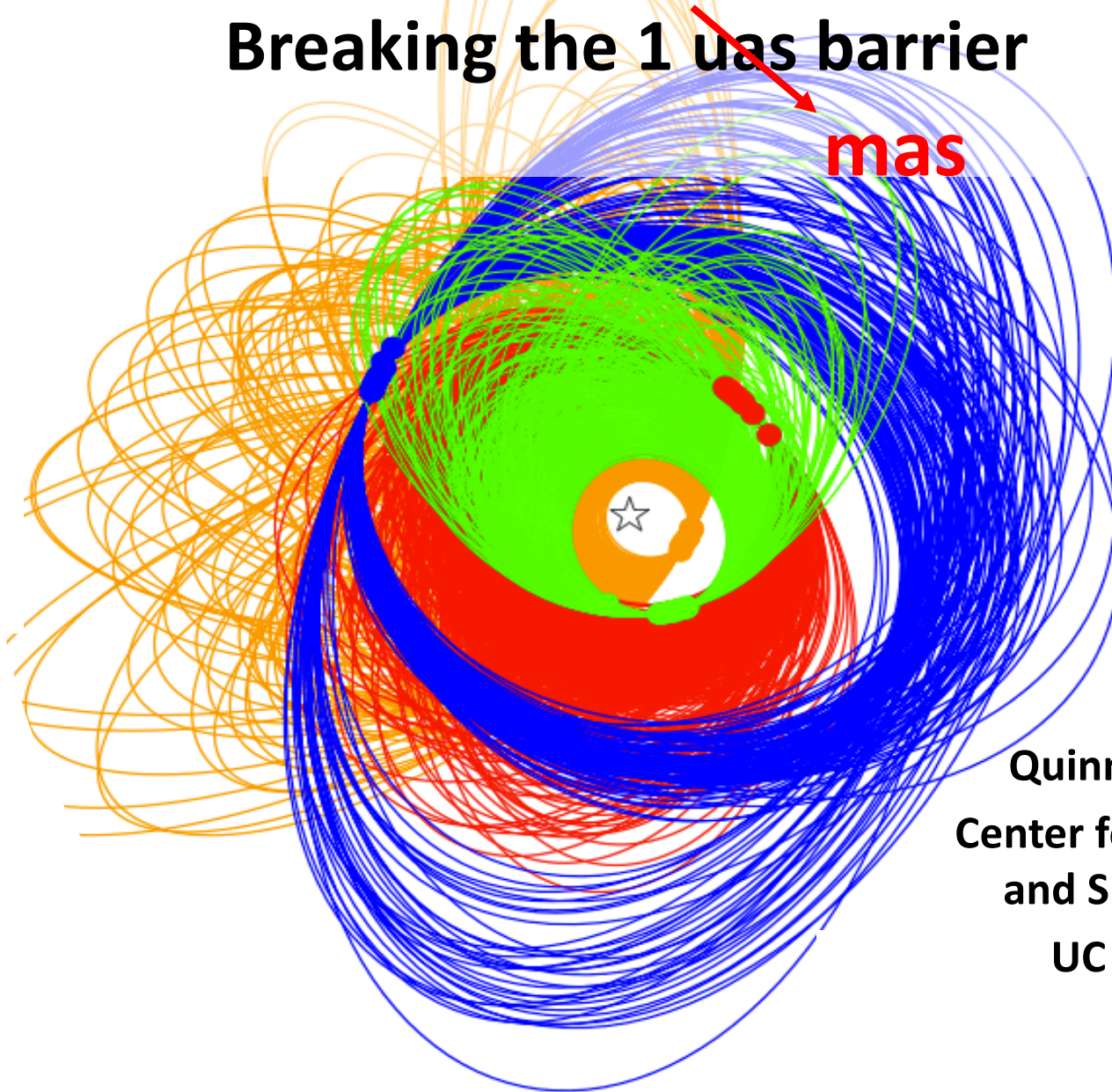


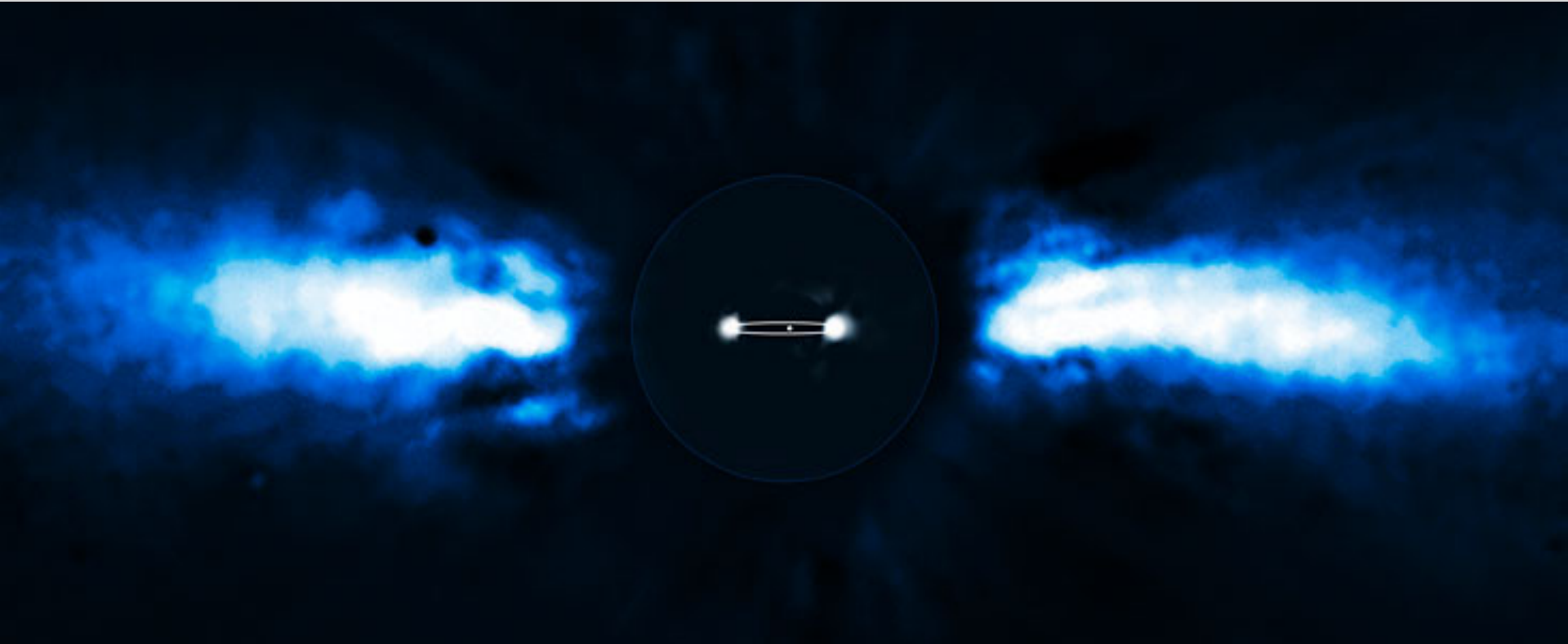
# Combining Astrometry and Direct Imaging:

## Breaking the 1 $\mu$ as barrier



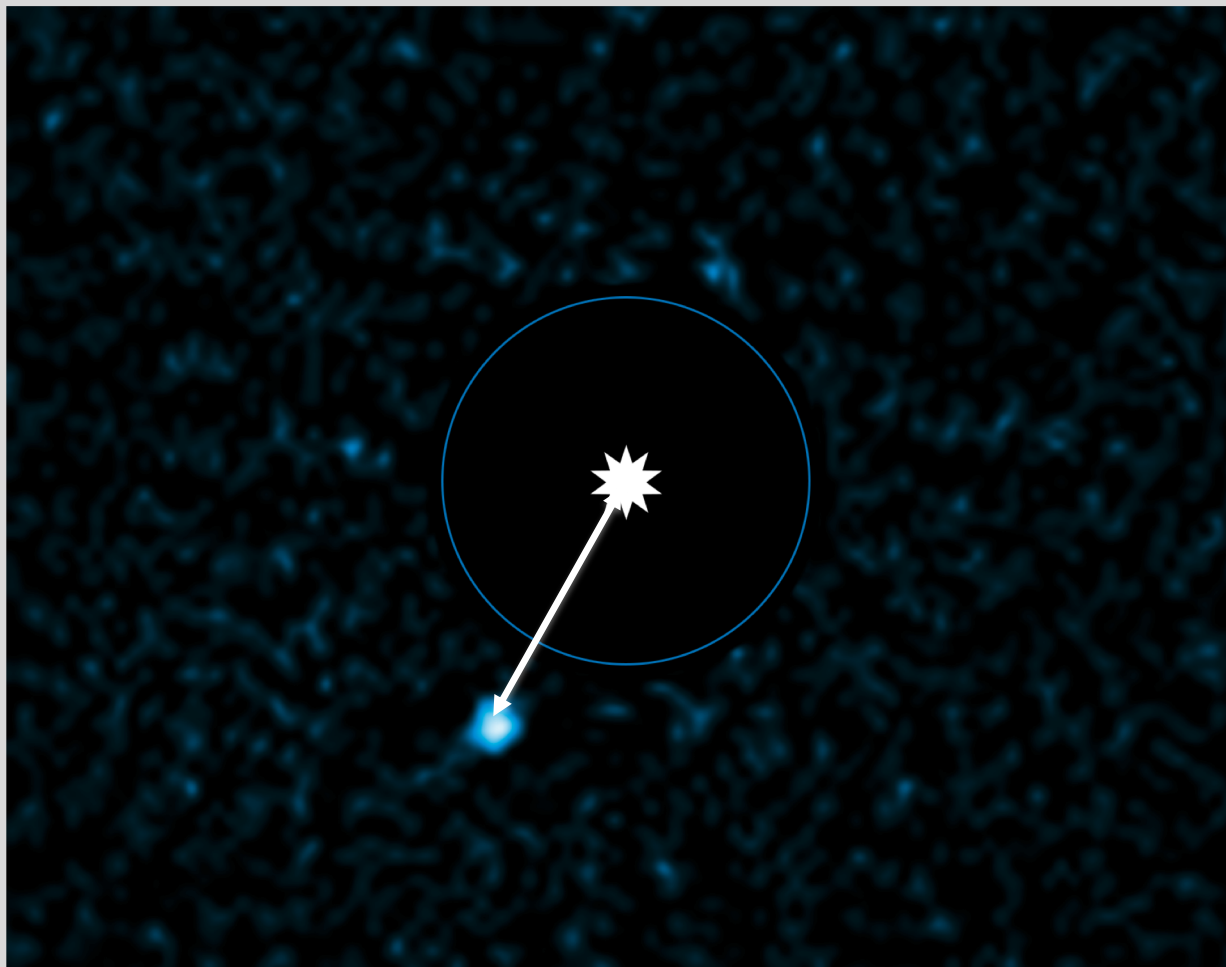
Quinn Konopacky  
Center for Astrophysics  
and Space Science  
UC San Diego

