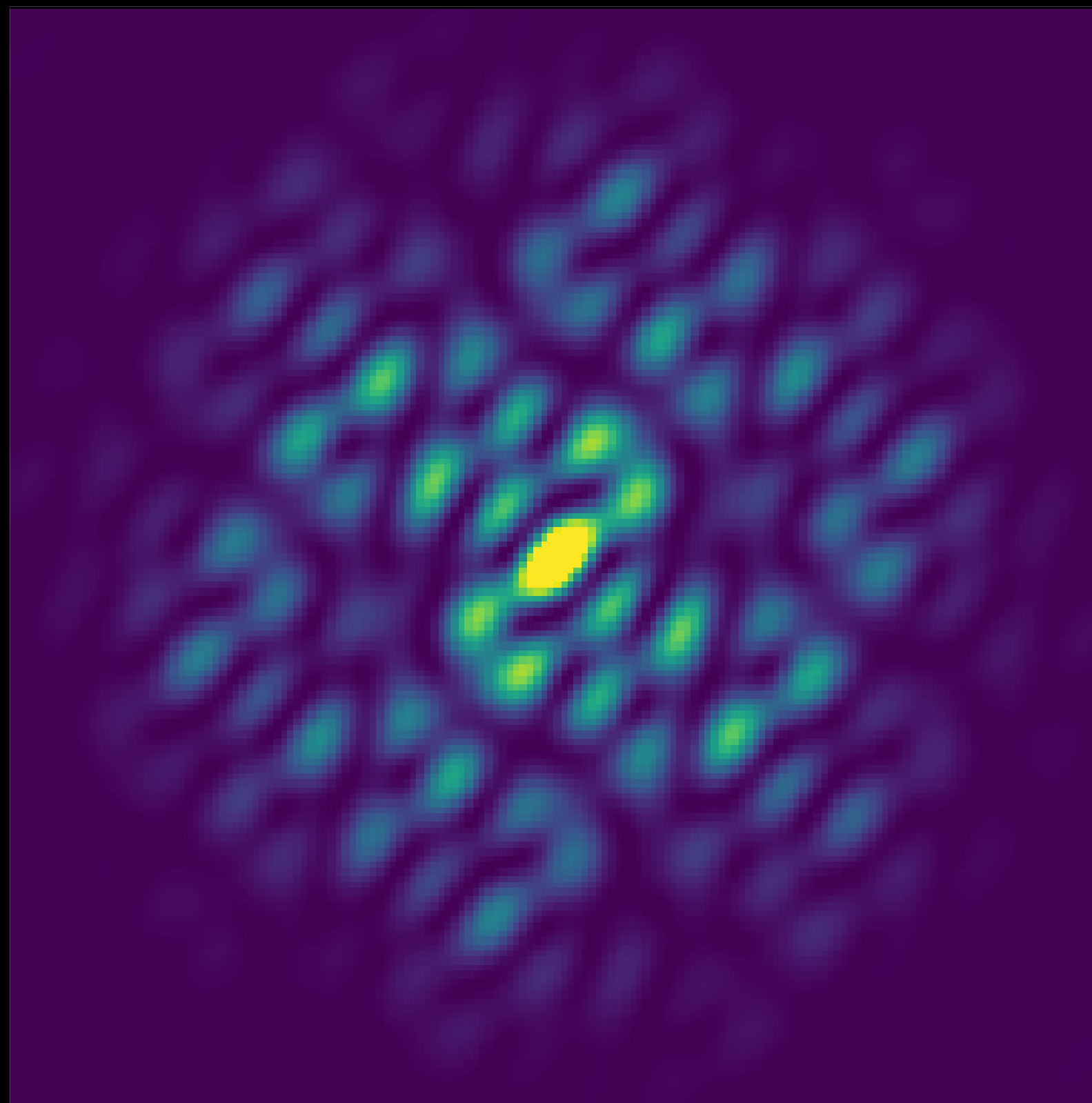


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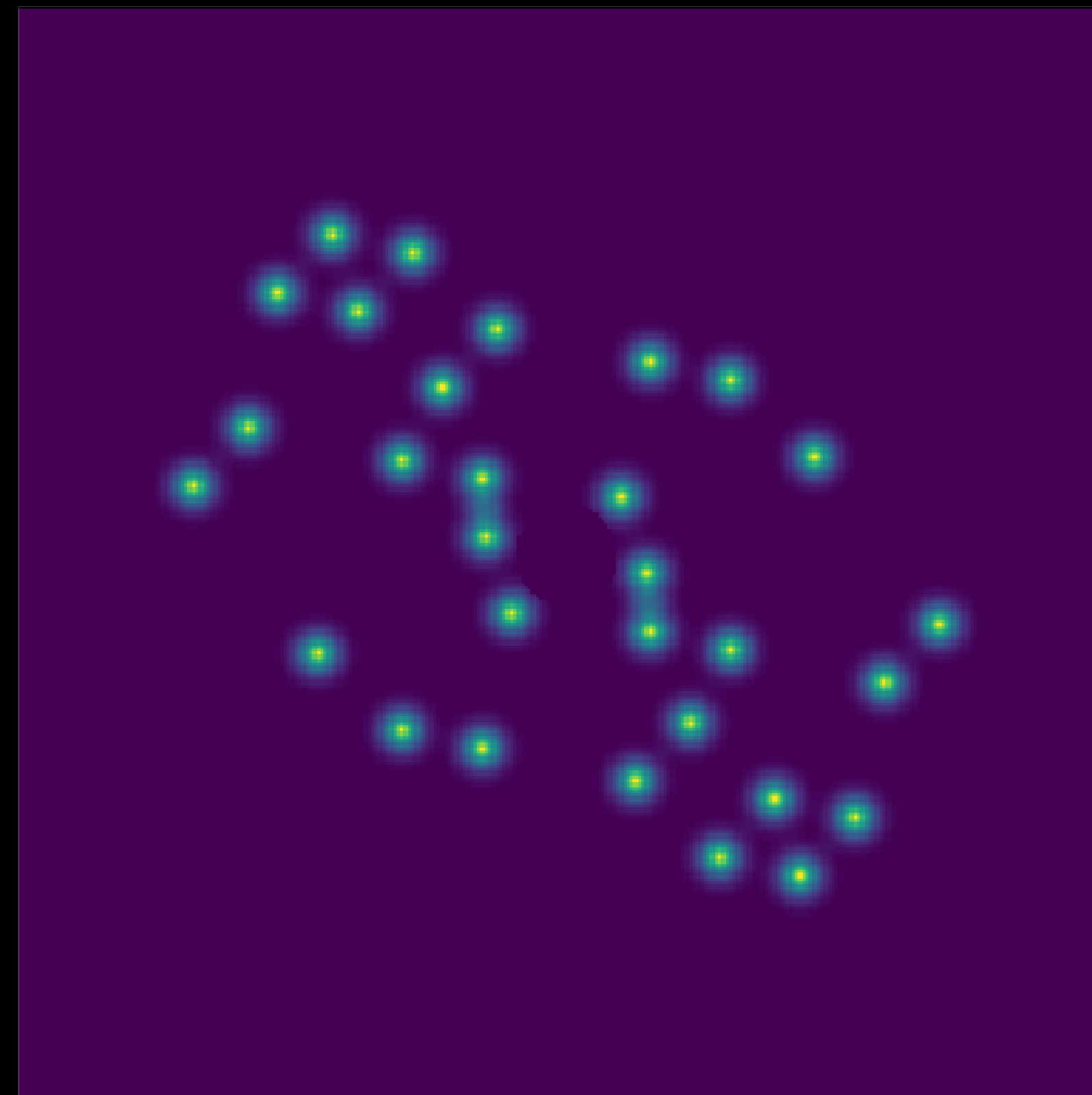
Pupil



Image

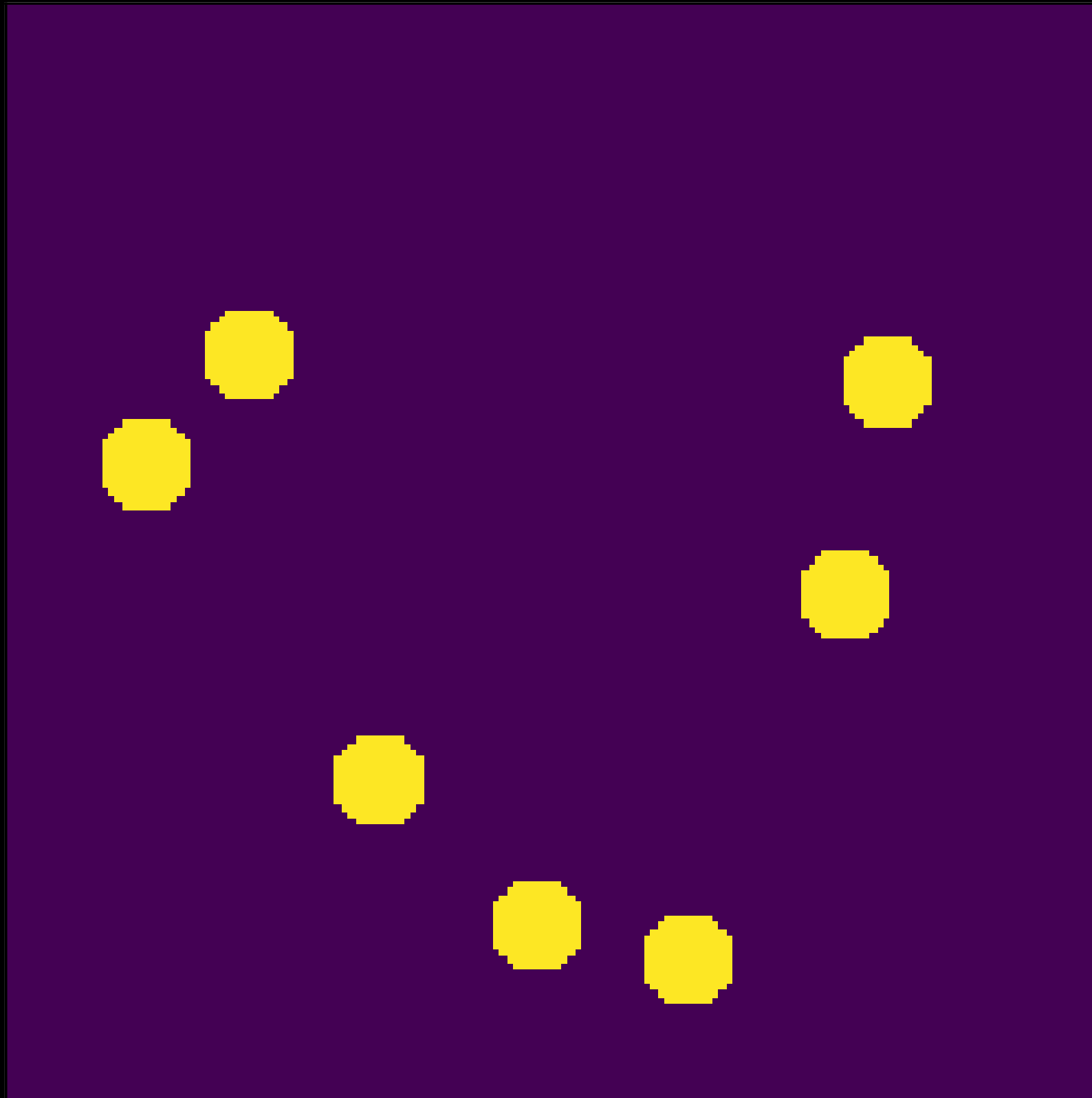


Complex Visibilities

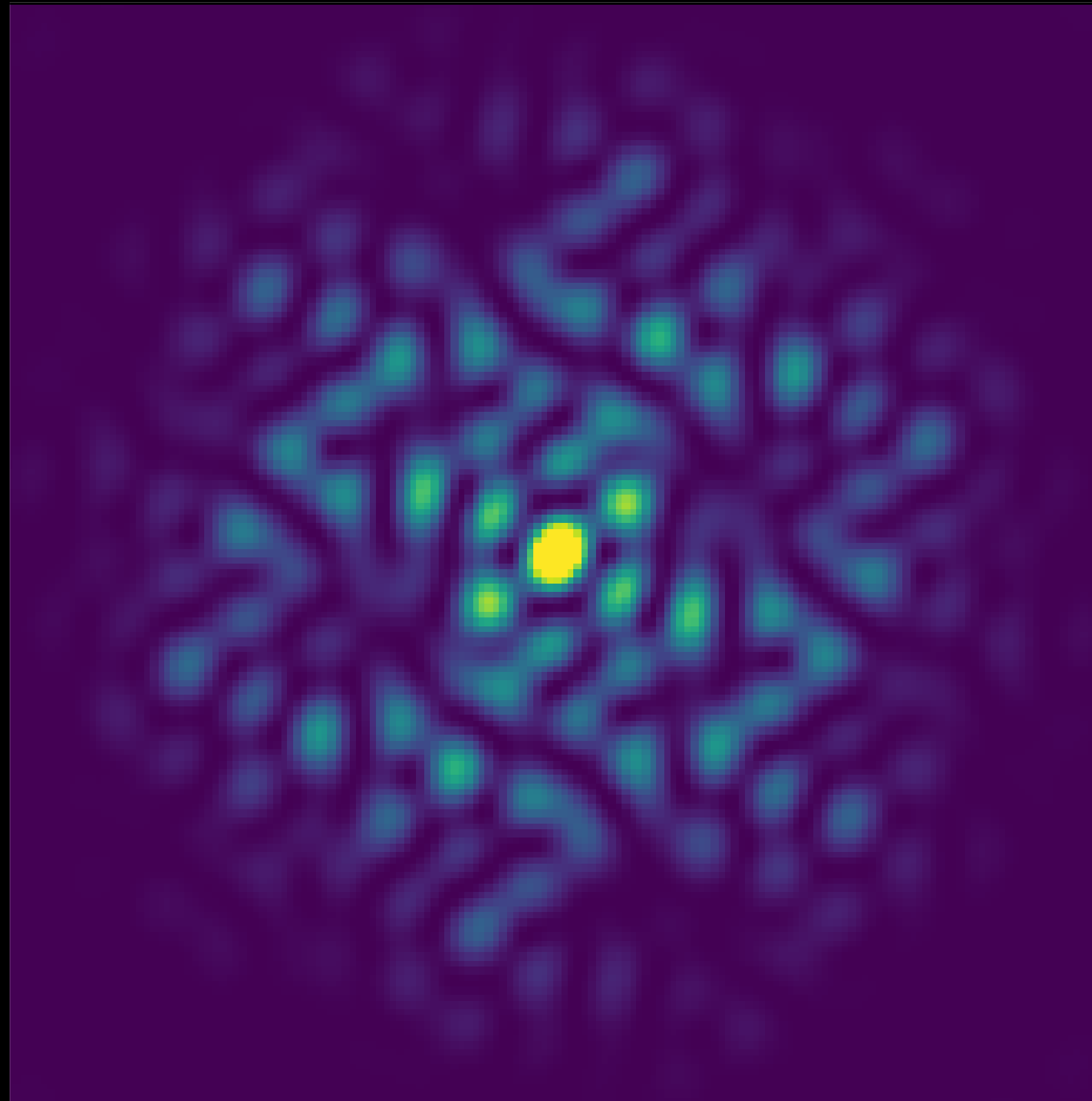


Non-Redundant Masking

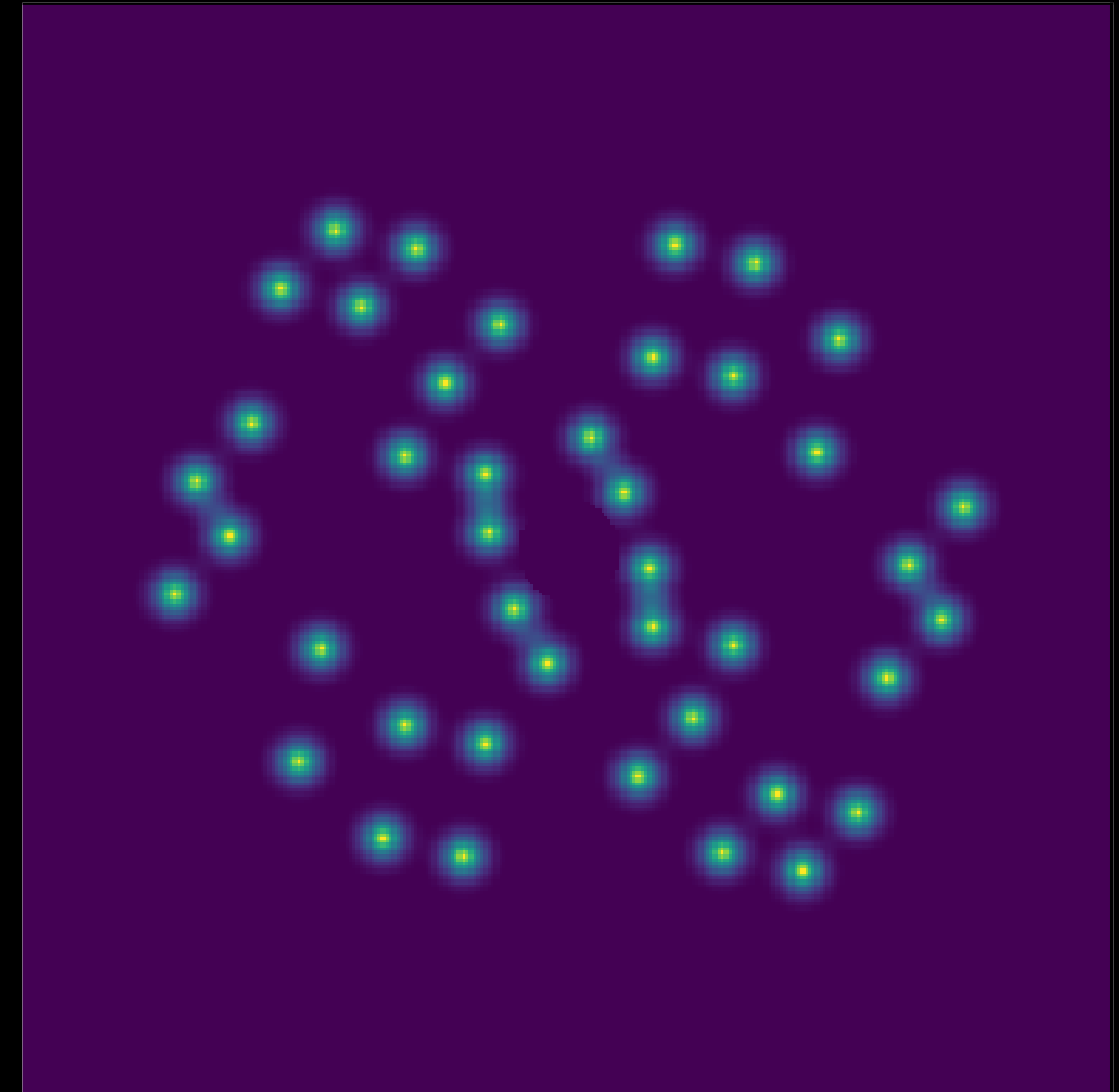
Pupil



Image

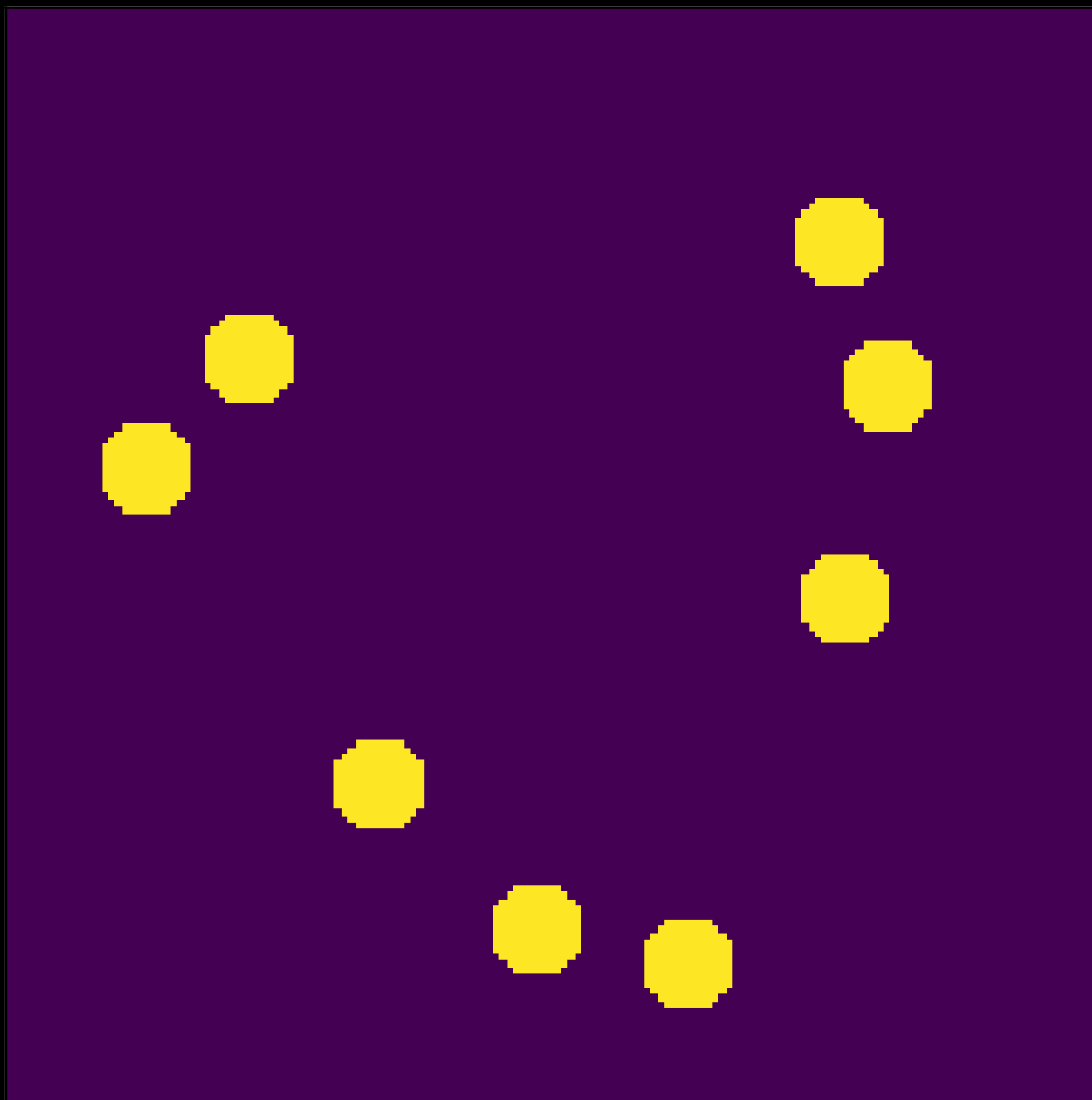


Complex Visibilities

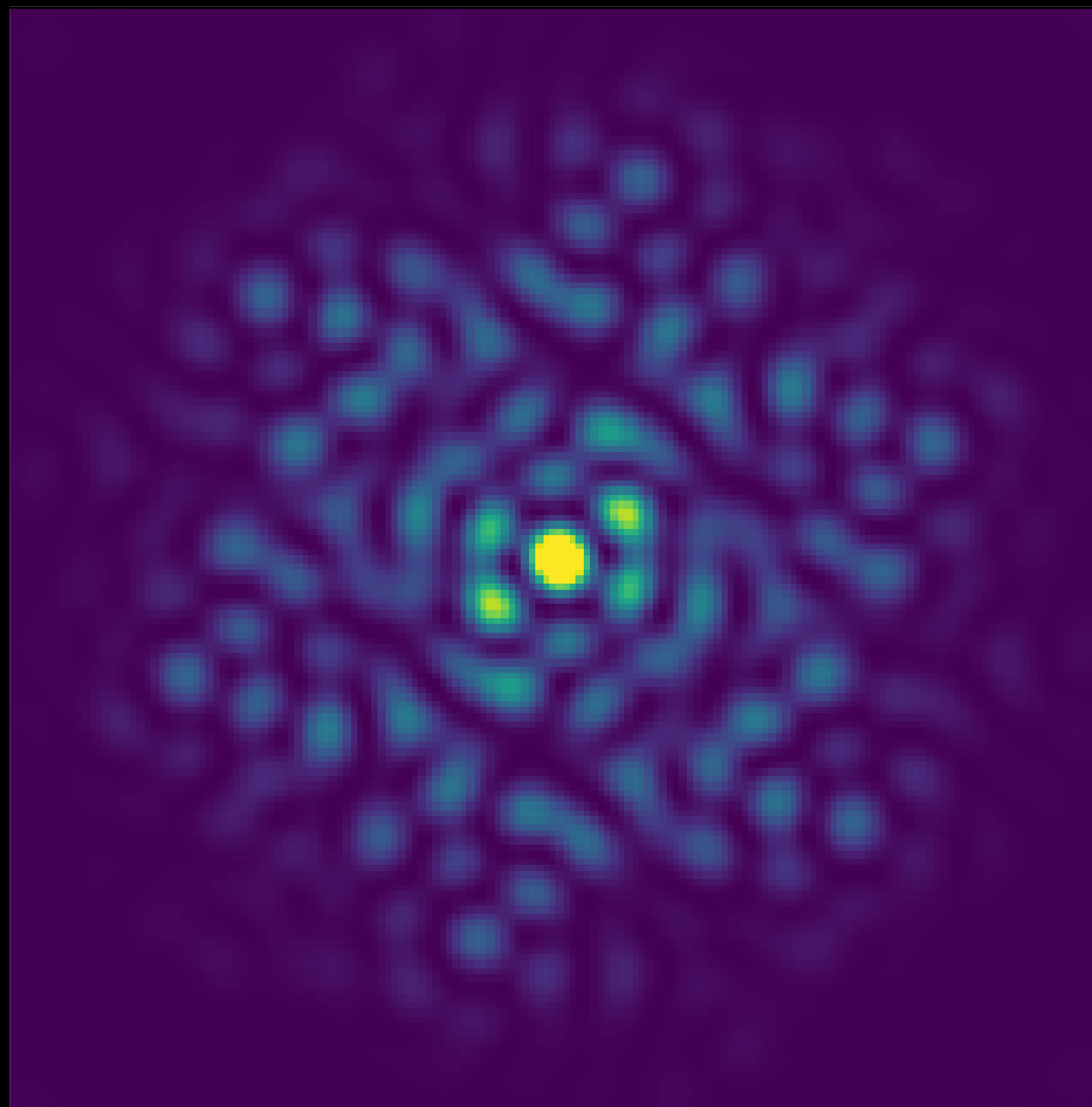


Non-Redundant Masking

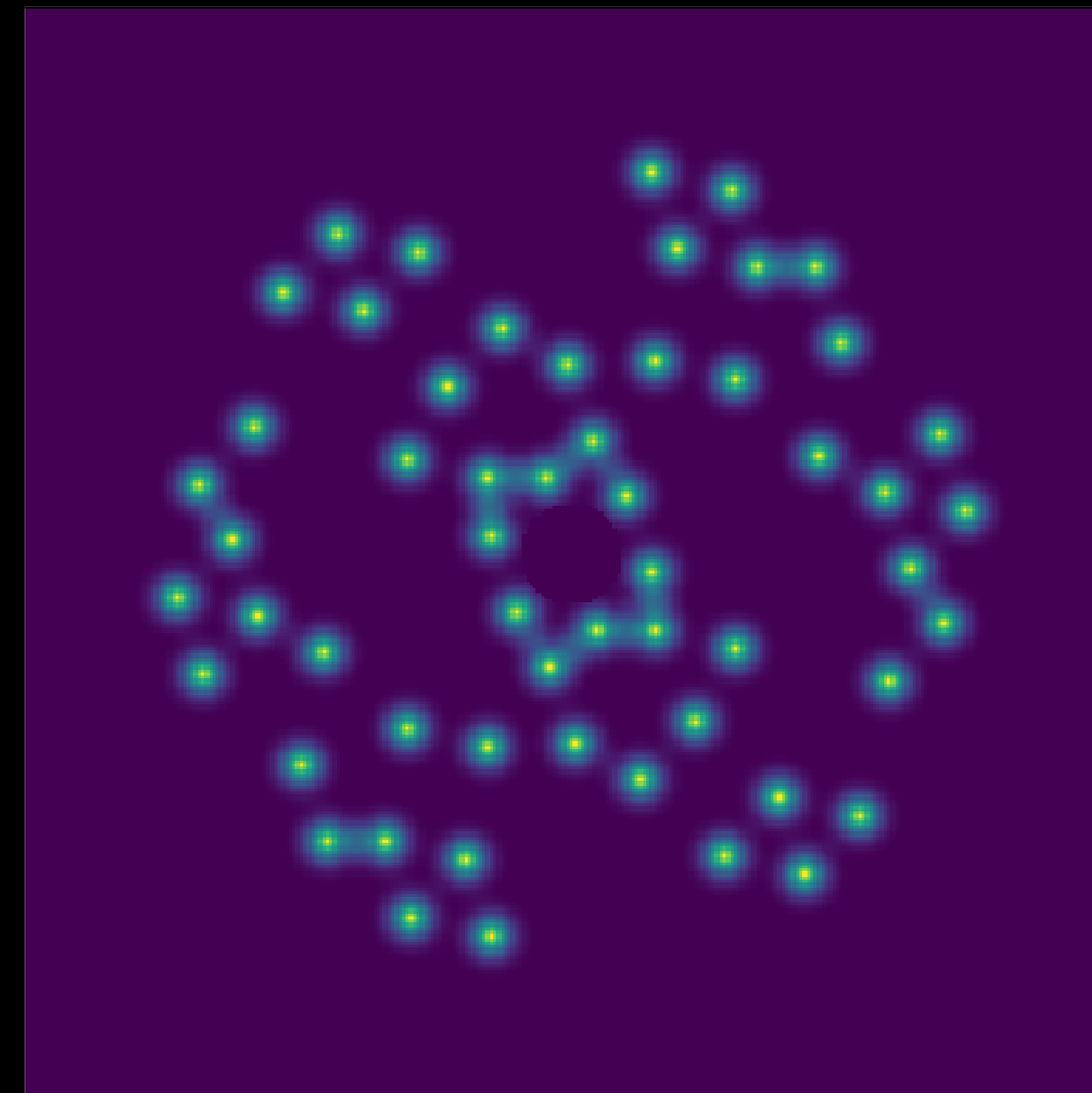
Pupil



Image

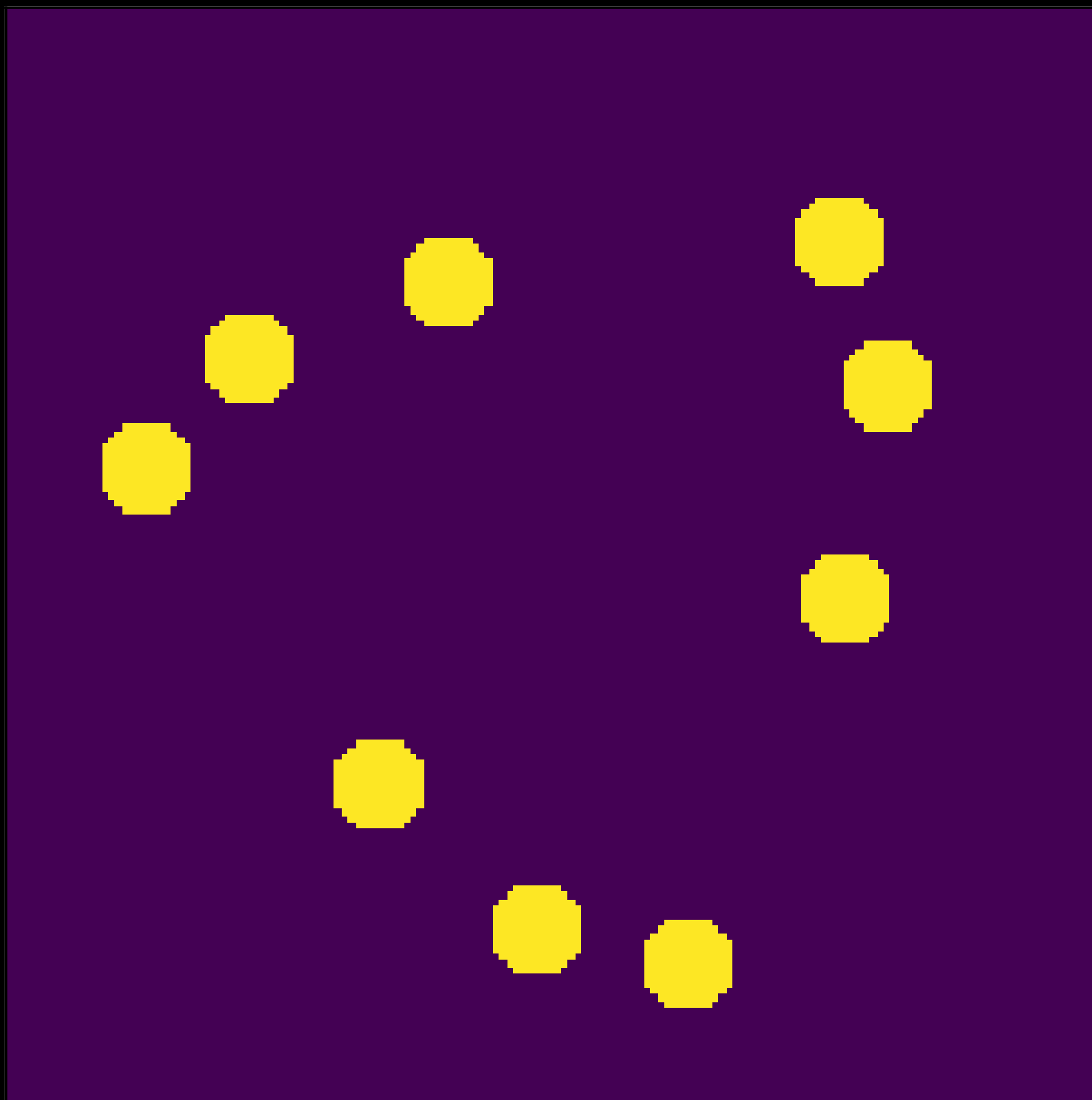


Complex Visibilities

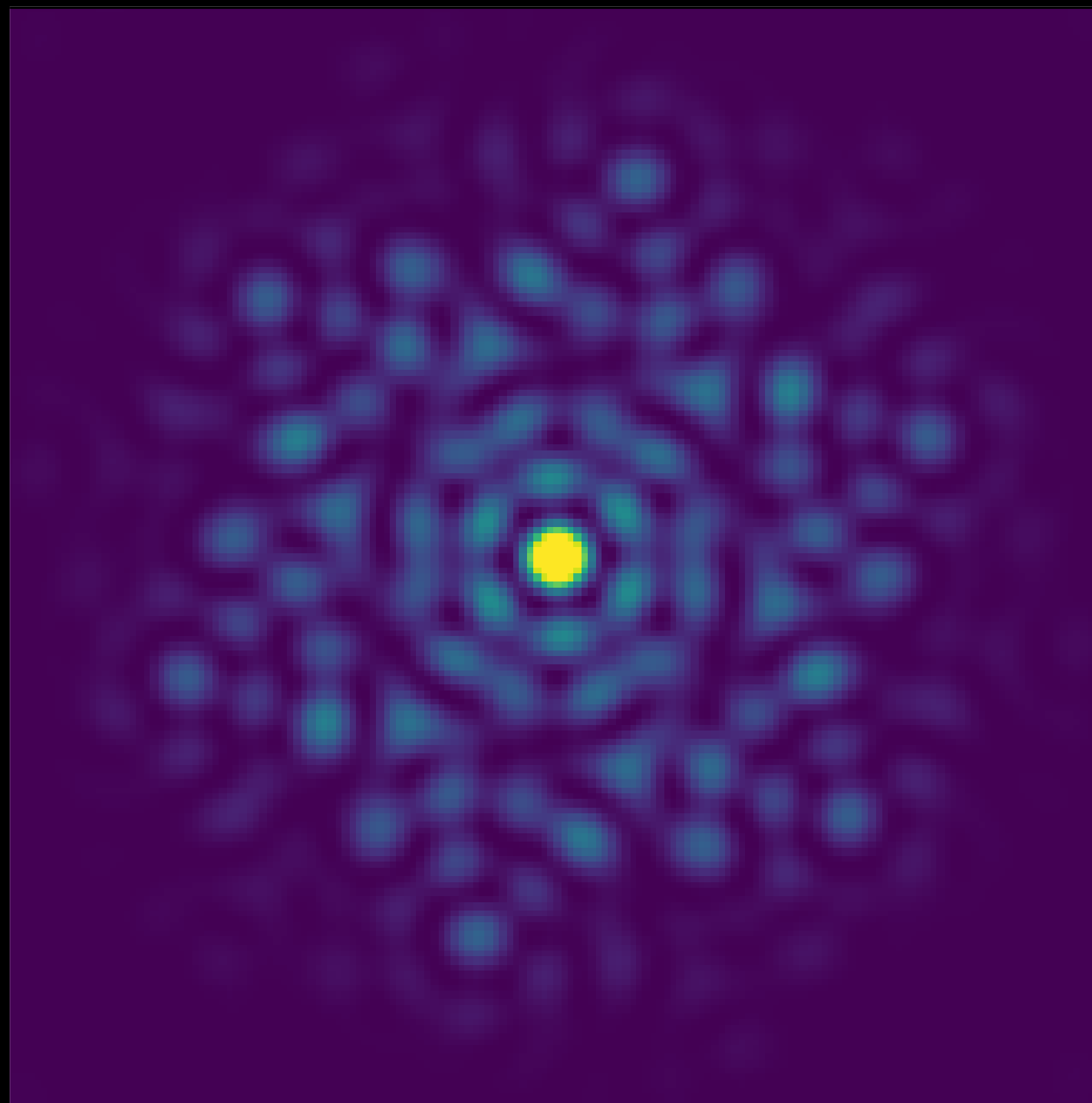


Non-Redundant Masking

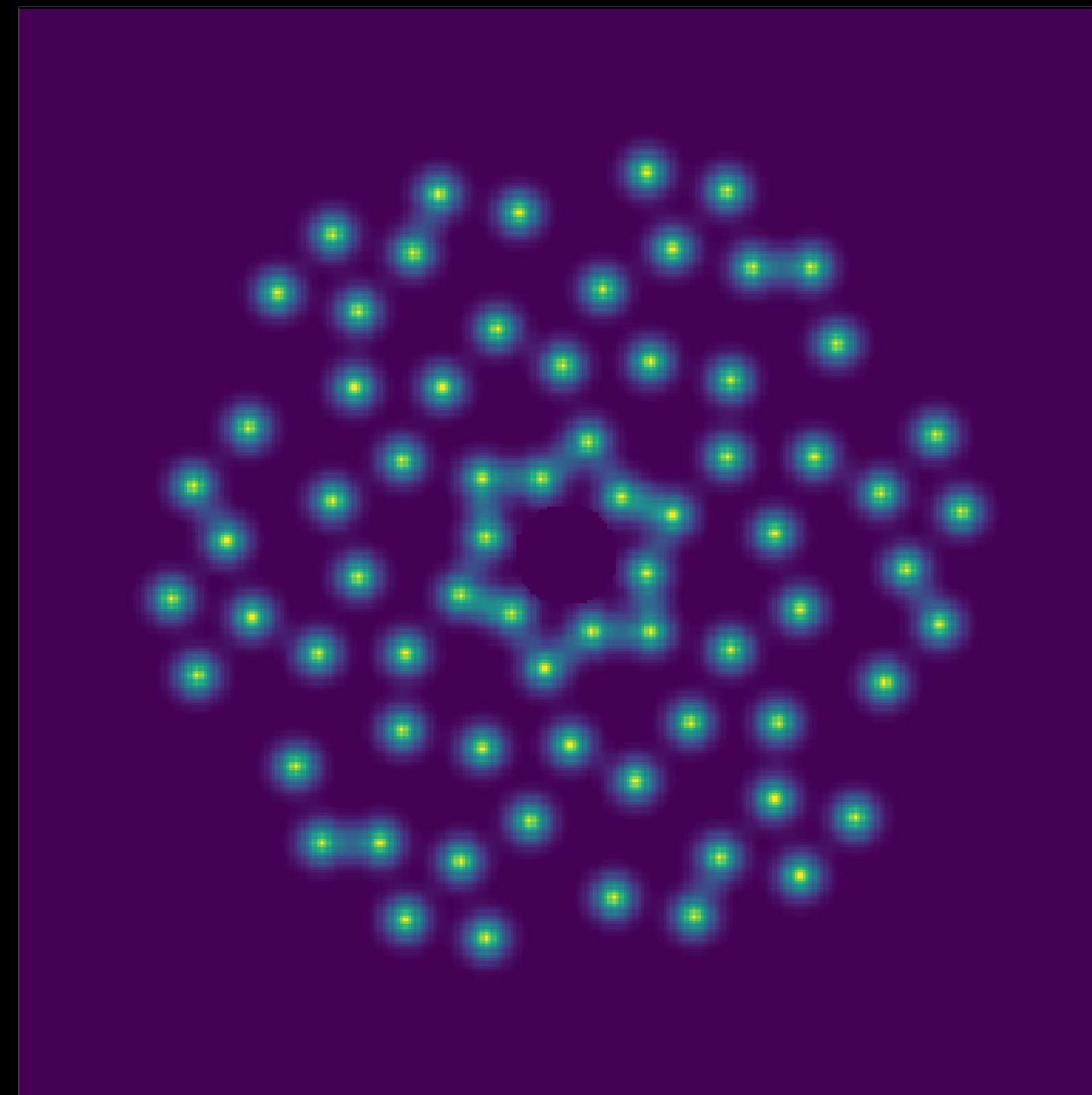
Pupil



Image



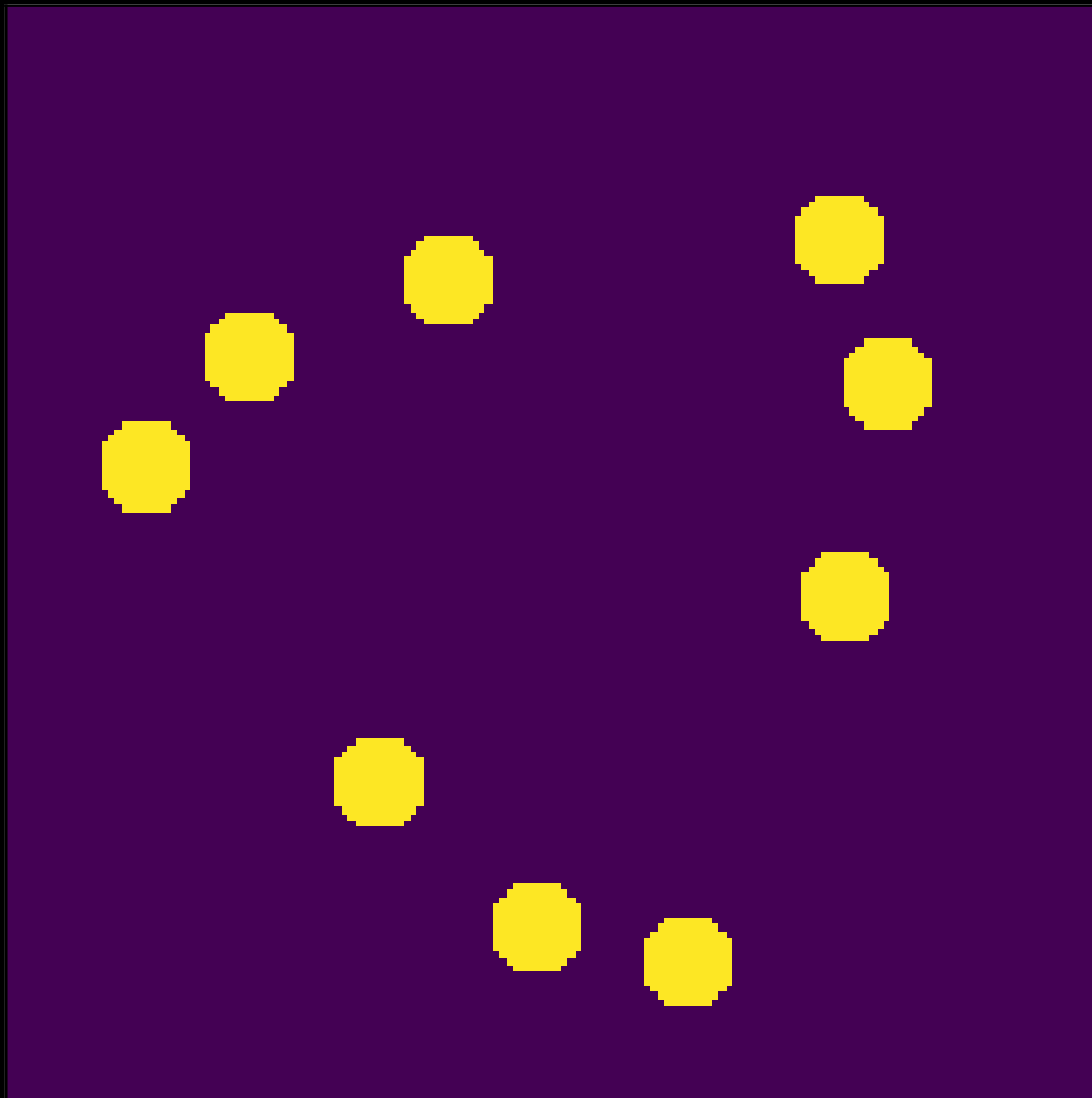
Complex Visibilities



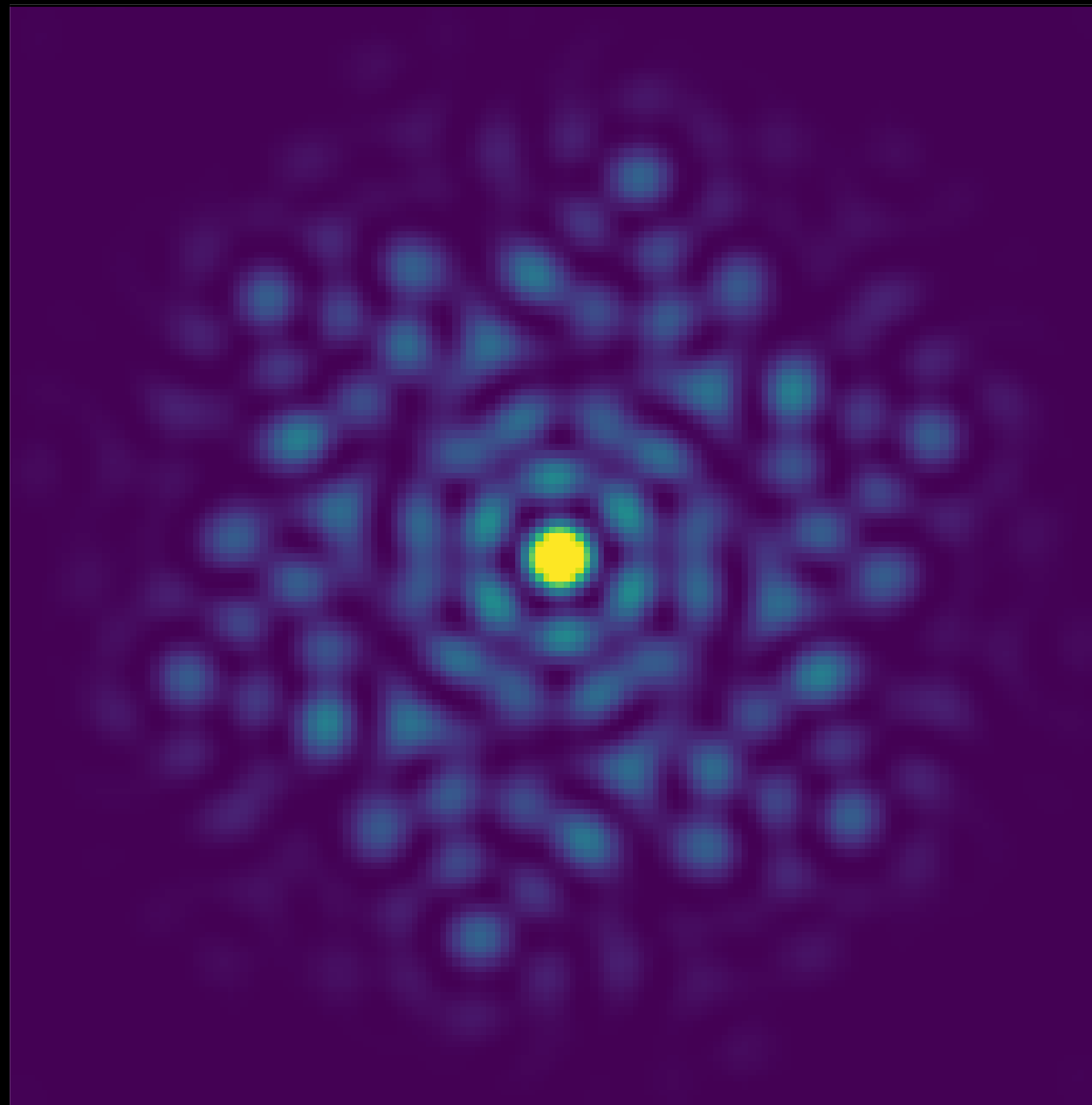
Non-Redundant Masking

Using NRM to measure stellar diameters was first suggested by Fizeau in 1868!