**Understanding the orbital properties of directly imaged planets can provide powerful constraints on their evolution.**



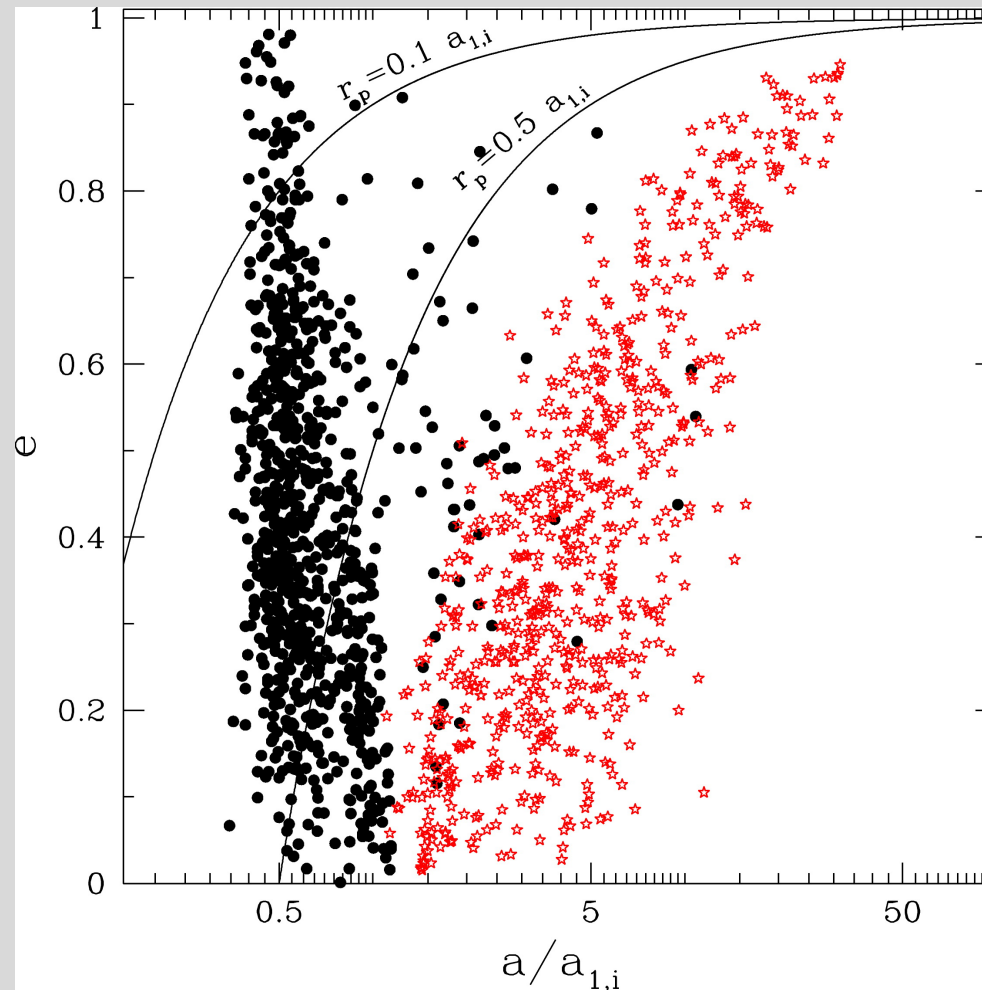
ESO

**Astrometric (positional) measurements of directly imaged planets are used to confirm their association with the star and to learn about their orbits.**



**HD 95086b (VLT/NACO)  
Rameau et al. 2013**

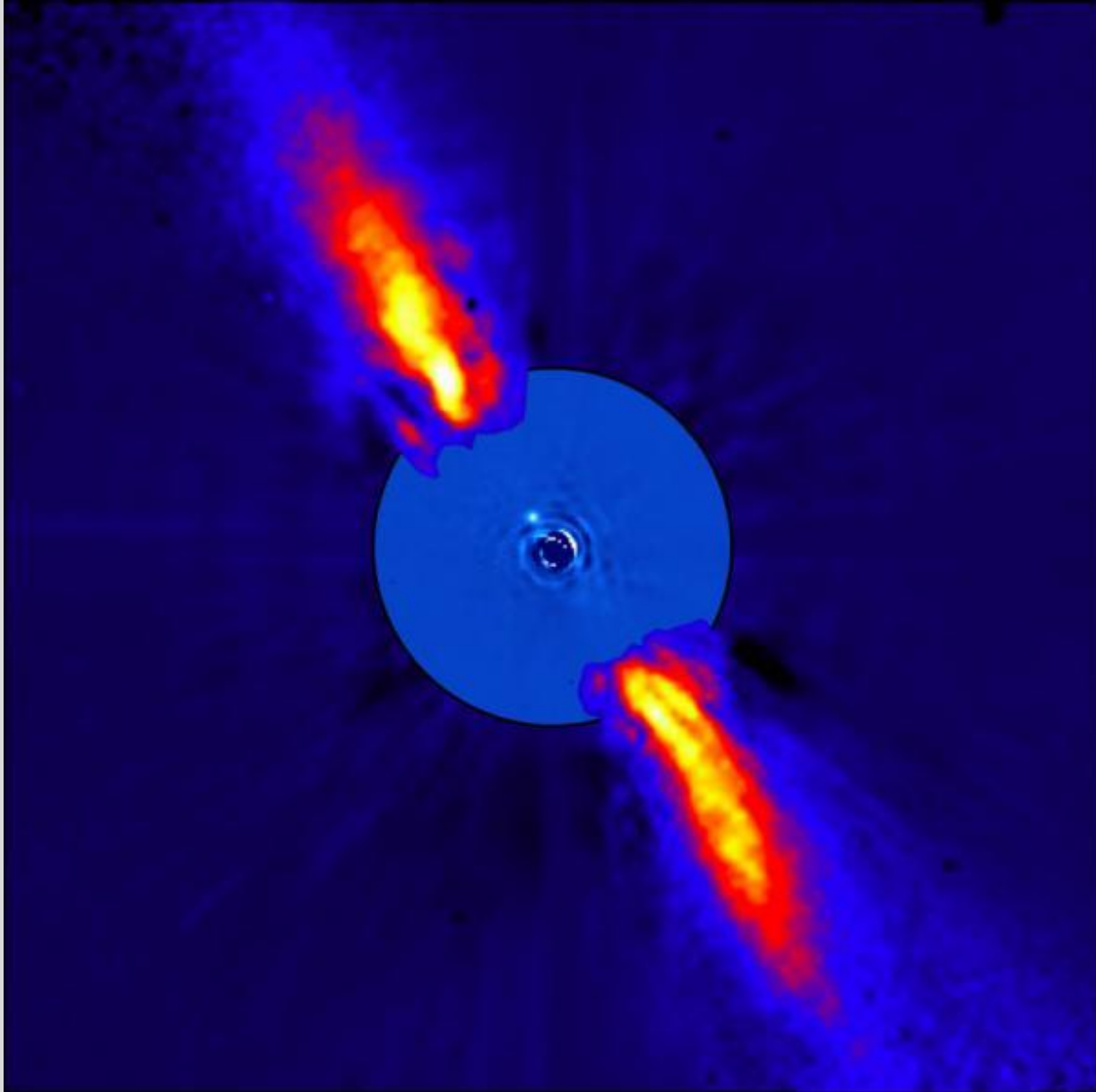
Orbital eccentricities can be used as a tracer of formation or subsequent dynamical processes.



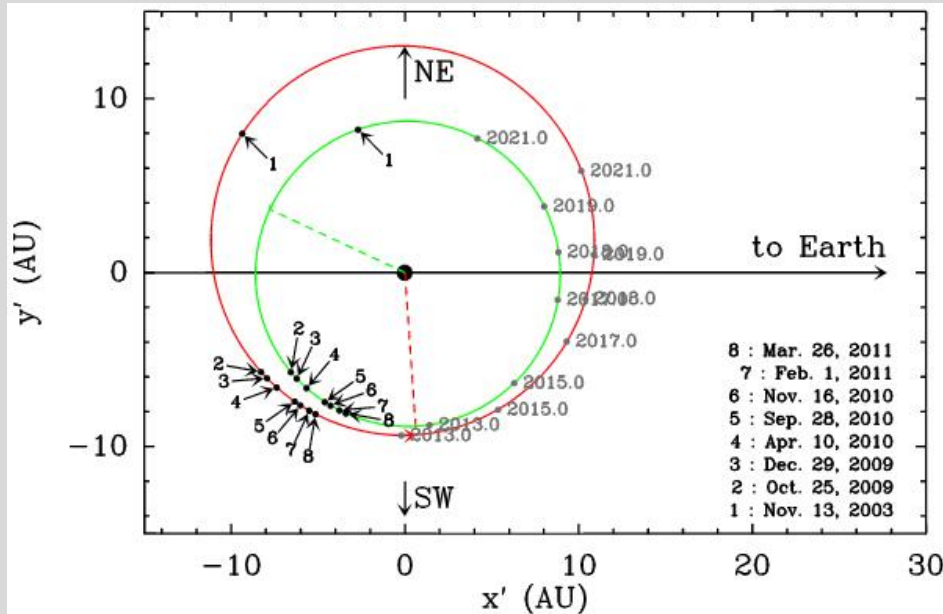
Chatterjee et al. 2008

Orbital information can highlight when interesting events may occur in a system – e.g., the  $\beta$  Pic transit.

Lagrange et al. 2009

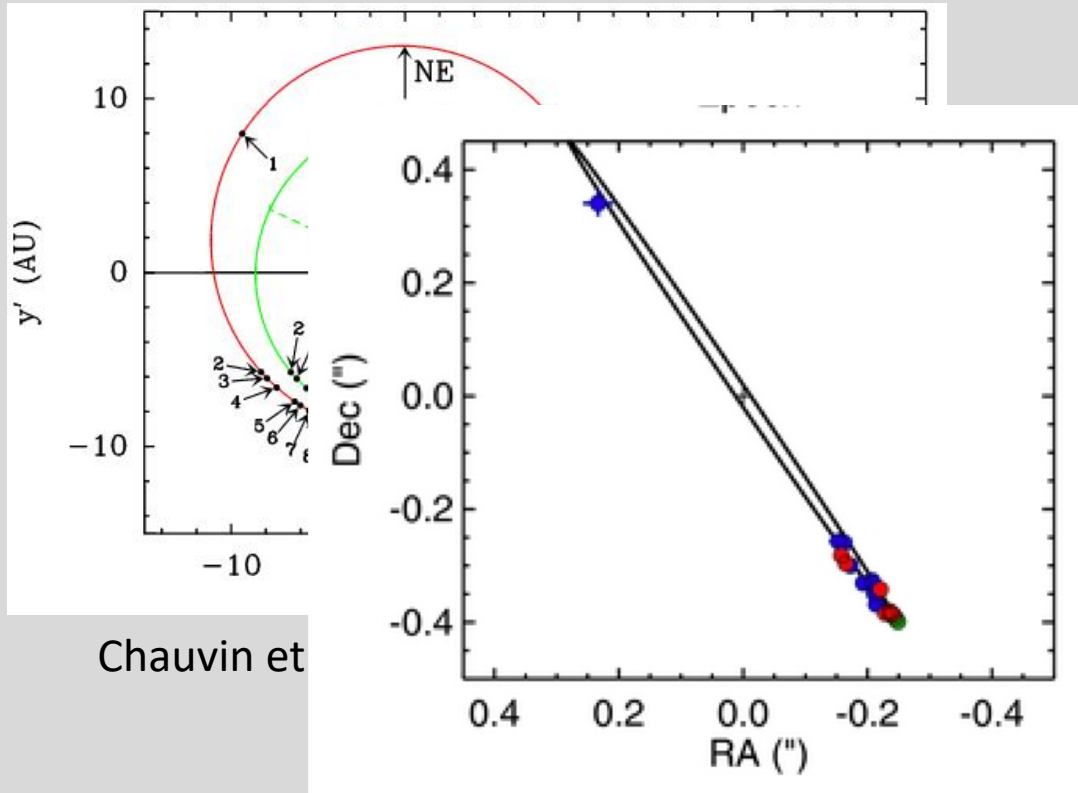


Orbital information can highlight when interesting events may occur in a system – e.g., the  $\beta$  Pic transit.



Chauvin et al. 2012 – Allowed with  $1 \sigma$

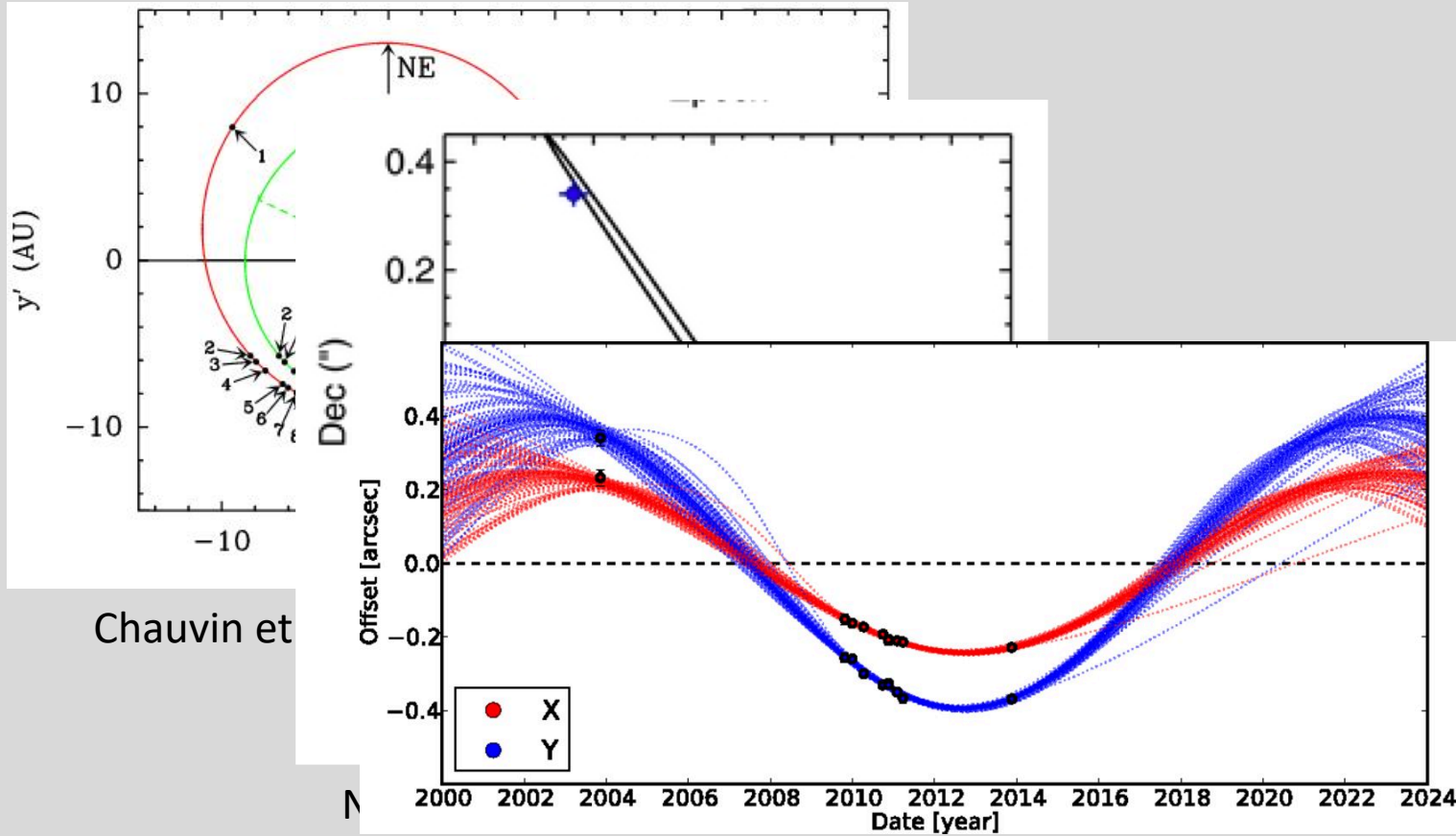
Orbital information can highlight when interesting events may occur in a system – e.g., the  $\beta$  Pic transit.