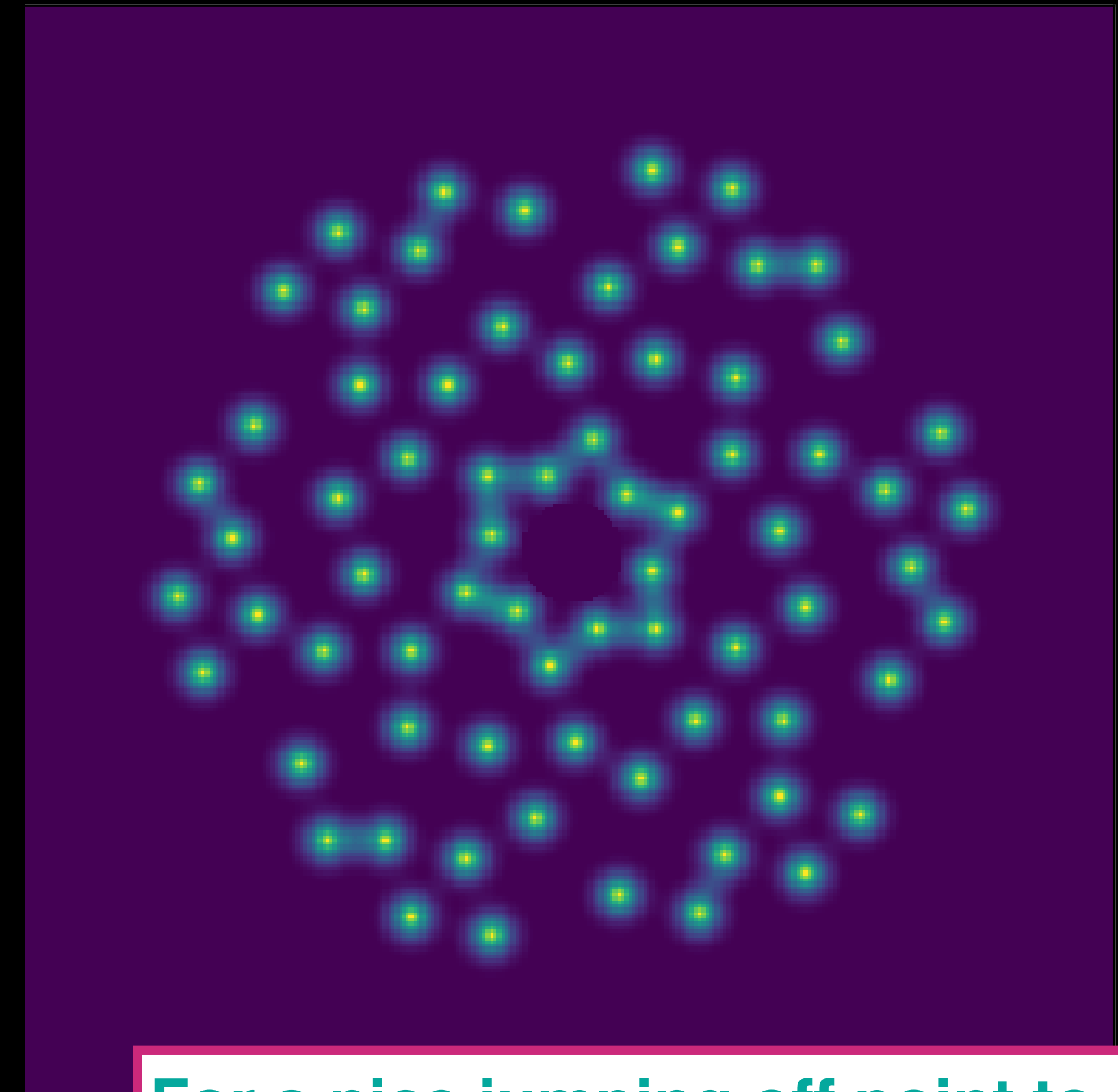
Pupil



Image



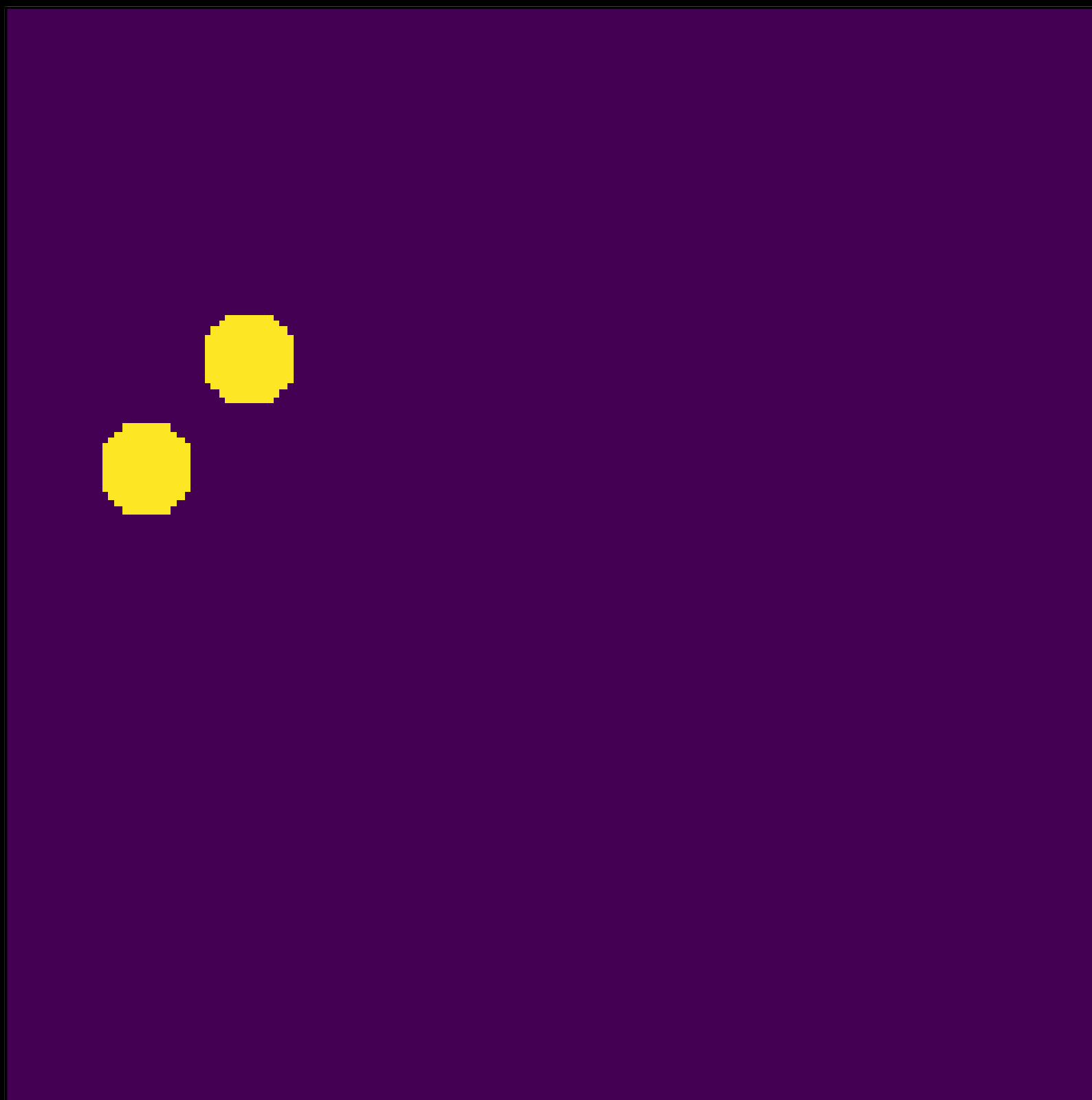
Complex Visibilities



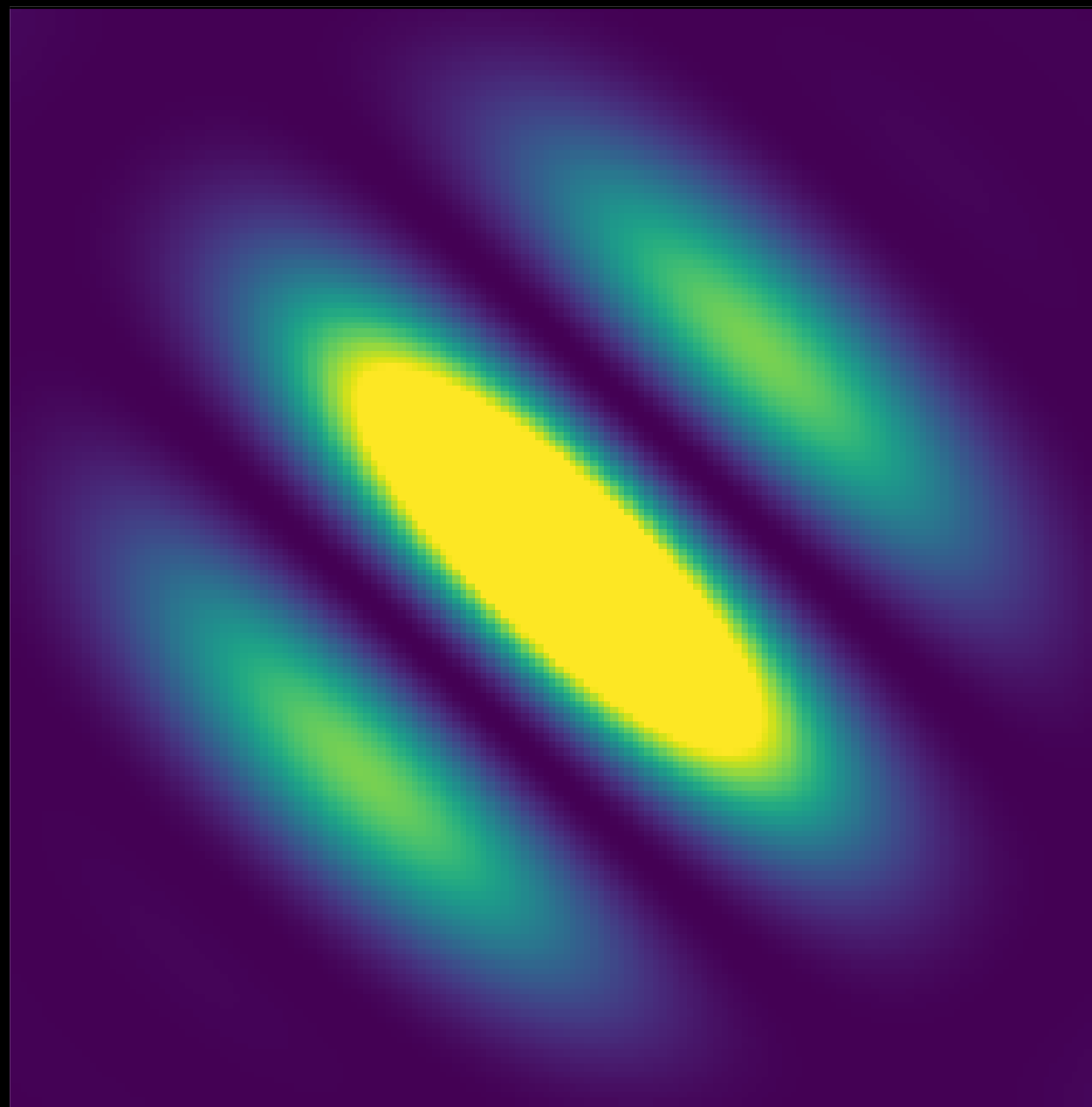
For a nice jumping off point to explore the history of AMI, see Tuthill 2012!

NRM fringes can be described by amplitude and phase.

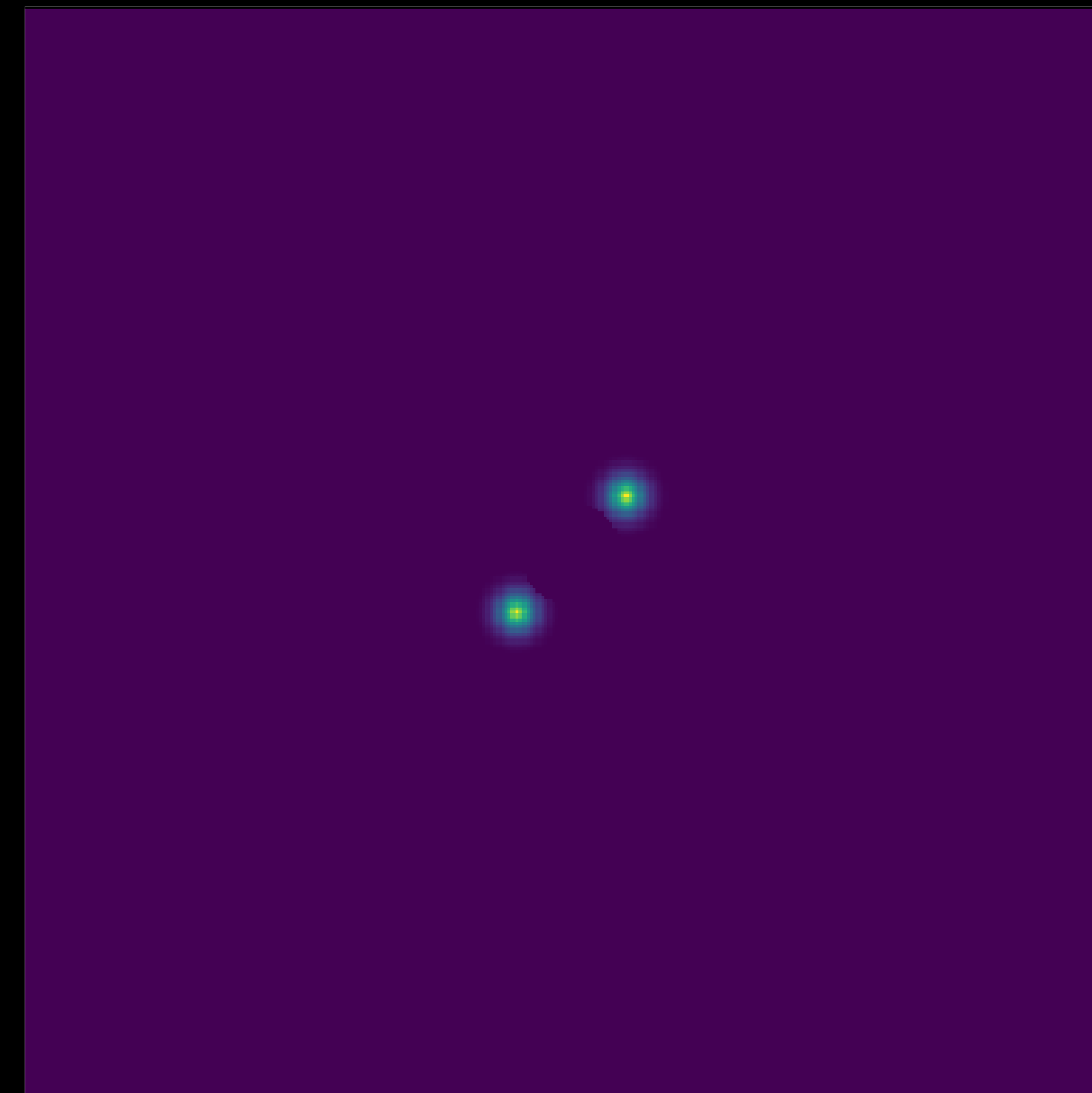
Pupil



Image

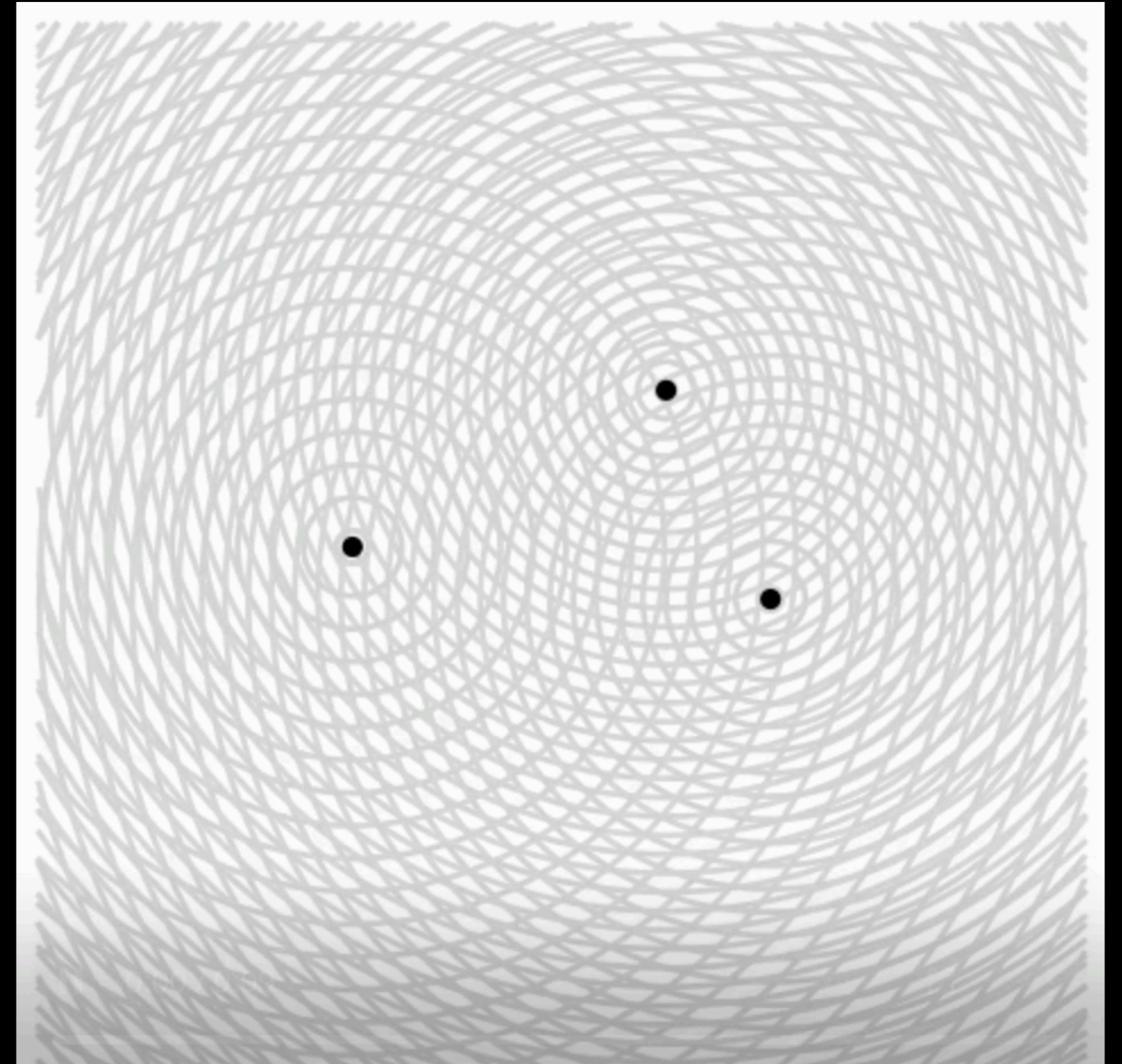


Complex Visibilities



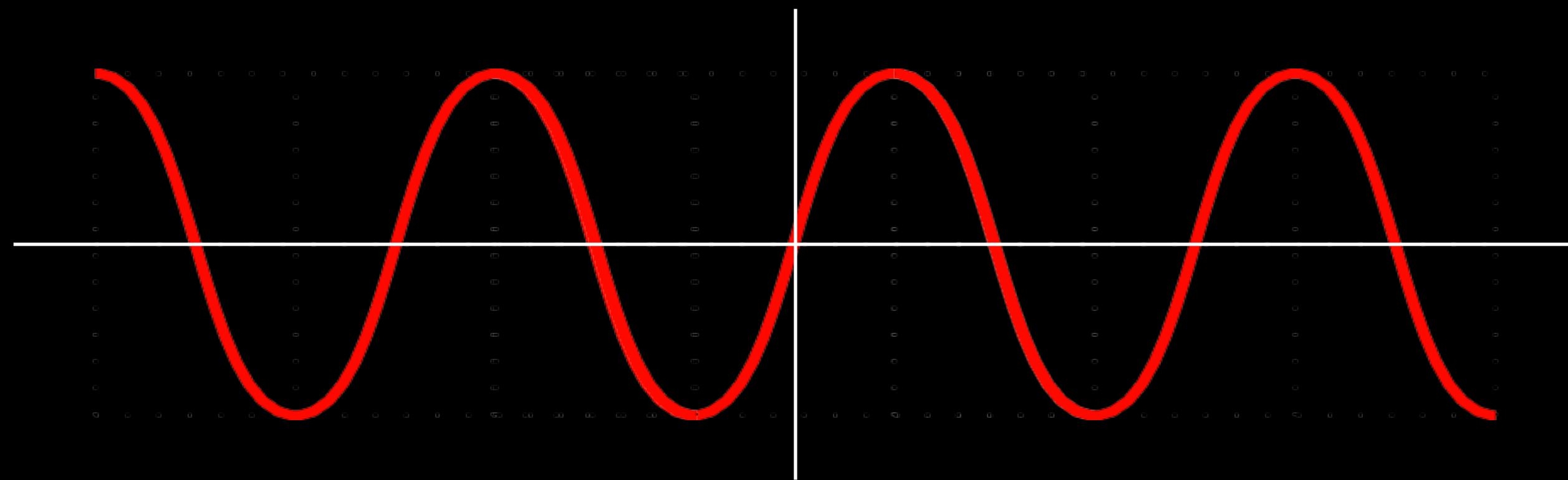
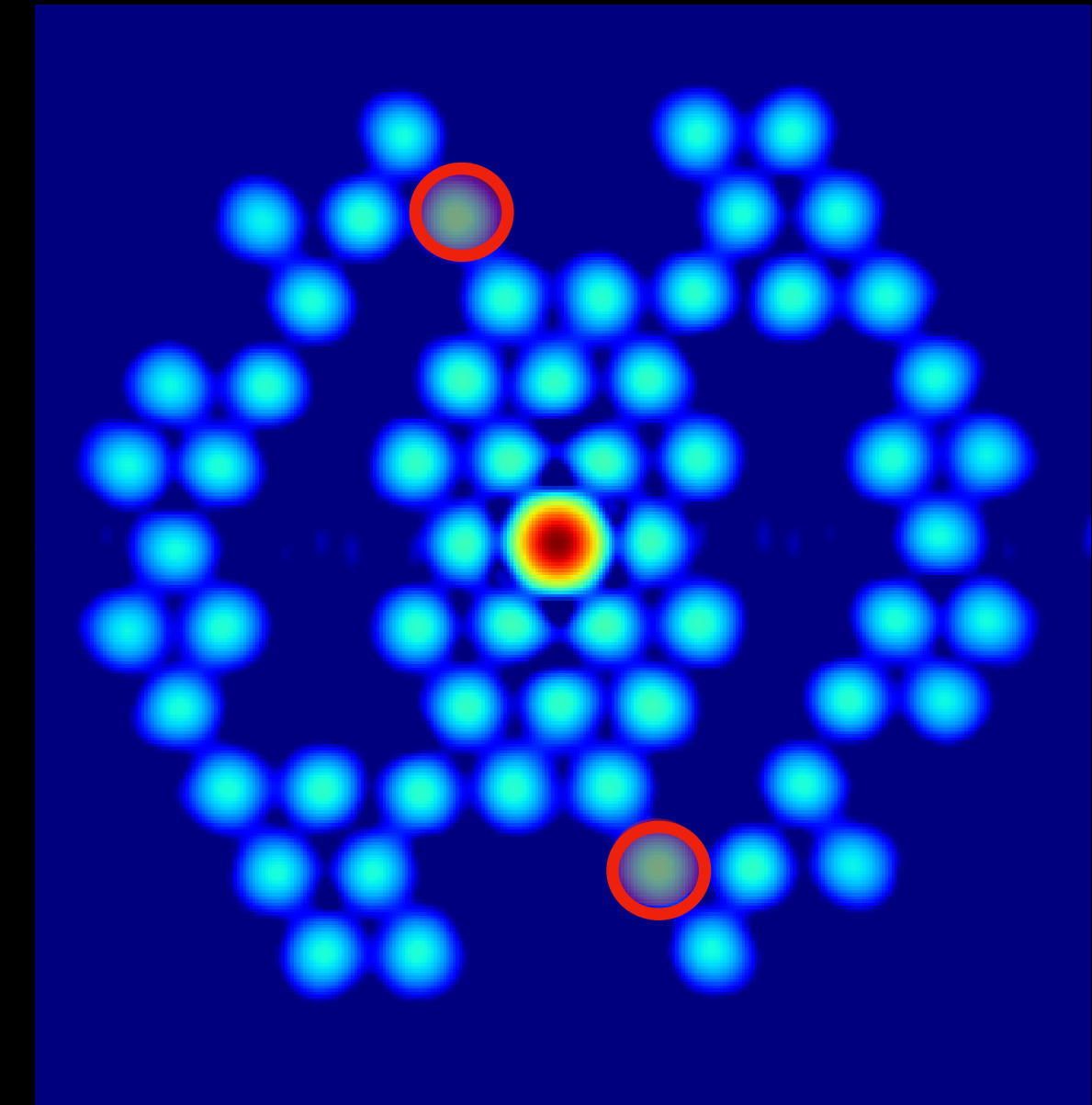
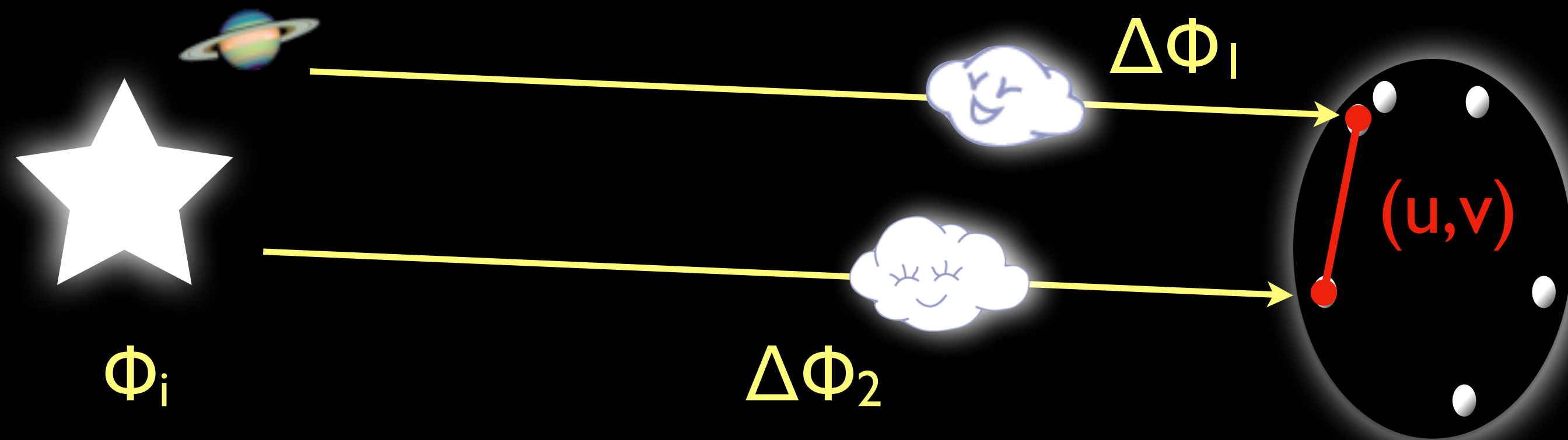
Interpreting Interferometric Observables

van Cittert-Zernike Theorem: the complex visibilities of an incoherent source at great distance are equal to the Fourier transform of the source brightness distribution



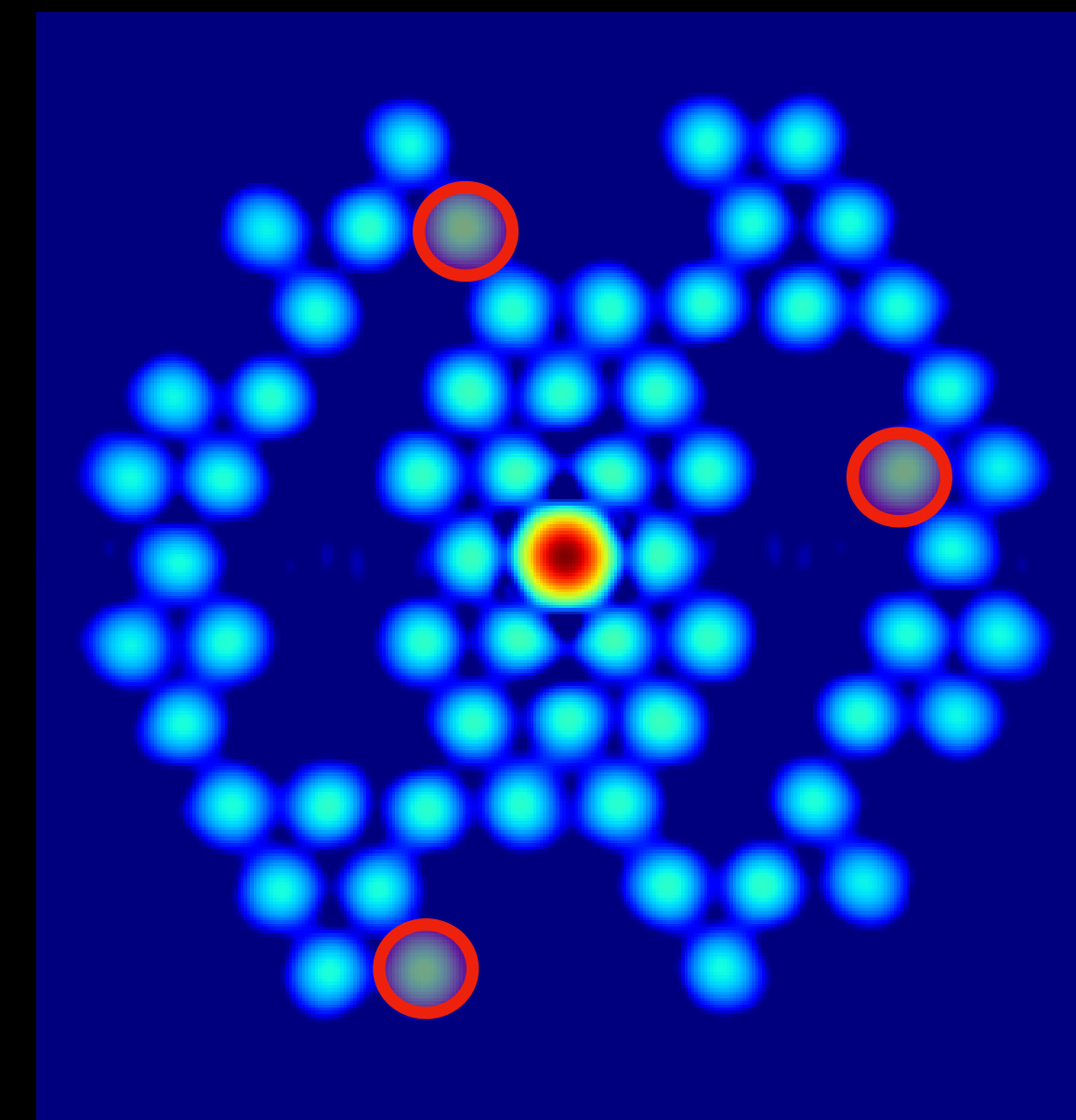
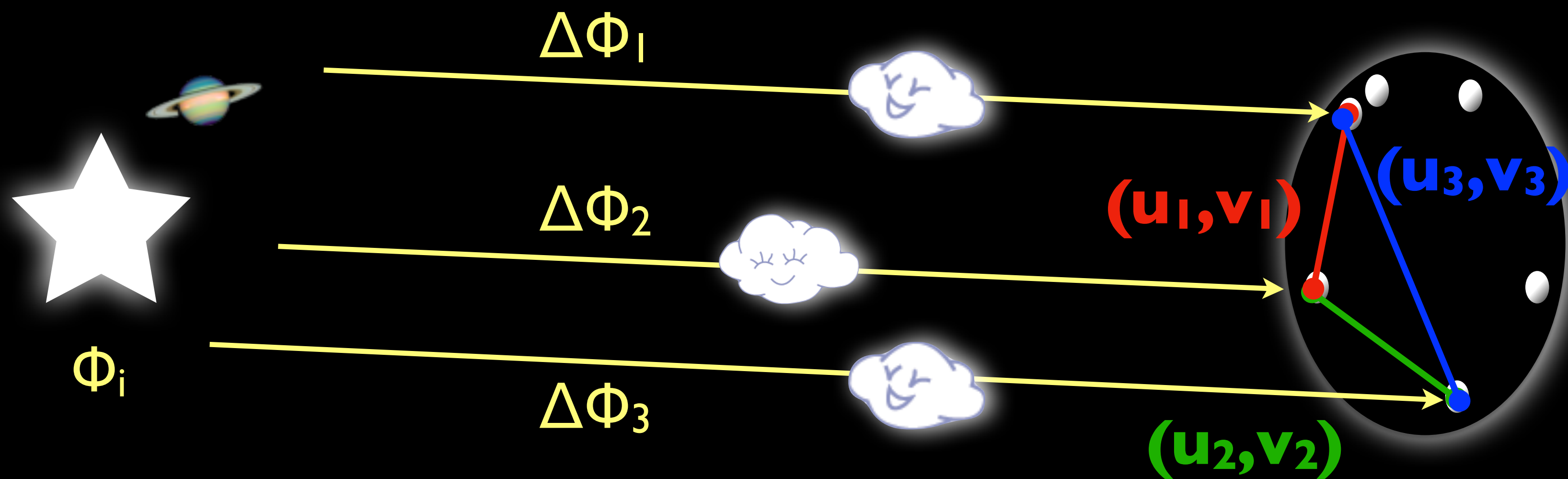
Source: [Jacopo Bertolotti https://twitter.com/j_bertolotti/status/1674801693228417031?s=20](https://twitter.com/j_bertolotti/status/1674801693228417031?s=20)

NRM observables are linear in instrumental phase...



$$Ae^{i\Phi(u,v)} = Ae^{i[\Phi_i + (\Delta\Phi_2 - \Delta\Phi_1)]}$$
$$\Phi(u_1, v_1) = \Phi_i(u_1, v_1) + (\Delta\Phi_2 - \Delta\Phi_1)$$

...and closure phases are robust to instrumental phase.

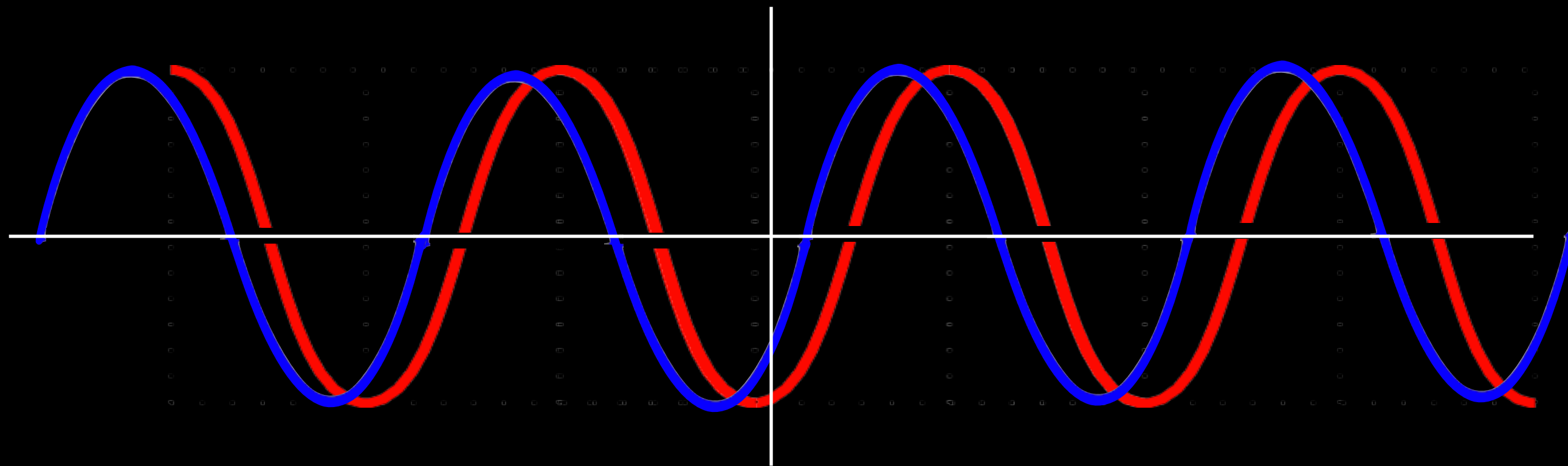
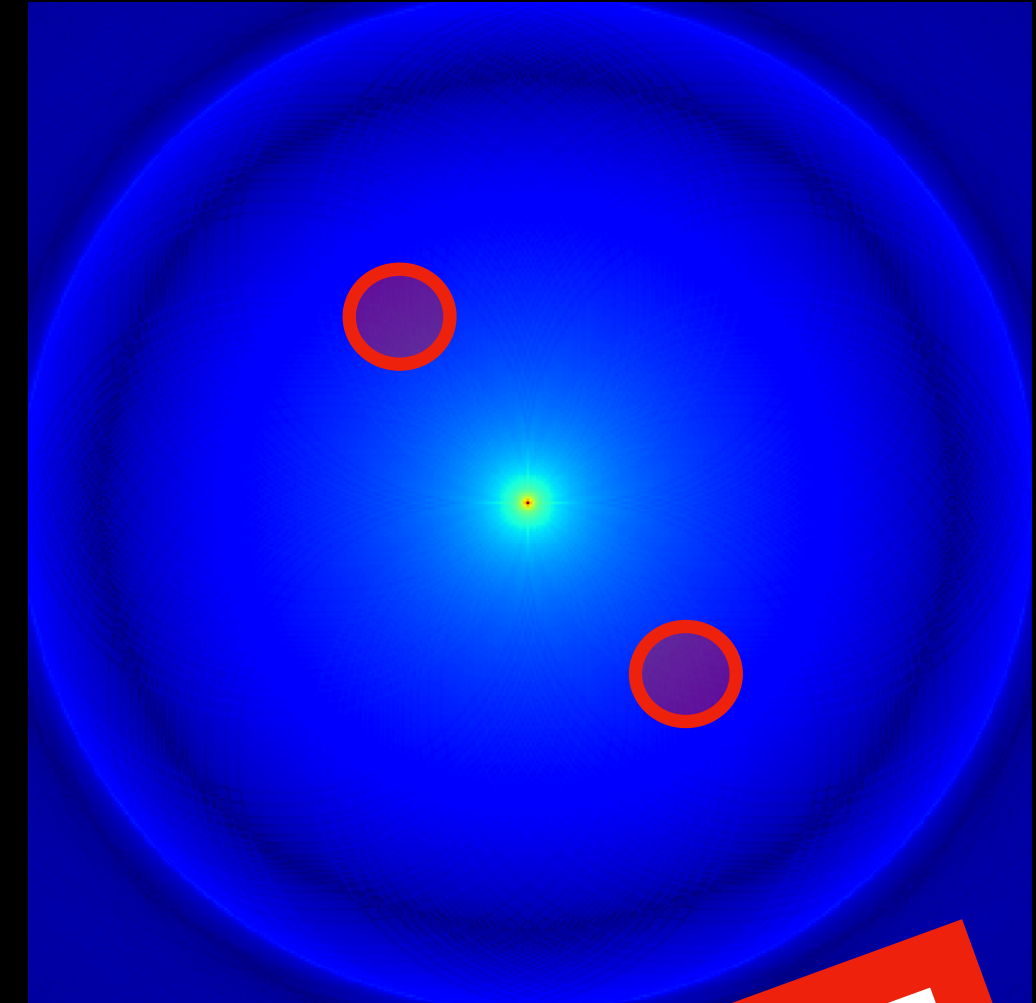
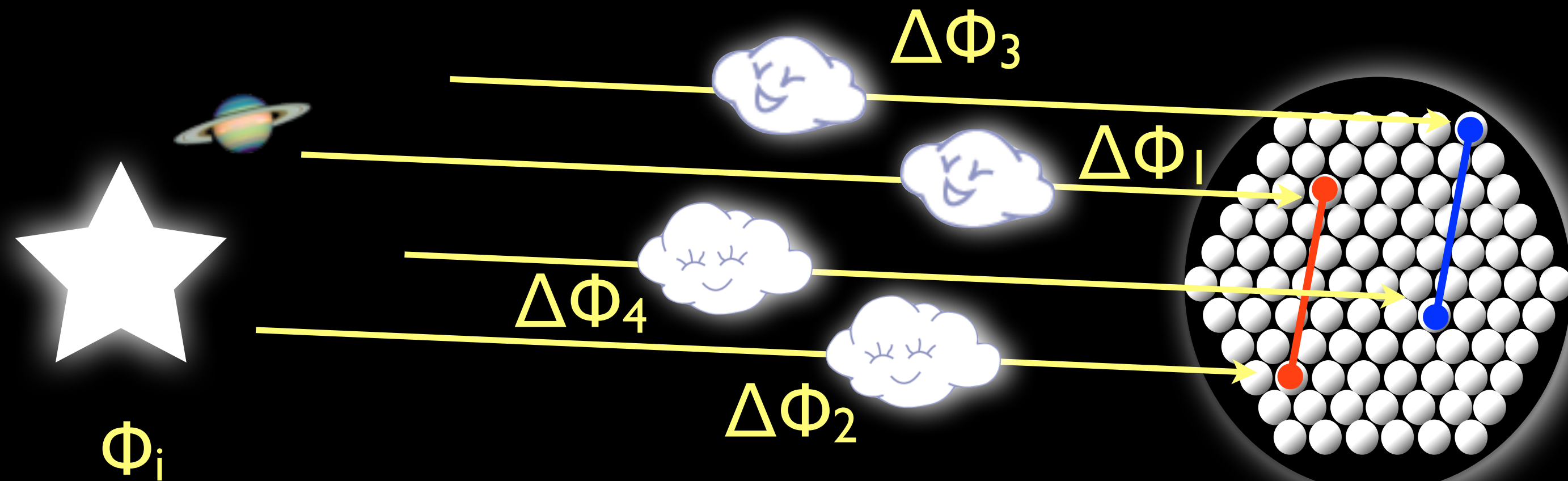


$$\begin{aligned} \Phi(u_1, v_1) &= \Phi_i(u_1, v_1) + (\Delta\Phi_2 - \Delta\Phi_1) \\ + \Phi(u_2, v_2) &= \Phi_i(u_2, v_2) + (\Delta\Phi_3 - \Delta\Phi_2) \\ + \Phi(u_3, v_3) &= \Phi_i(u_3, v_3) + (\Delta\Phi_1 - \Delta\Phi_3) \end{aligned}$$

$$\Phi(u_1, v_1) + \Phi(u_2, v_2) + \Phi(u_3, v_3) = \Phi_i(u_1, v_1) + \Phi_i(u_2, v_2) + \Phi_i(u_3, v_3)$$

For a thorough discussion of phase errors in AMI, see Ireland 2013.