Chauvin et

Nielsen et al. 2014 – Allowed with  $1 \sigma$

Orbital information can highlight when interesting events may occur in a system – e.g., the  $\beta$  Pic transit.

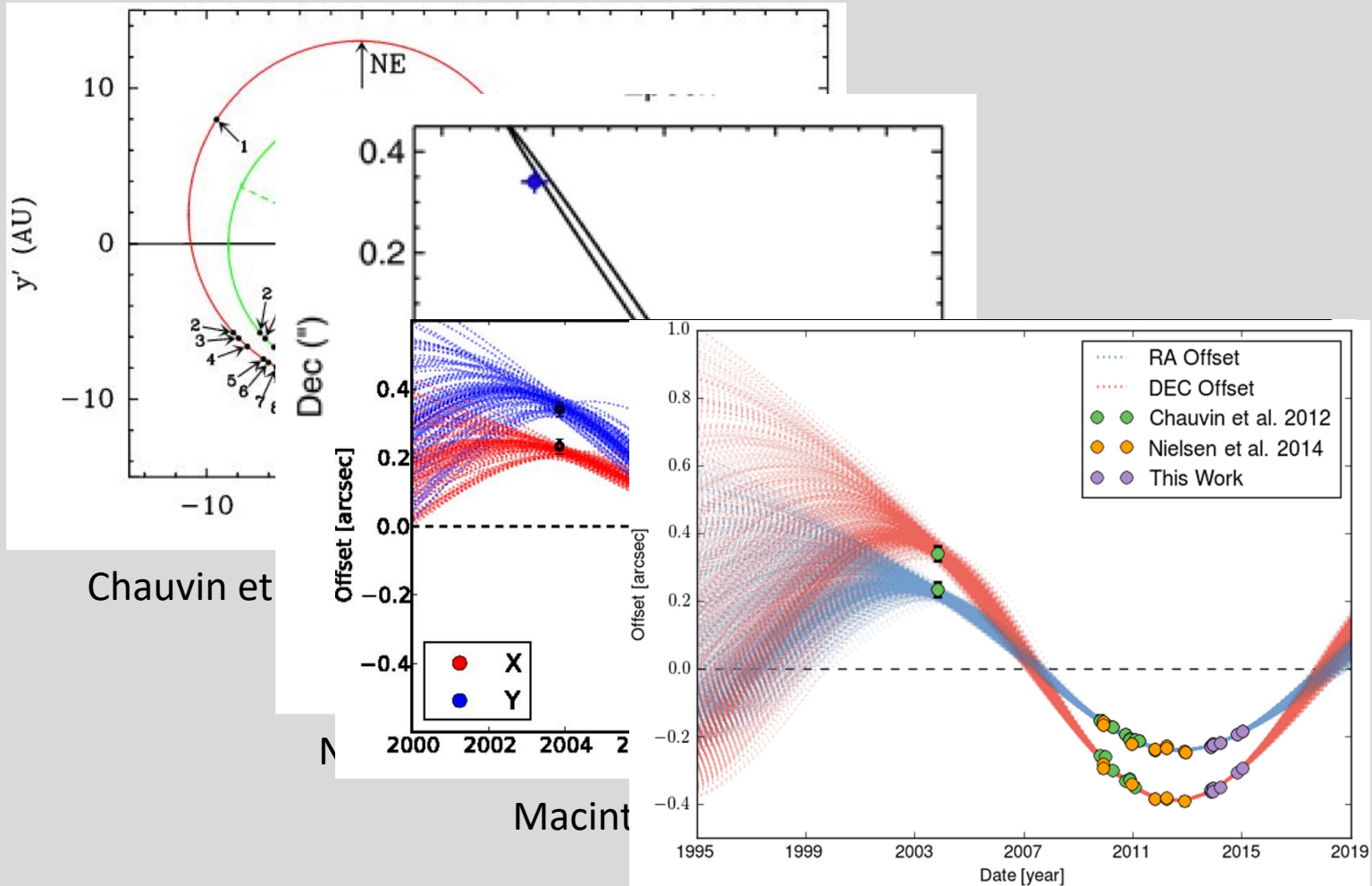


Chauvin et

Macintosh et al. 2014 – 4% transit probability



# Orbital information can highlight when interesting events may occur in a system – e.g., the $\beta$ Pic transit.



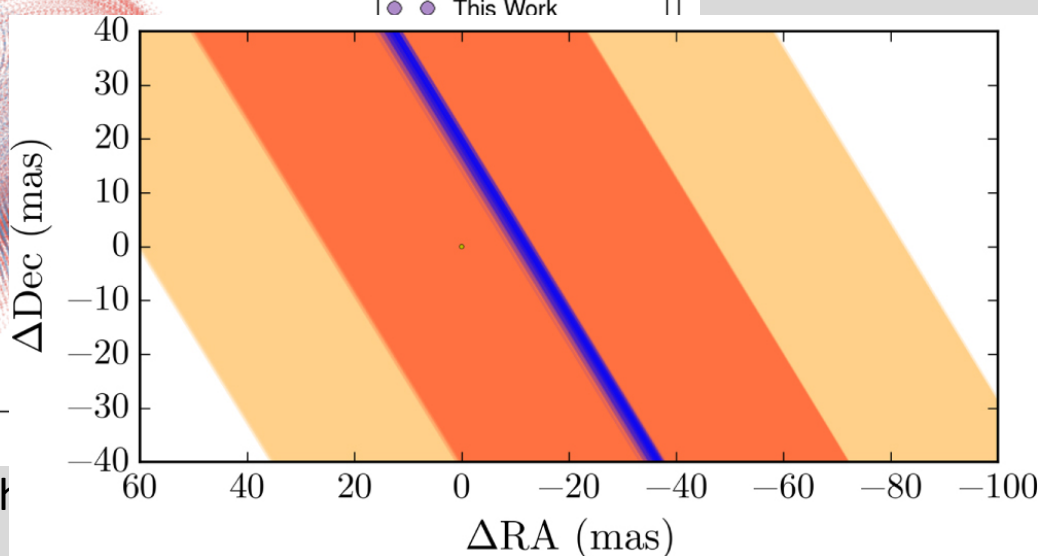