What about a redundant aperture?



$$Ae^{i\Phi(u,v)} = A e^{i(\Phi_i + \Delta\Phi_1)}$$

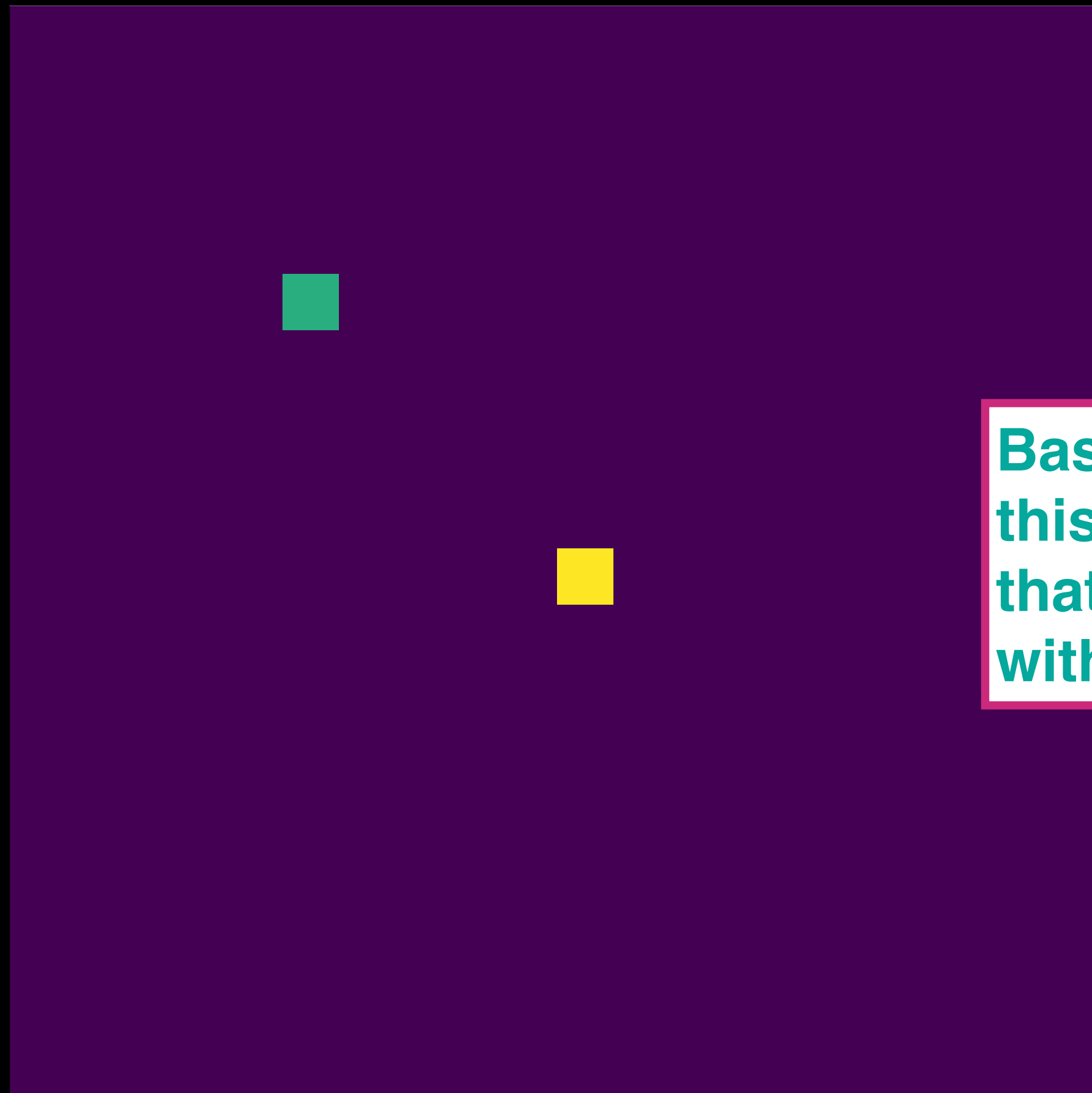
$$\Phi(u,v) = \Phi_i + (\Delta\Phi_2 - \Delta\Phi_1) + (\Delta\Phi_4 - \Delta\Phi_3)$$

Not linear in instrumental phase :(

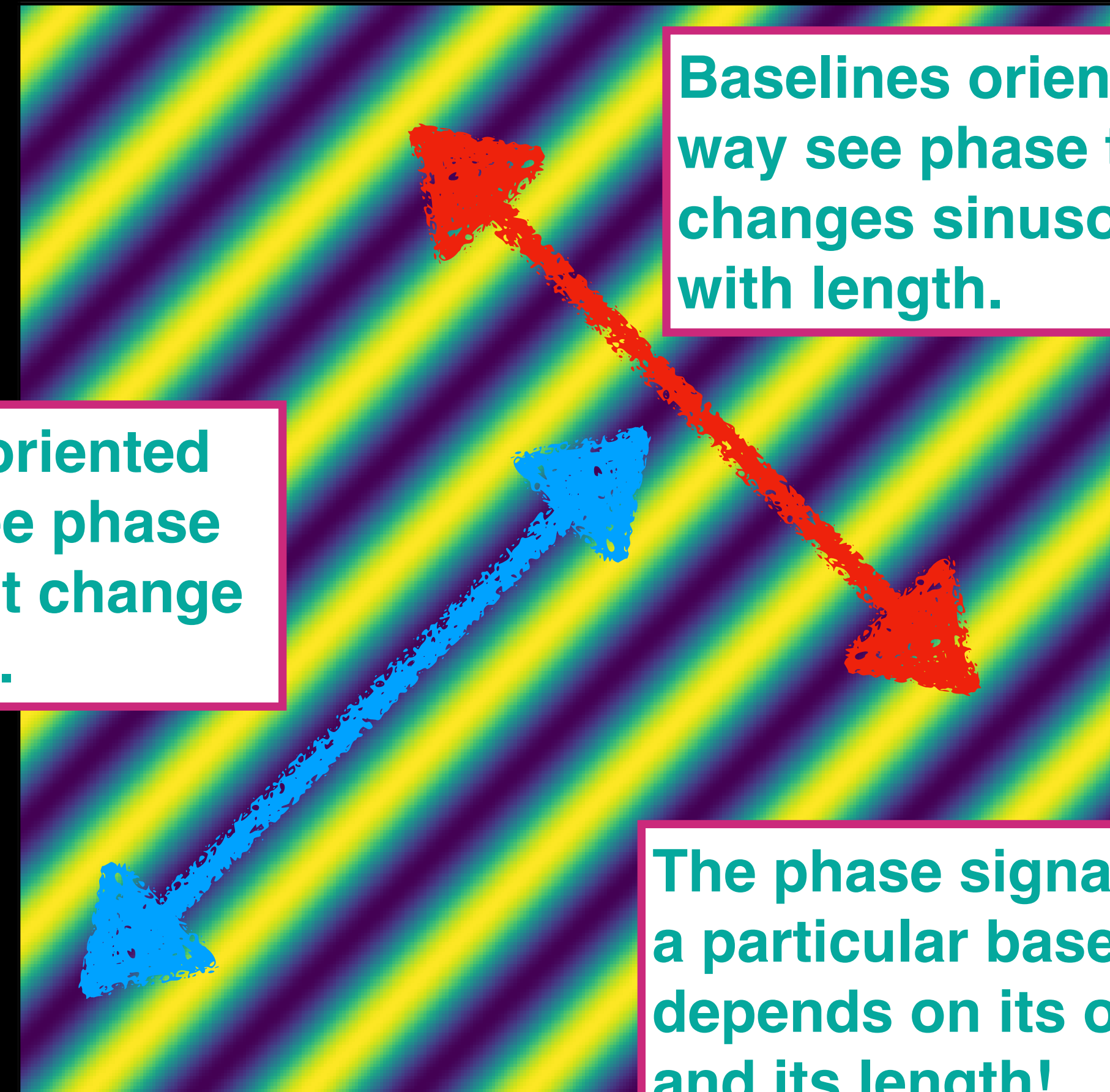
Note: Kernel phase interferometry can overcome this issue if you have high image quality! (Ask me after!)

Interpreting NRM Observables: Closure Phases (Sums of) Fourier Phases Intrinsic to the Source

Binary Image



Fourier Phase



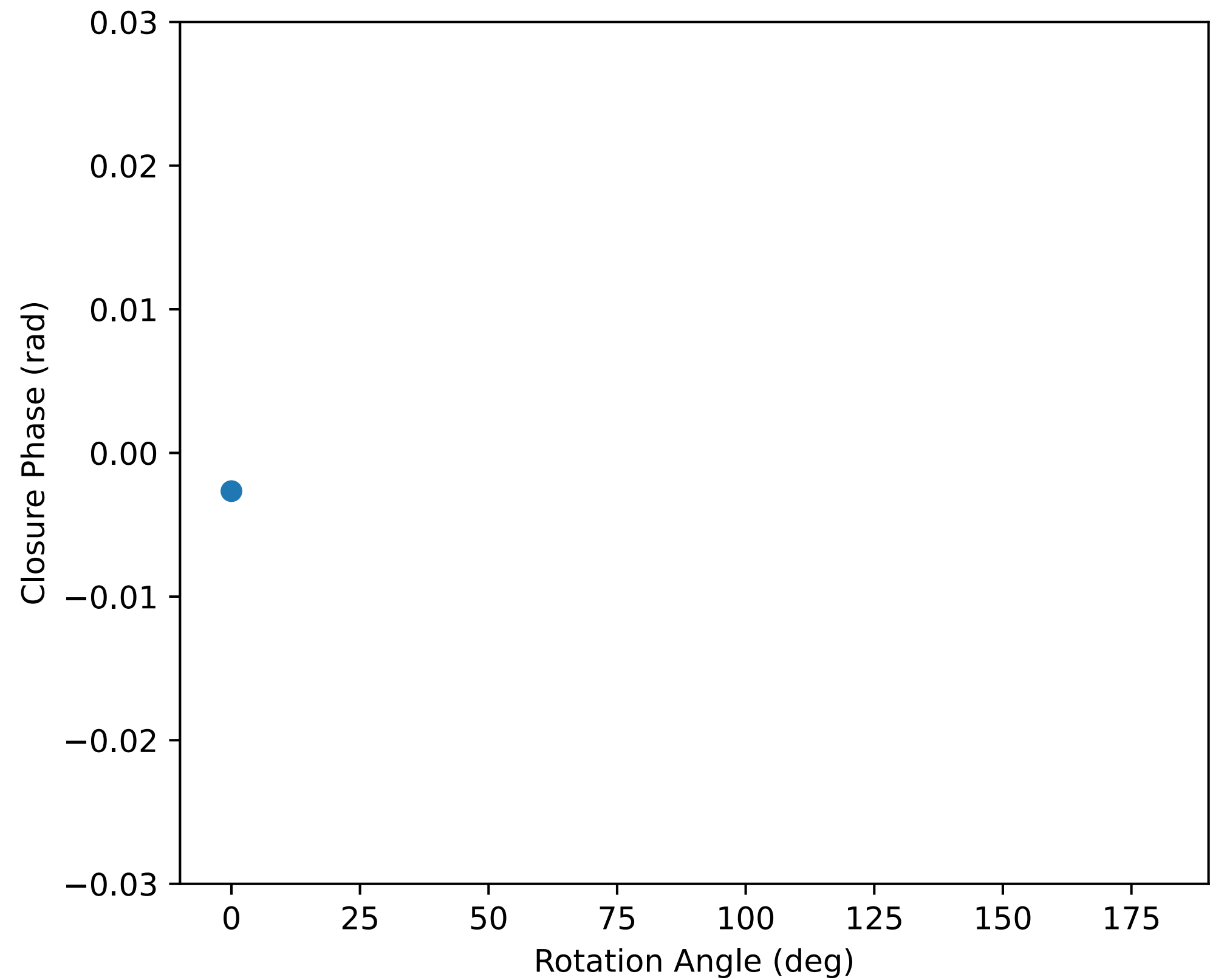
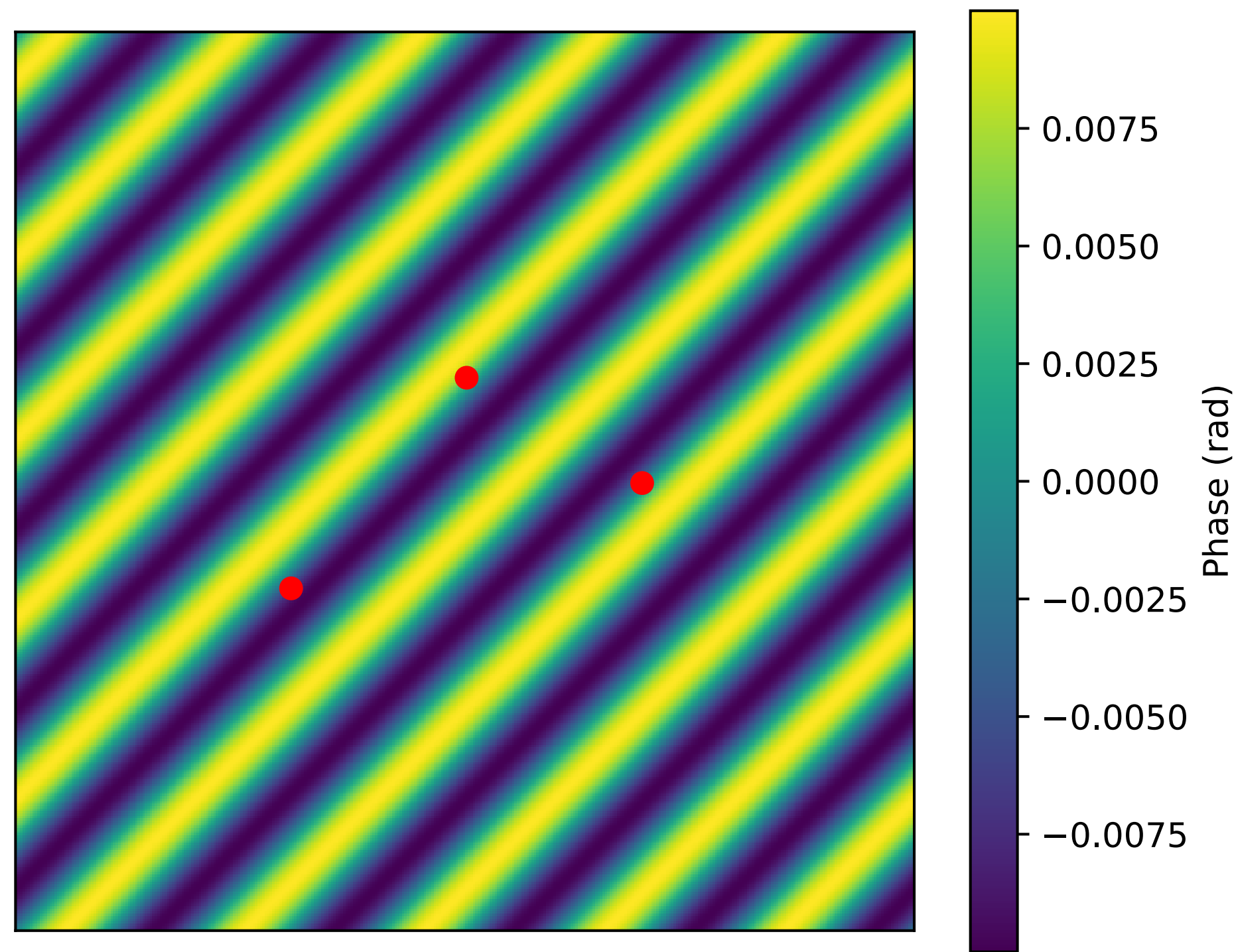
Baselines oriented this way see phase that changes sinusoidally with length.

Baselines oriented this way see phase that doesn't change with length.

The phase signal seen by a particular baseline depends on its orientation and its length!

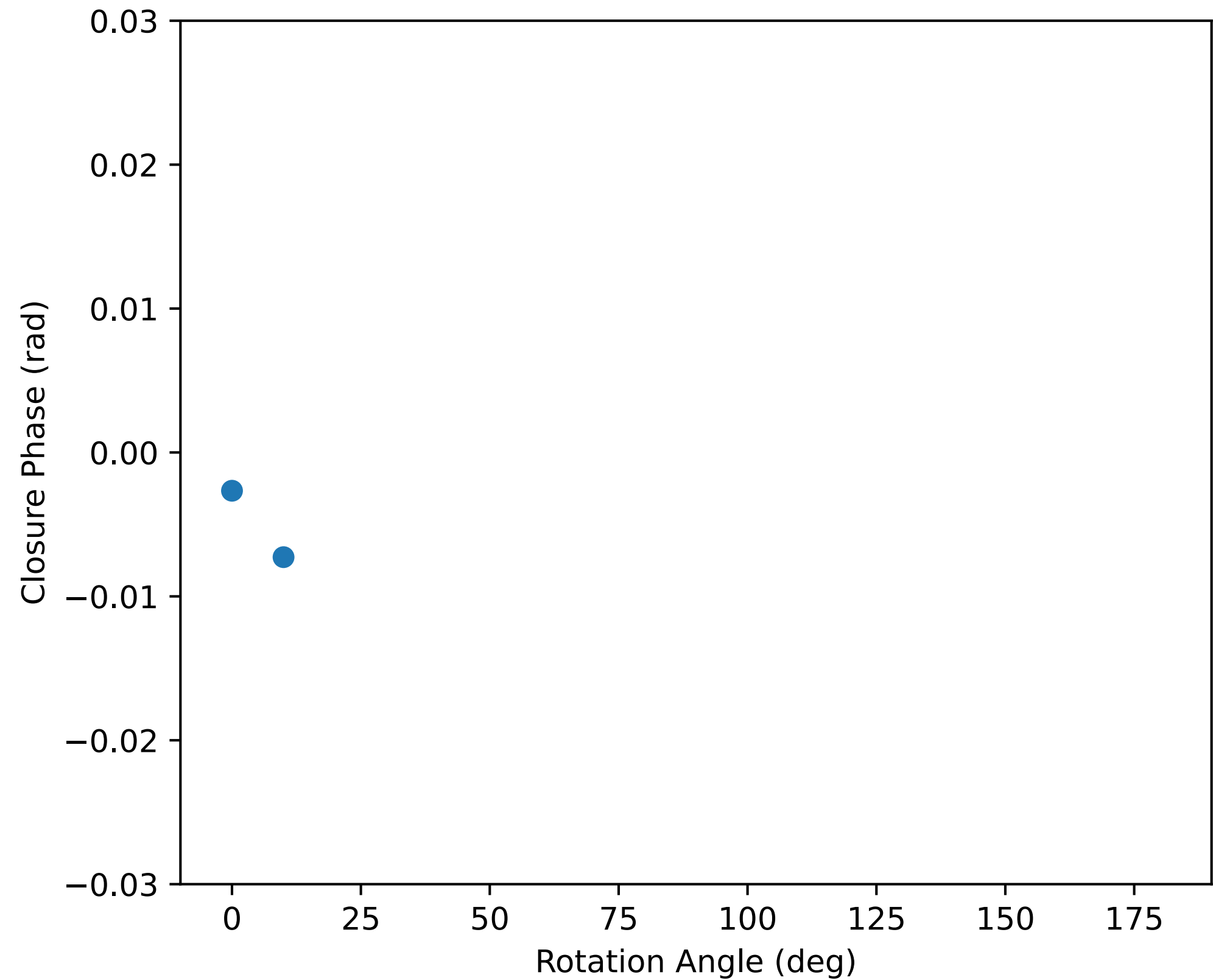
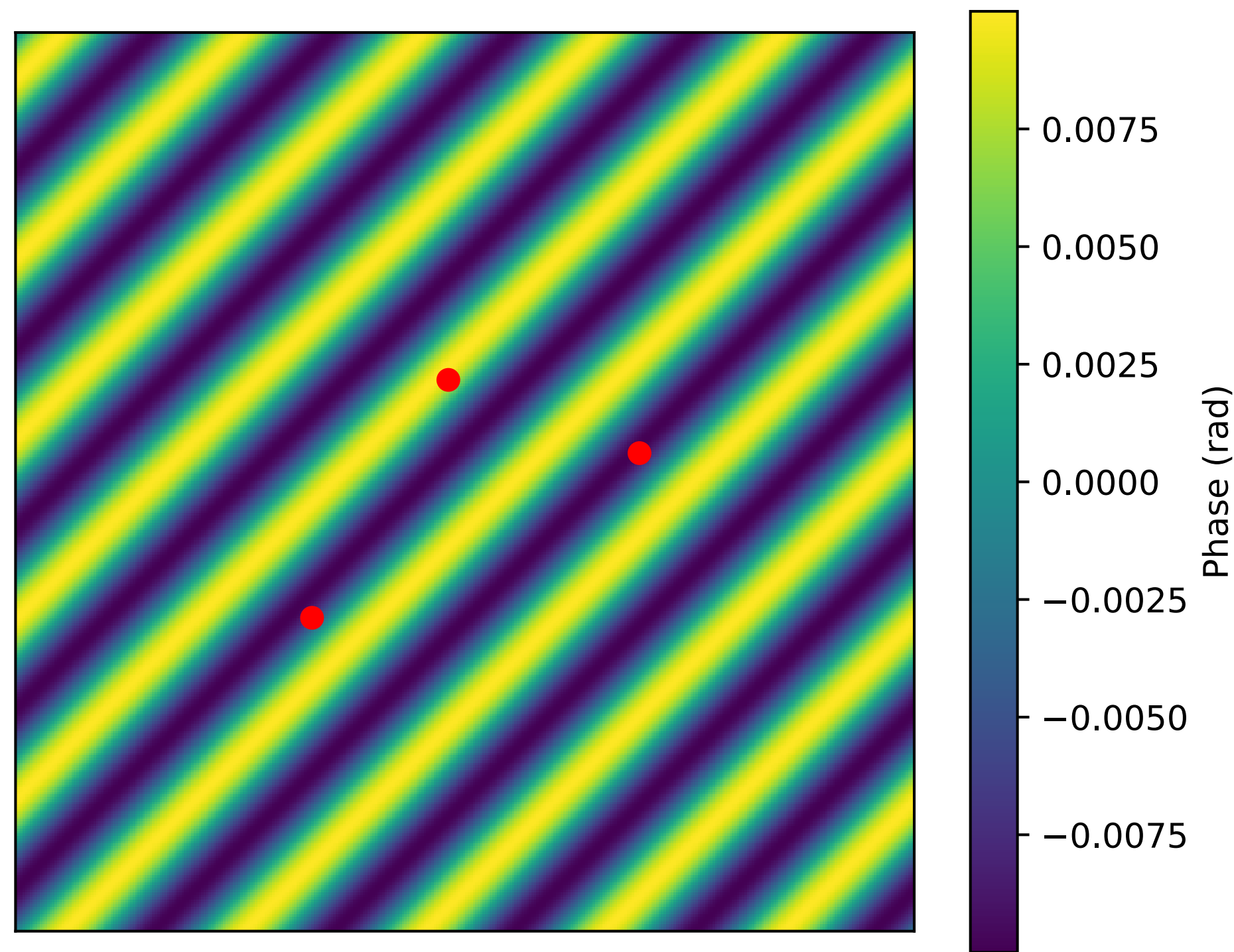
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



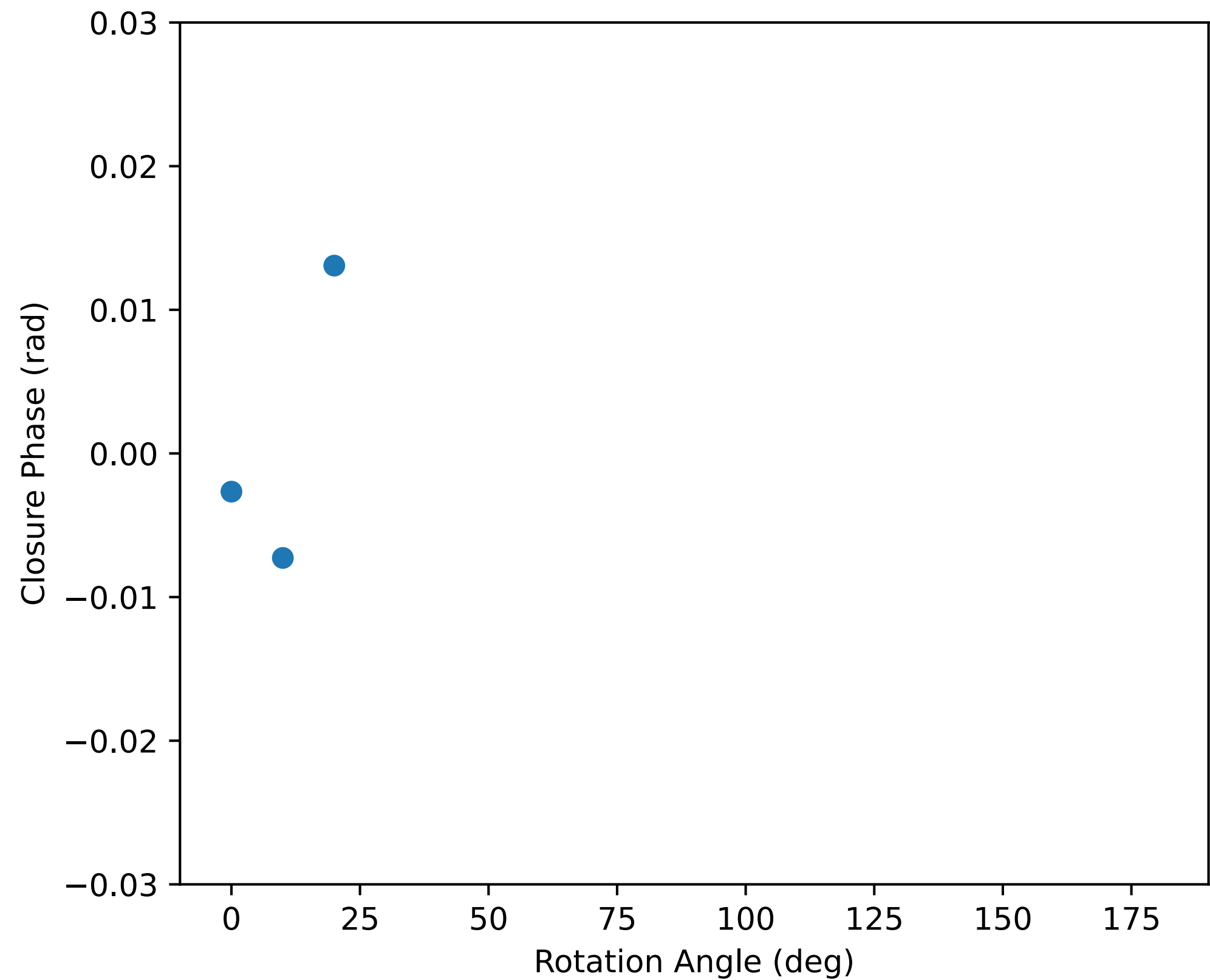
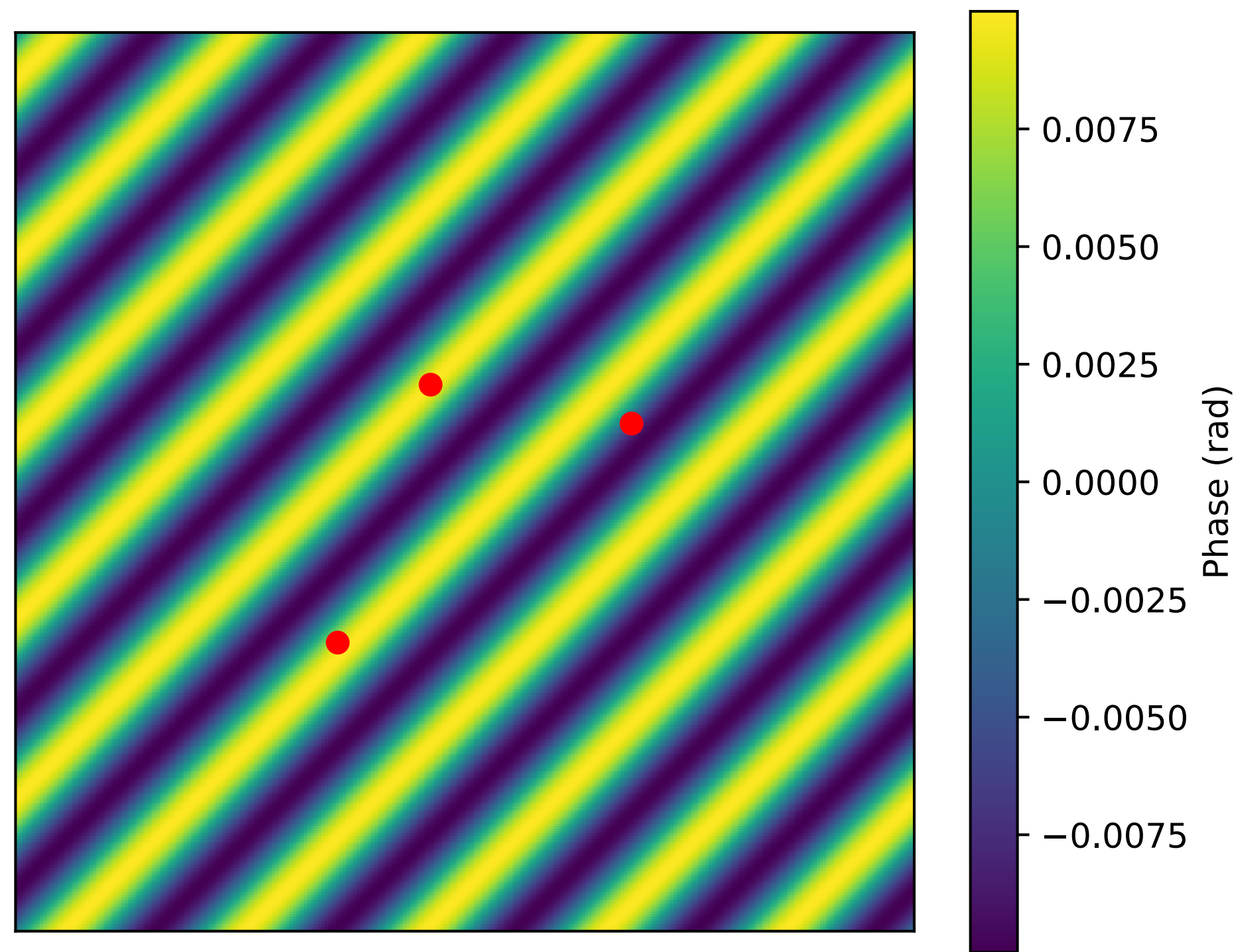
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



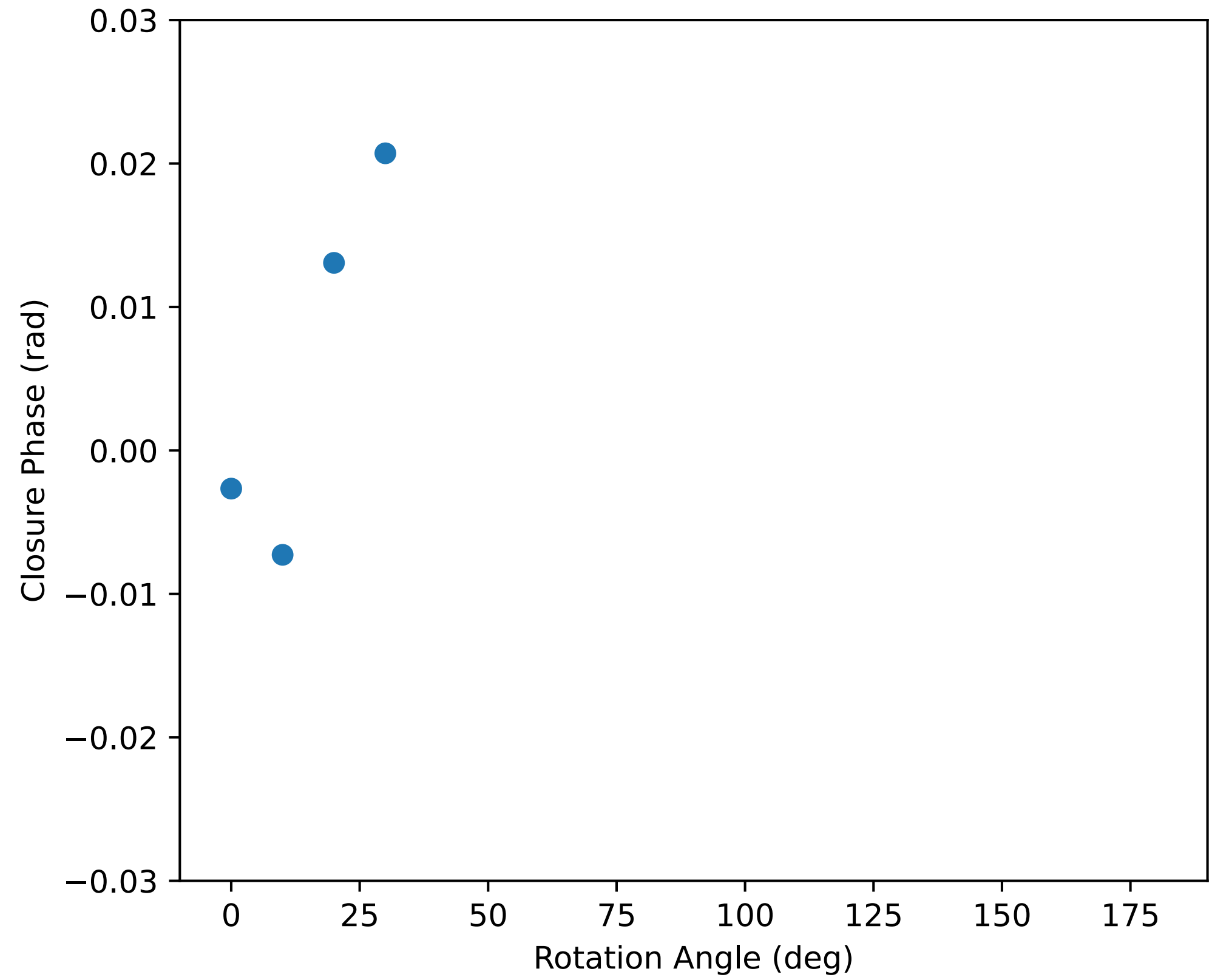
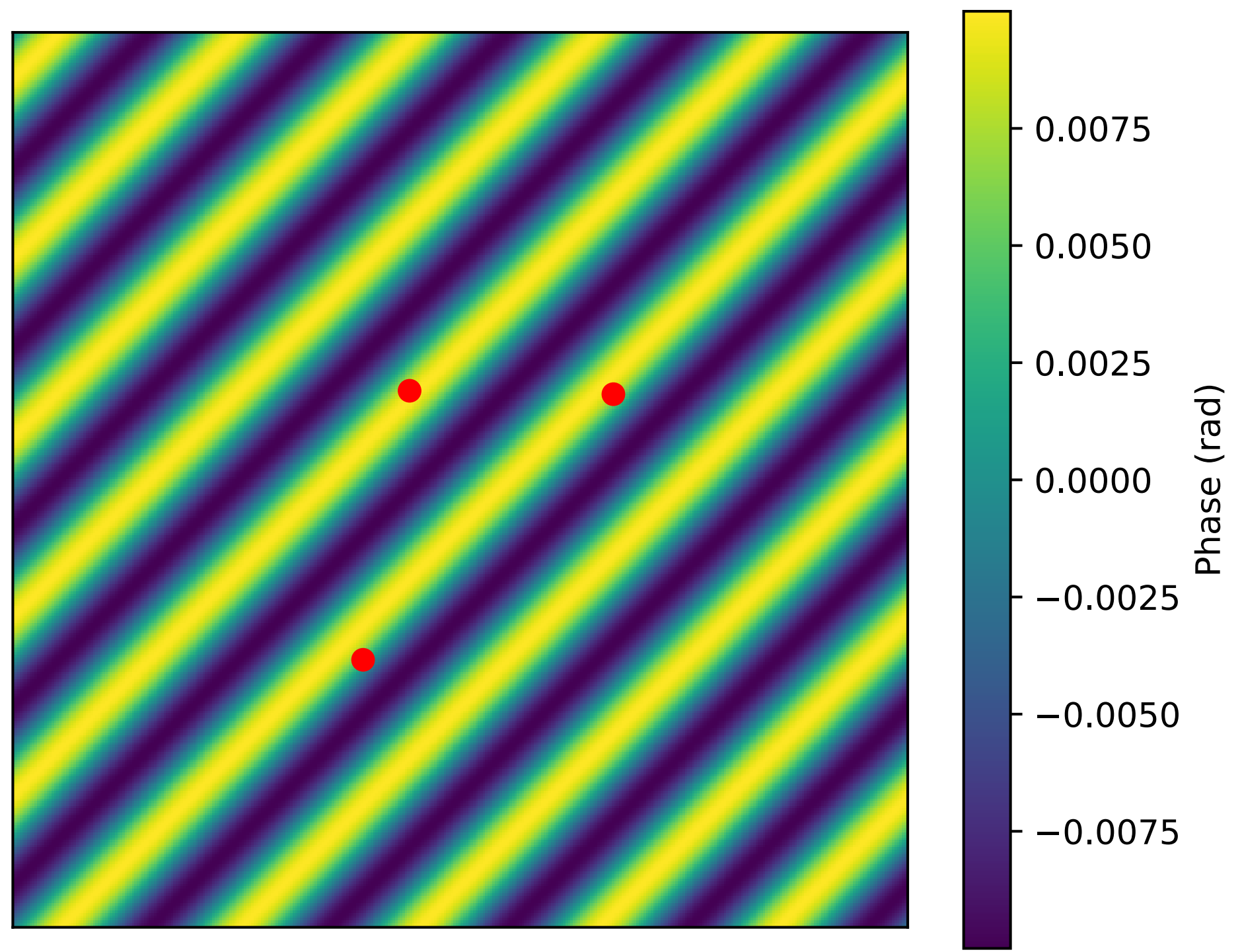
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



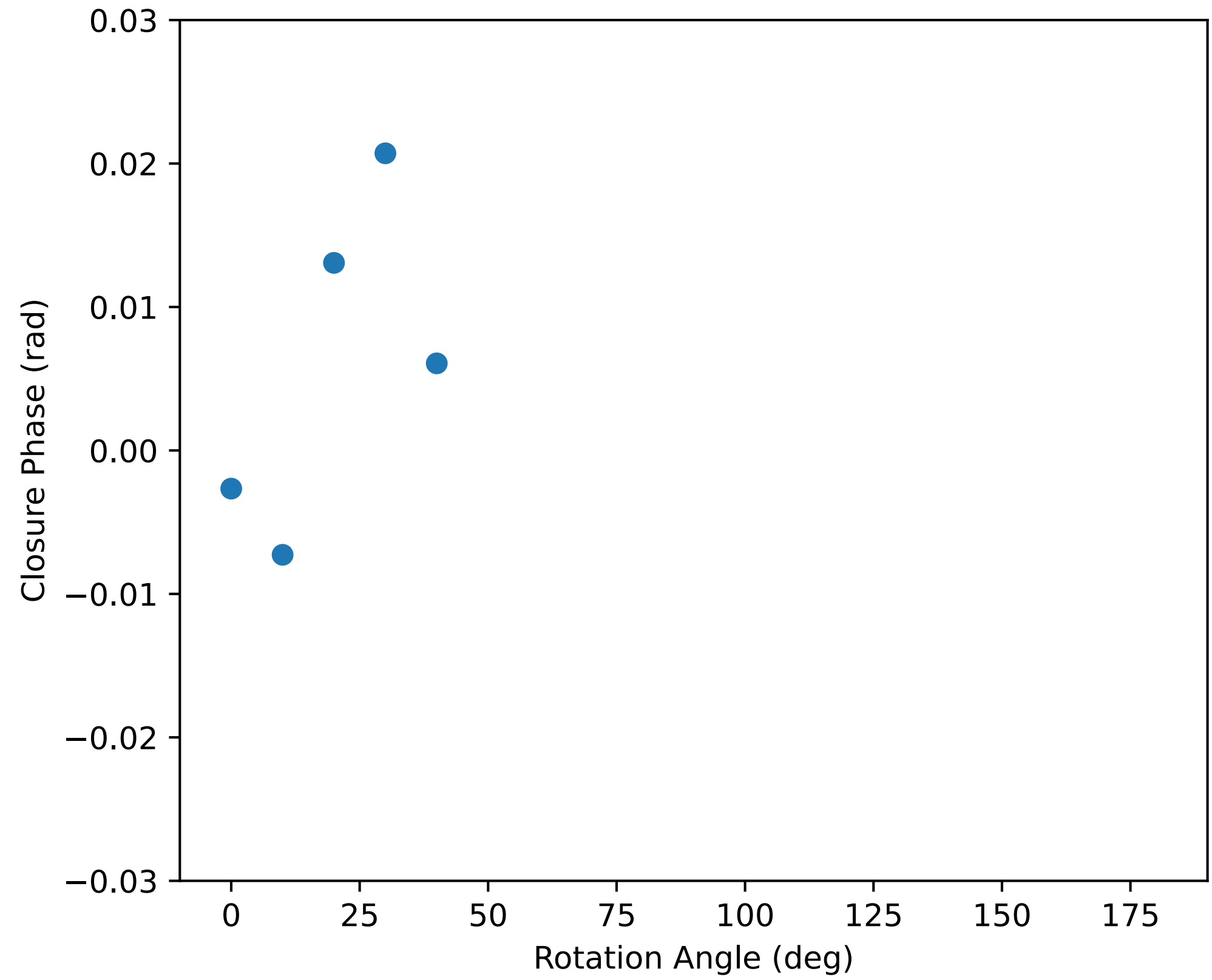
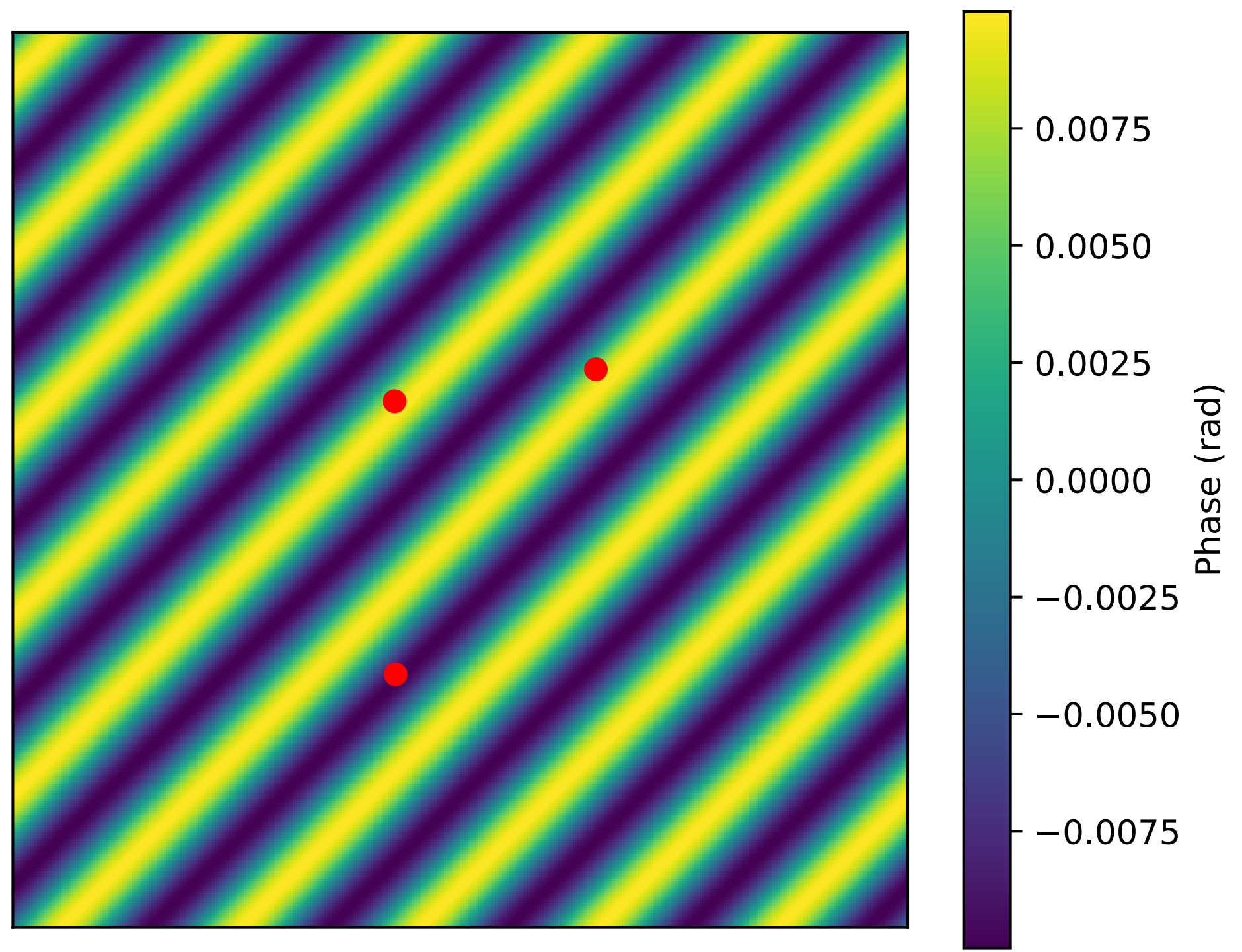
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



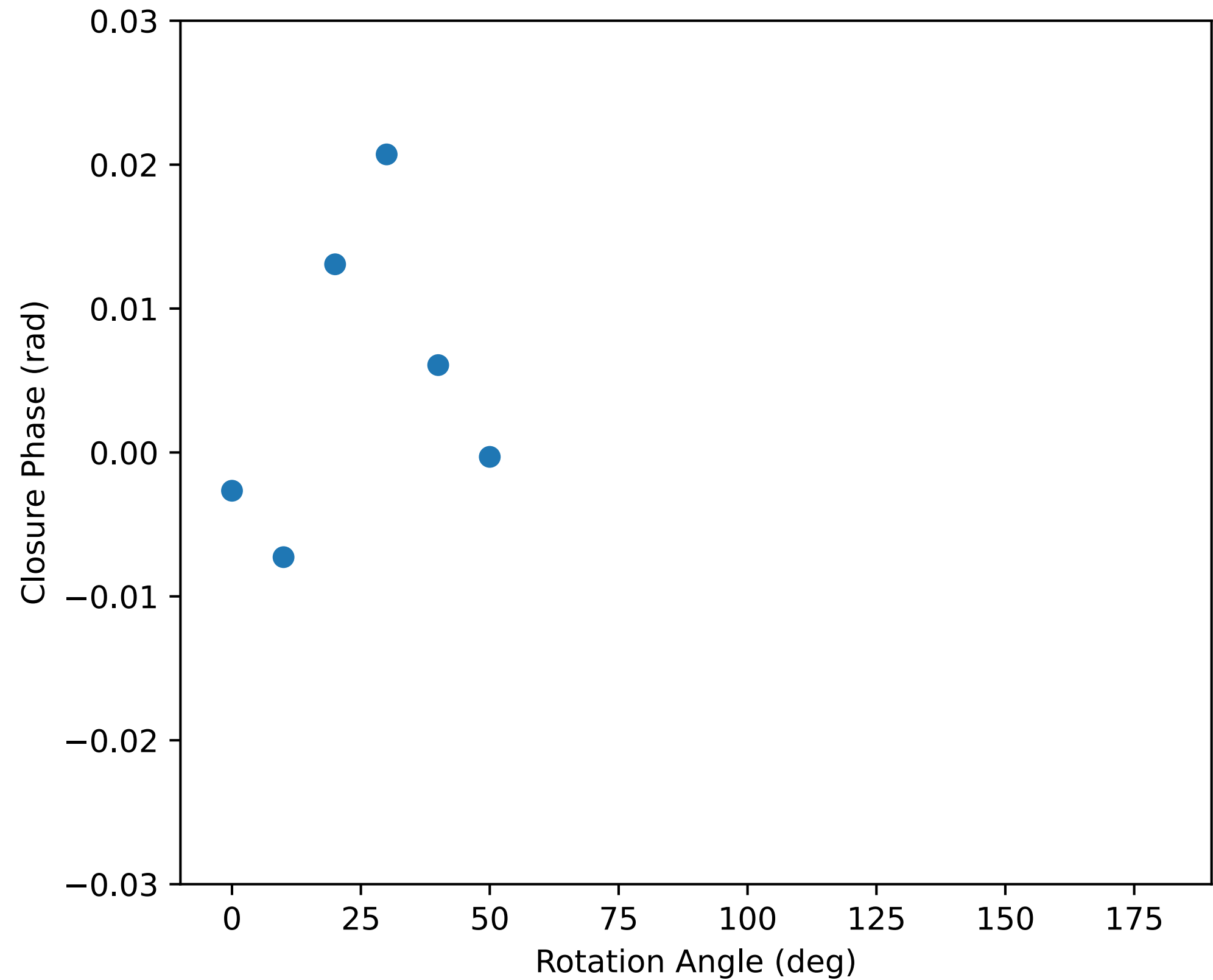
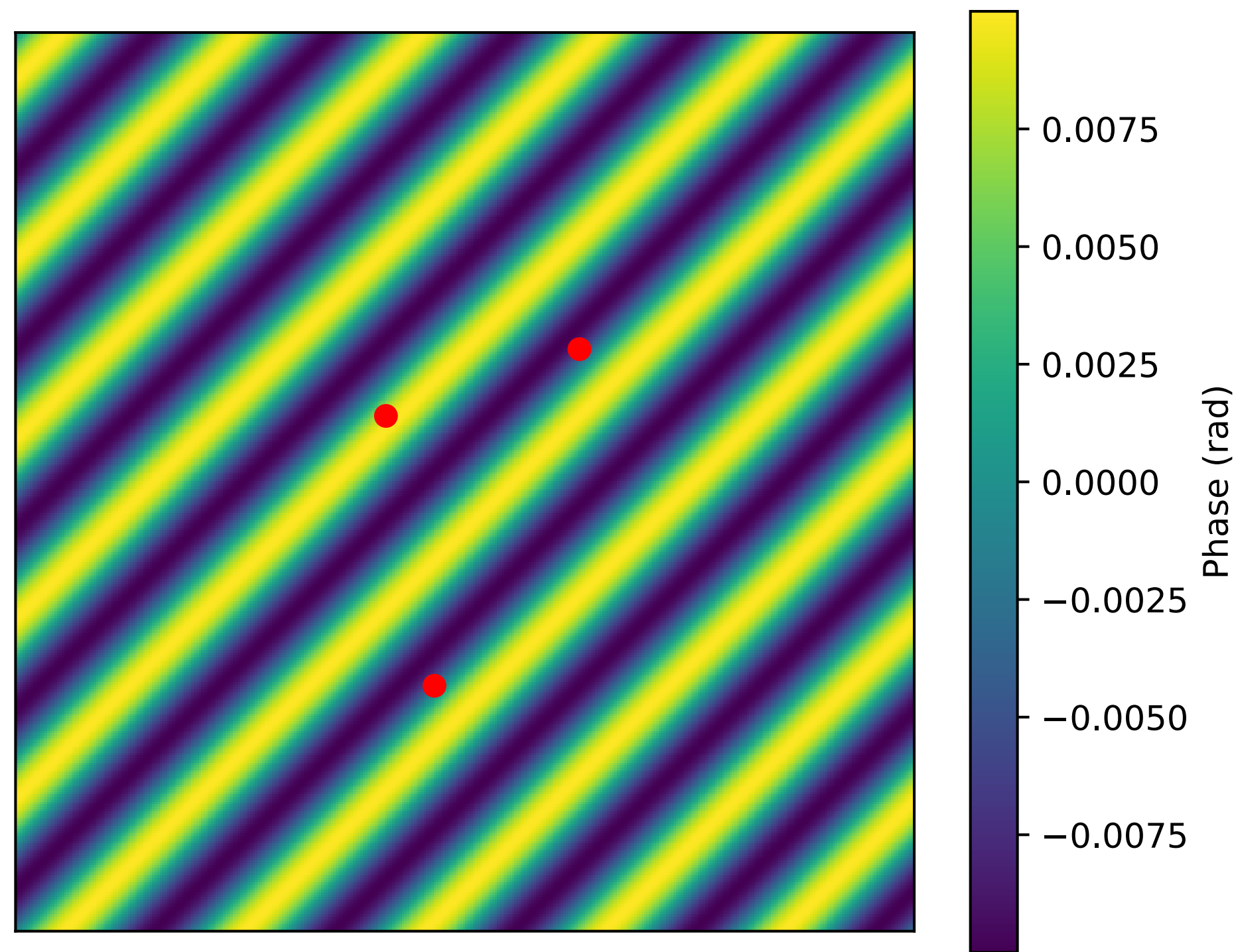
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



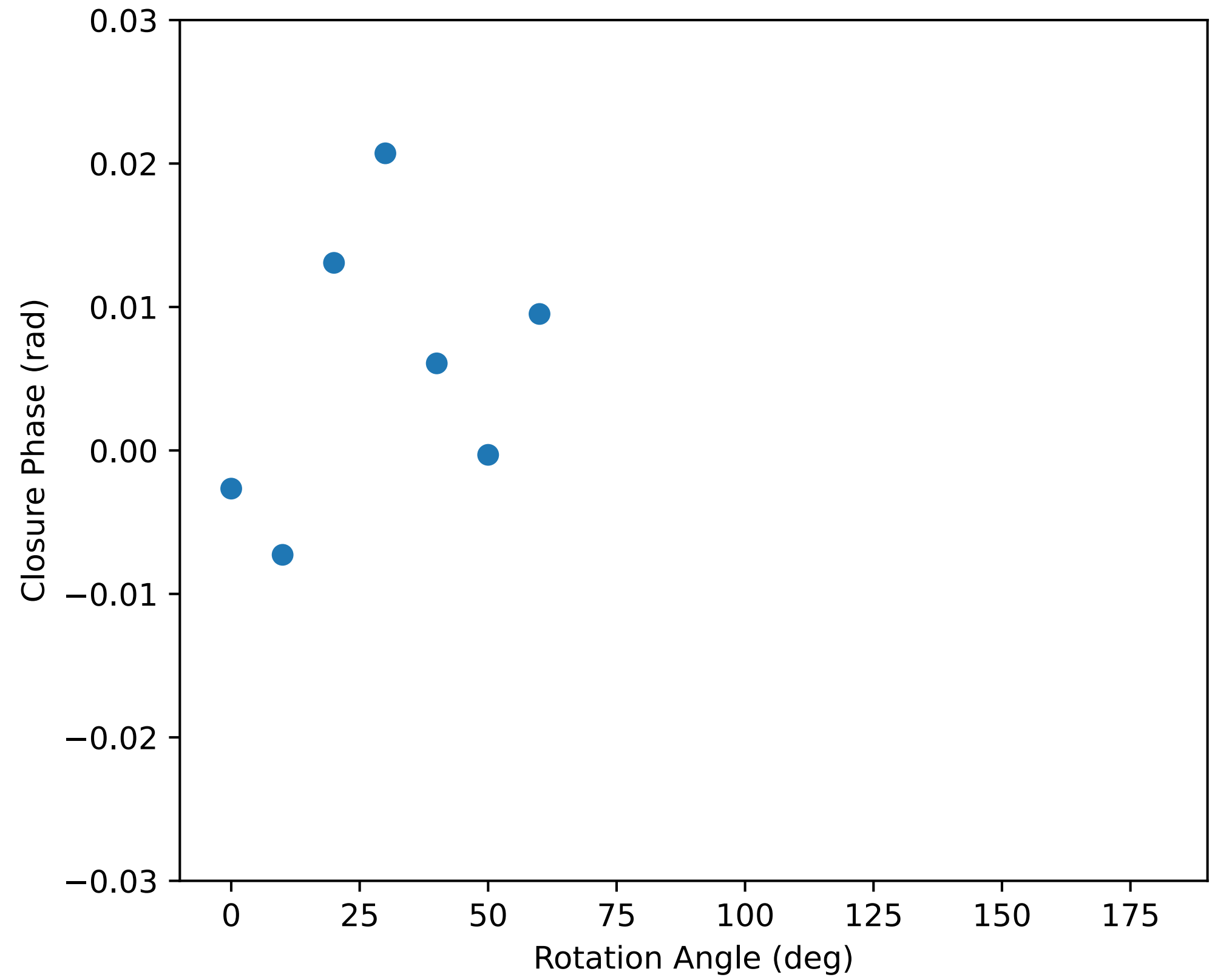
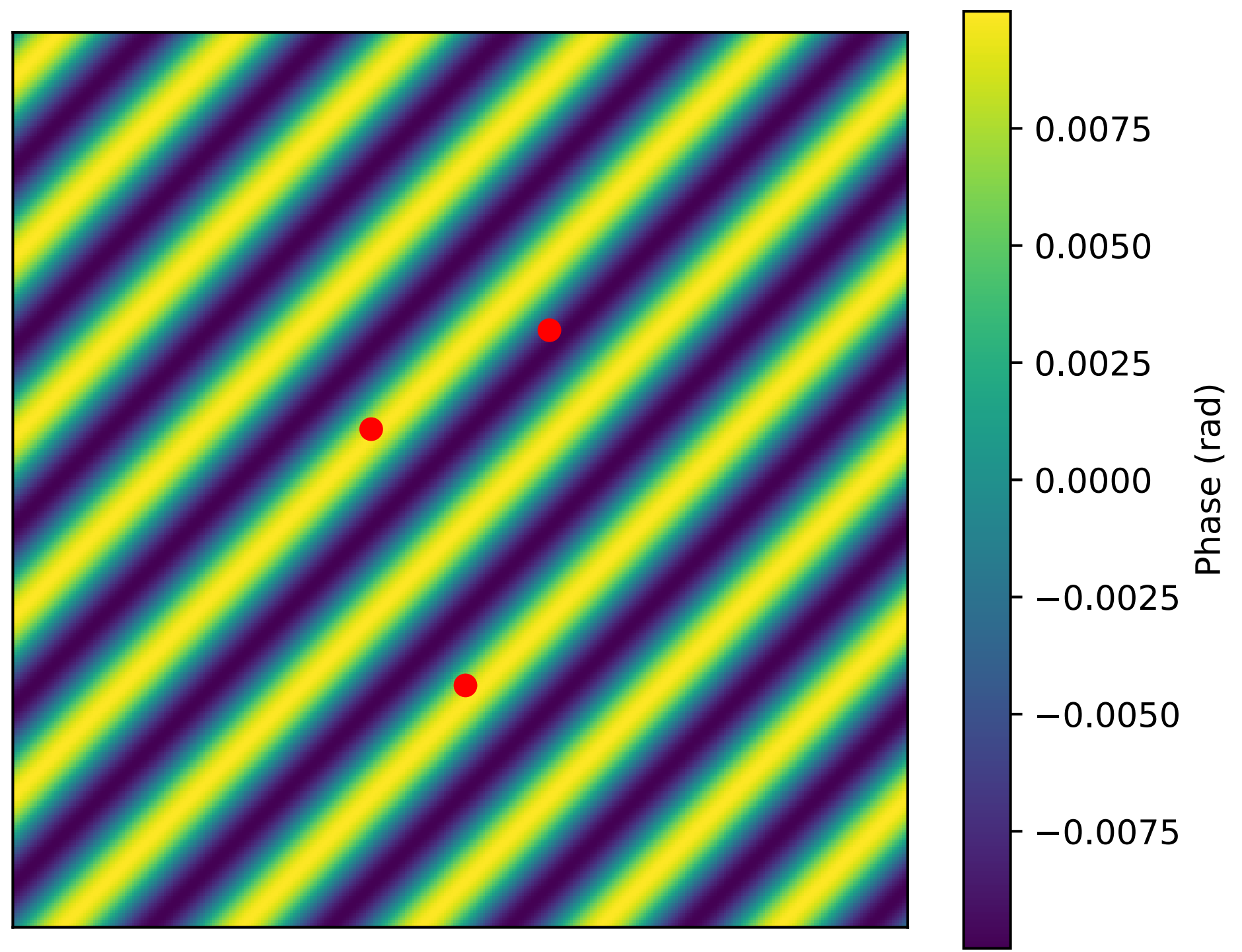
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



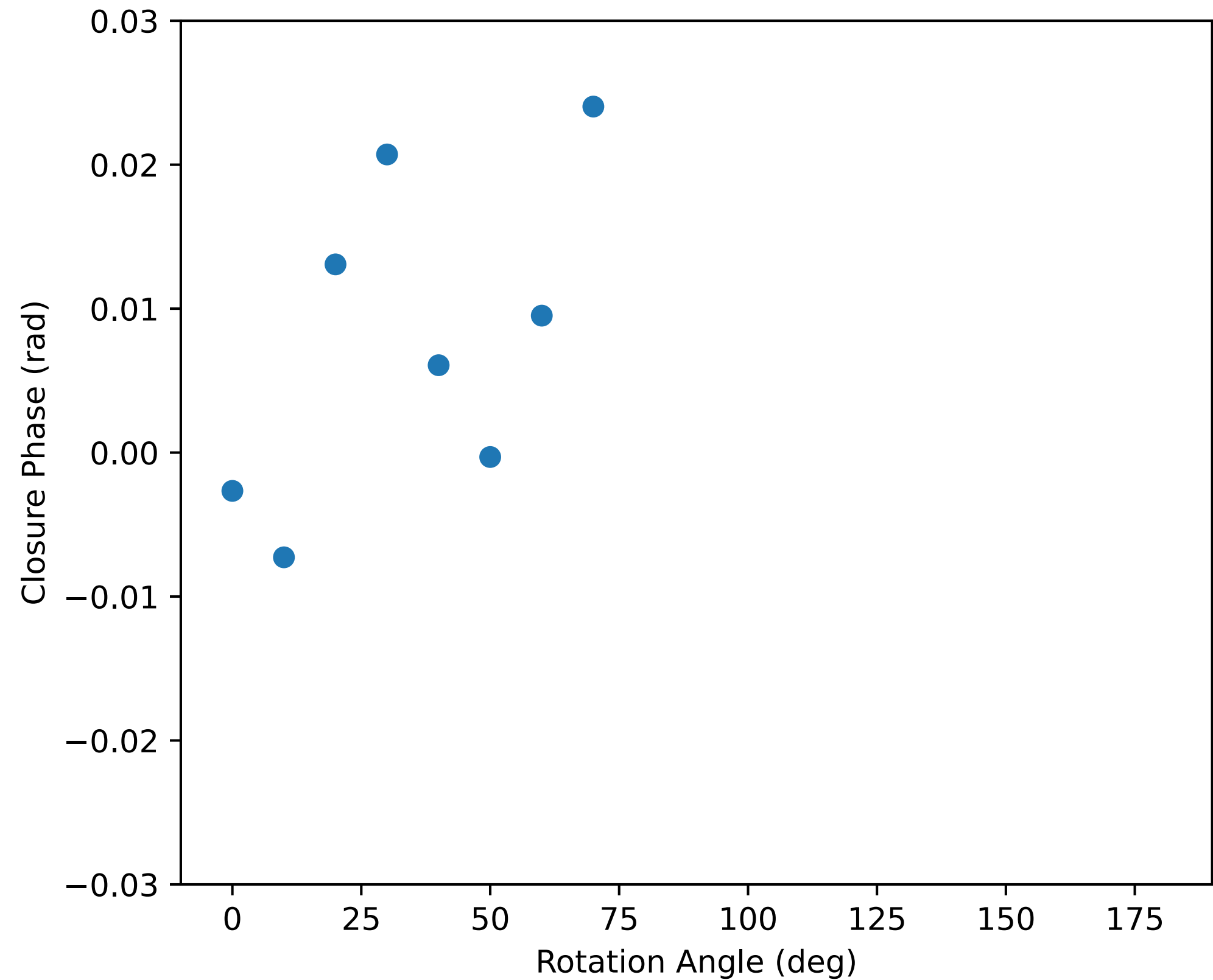
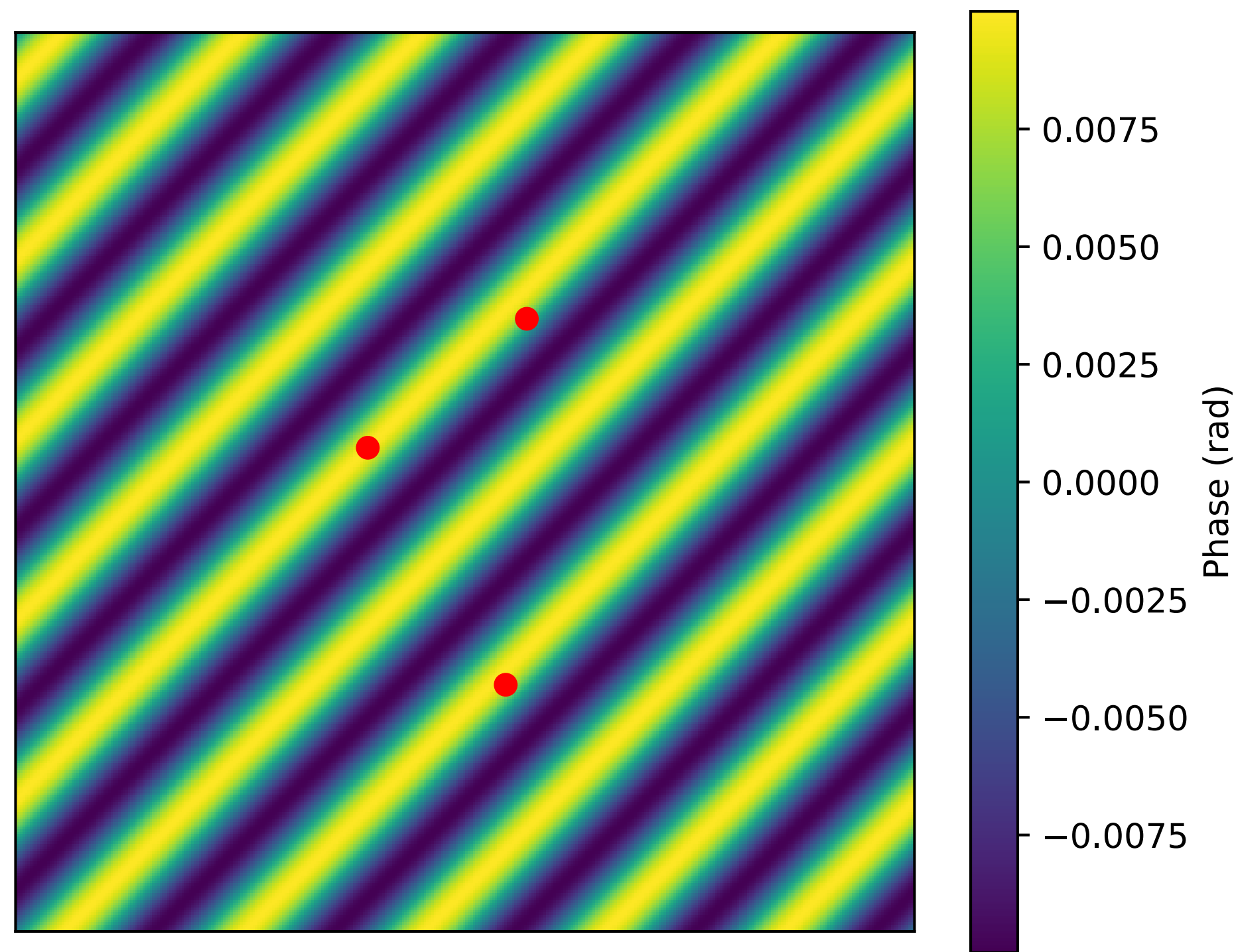
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



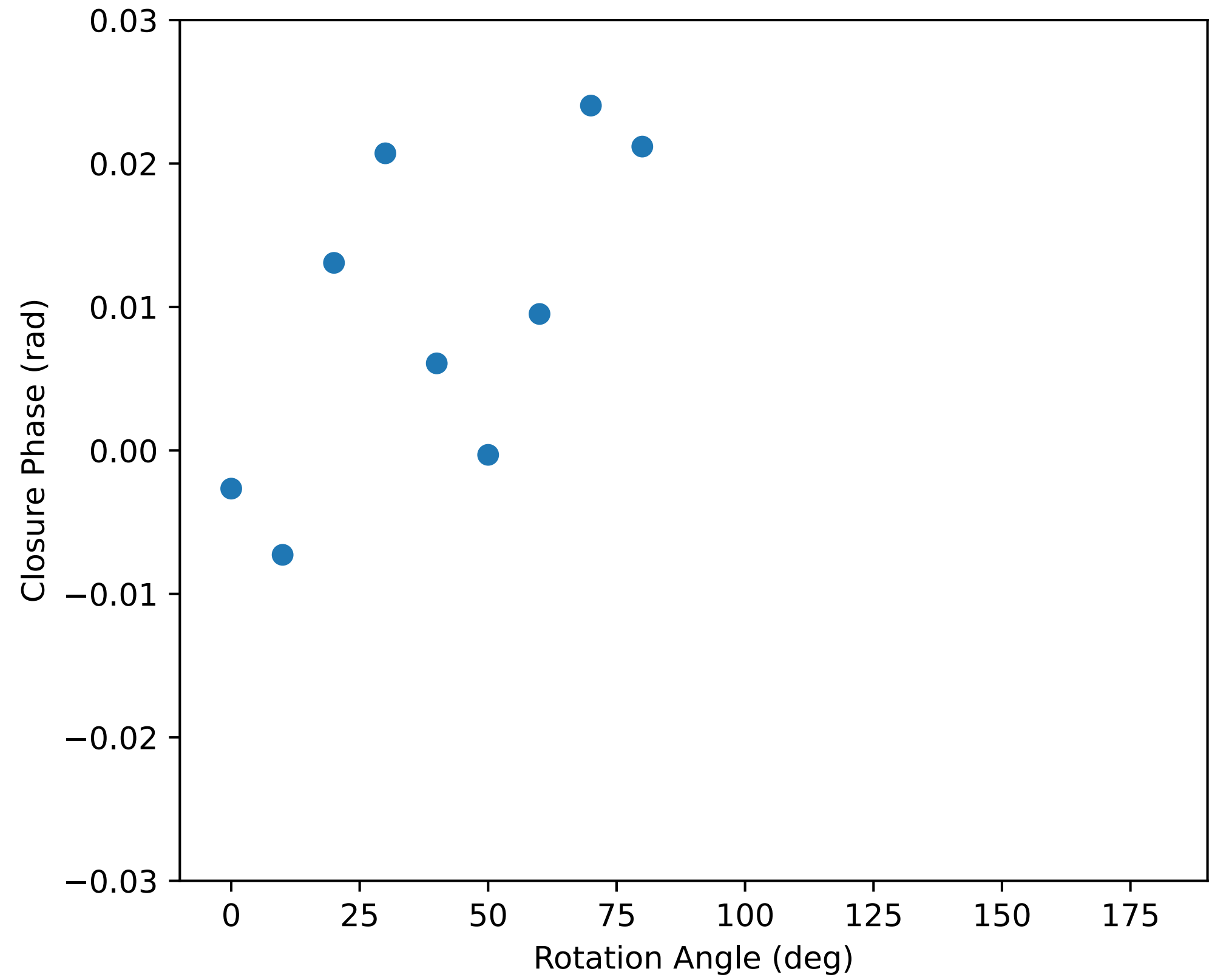
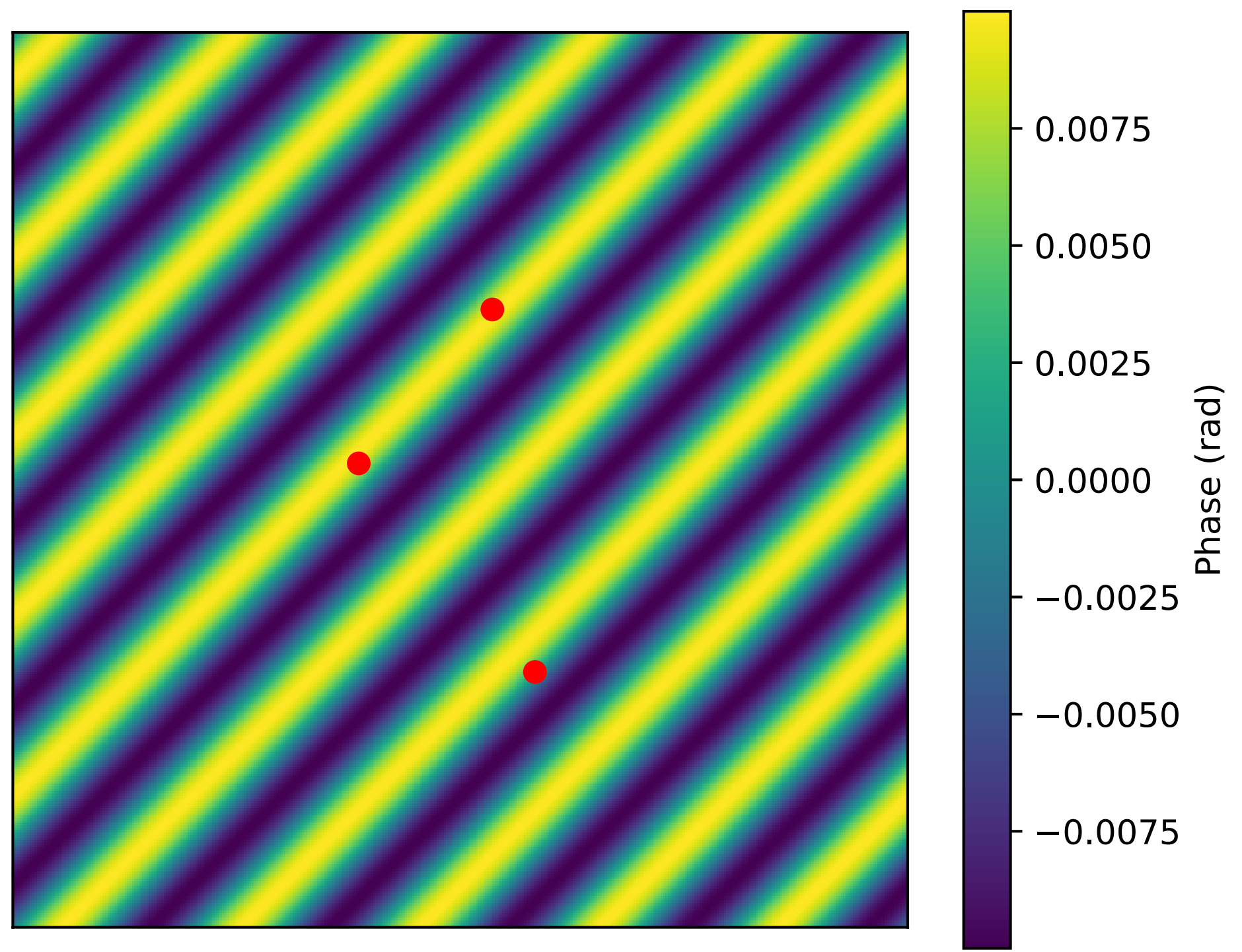
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



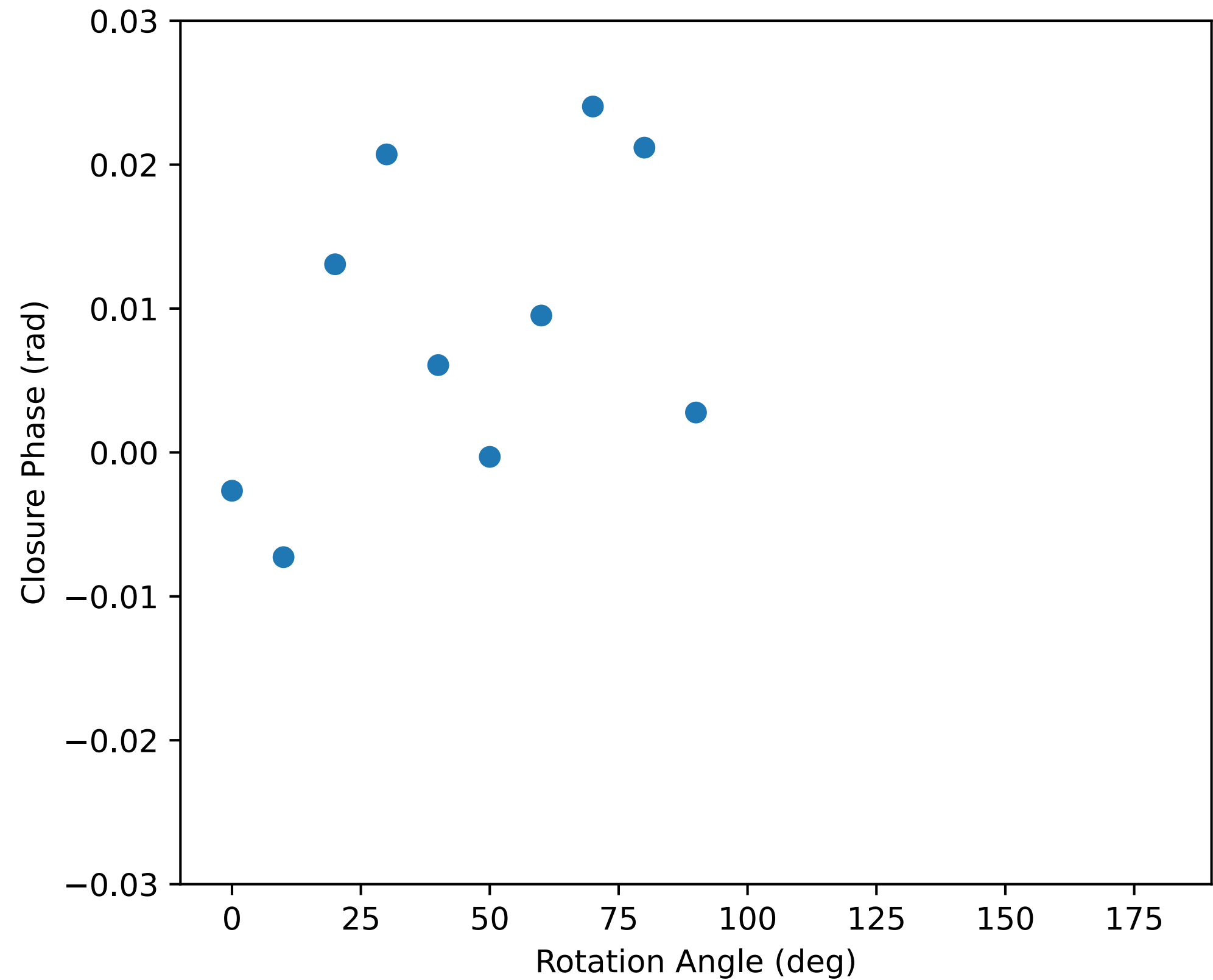
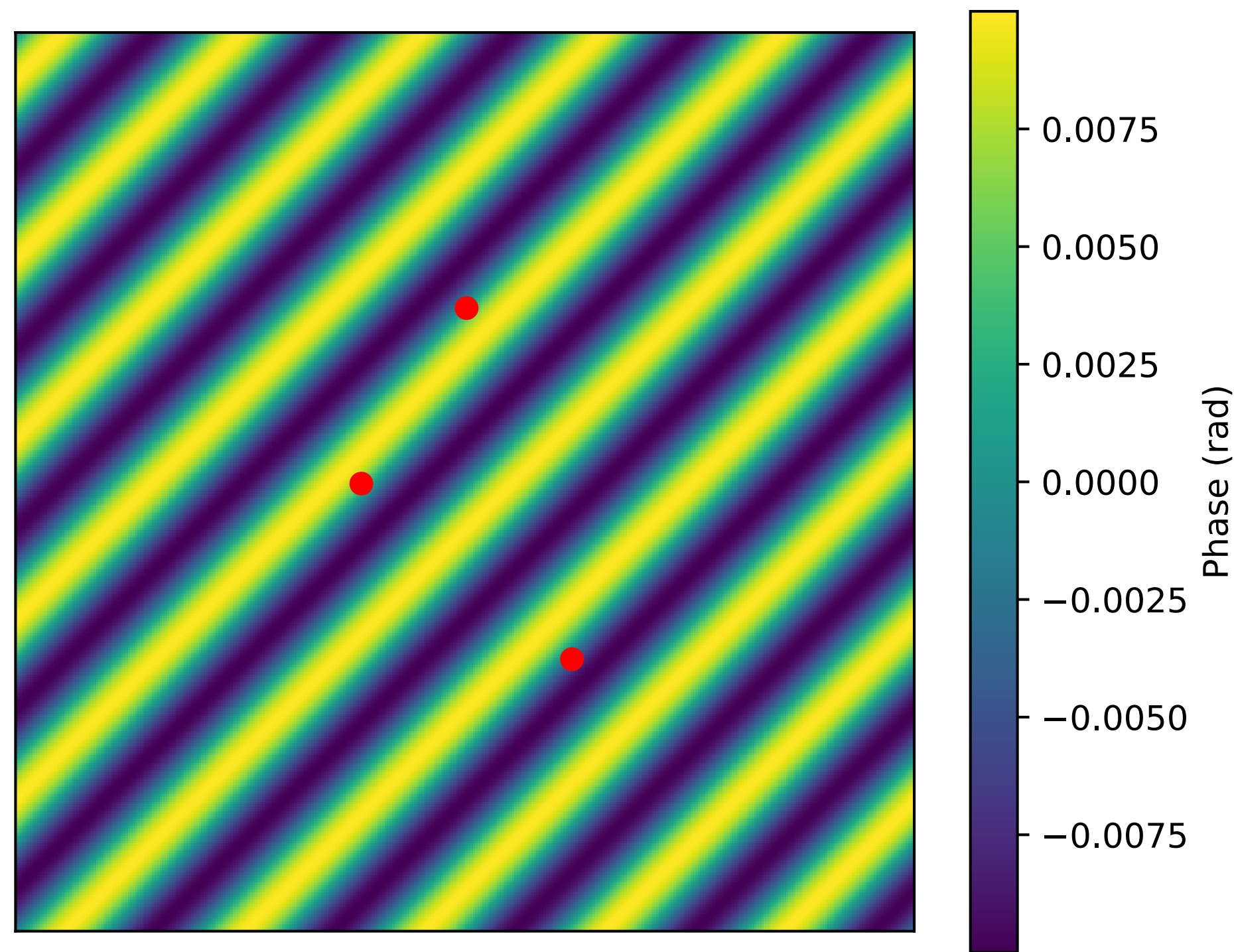
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



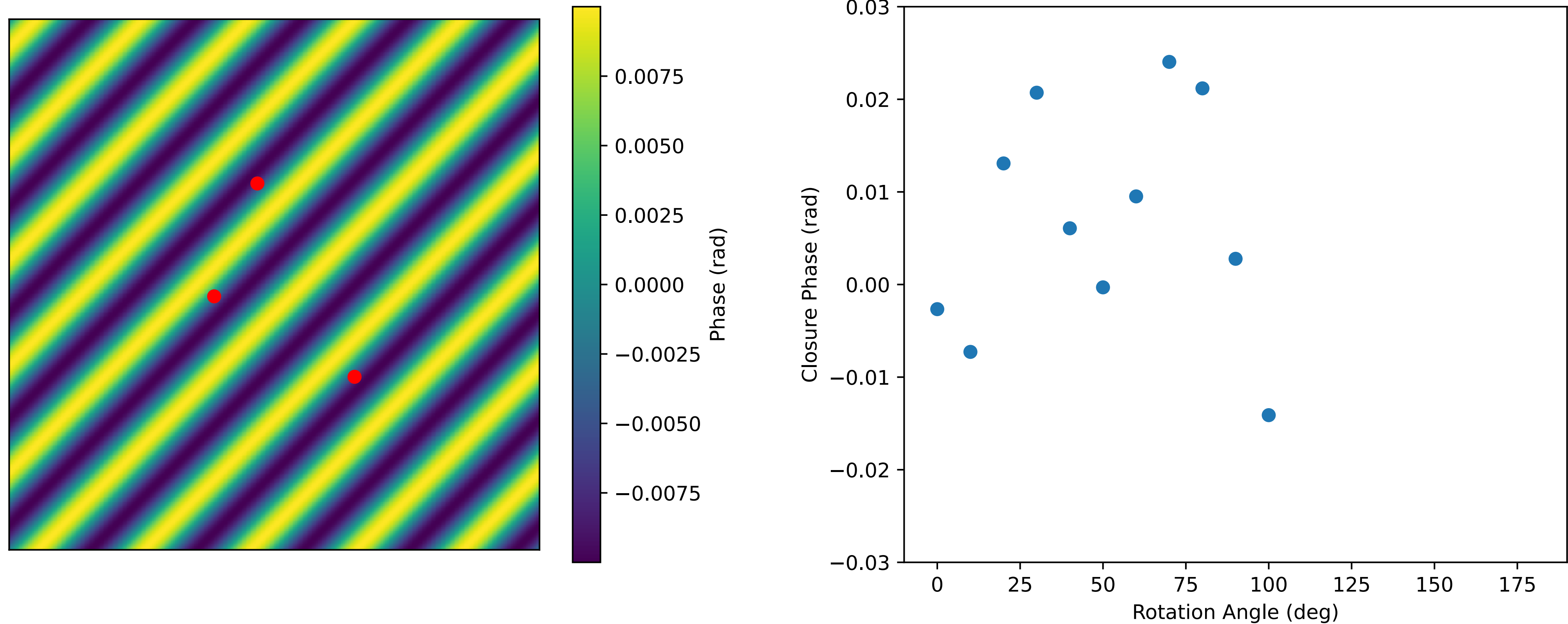
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



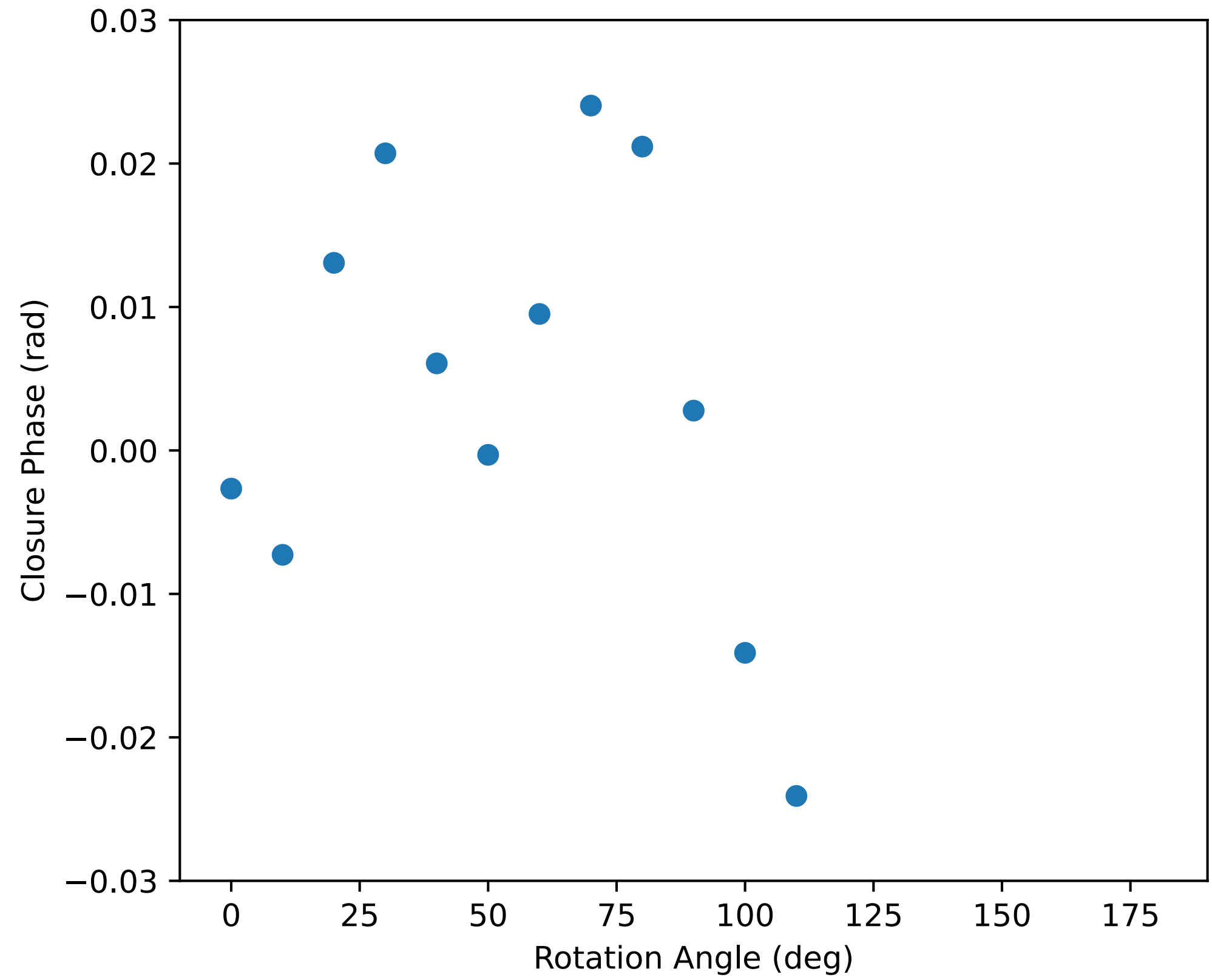
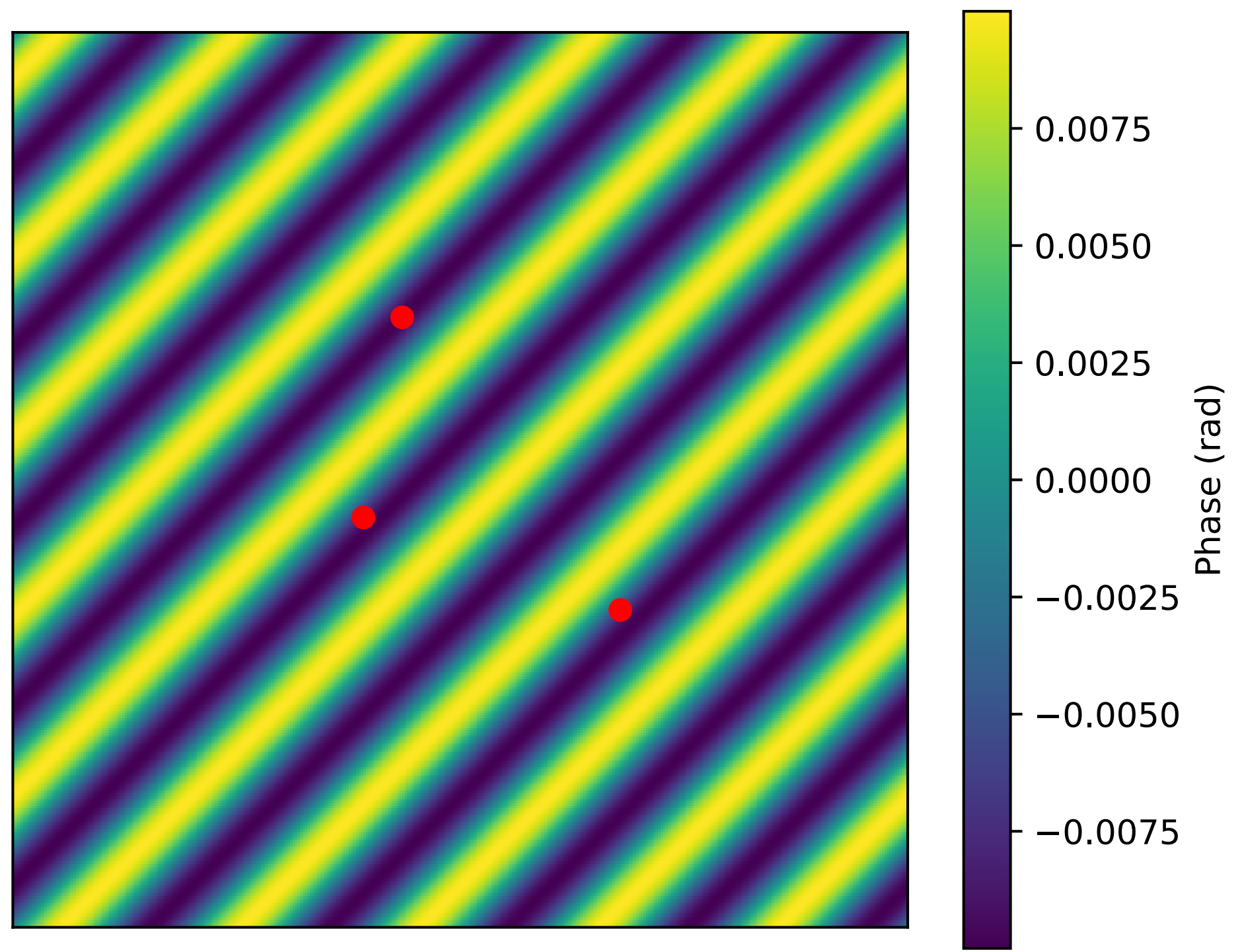
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



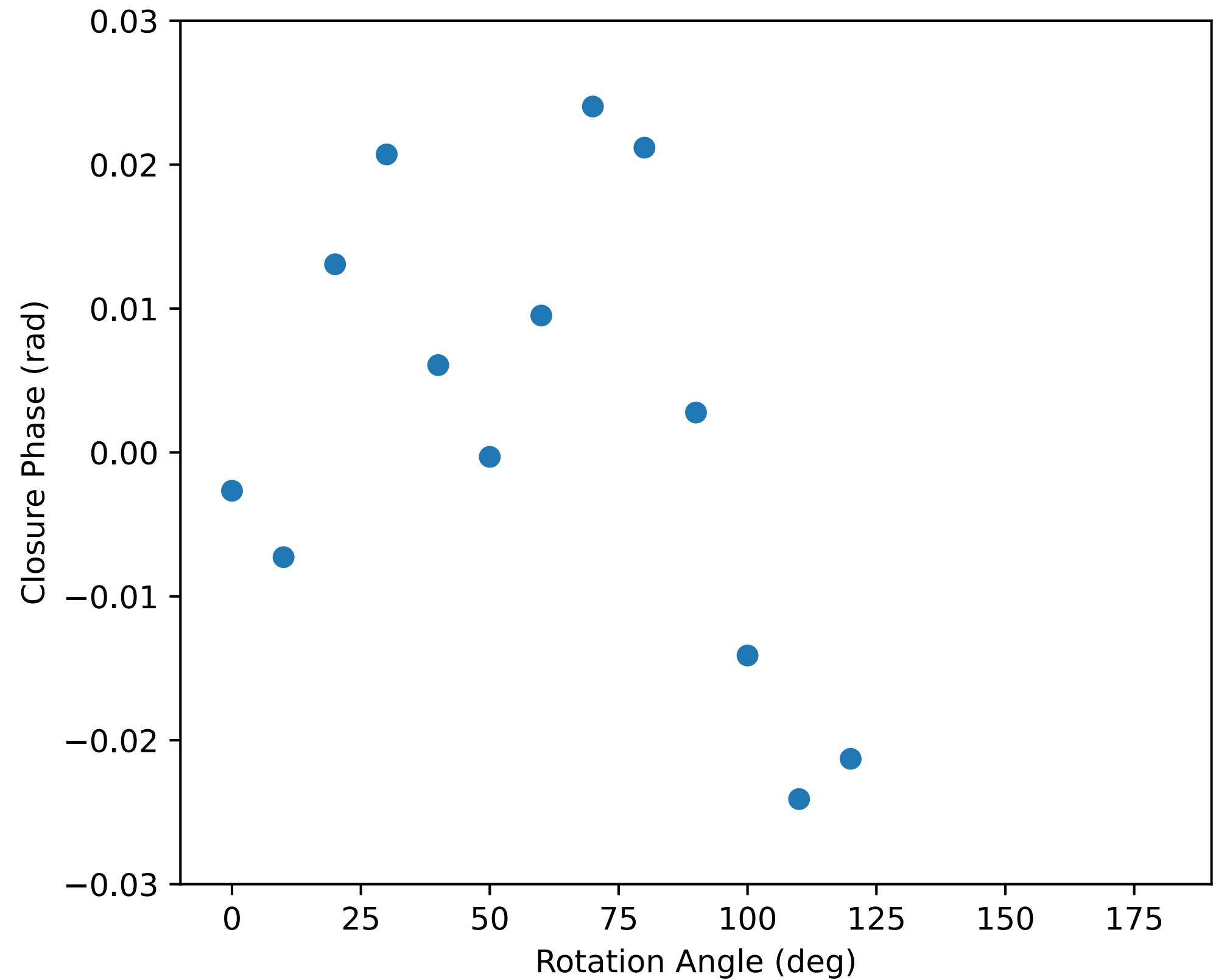
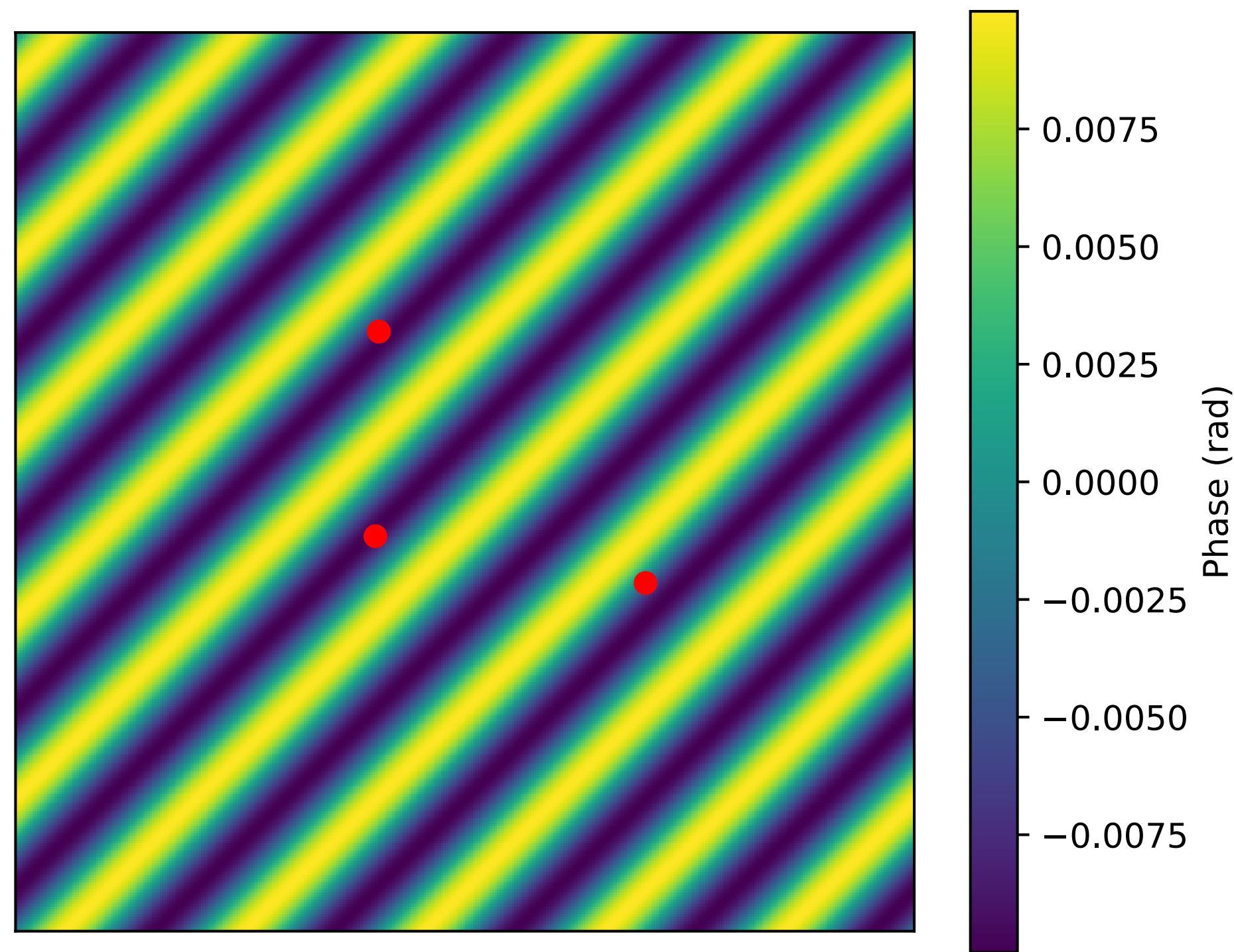
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