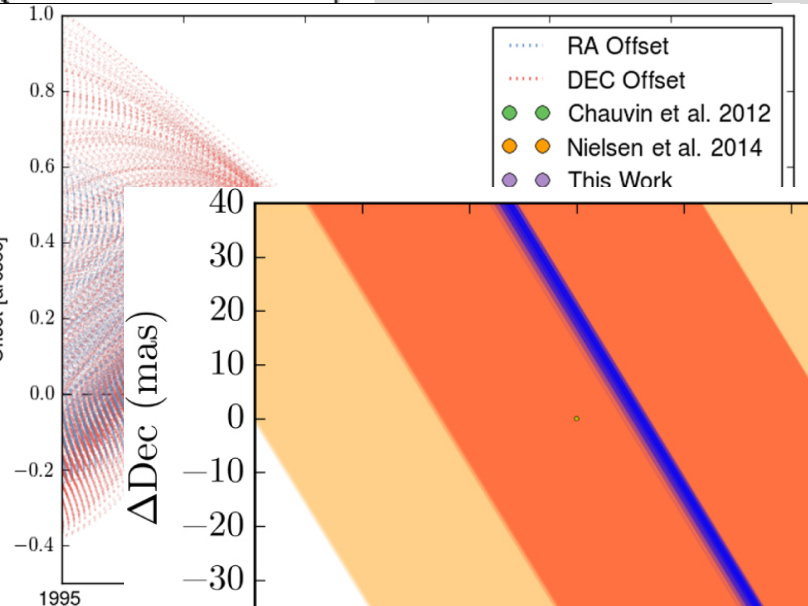
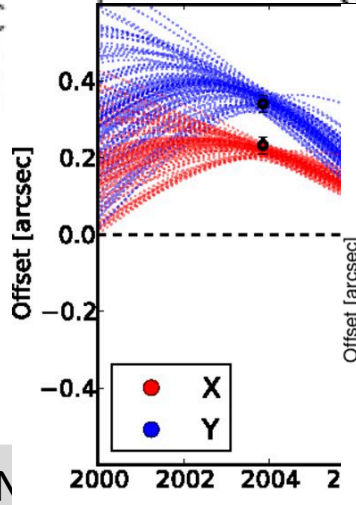
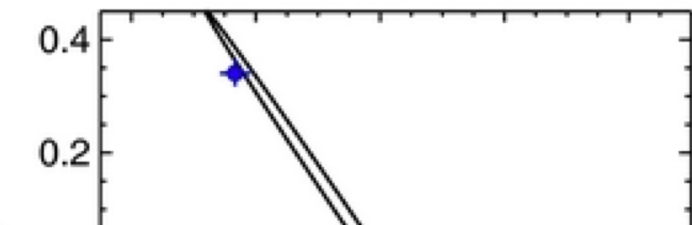
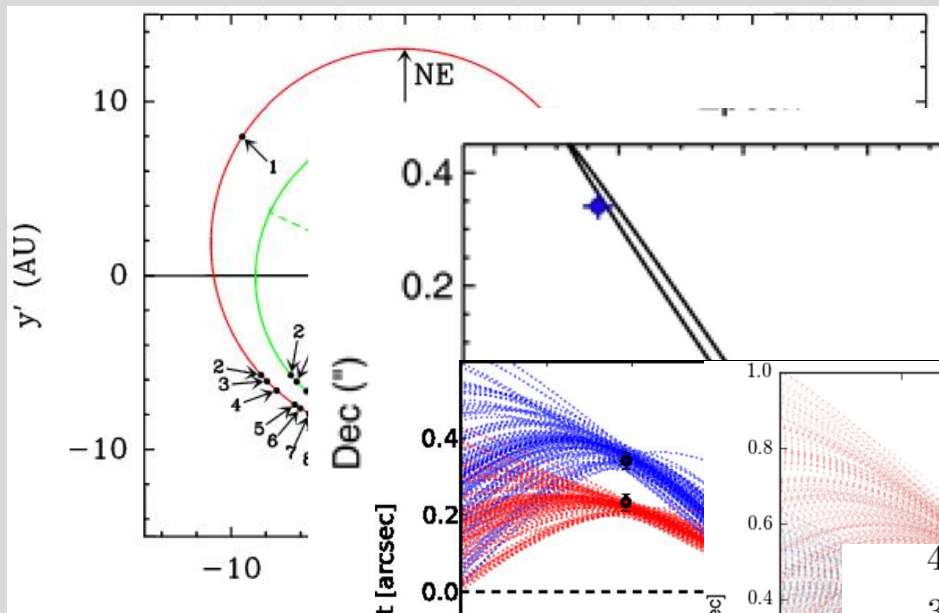
Chauvin et

N

Macint

Millar-Blanchaer et al. 2015 – 0.06% transit probability

Orbital information can highlight when interesting events may occur in a system – e.g., the  $\beta$  Pic transit.