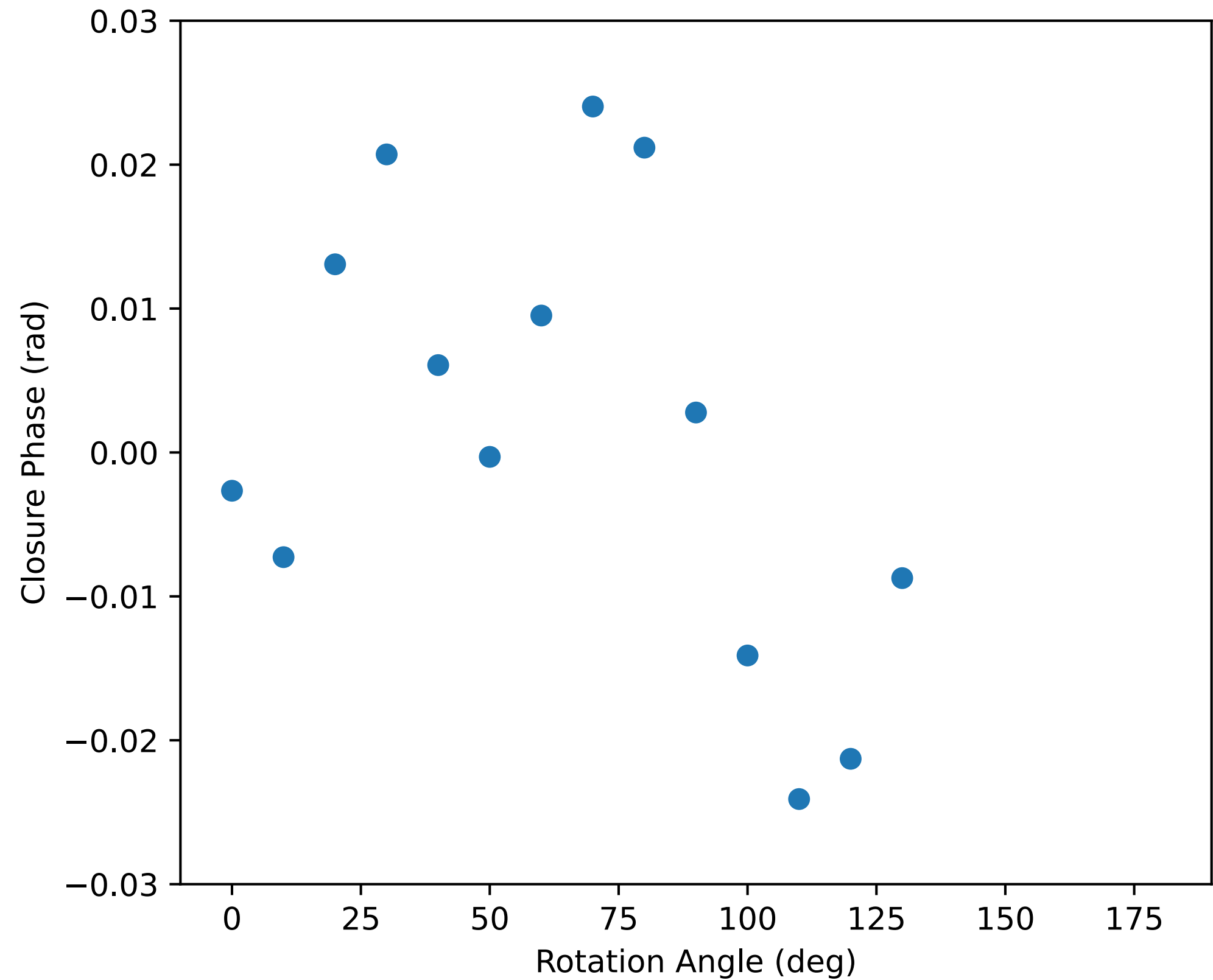
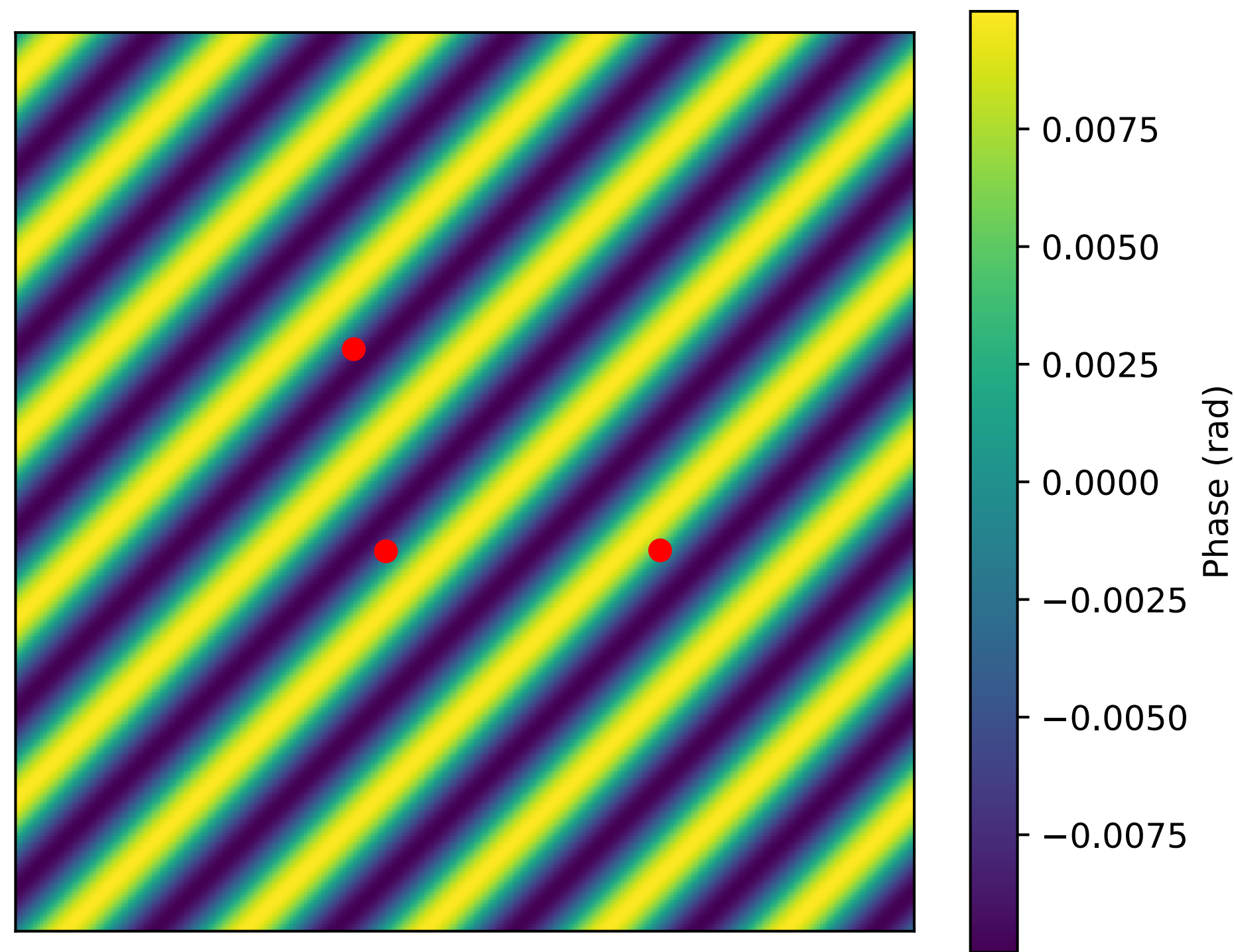
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



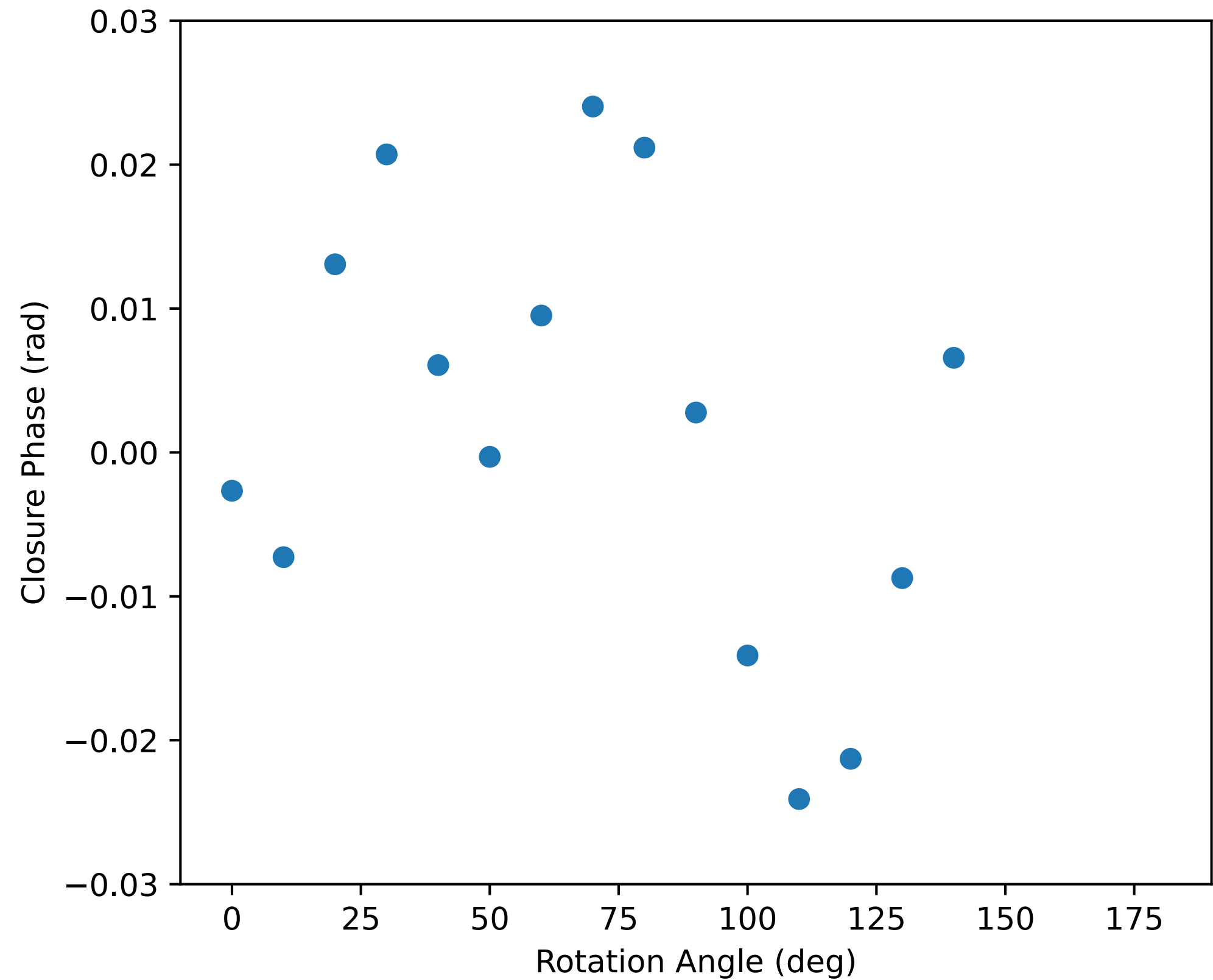
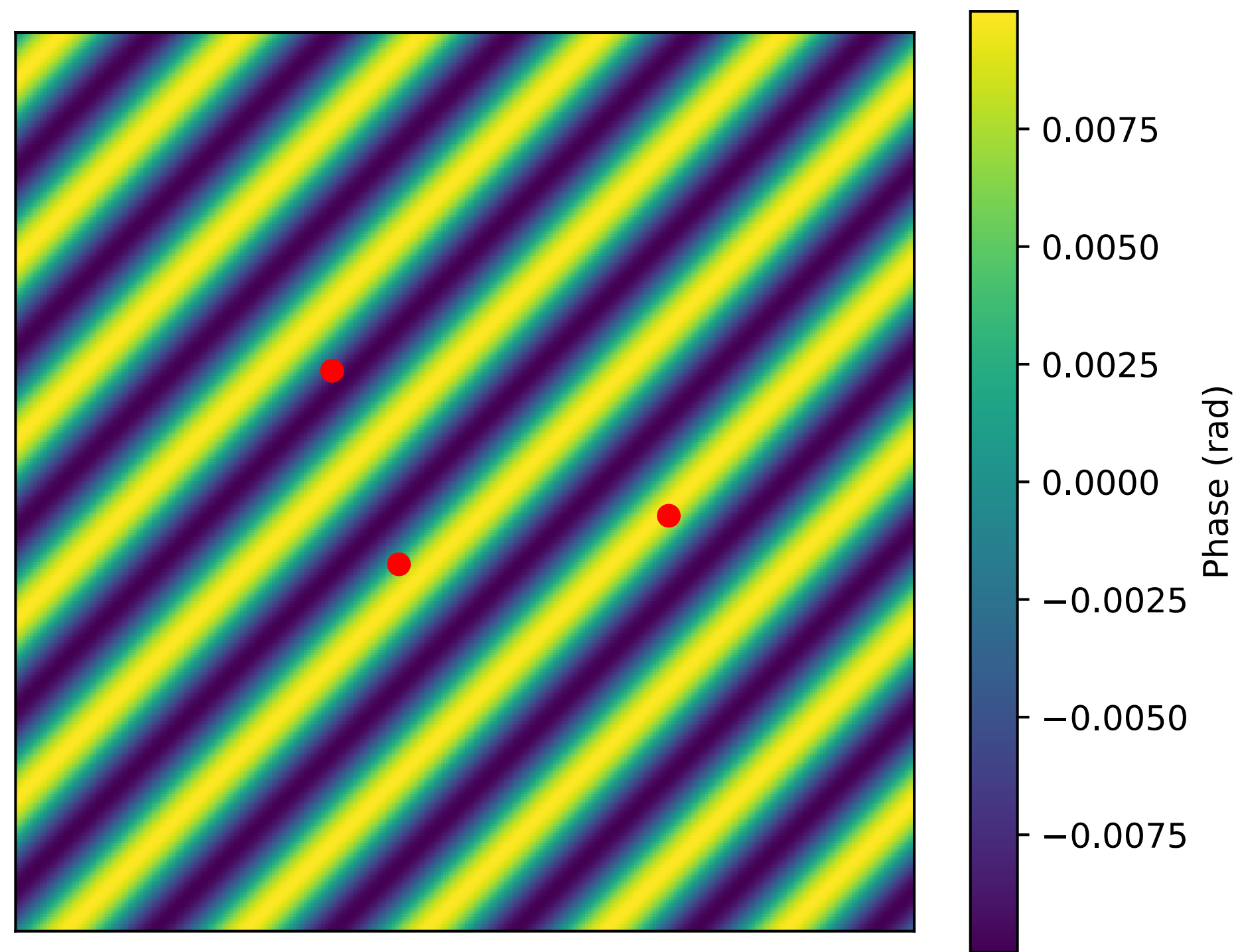
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



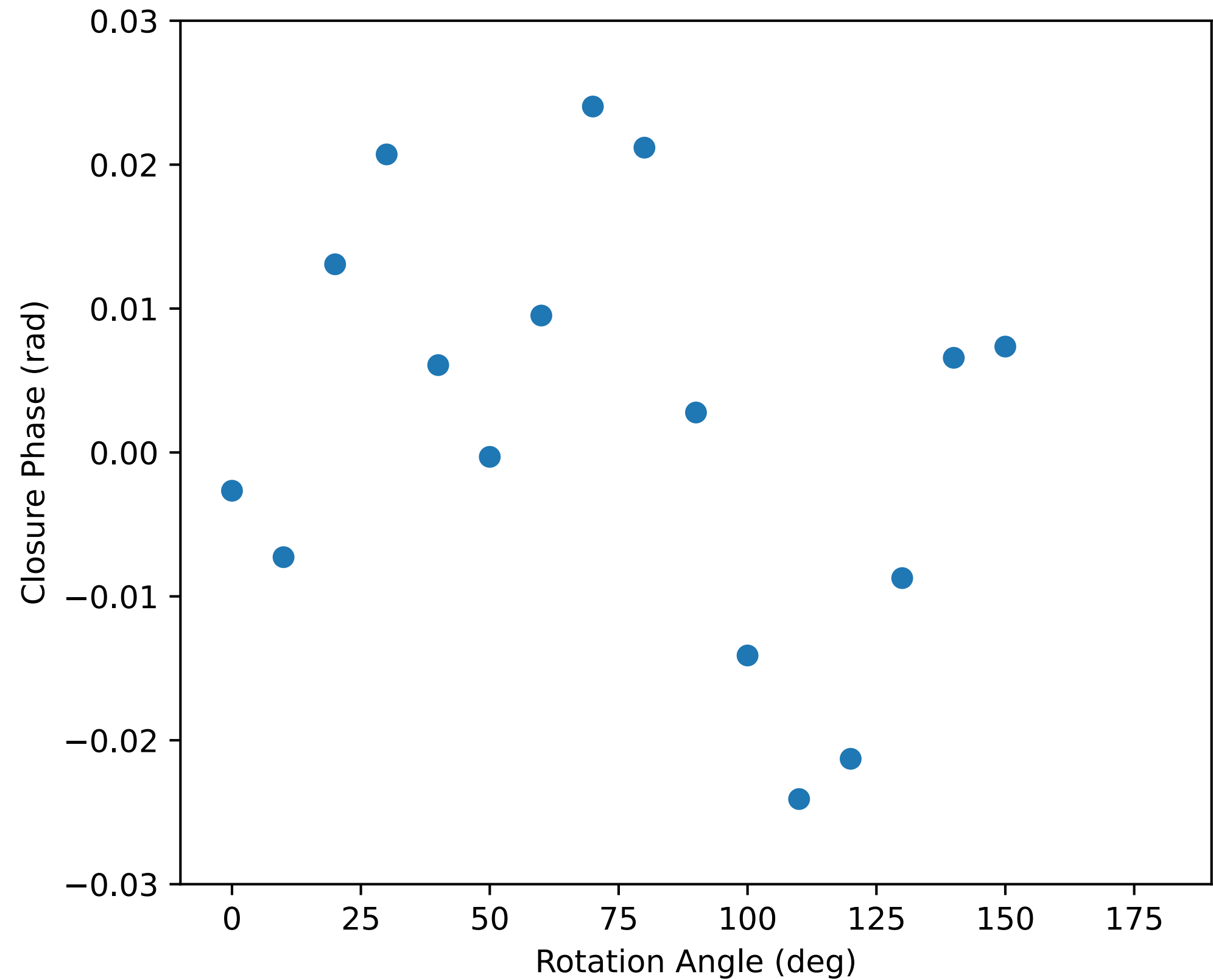
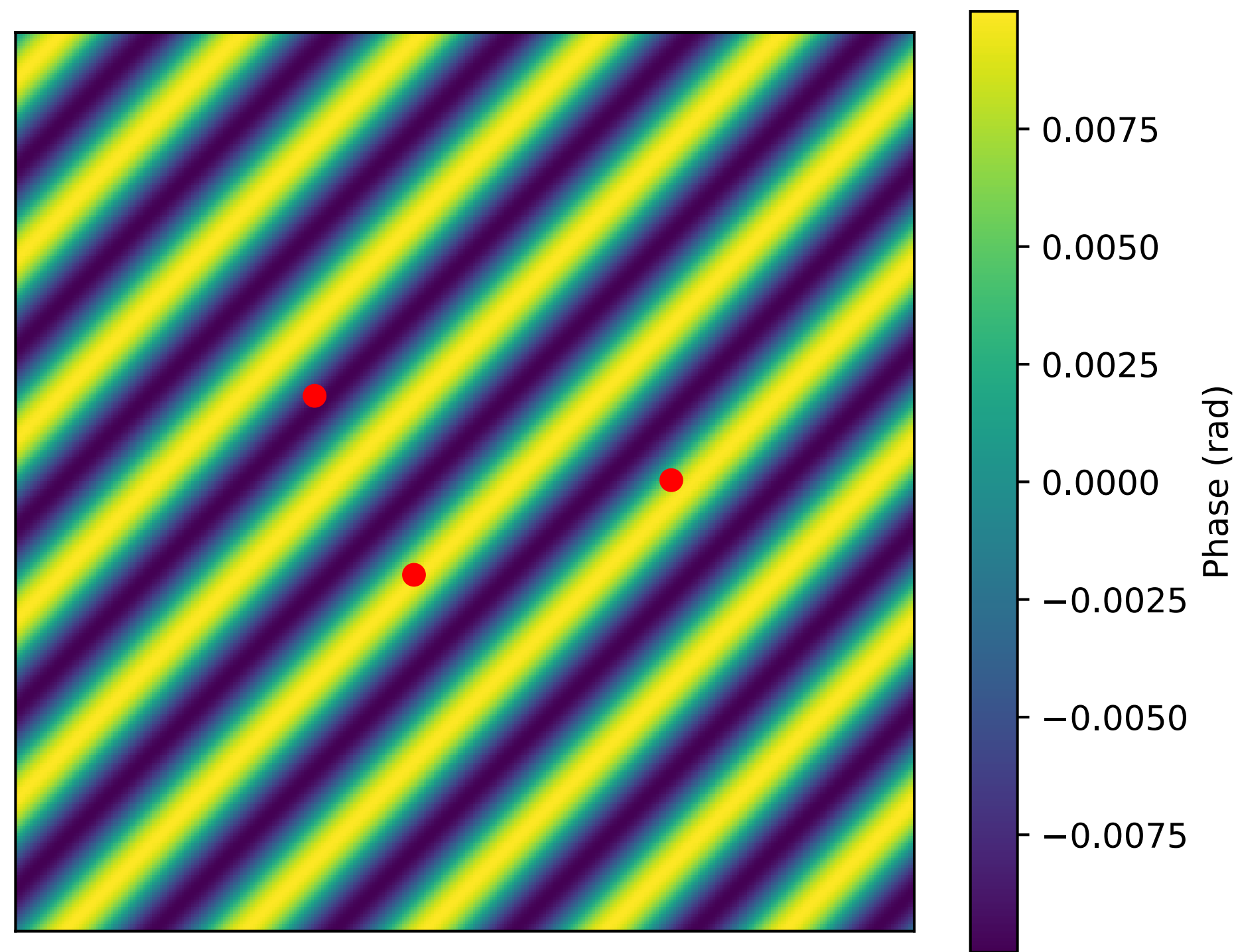
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



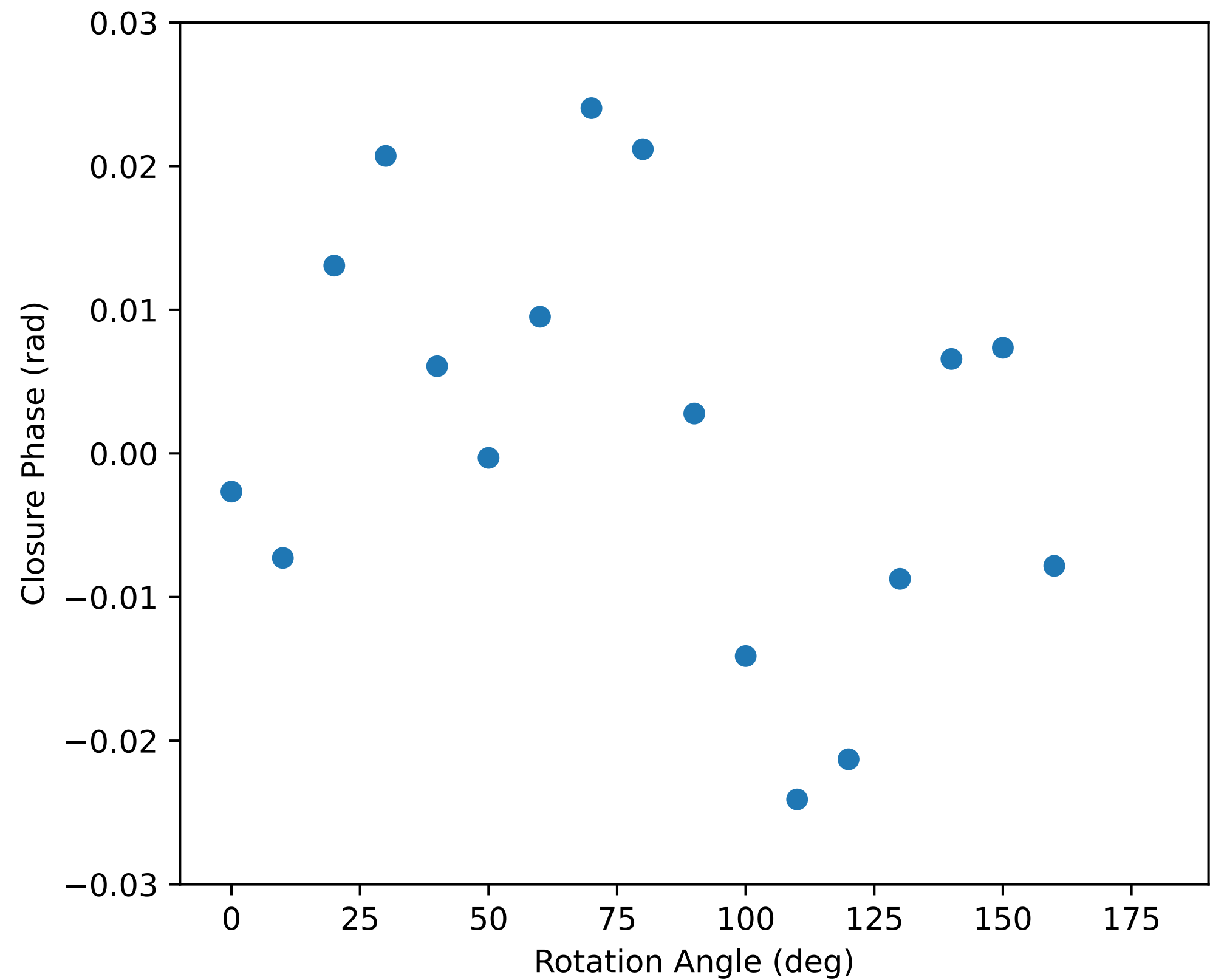
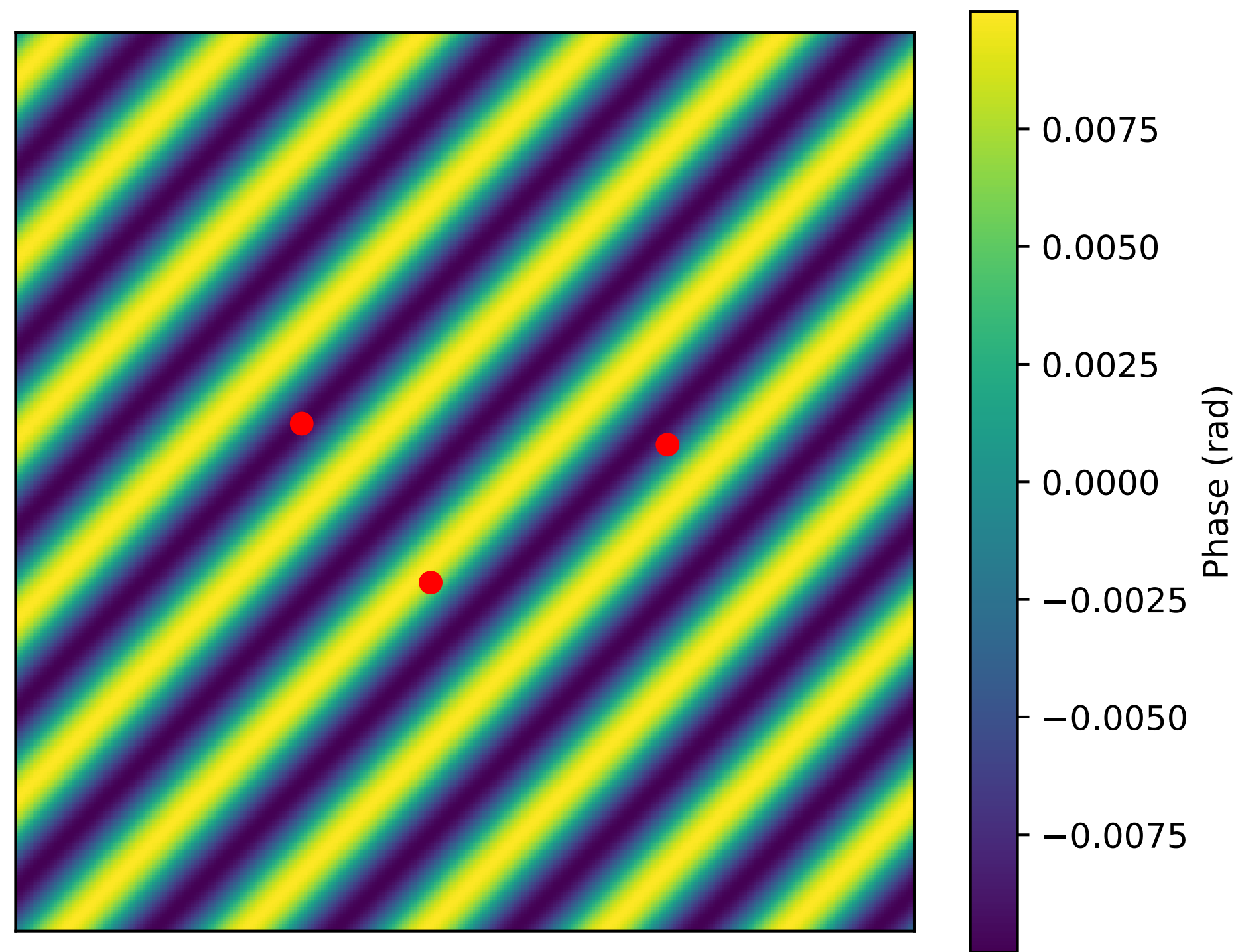
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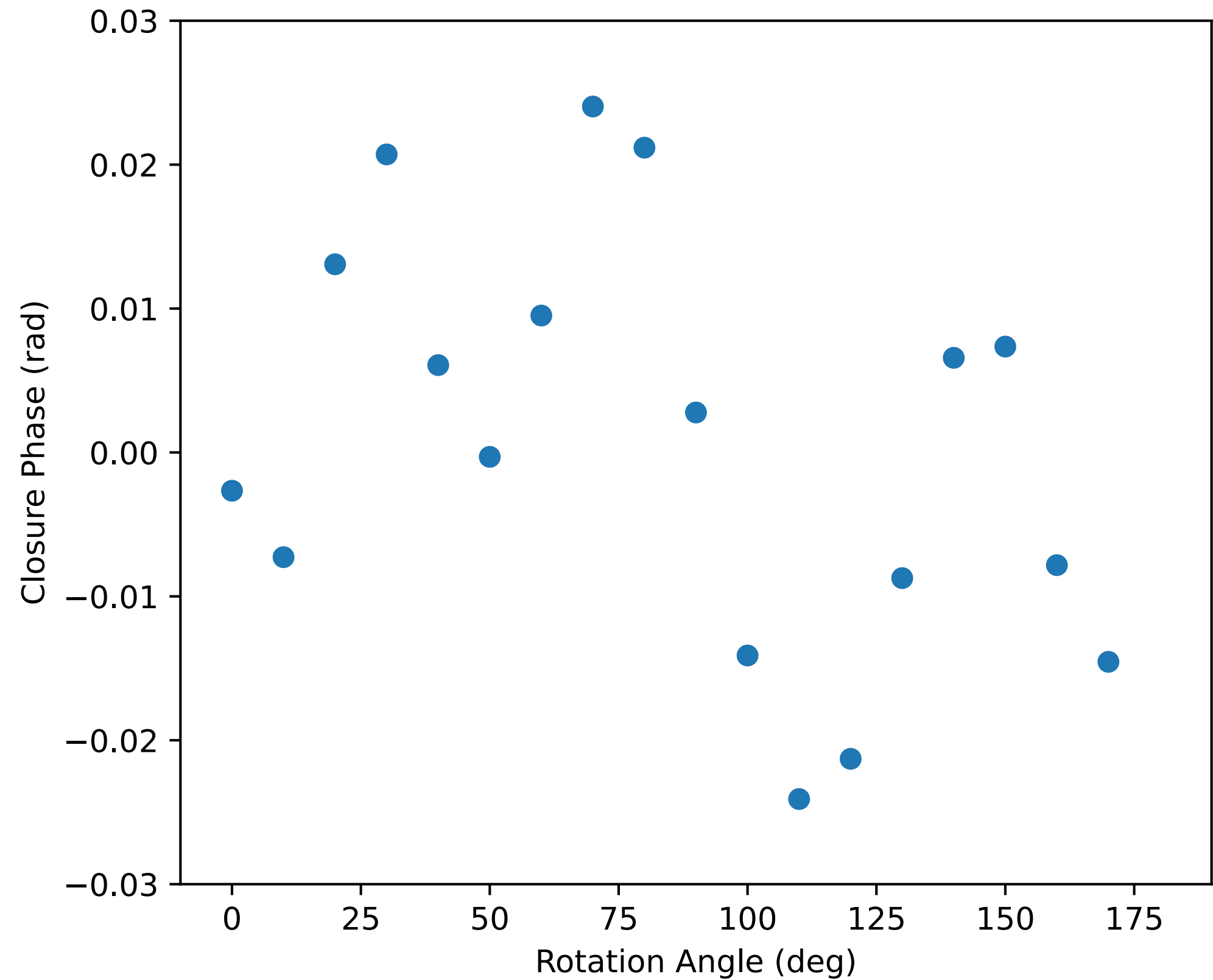
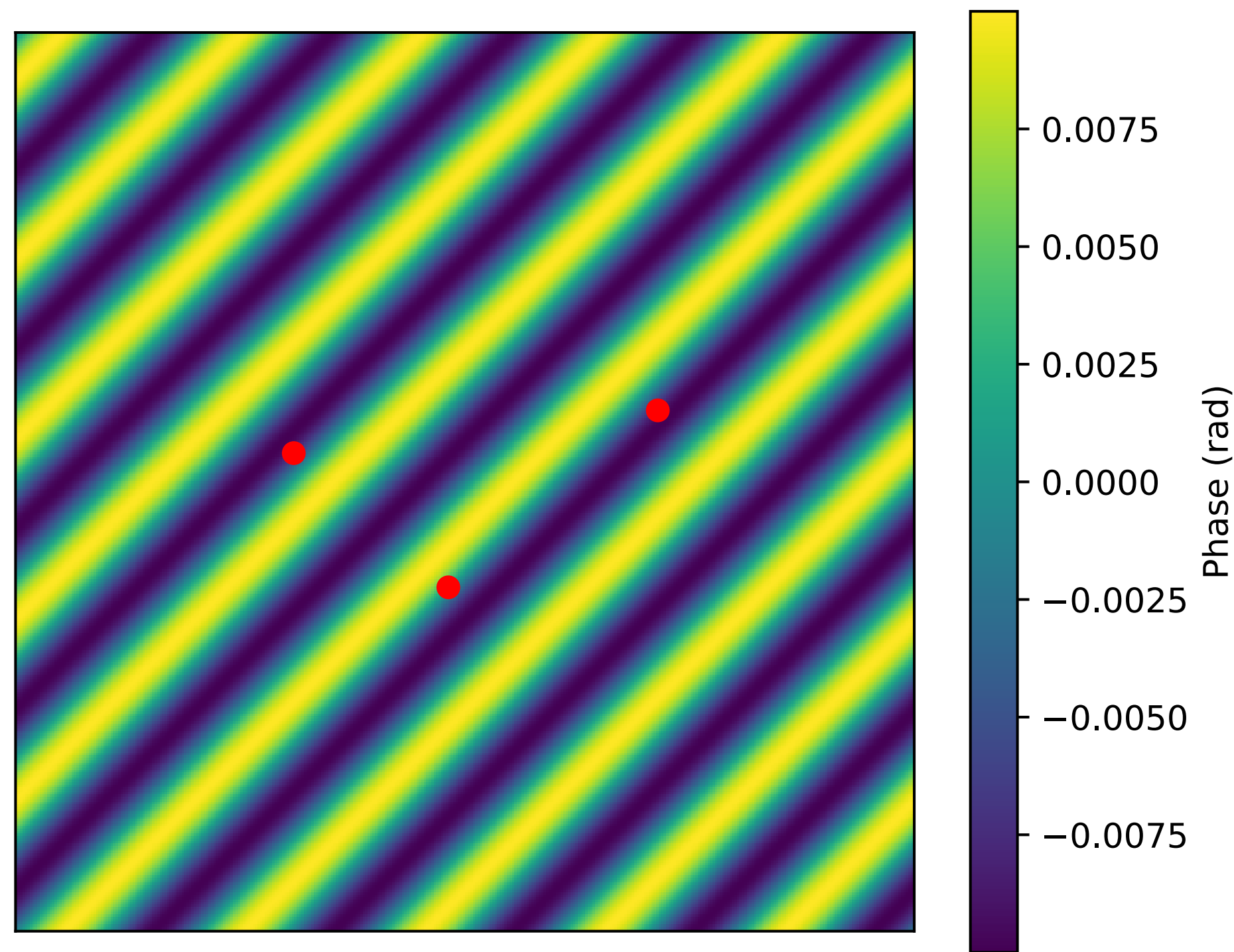
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



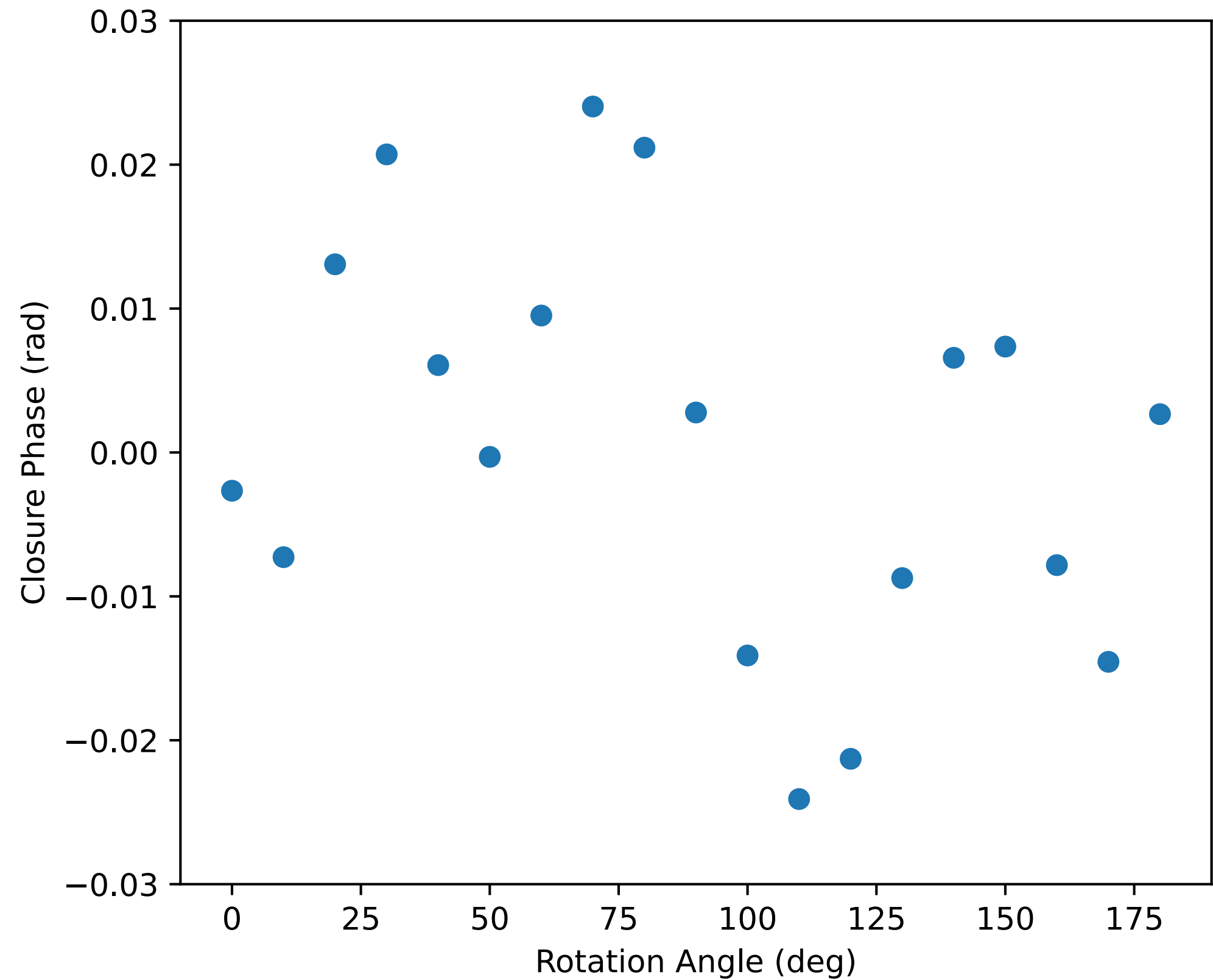
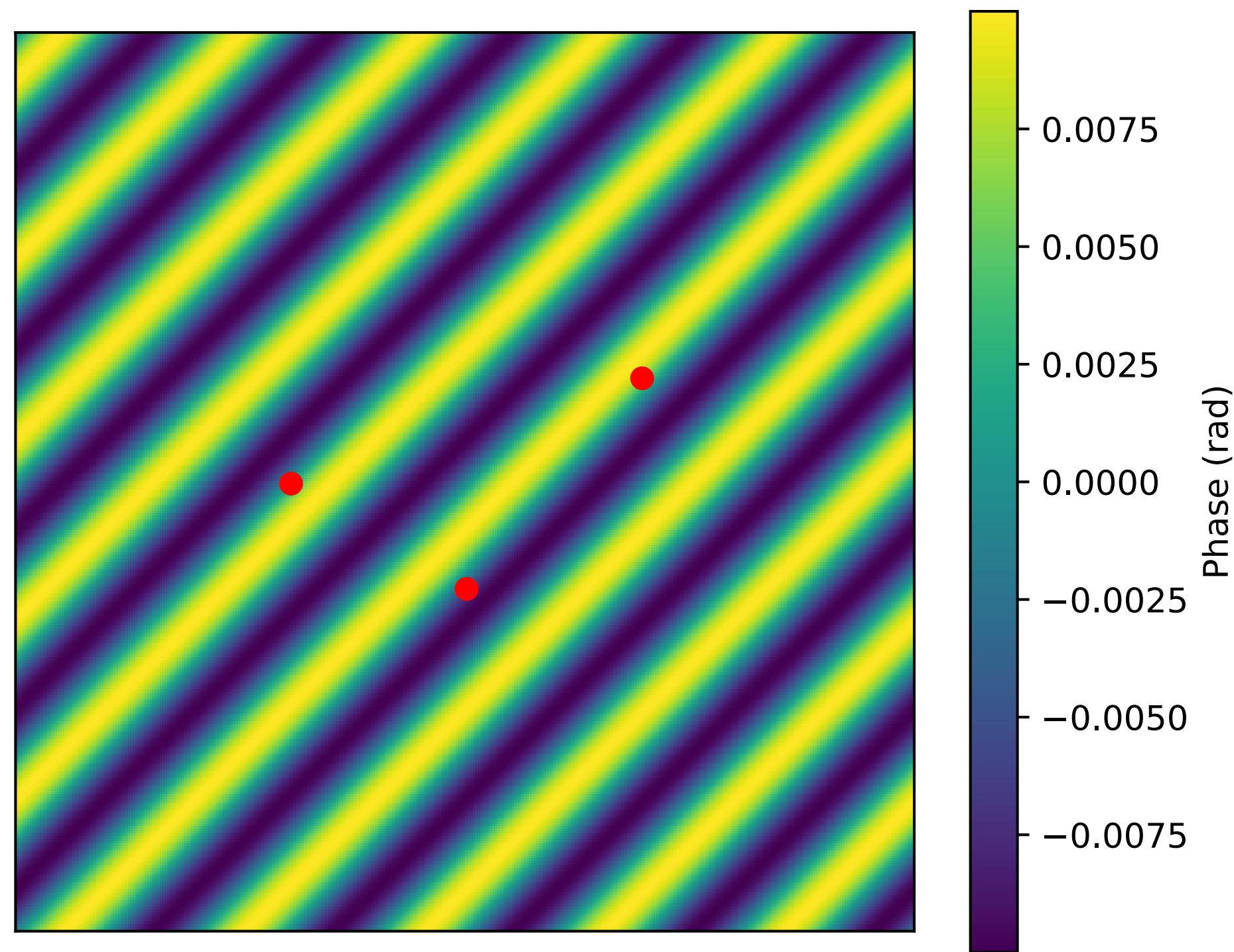
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source



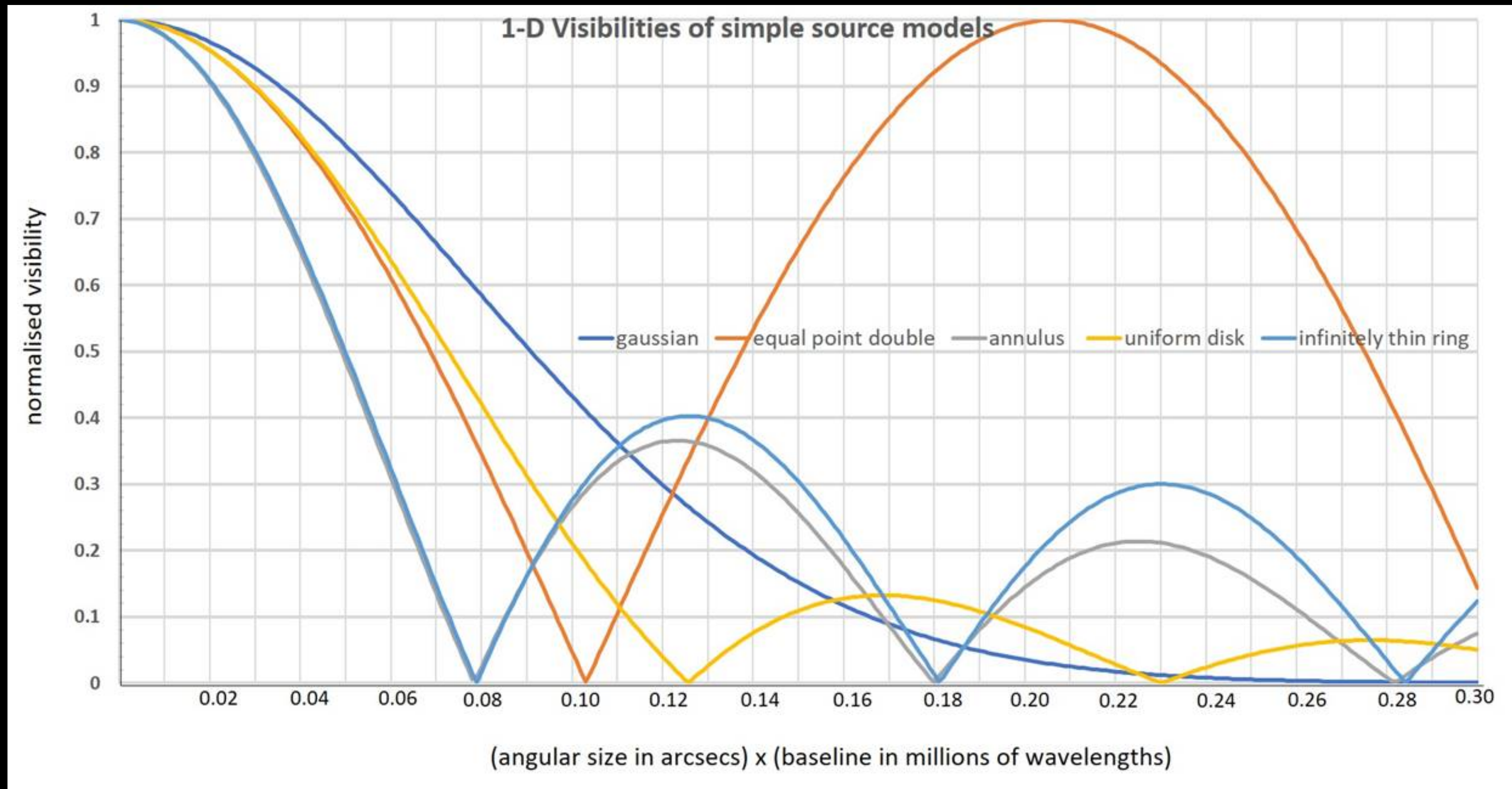
Interpreting NRM Observables: Closure Phases

Sums of Fourier Phases Intrinsic to the Source

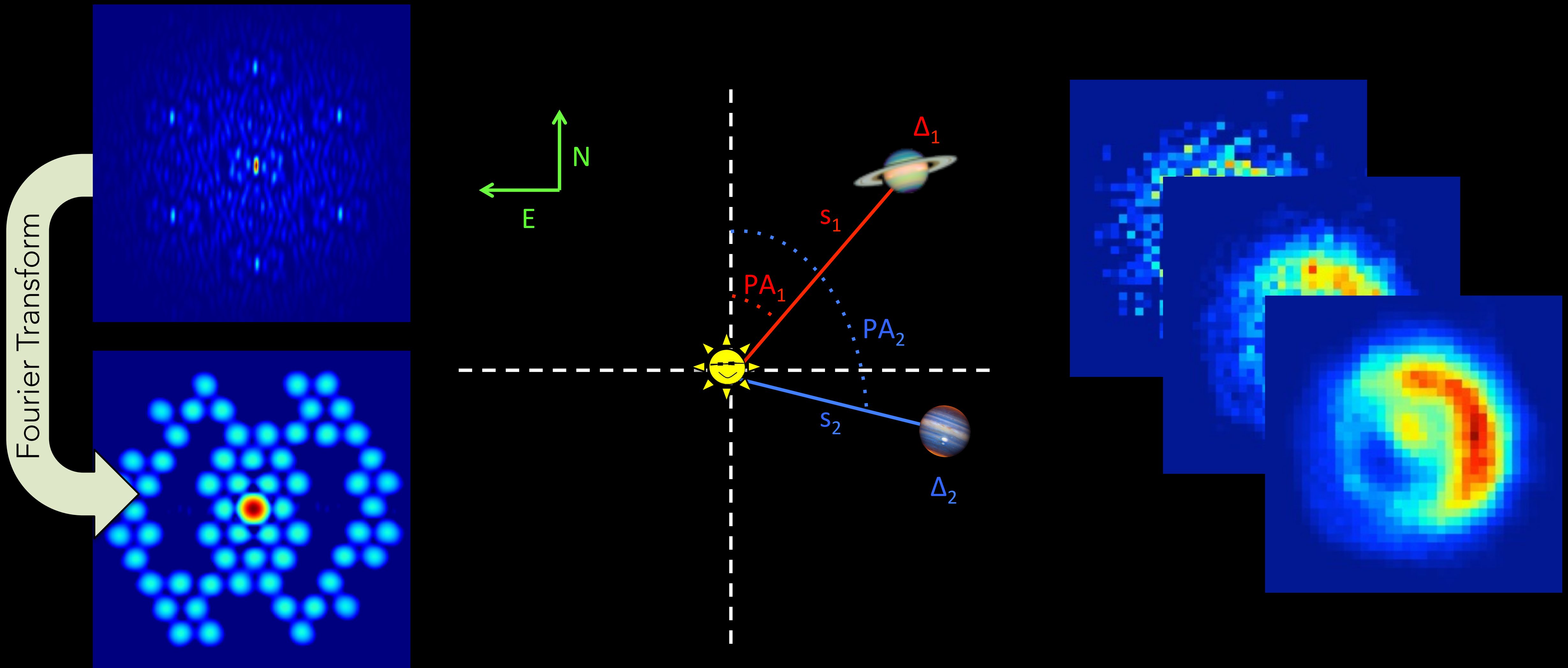


Interpreting NRM Observables: Visibilities

Fourier Amplitudes Intrinsic to the Source

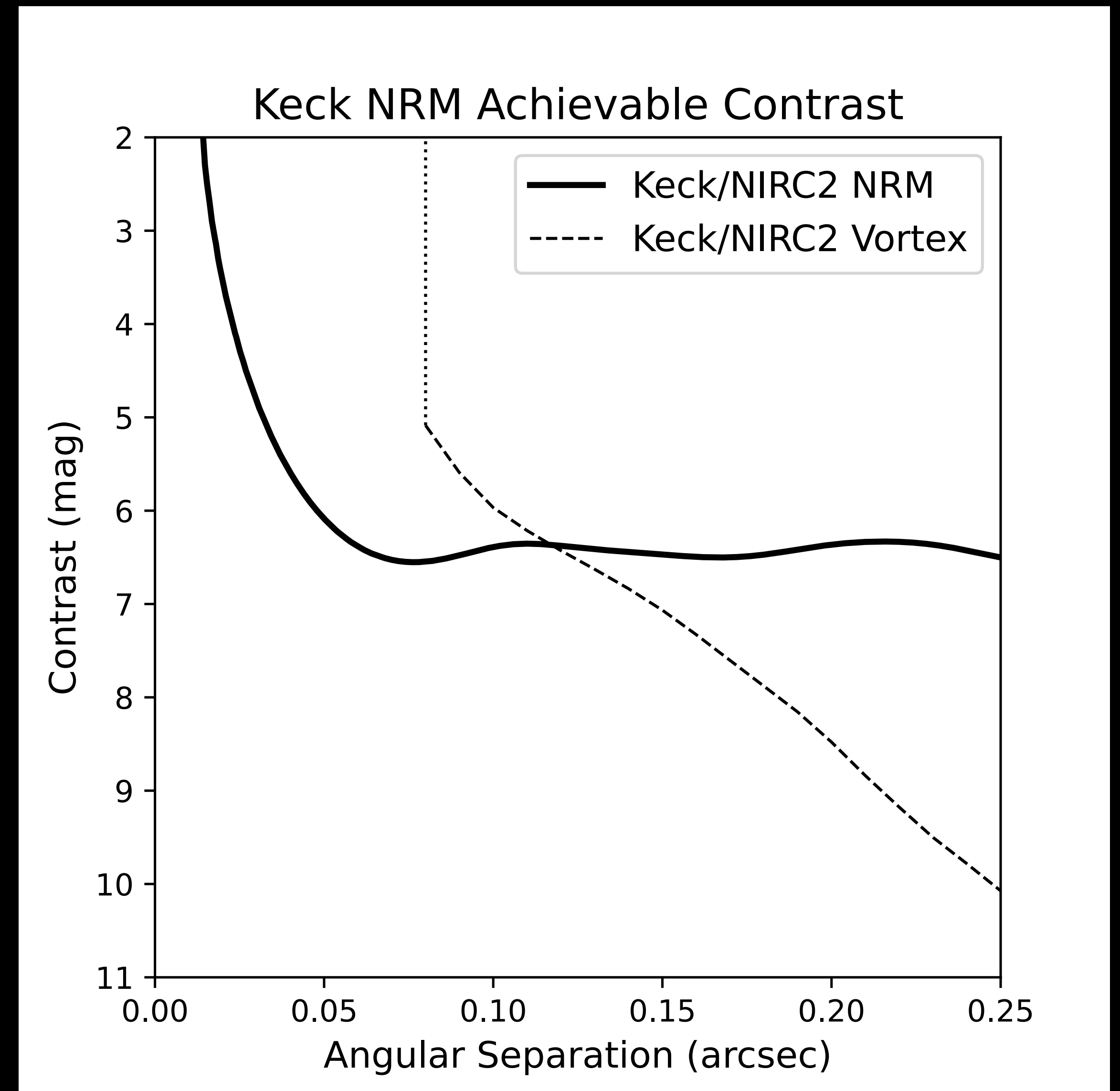


Images to Source Brightness Distribution



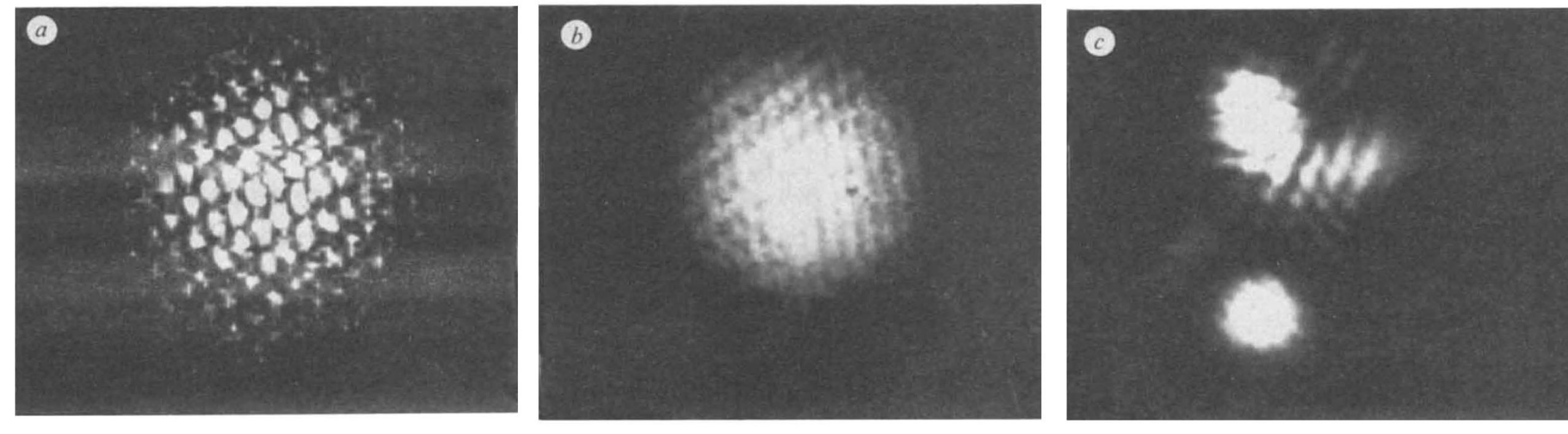
NRM Contrast

- NRM's self-calibrating observables enable “*super-resolution*”: moderate contrast down to and within the diffraction limit
- We can re-project closure phases in a statistically independent way to make the wide-separation NRM contrast curve deeper (Ireland 2013; not shown on the right)



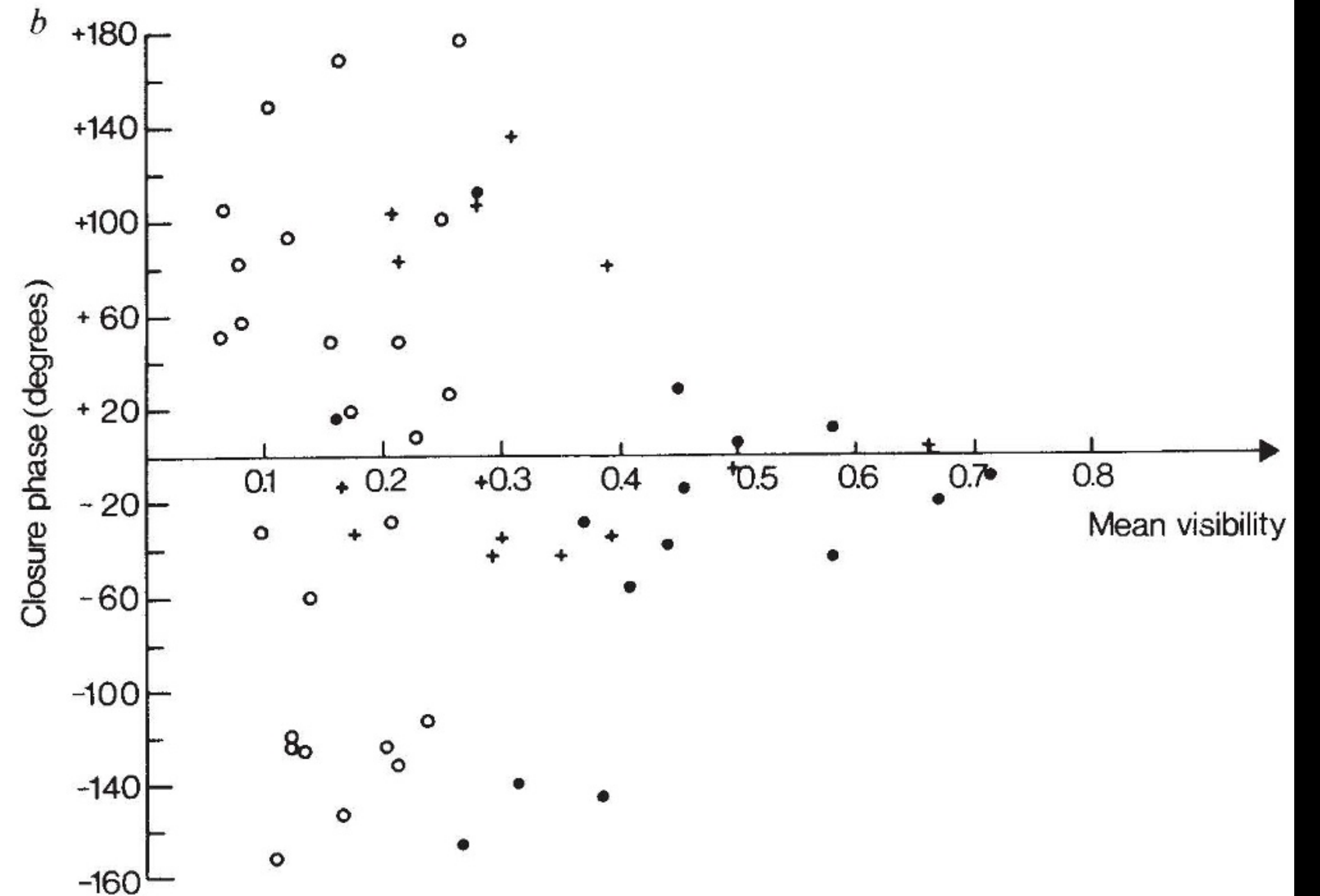
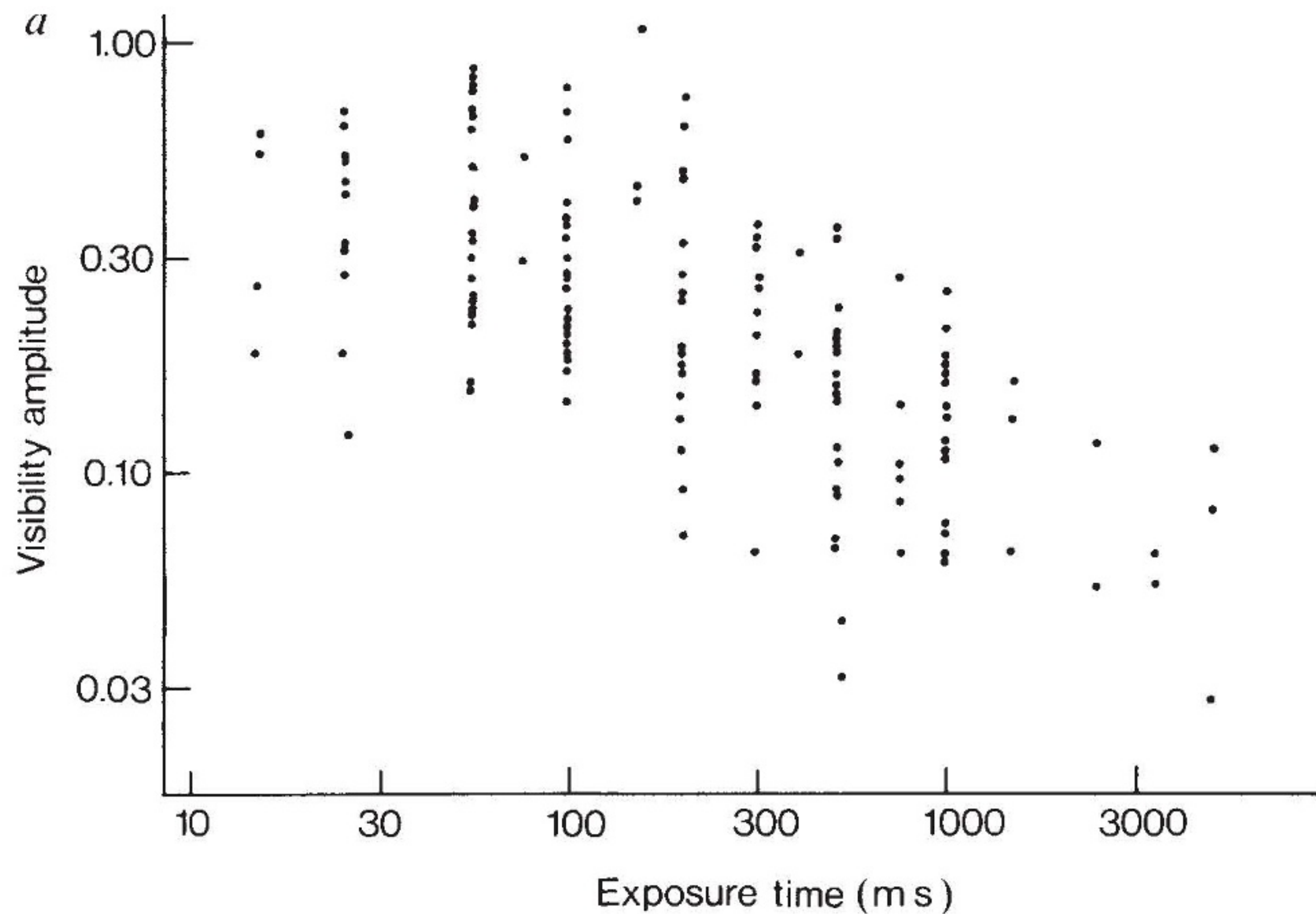
Ground-Based AMI

Early Demonstrations with UH 88, AAT, Hale



Early AMI observations did not use AO, and required short exposure times to “freeze-out” the atmosphere!

Baldwin et al. 1986; Frater et al. 1986;
Readhead et al. 1988; Haniff et al. 1987



10m-Class AMI Beginning with Keck

Evolved Stars, YSOs, Colliding Binaries' Plumes and Wakes

IRC+10216

WR 98A

WR 140

WR 112



WR140
1999 Jul

Red Rectangle

MWC 349A

WR 104

LkH α 101

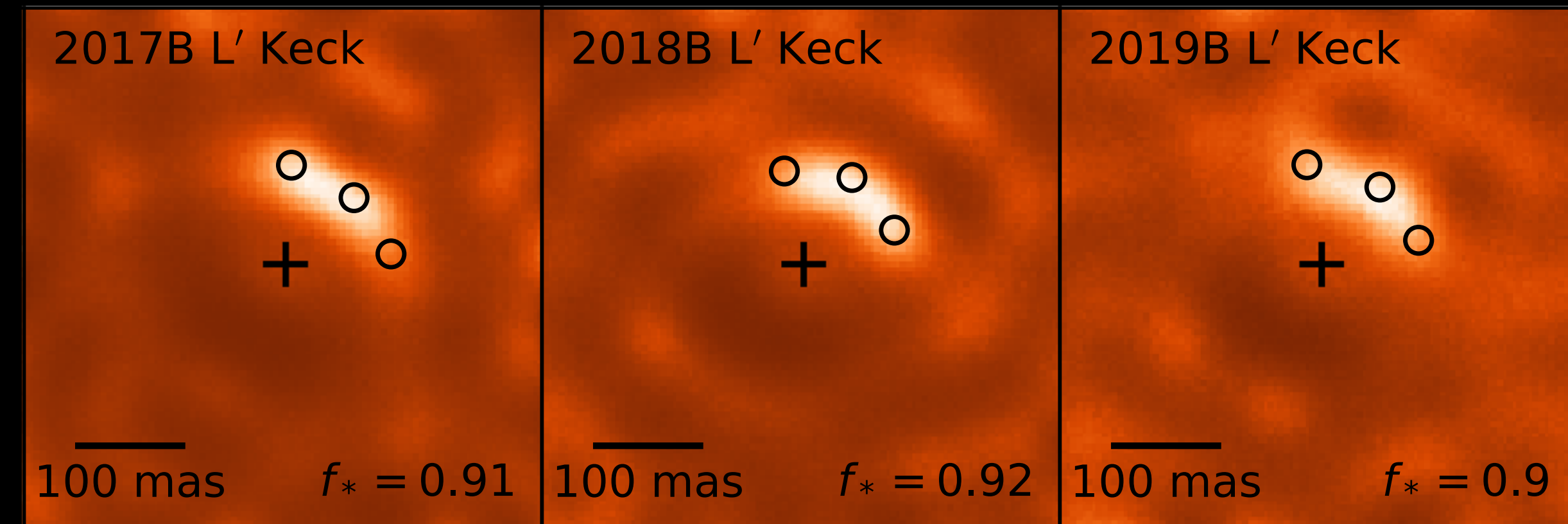
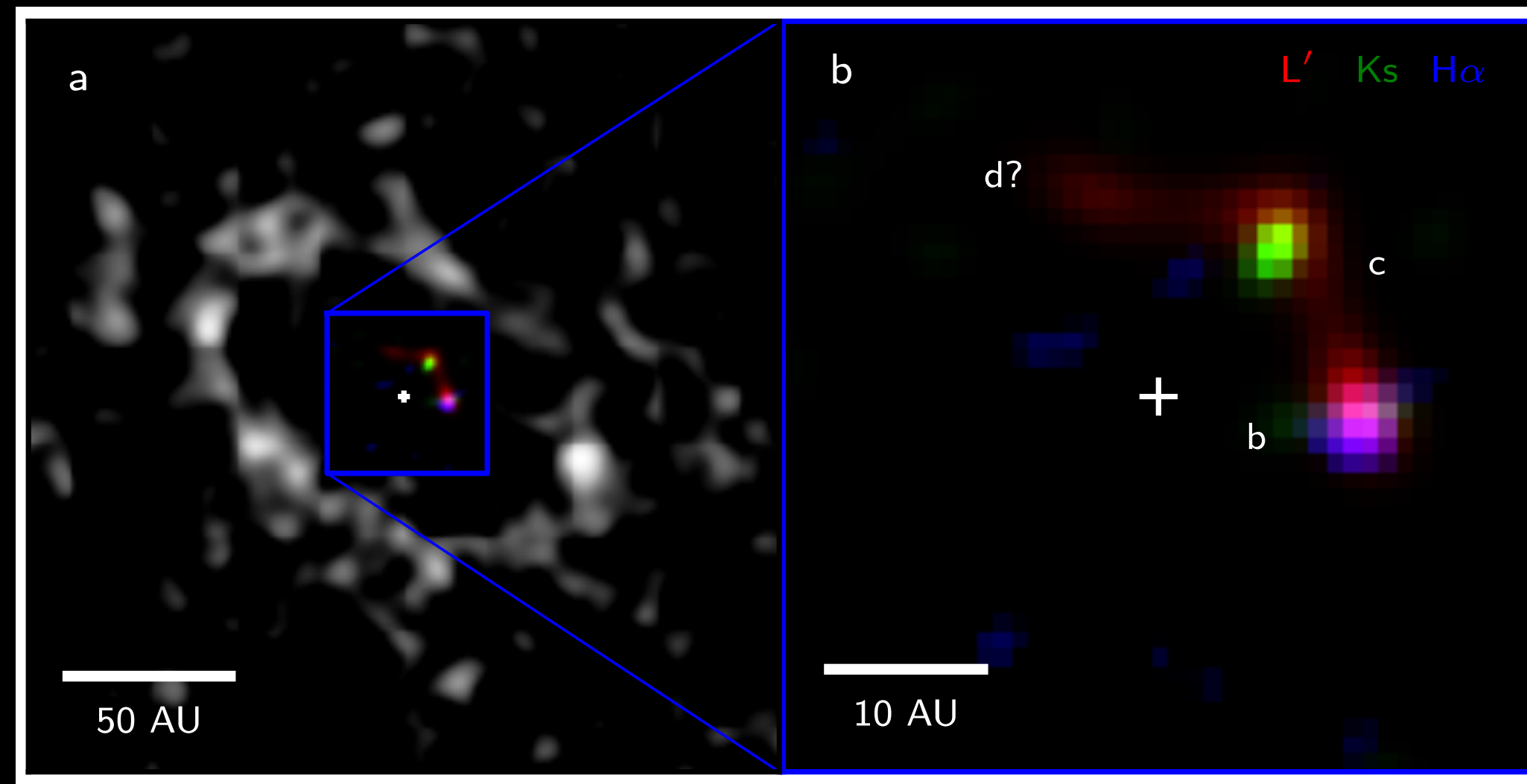
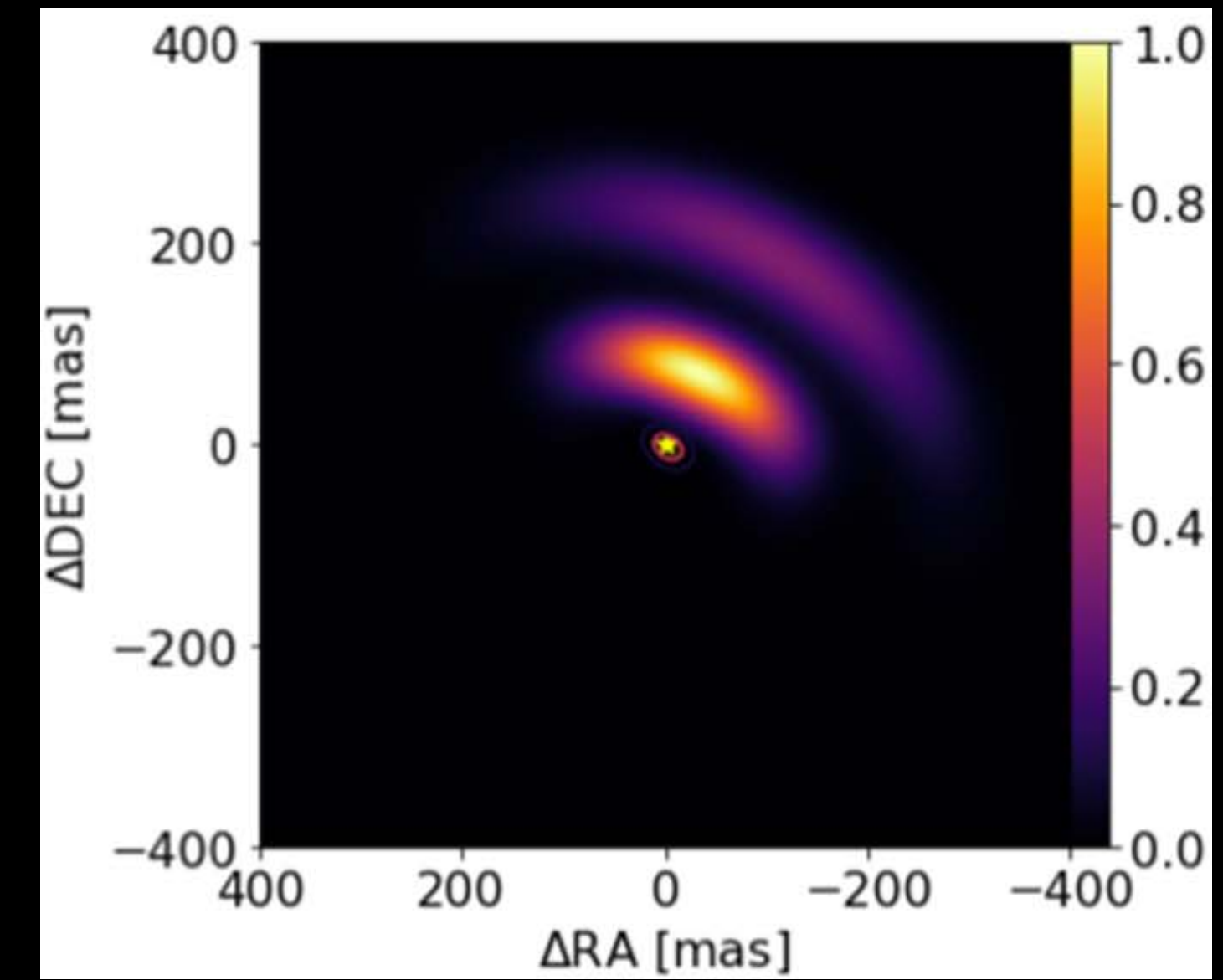
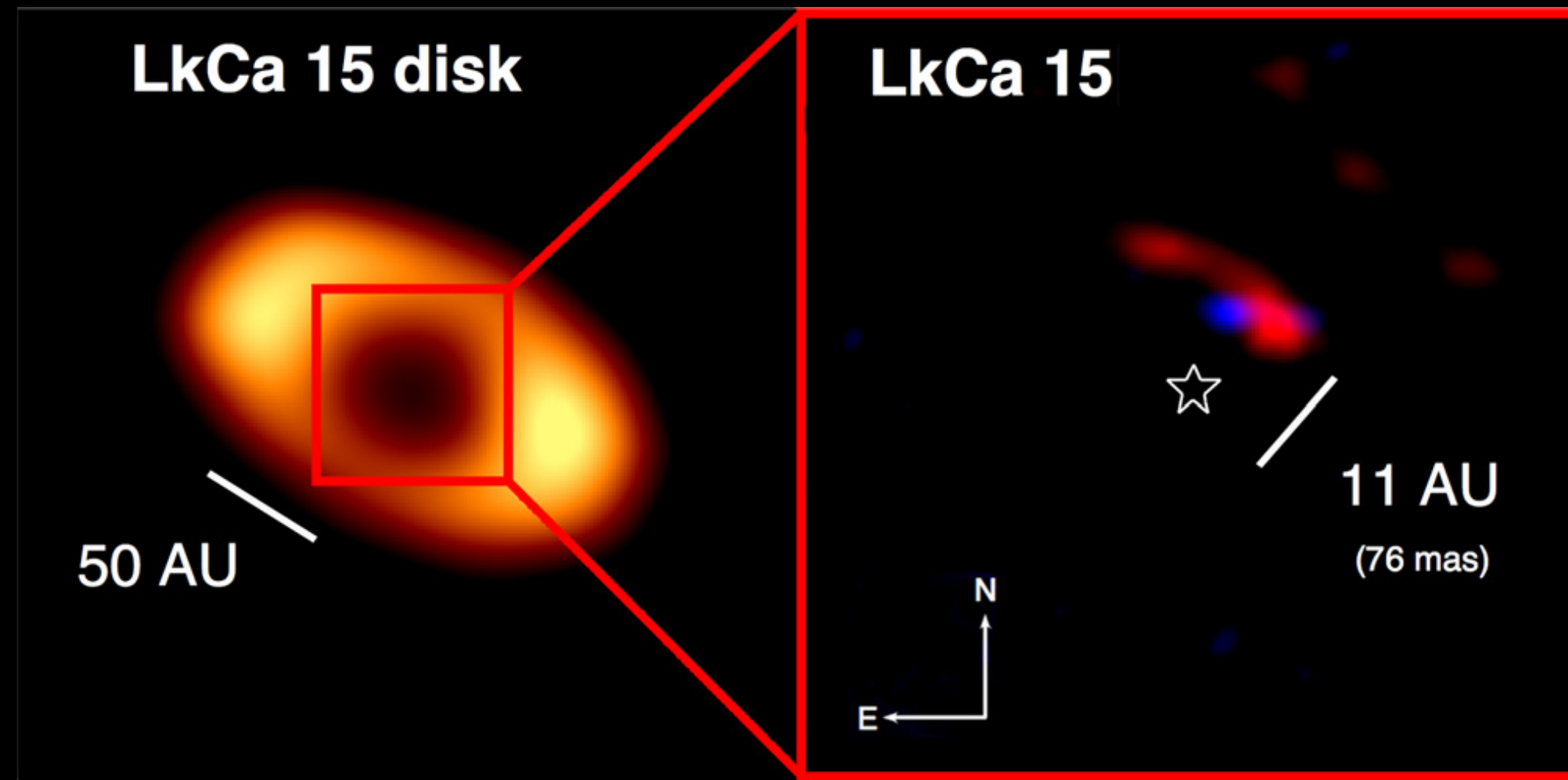


200 mas

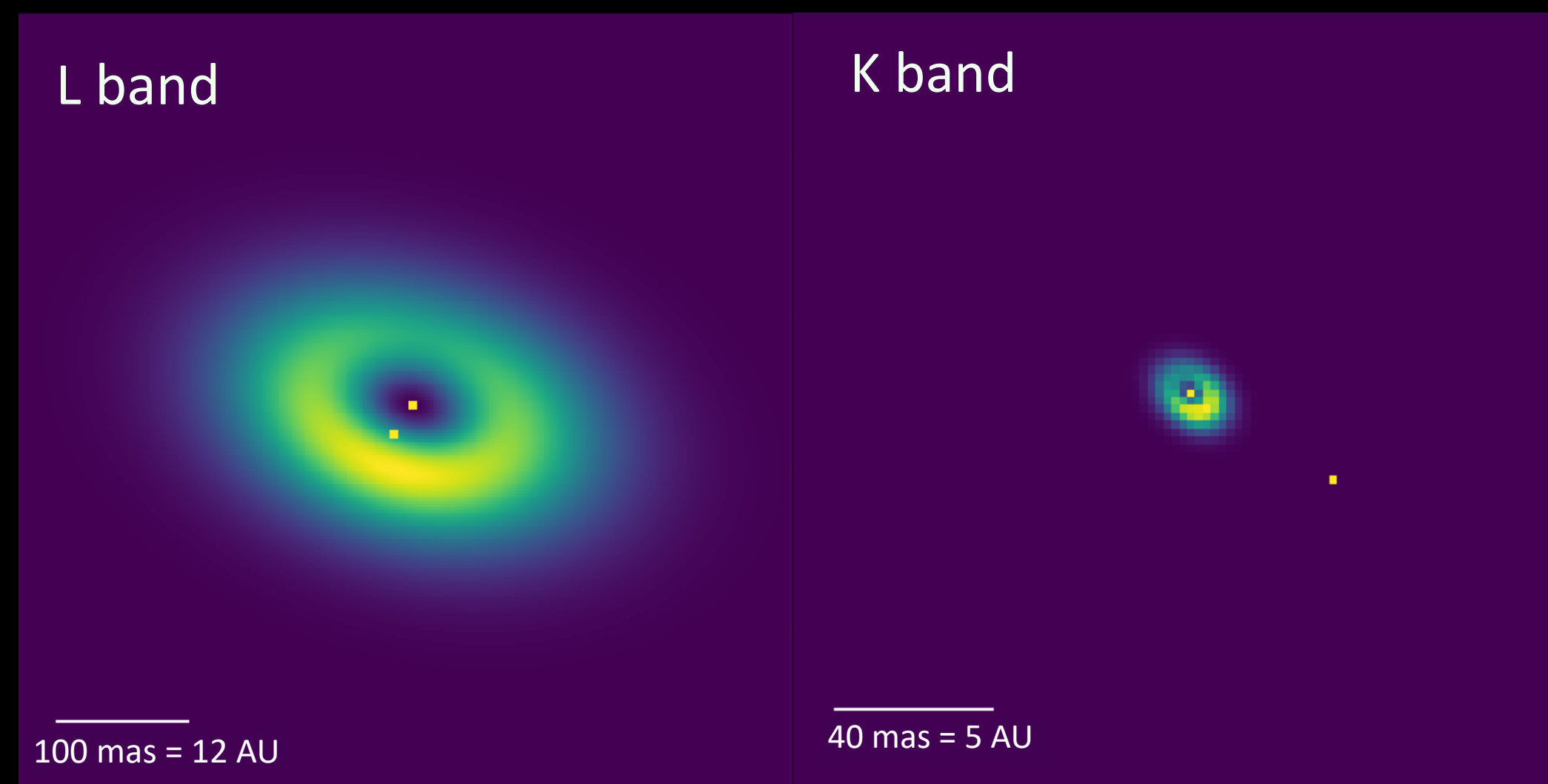
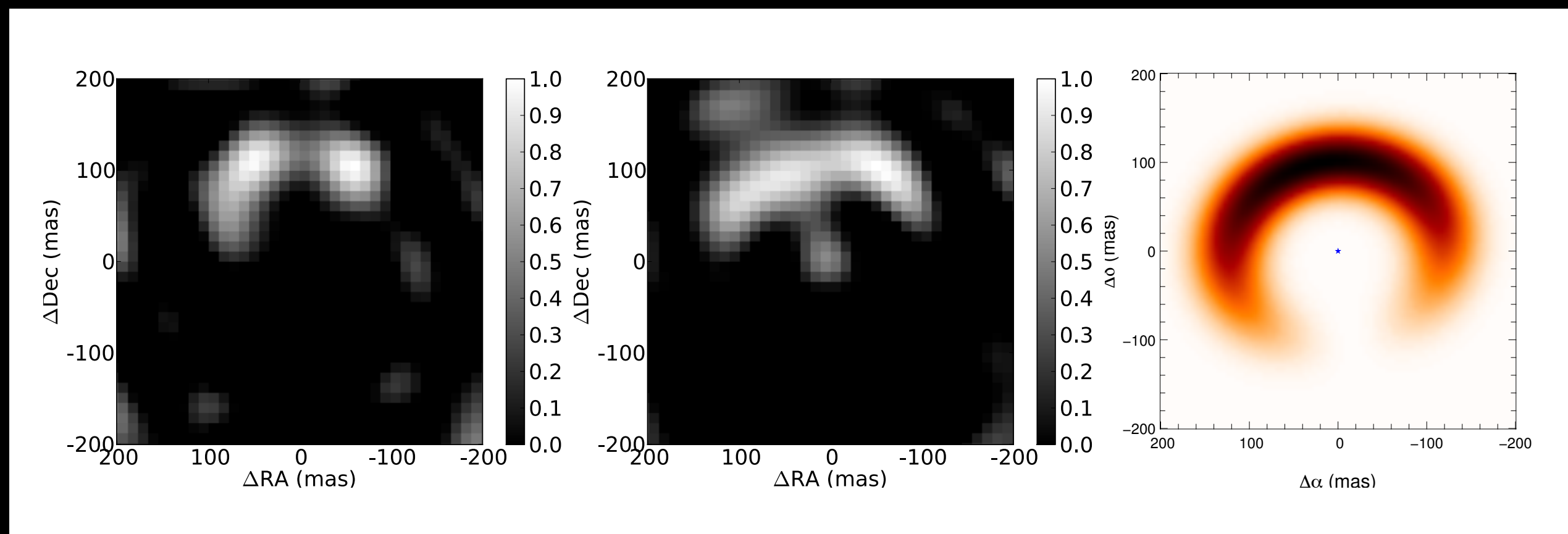
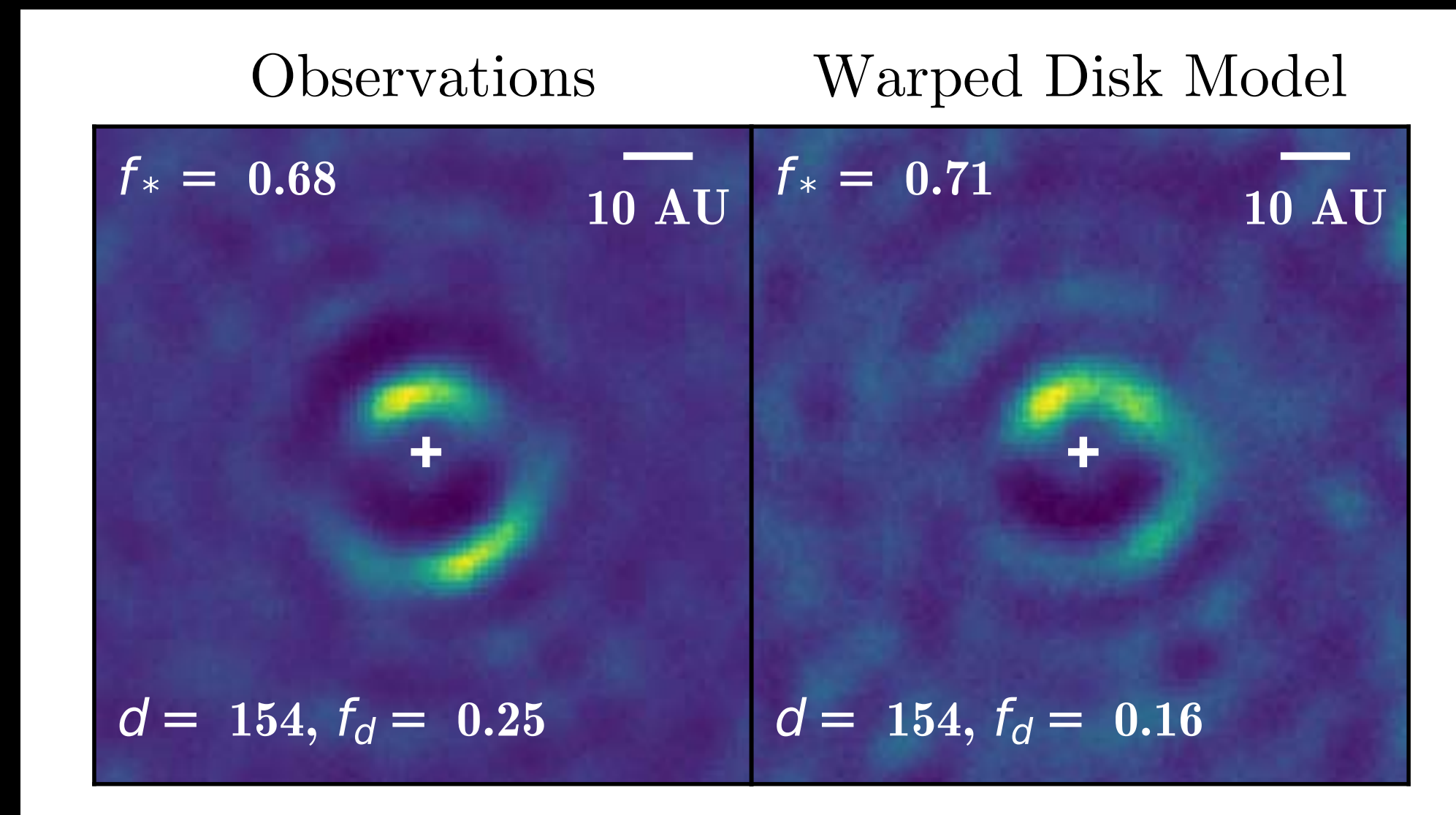
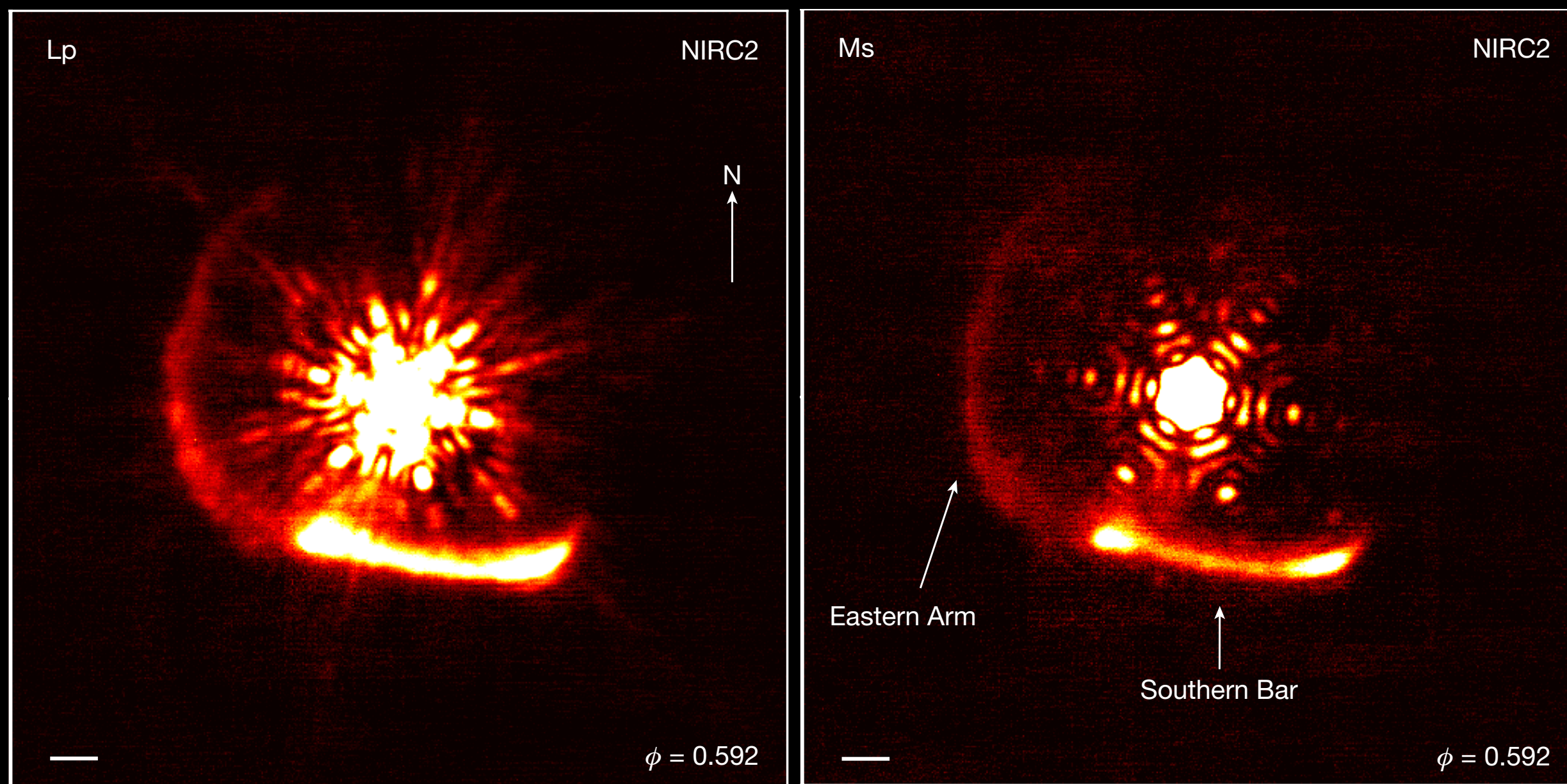
2.20 μm (K_s)