Chauvin et

N

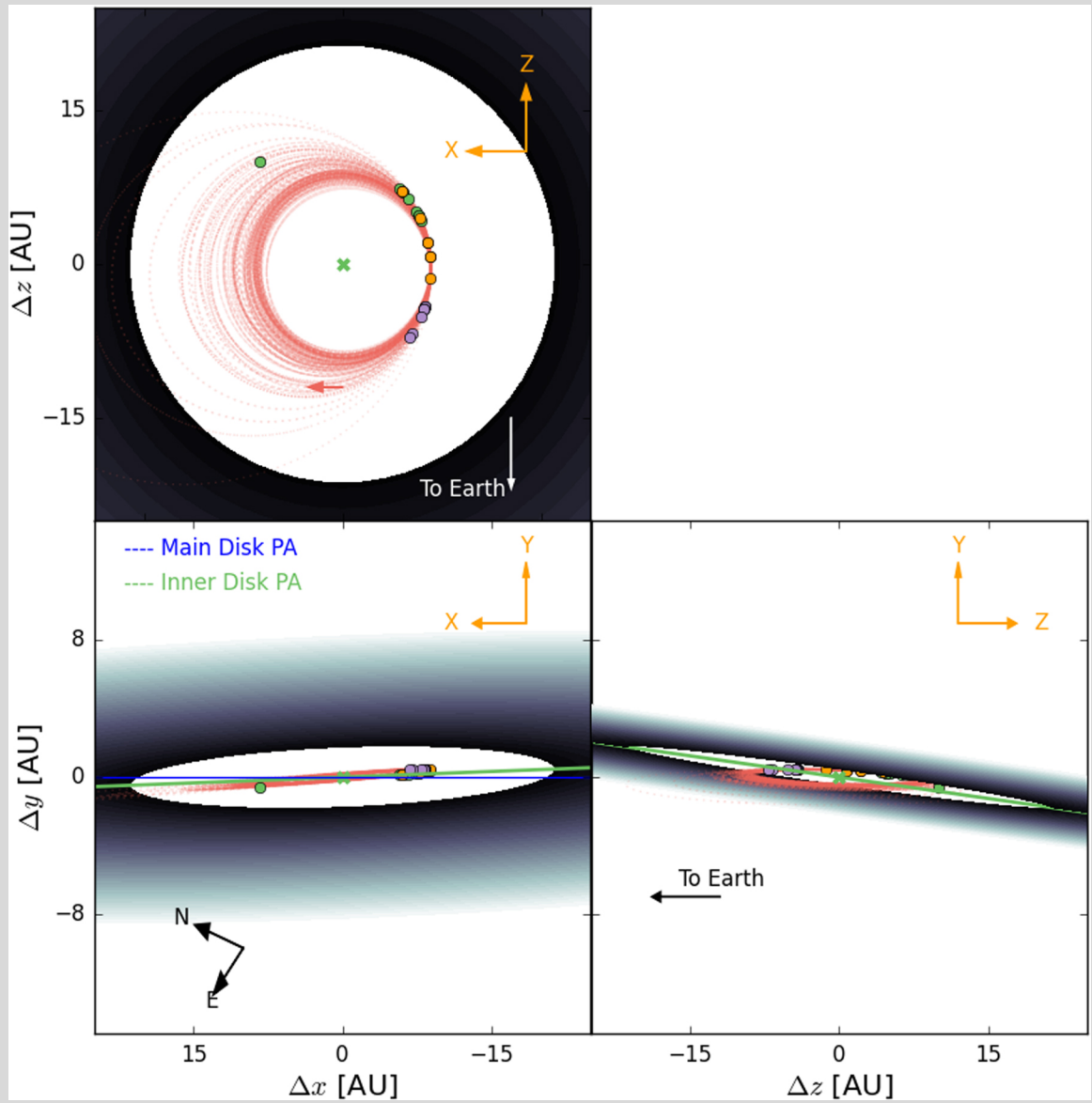
Macint

Millar-Blanch

Wang et al. 2016 – Ruled out to  $10\sigma$

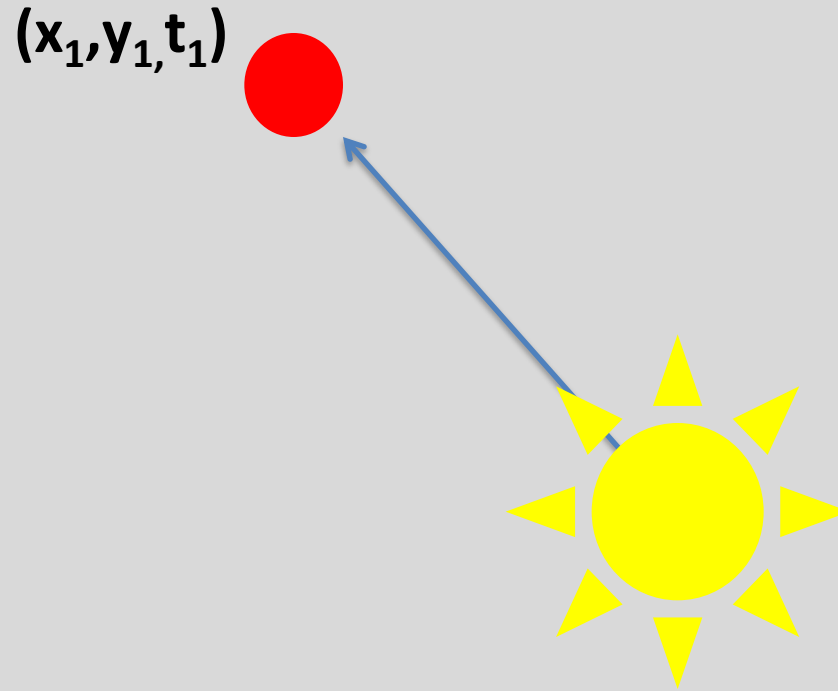


# Orbits can be compared with disk structure to illuminate the cause of the structure and probe formation outcomes.

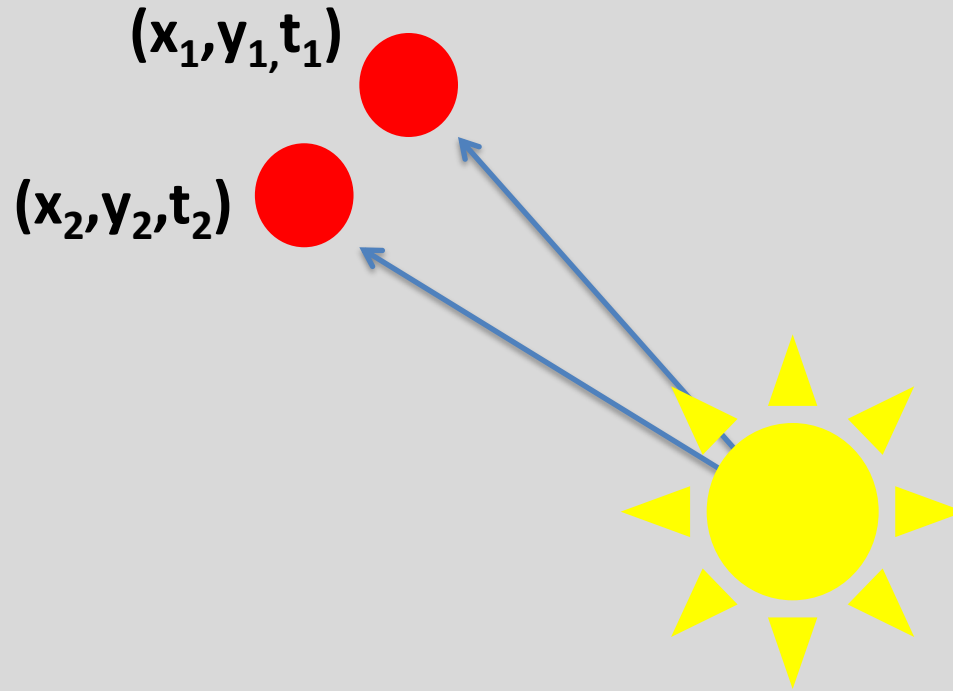