e.g. Tuthill et al. 2000, 2001; Danchi, Tuthill, & Monnier 2001

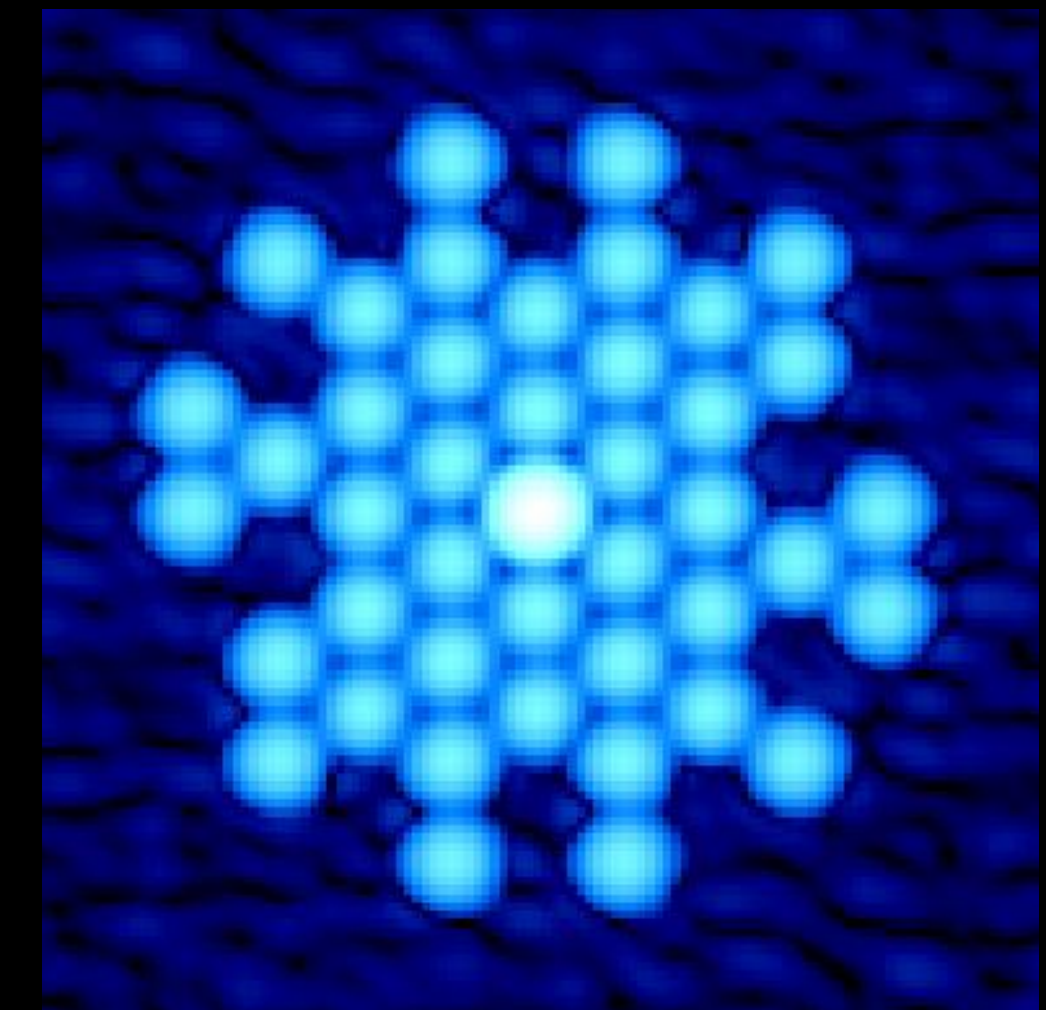
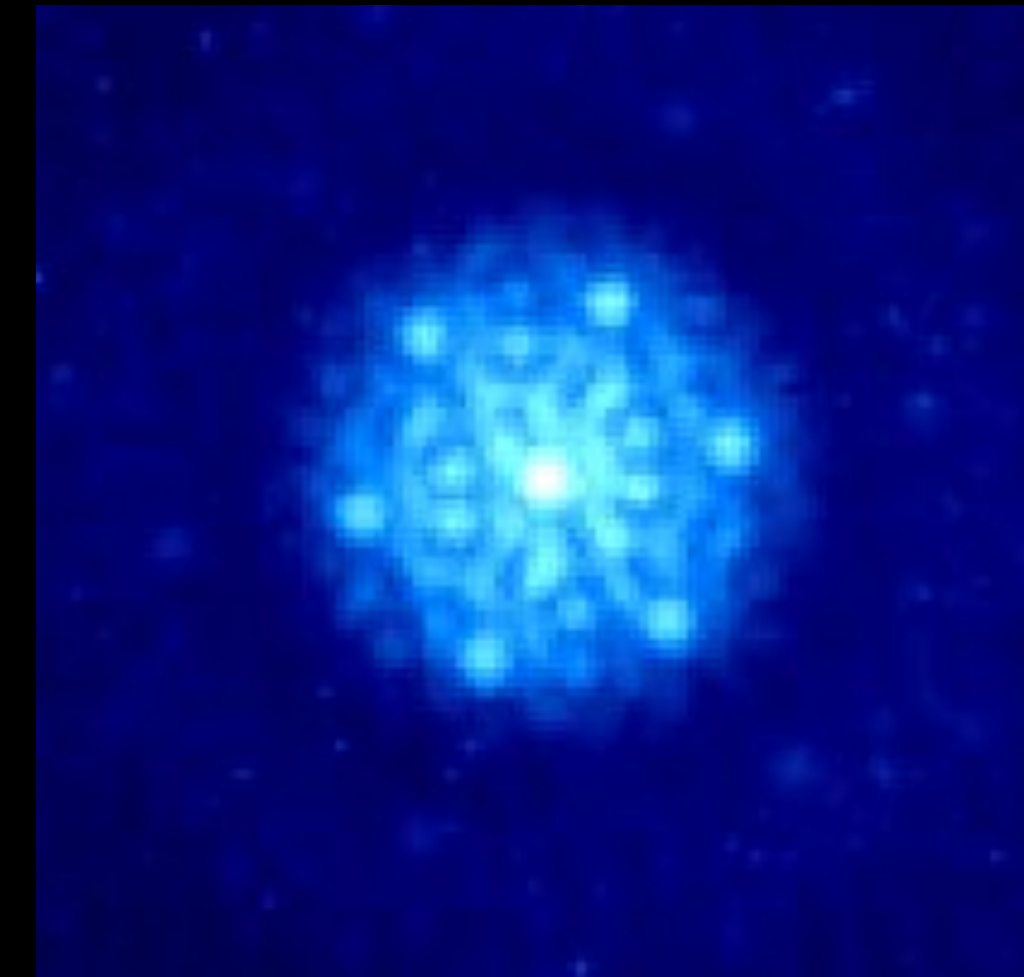
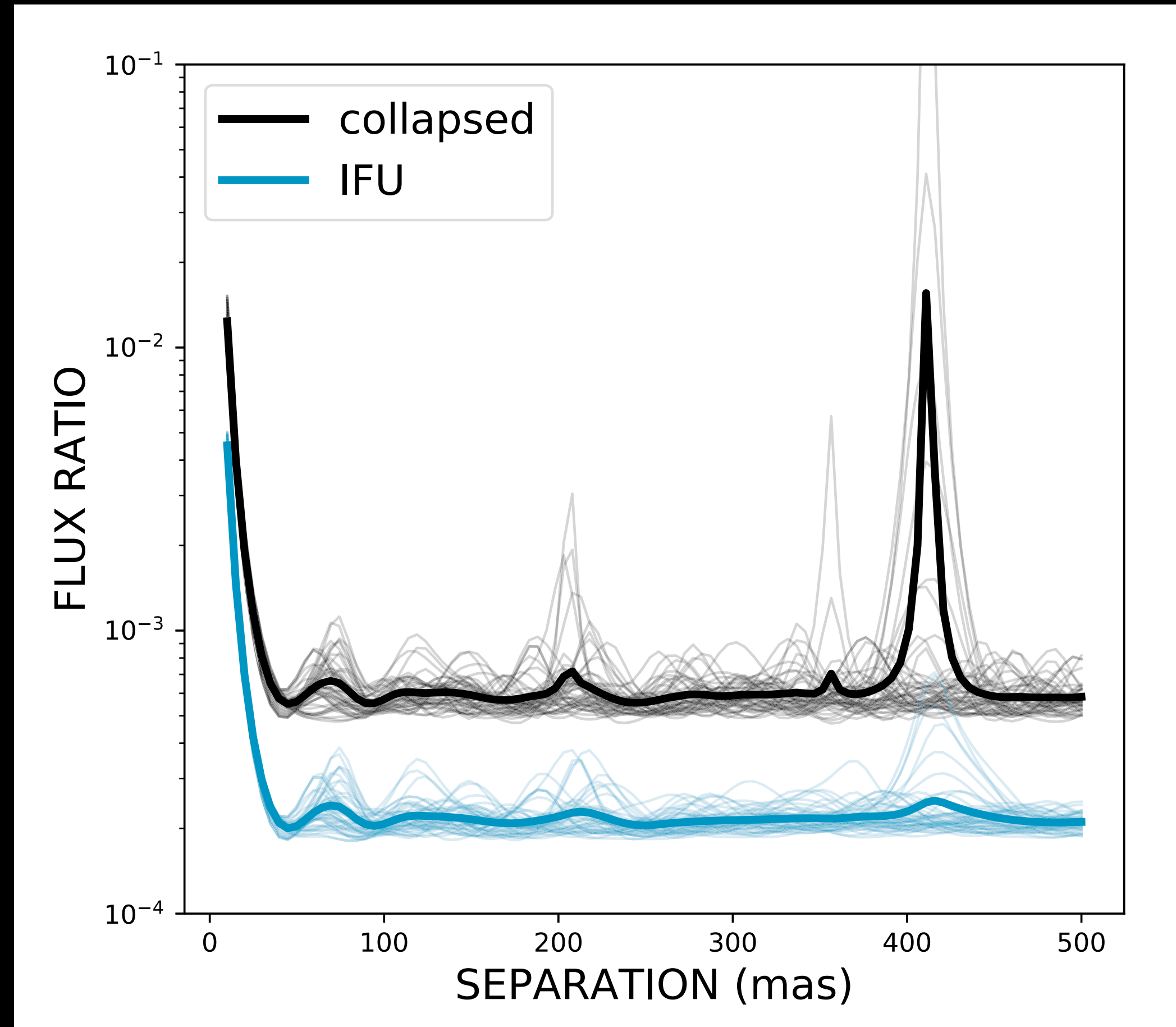
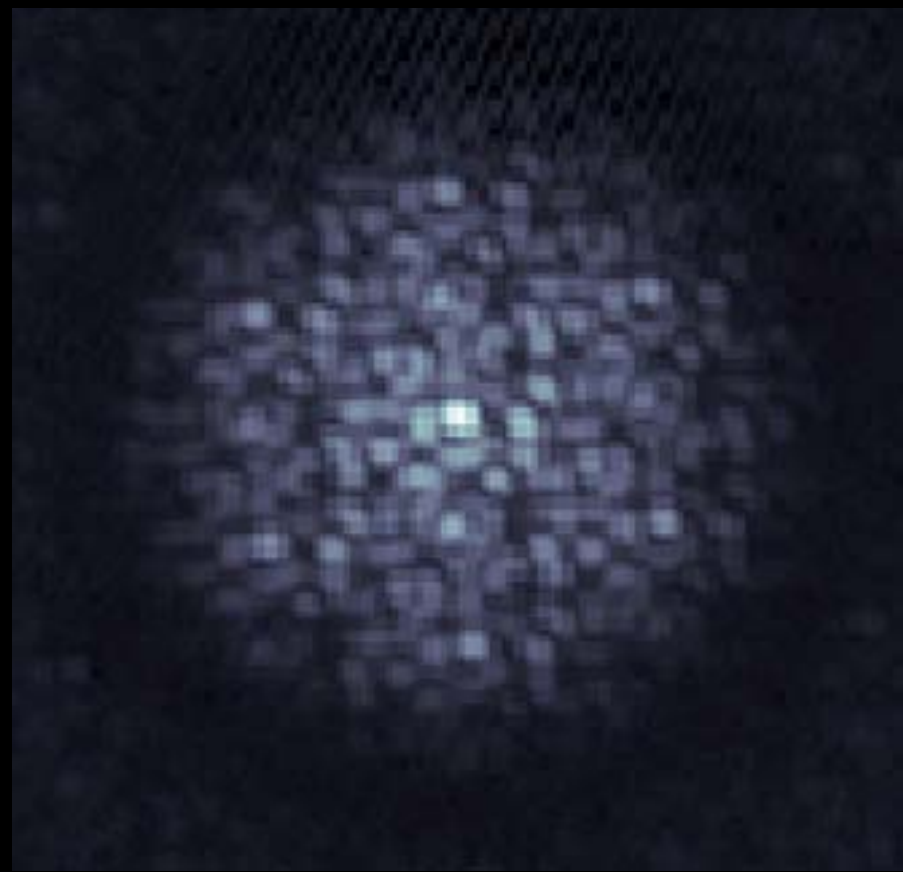
AMI + Adaptive Optics on 10m Class Telescopes



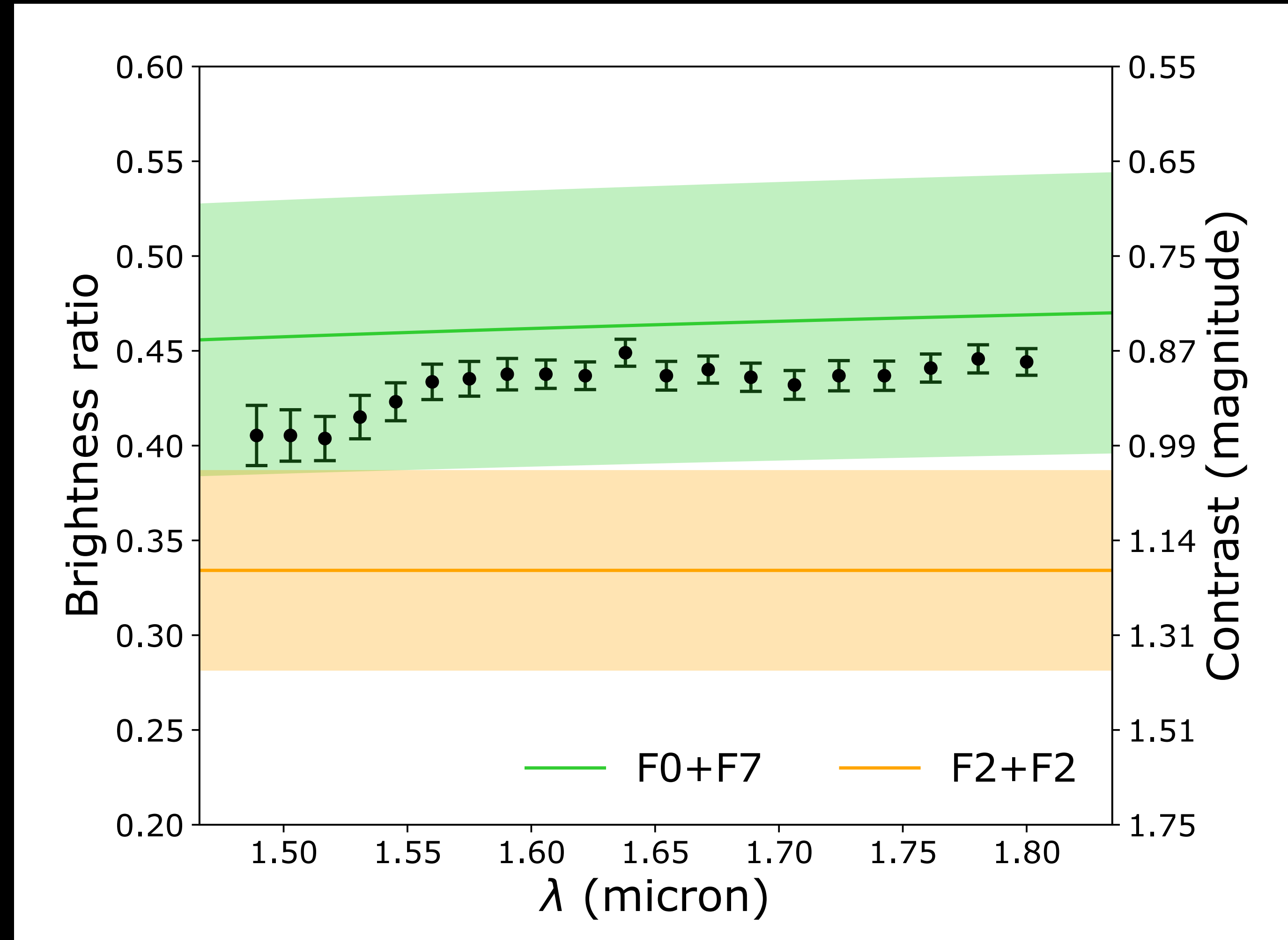
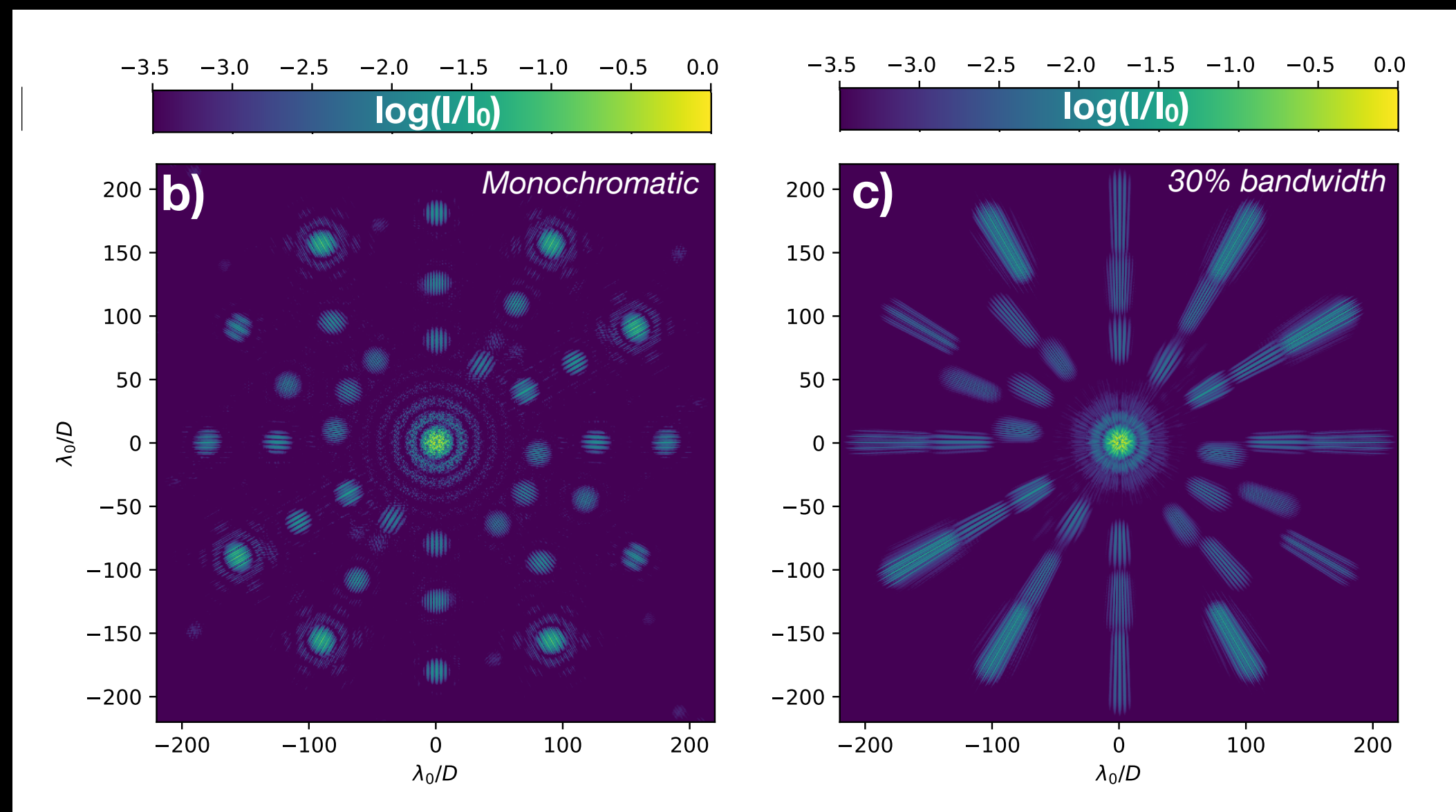
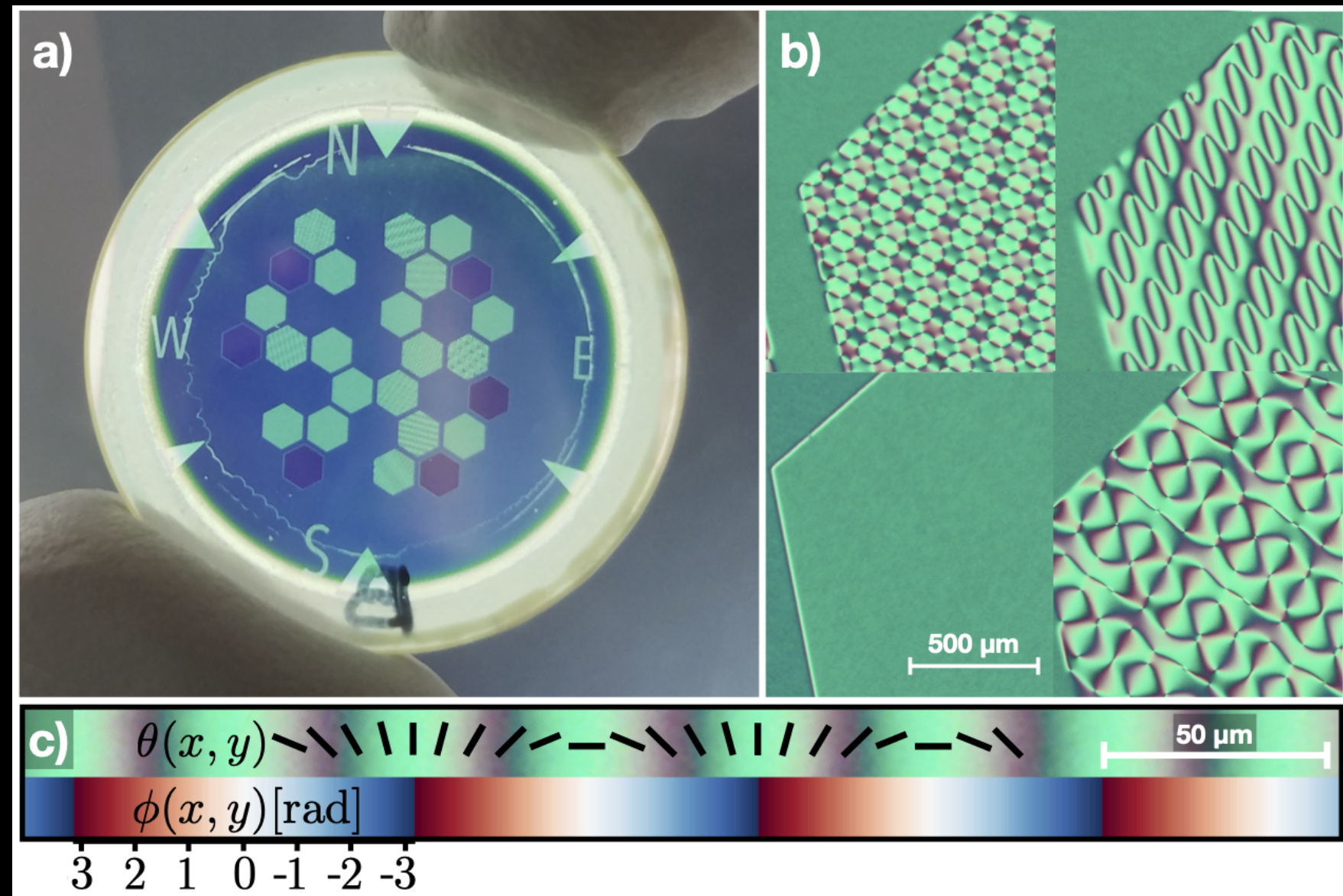
High-Contrast AMI Science



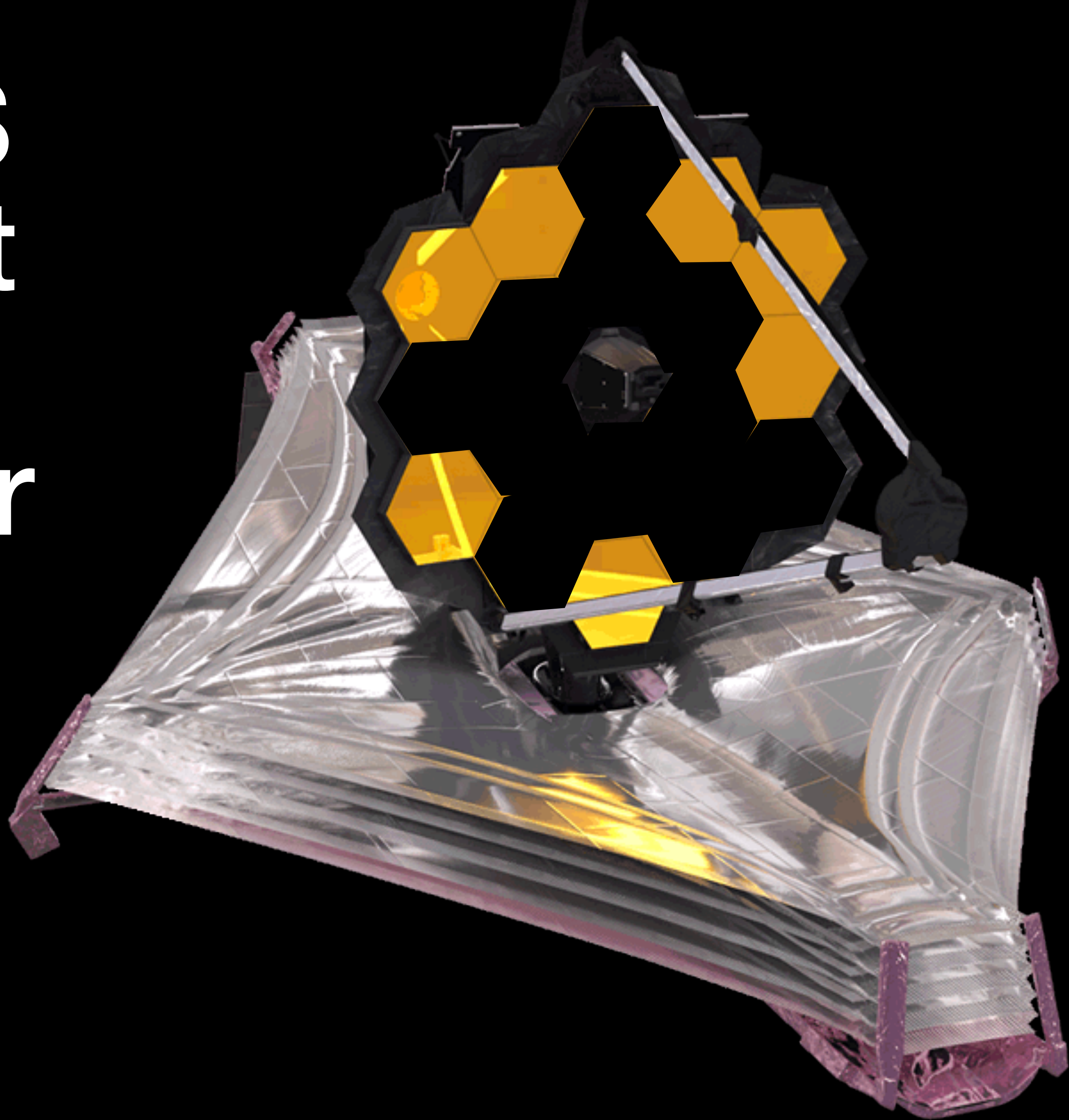
Spectrally-Dispersed AMI on Integral Field Spectrographs



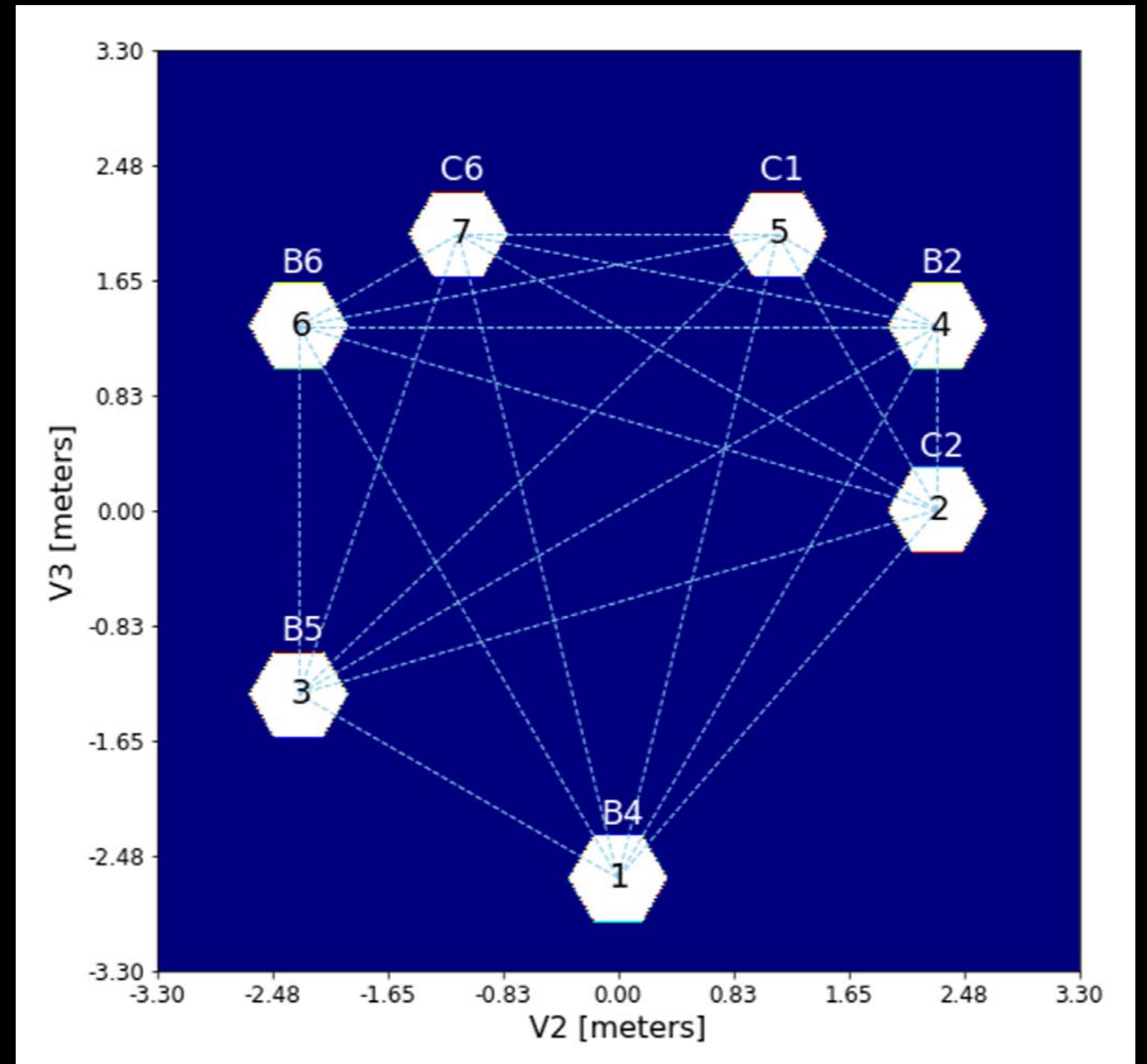
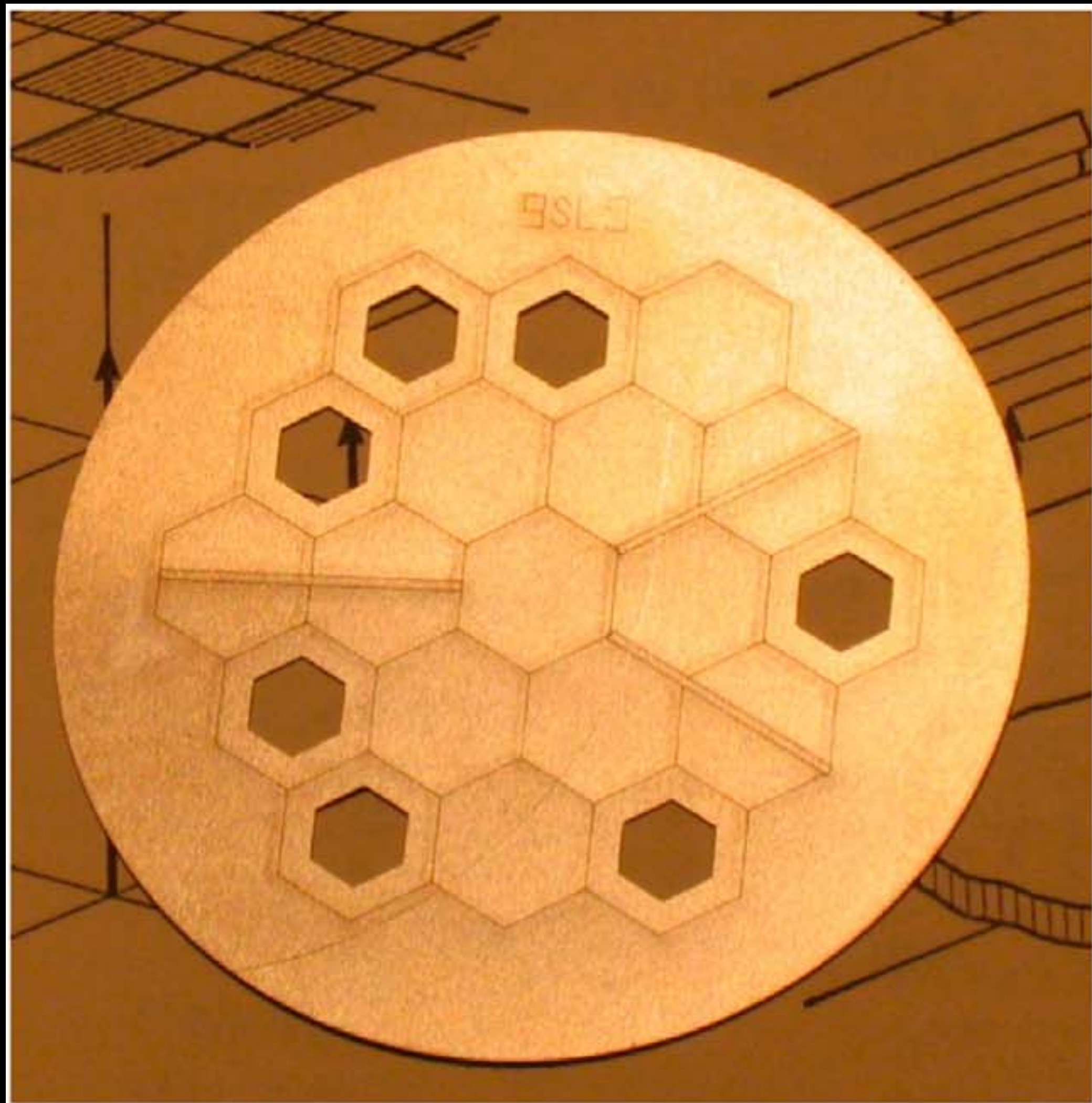
Holographic Aperture Masking



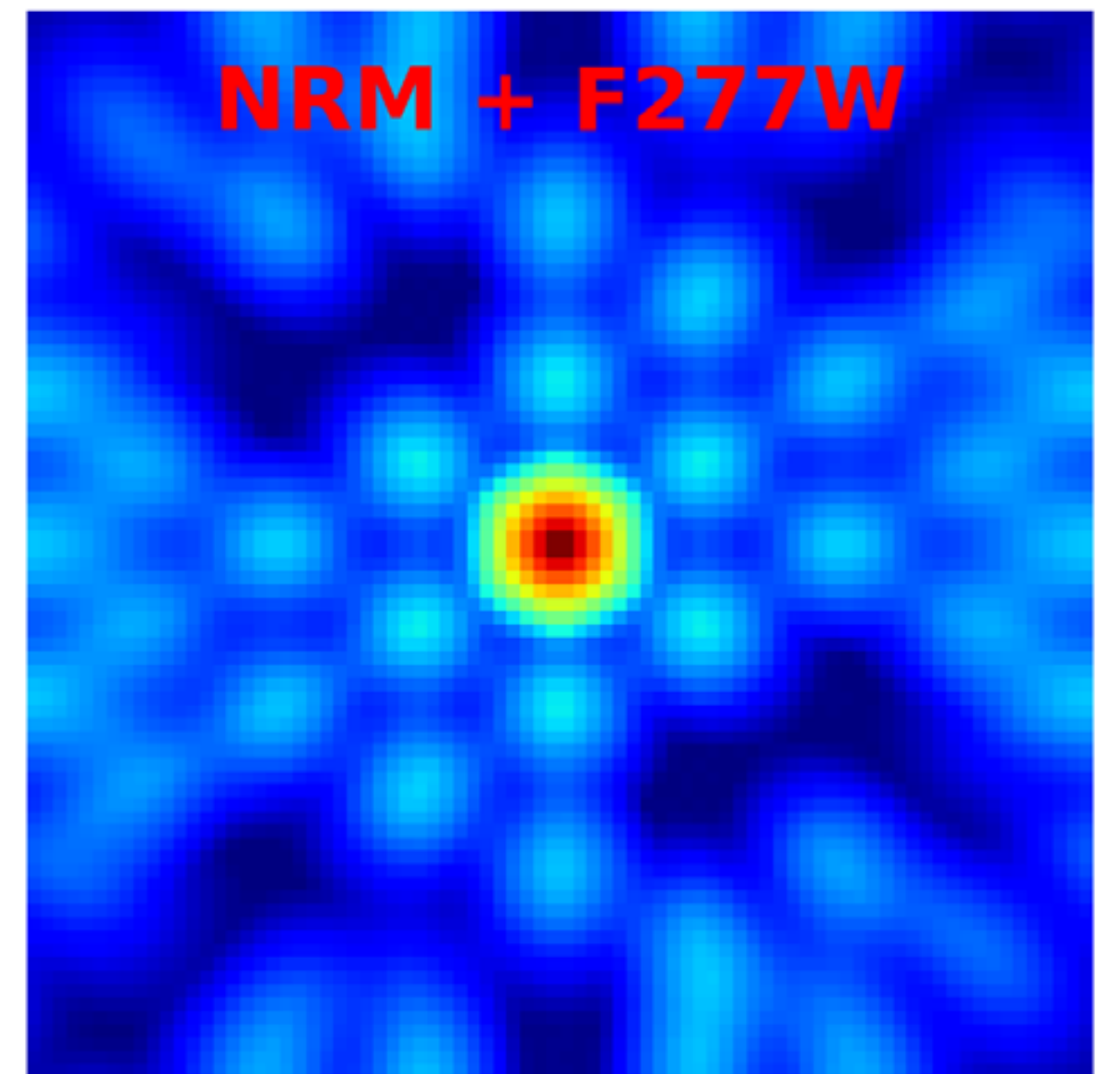
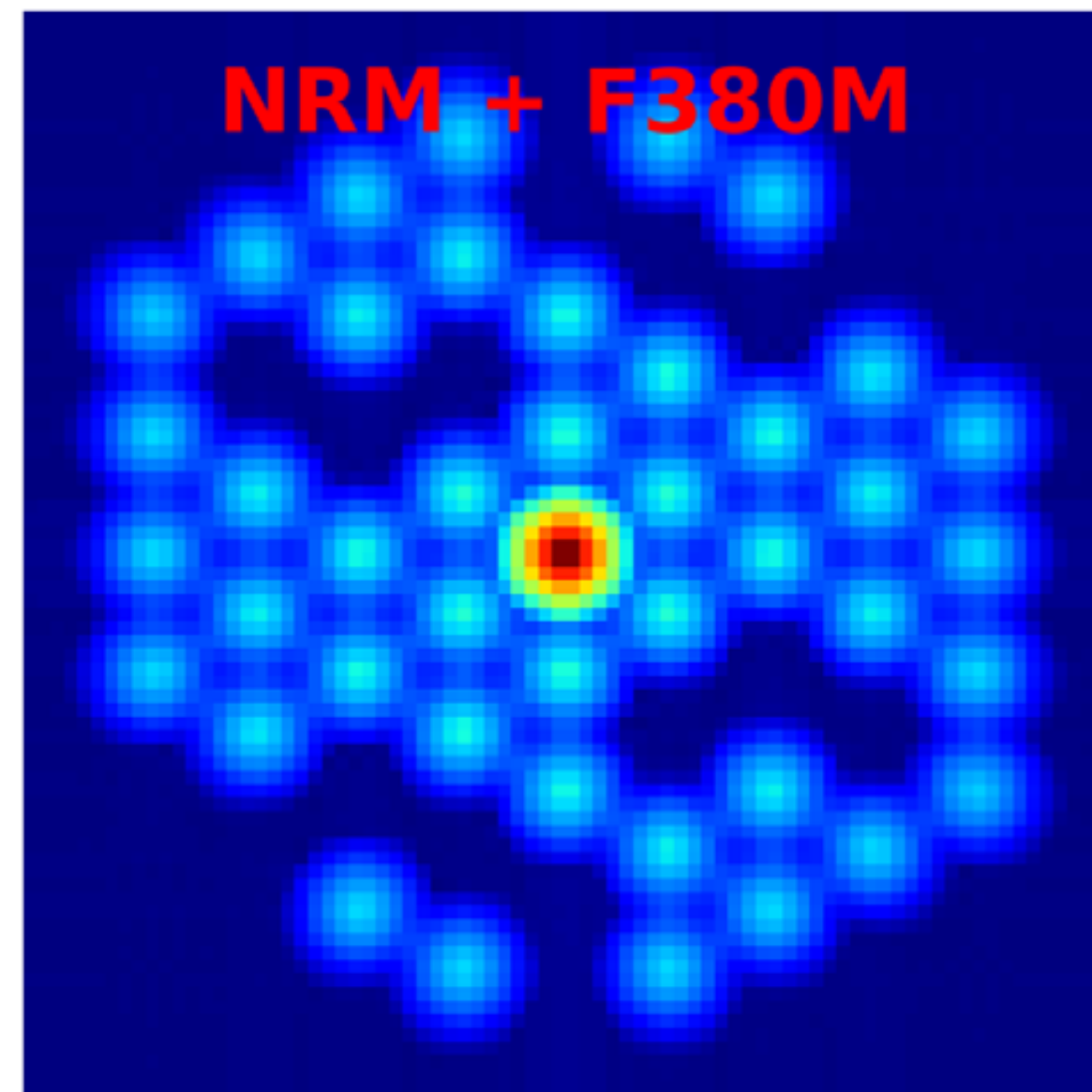
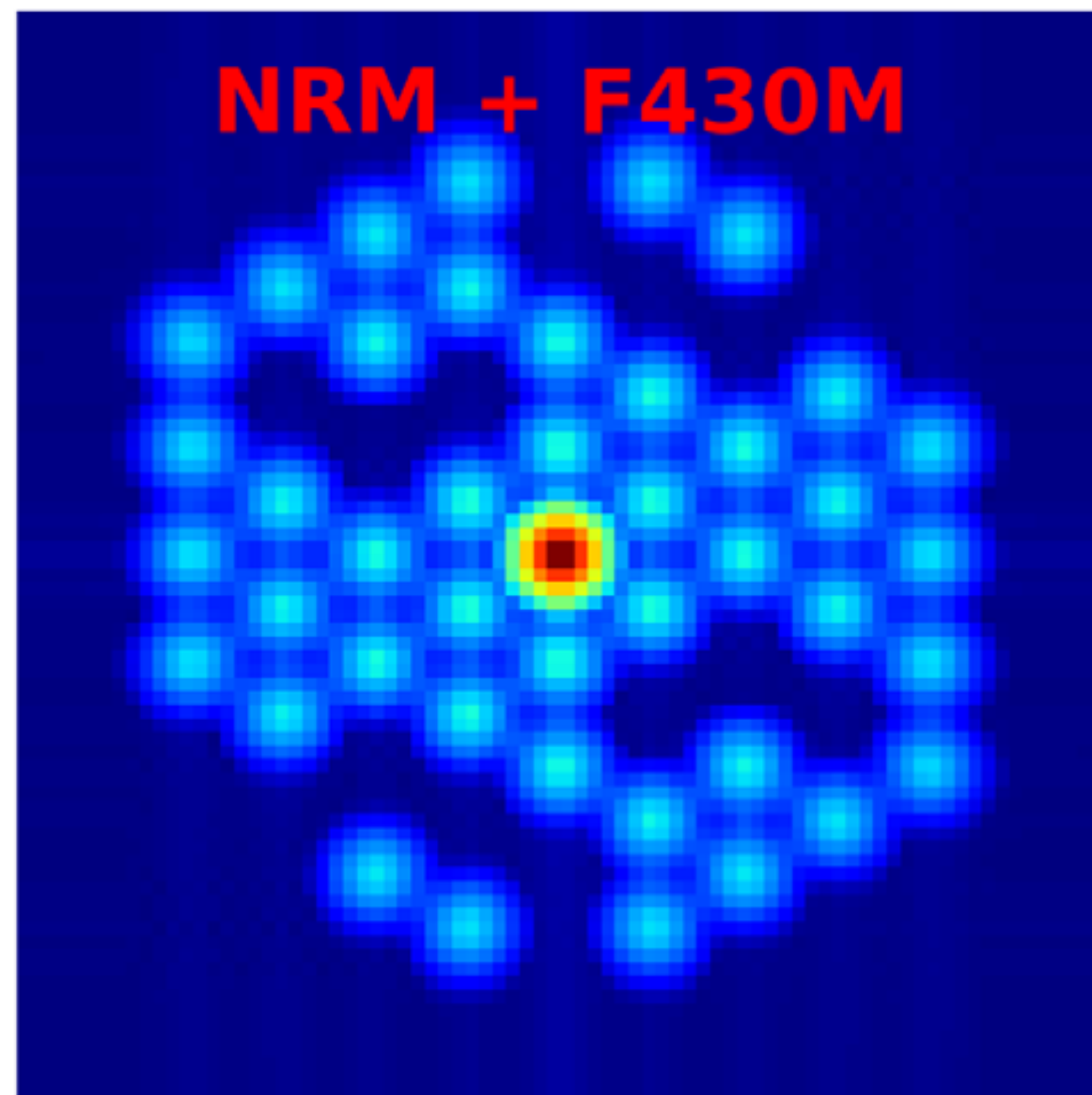
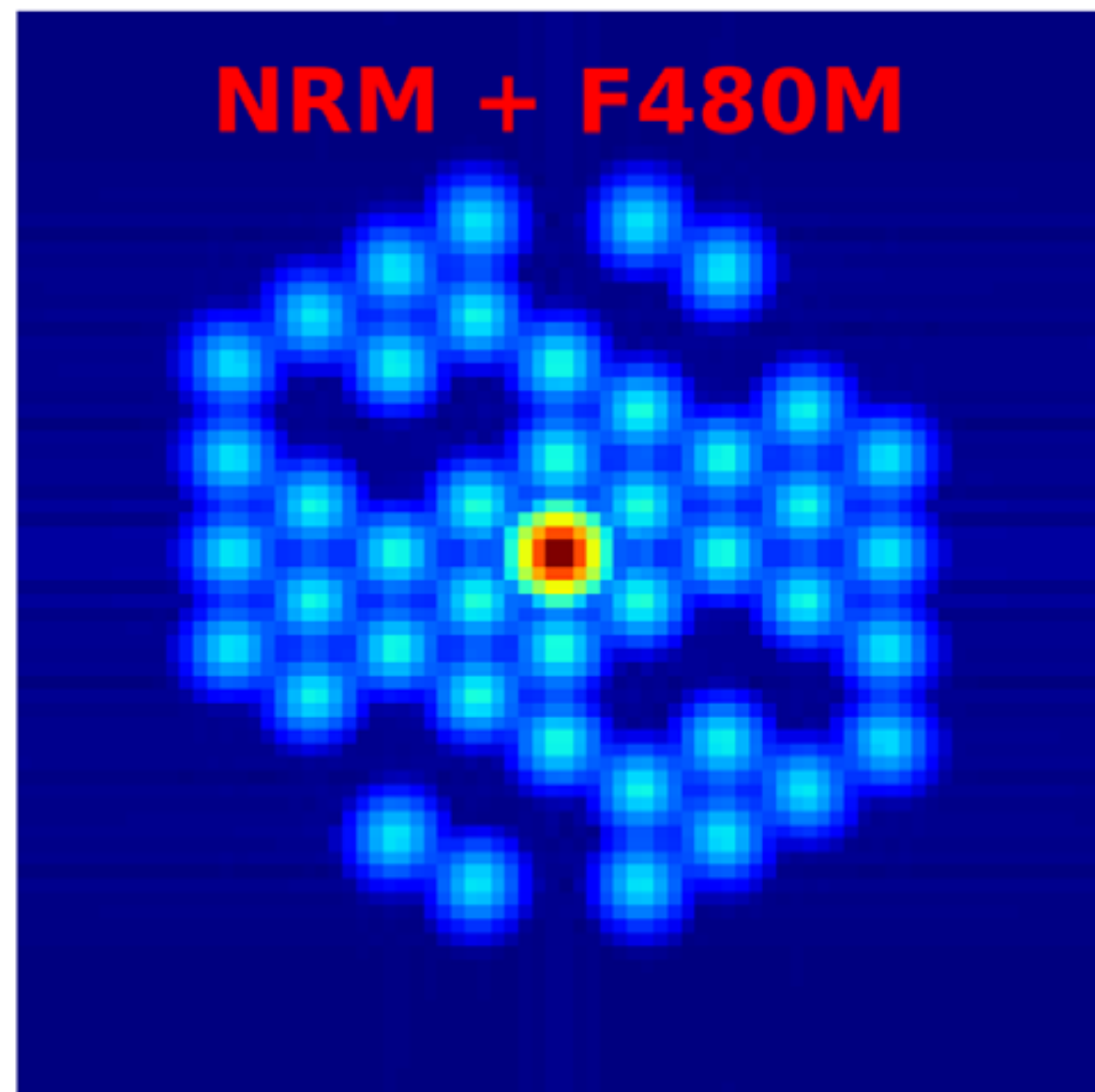
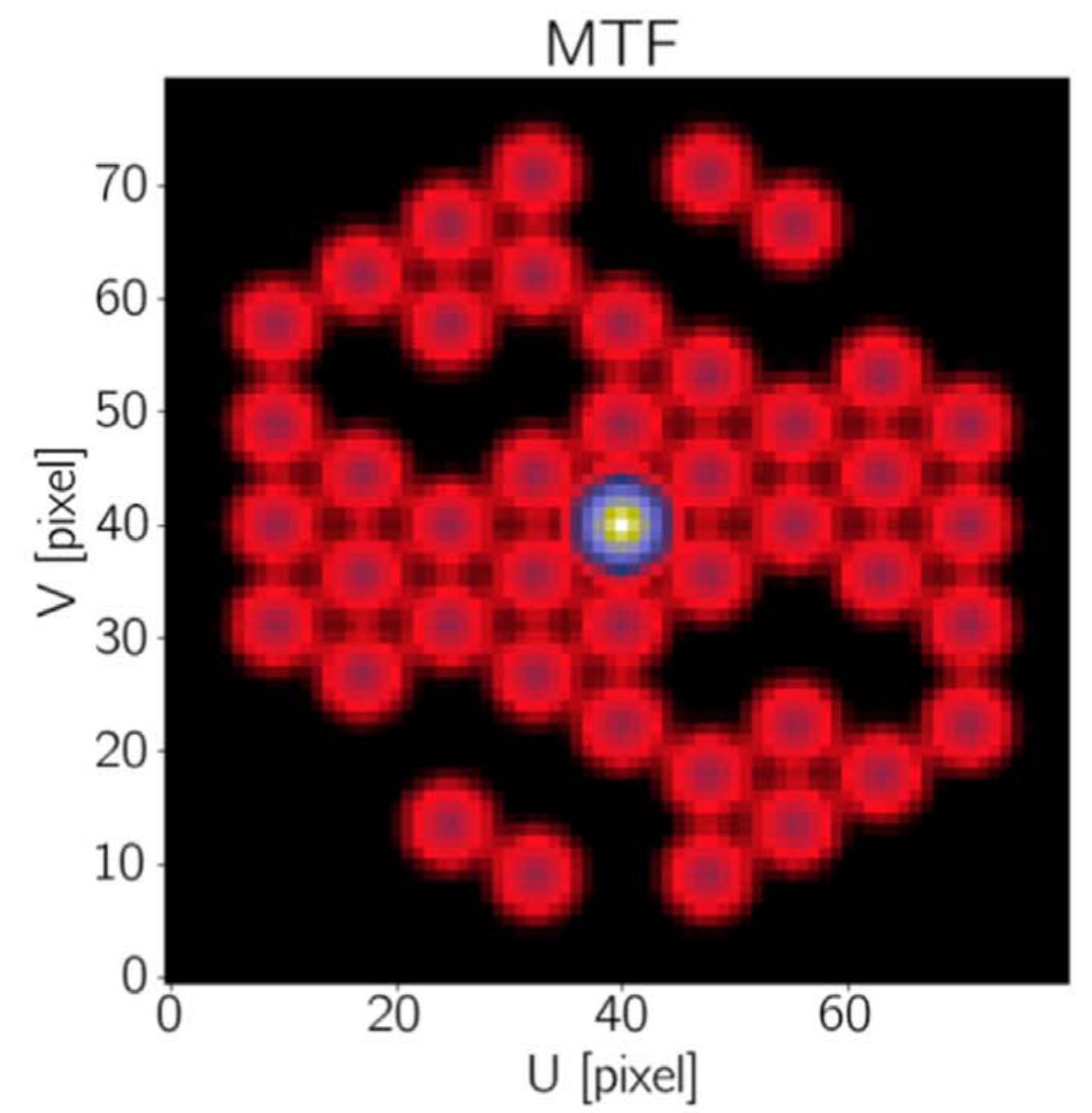
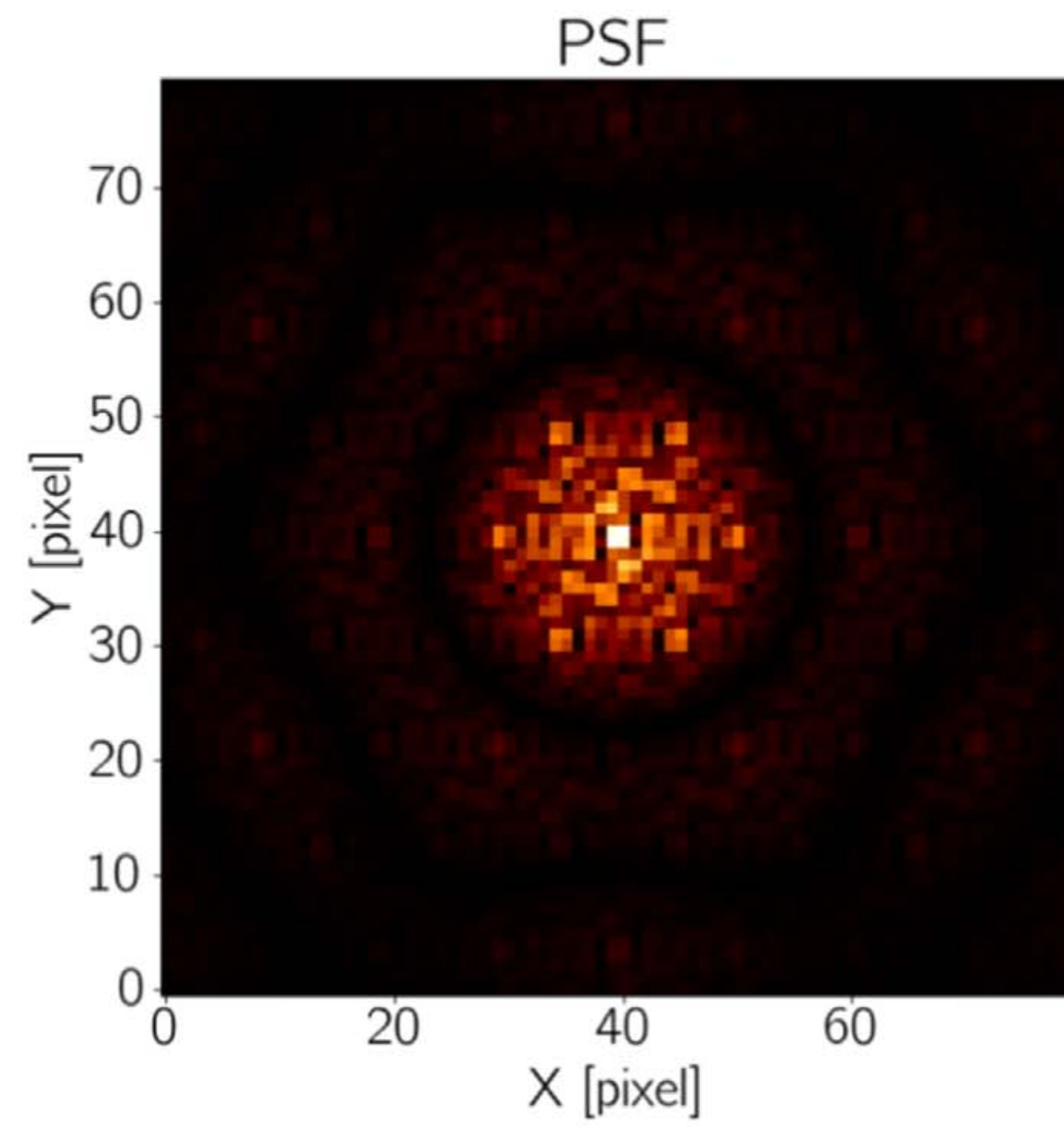
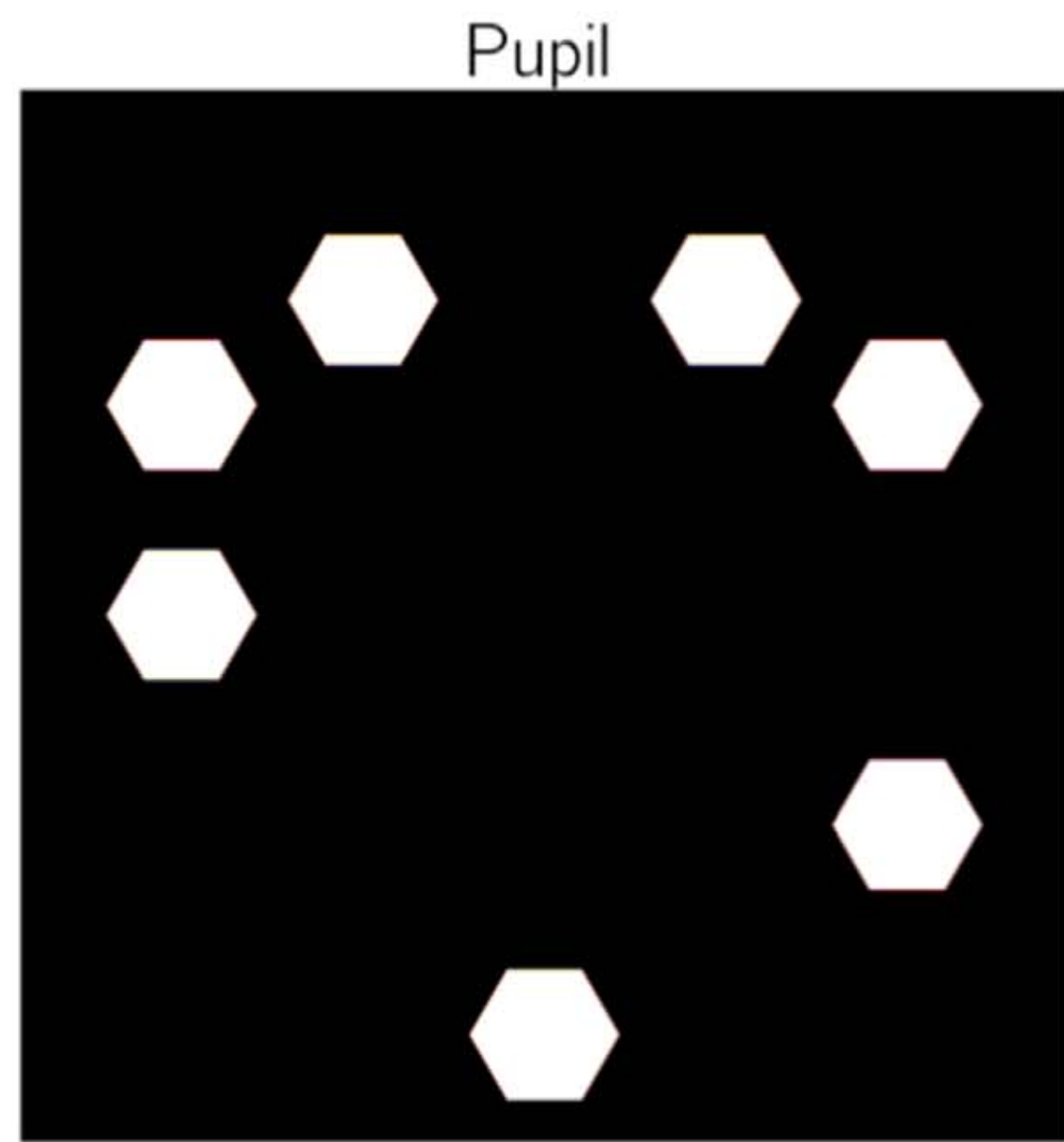
JWST/NIRISS AMI: The First O/IR Space Interferometer



NIRISS AMI

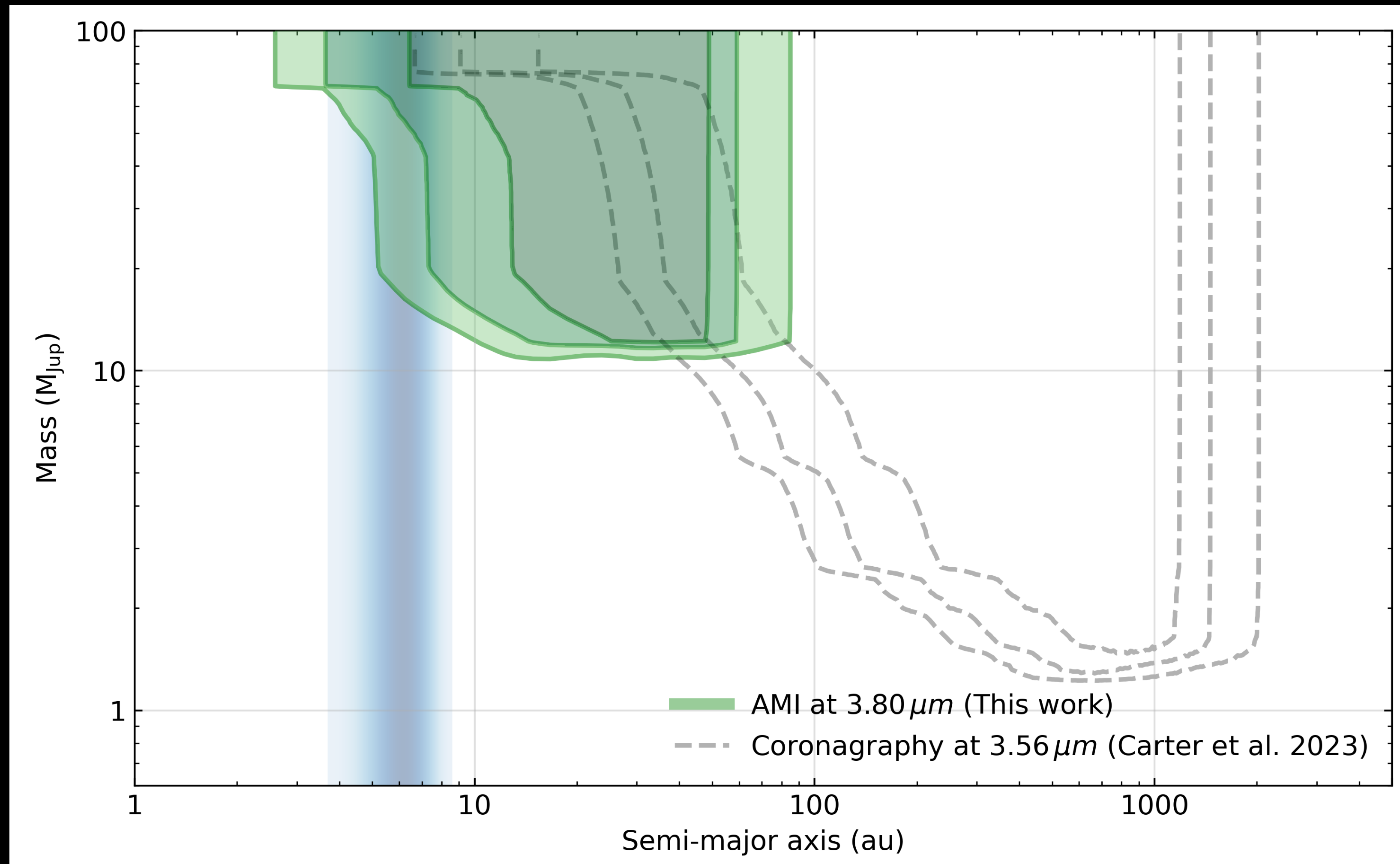


NIRISS AMI



Deep JWST AMI Mass Sensitivity

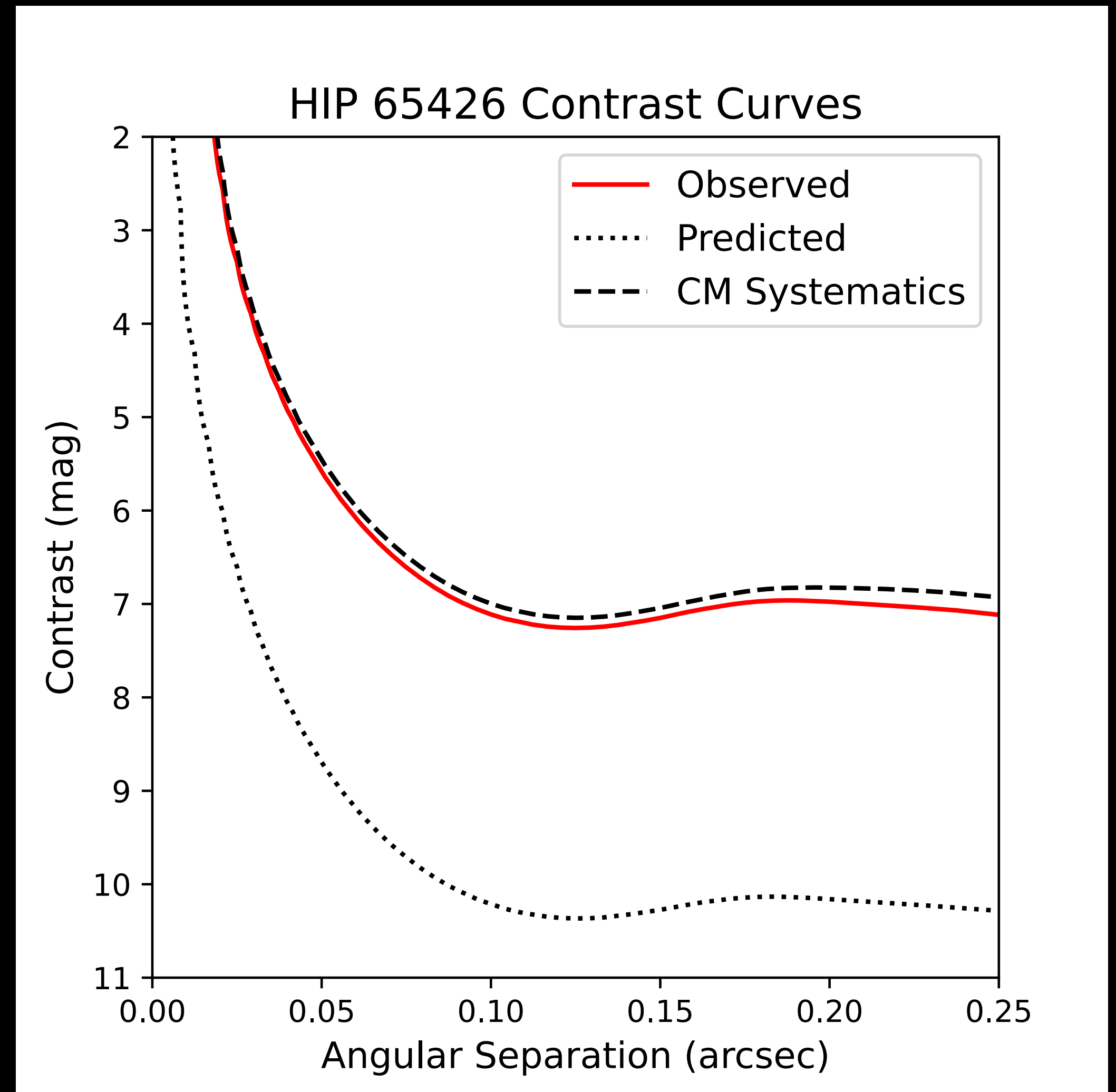
Comparison to NIRCcam Coronagraphy



ERS 1386 AMI Observed Contrast

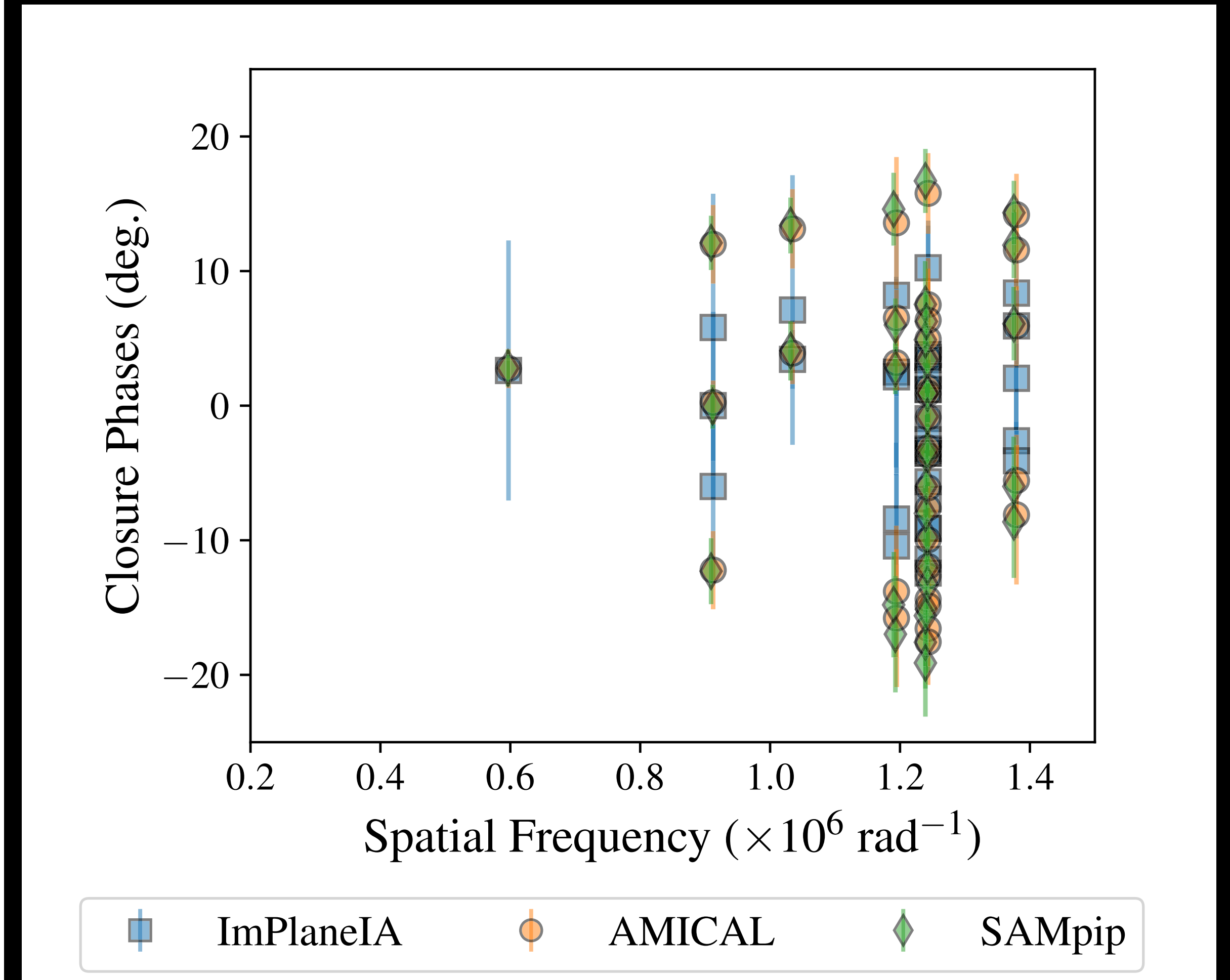
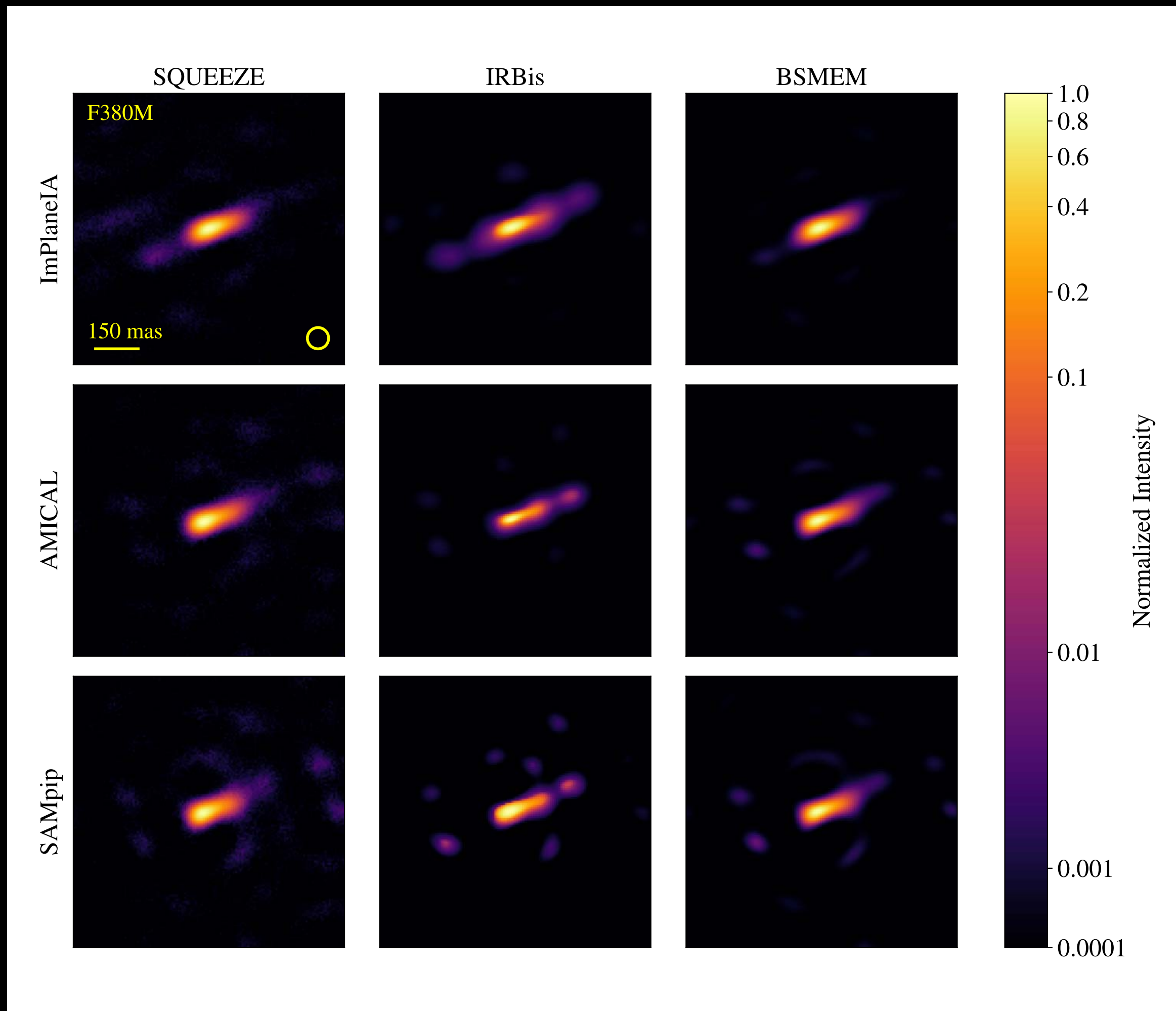
Comparison to Photon Noise Predictions

- Maximum contrast: ~ 7.2 mag at $\geq \lambda / D$
- Note: this is deeper than deep Keck/NIRC2 performance
- Expected contrast: ~ 10.5 mag at $\geq \lambda / D$
- Detector systematics (charge migration) can account for under-performance, and calibrations that eliminate charge migration bring you within a factor of a few of the photon noise floor!
- Observing strategy: look for flux-matched calibrators
- Careful calibration observations and computations in the works!

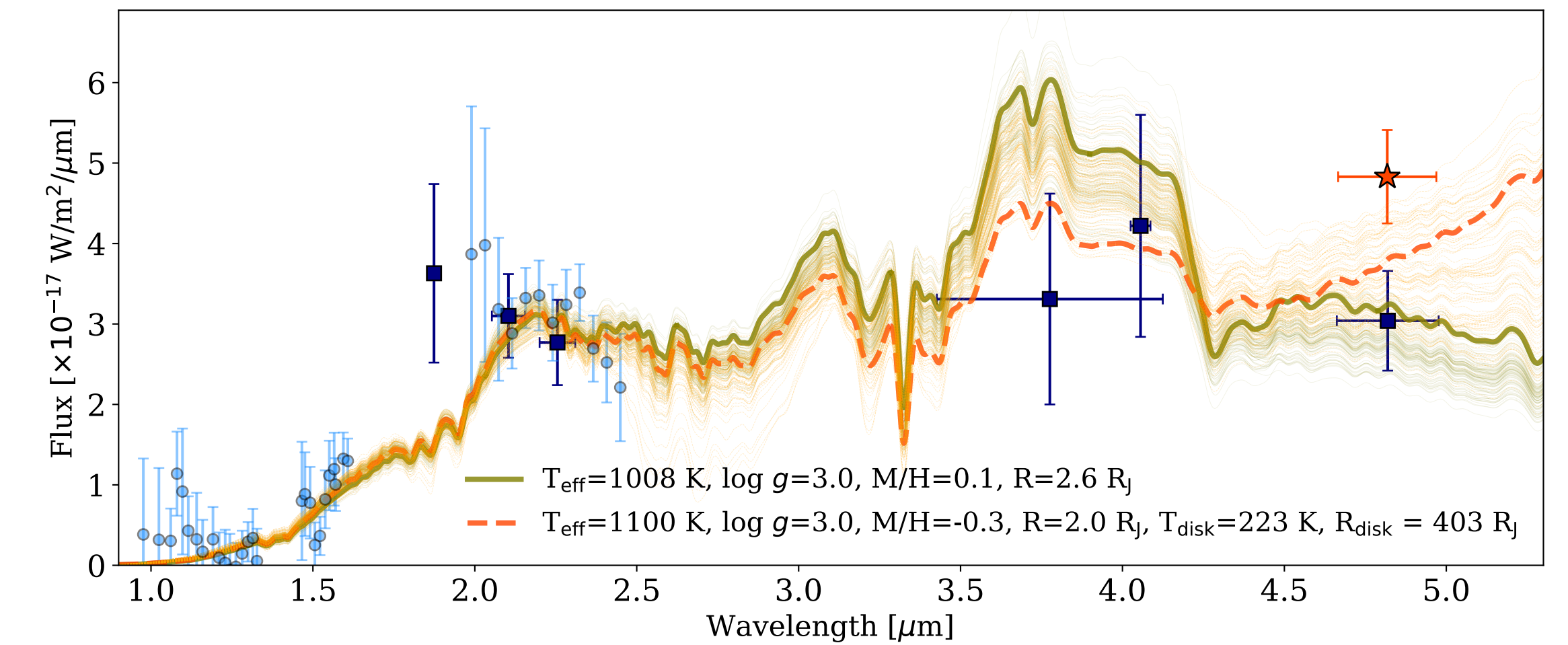
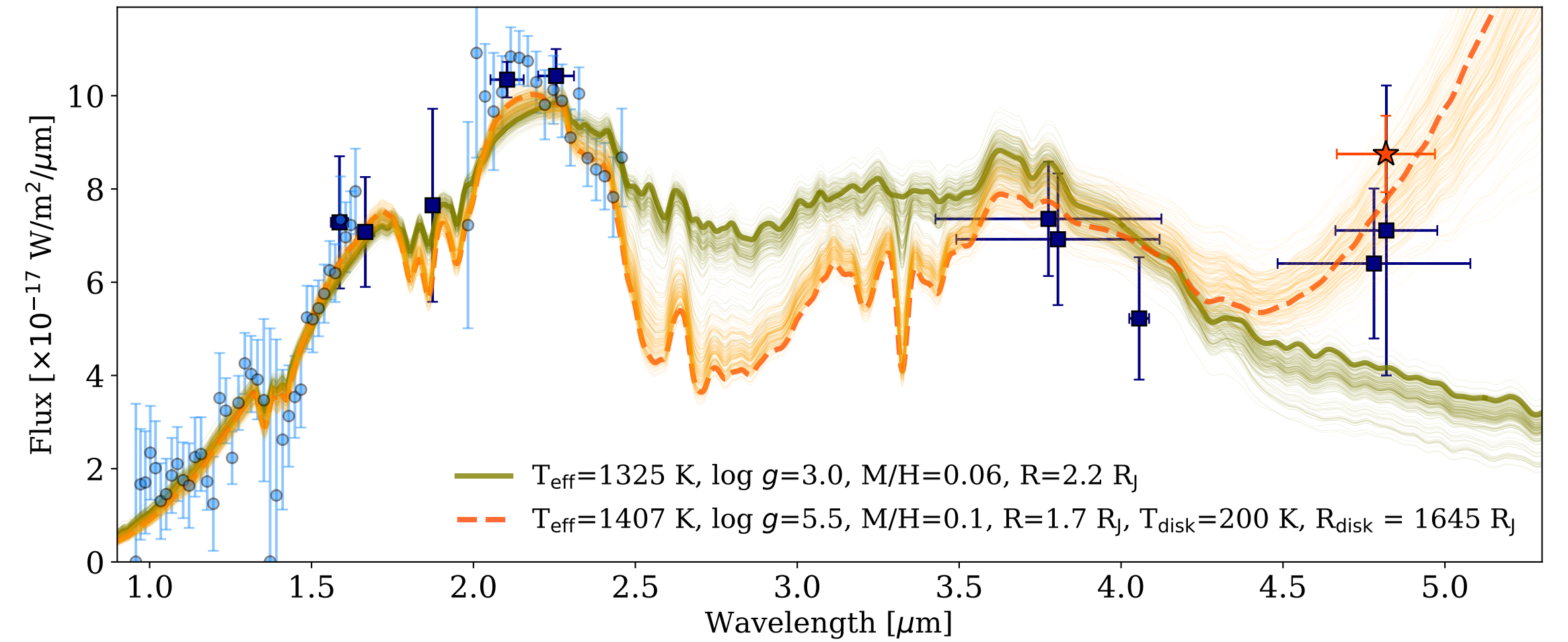
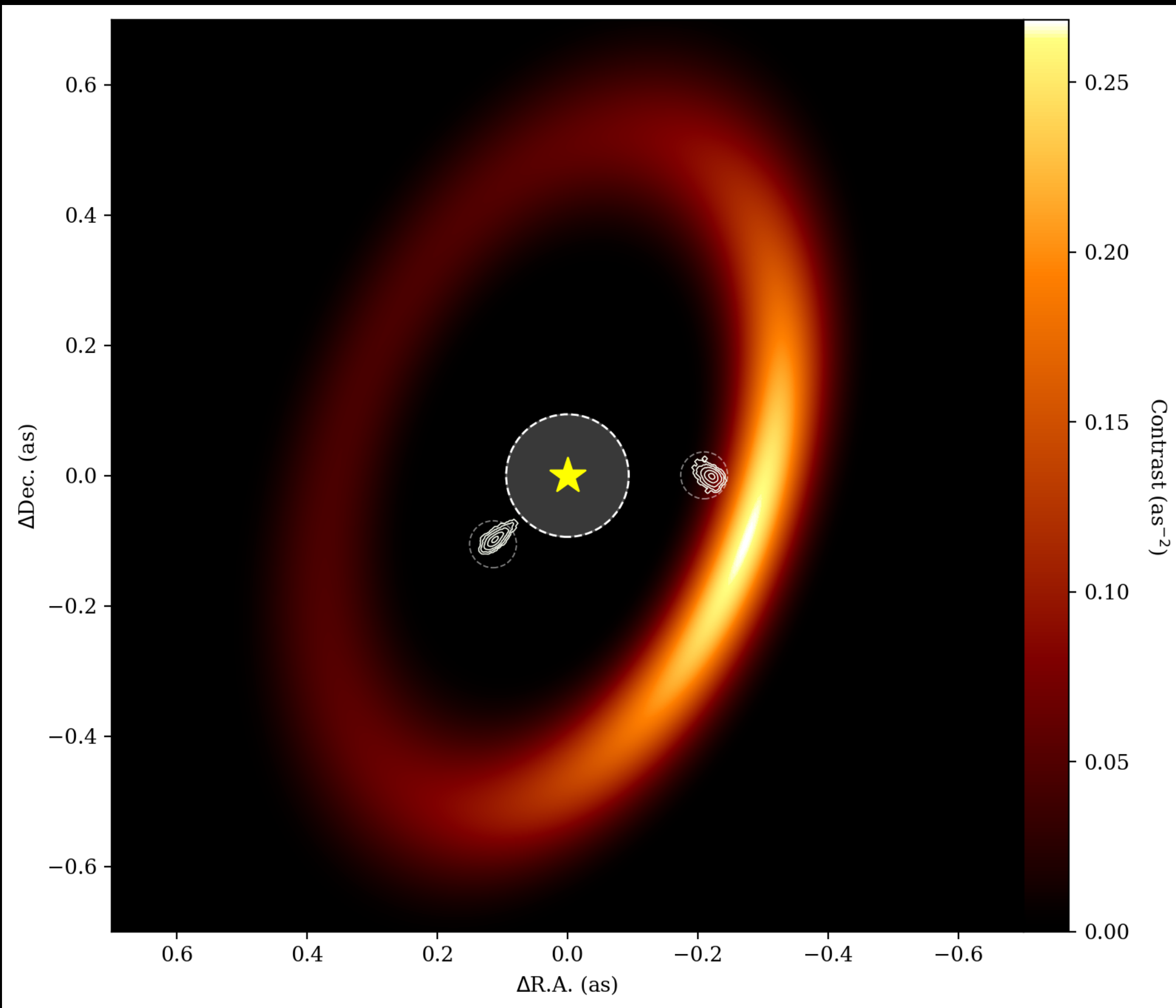


Resolving WR 137 with JWST AMI

Colliding Winds Plus Data Reduction and Image Reconstruction Tests

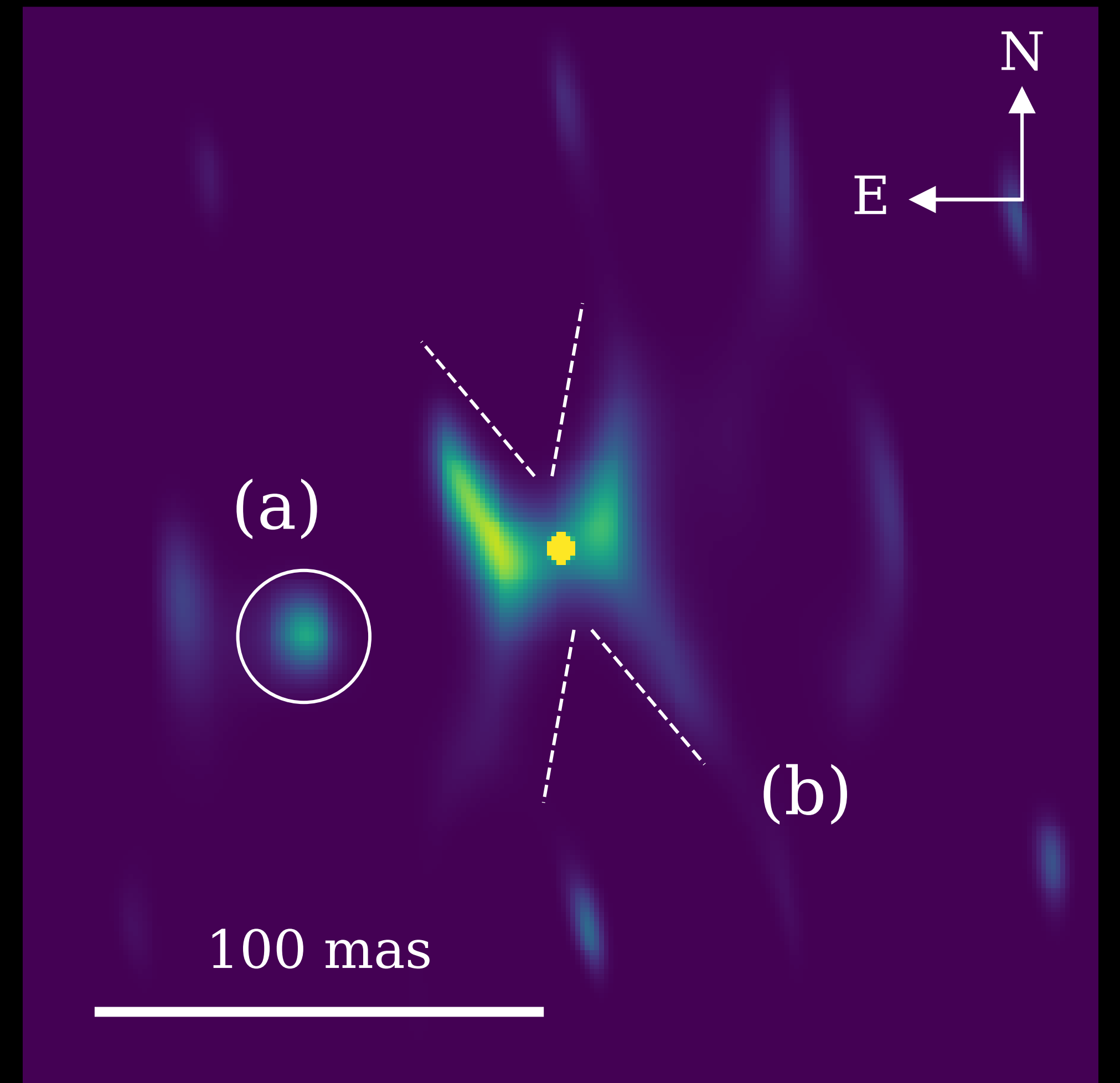
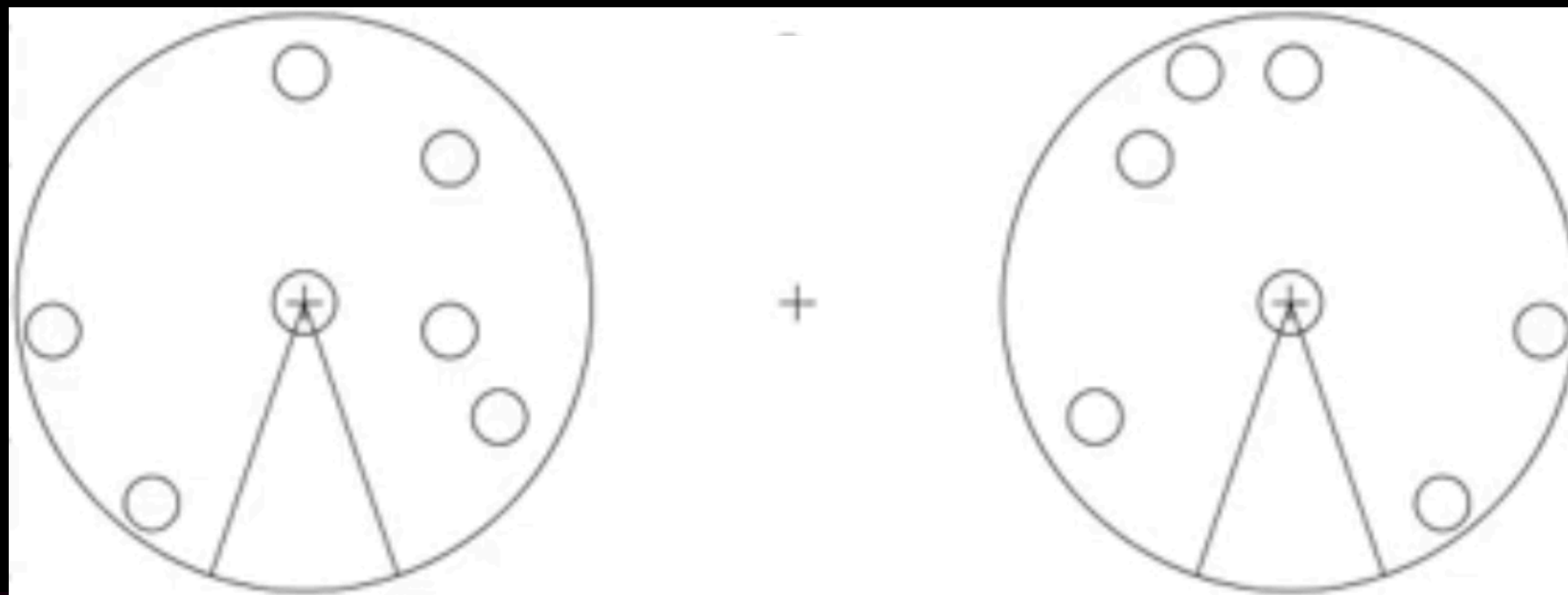


PDS 70 Observed by JWST/NIRISS AMI



Looking Ahead: AMI on the ELTs

- ELT facilities will have AMI modes, and tests with LBTI show that this is useful both scientifically and technically!



AMI Data Reduction Pipelines

Lots of Work, Some Pipeline Comparisons Thanks to *JWST*

- AMiCAL - Anthony Soulain - <https://github.com/SydneyAstrophotonicsInstrumentationLab/AMiCAL>
- ImplanelA - Alexandra Greenbaum - <https://github.com/agreenbaum/ImPlanelA>
- fouriever - Jens Kammerer - <https://github.com/kammerje/fouriever>
- SAMPip - Joel Sánchez Bermúdez - <https://cosmosz5.github.io/CASSINI/SAMPip/>
- SAMpy - Steph Sallum - <https://github.com/JWST-ERS1386-AMI/SAMpy>
- XARA - Frantz Martinache - <https://github.com/fmartinache/xara>
- ARGUS - Sam Factor - <https://github.com/smfactor/Argus>

A Handful of Interferometry and AMI References

- Lawson 2000, Principles of Long Baseline Stellar Interferometry, <https://ecommons.cornell.edu/items/8892b20f-eeb0-4dae-a845-ab1c53a31d19>
- Tuthill et al. 2000, Michelson Interferometry with the Keck I Telescope, <https://ui.adsabs.harvard.edu/abs/2000PASP..112..555T/abstract>
- Ireland 2013, Phase errors in diffraction-limited imaging: contrast limits for sparse aperture masking, <https://ui.adsabs.harvard.edu/abs/2013MNRAS.433.1718I/abstract>
- Martinache 2010, Kernel Phase in Fizeau Interferometry, <https://ui.adsabs.harvard.edu/abs/2010ApJ...724..464M/abstract>
- Tuthill 2012, The unlikely rise of masking interferometry: leading the way with 19th century technology, <https://ui.adsabs.harvard.edu/abs/2012SPIE.8445E..02T/abstract>

Thanks!