Millar-Blanchaer et al. 2015

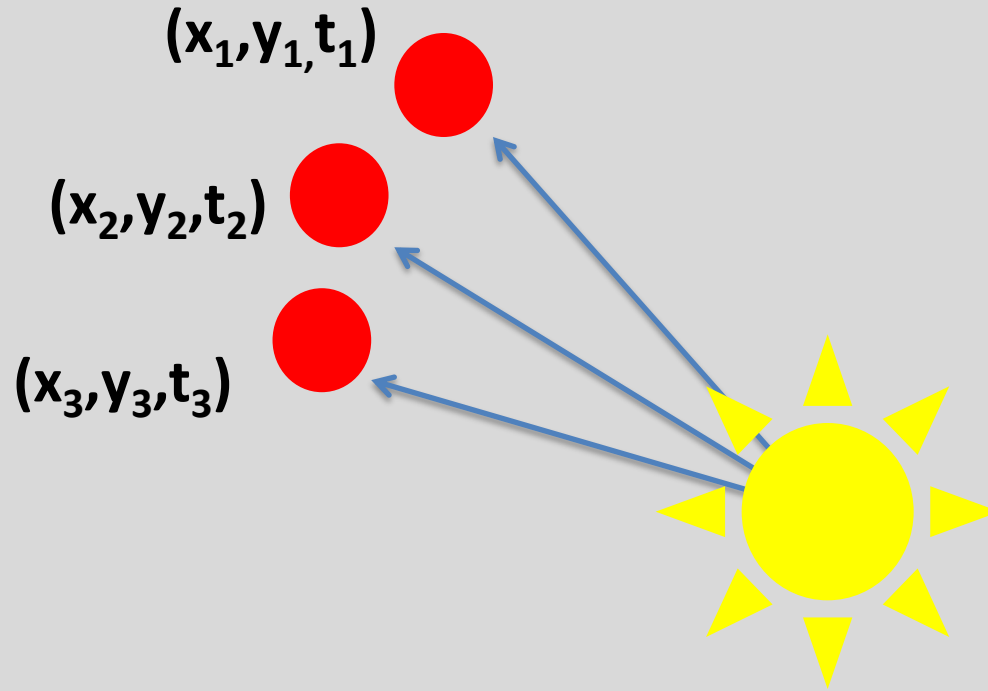
# With direct imaging, what do we actually want to measure?



# With direct imaging, what do we actually want to measure?

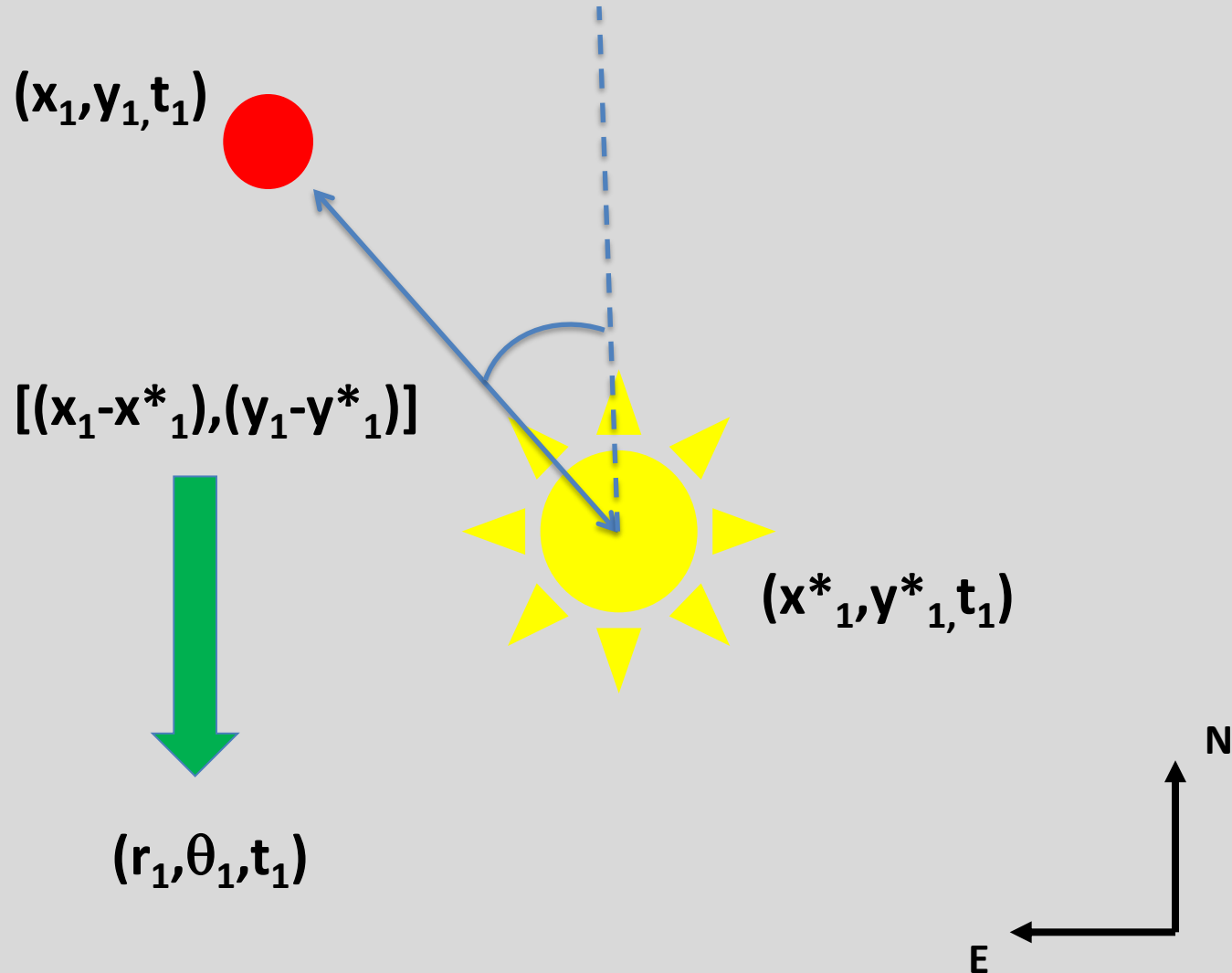


# With direct imaging, what do we actually want to measure?

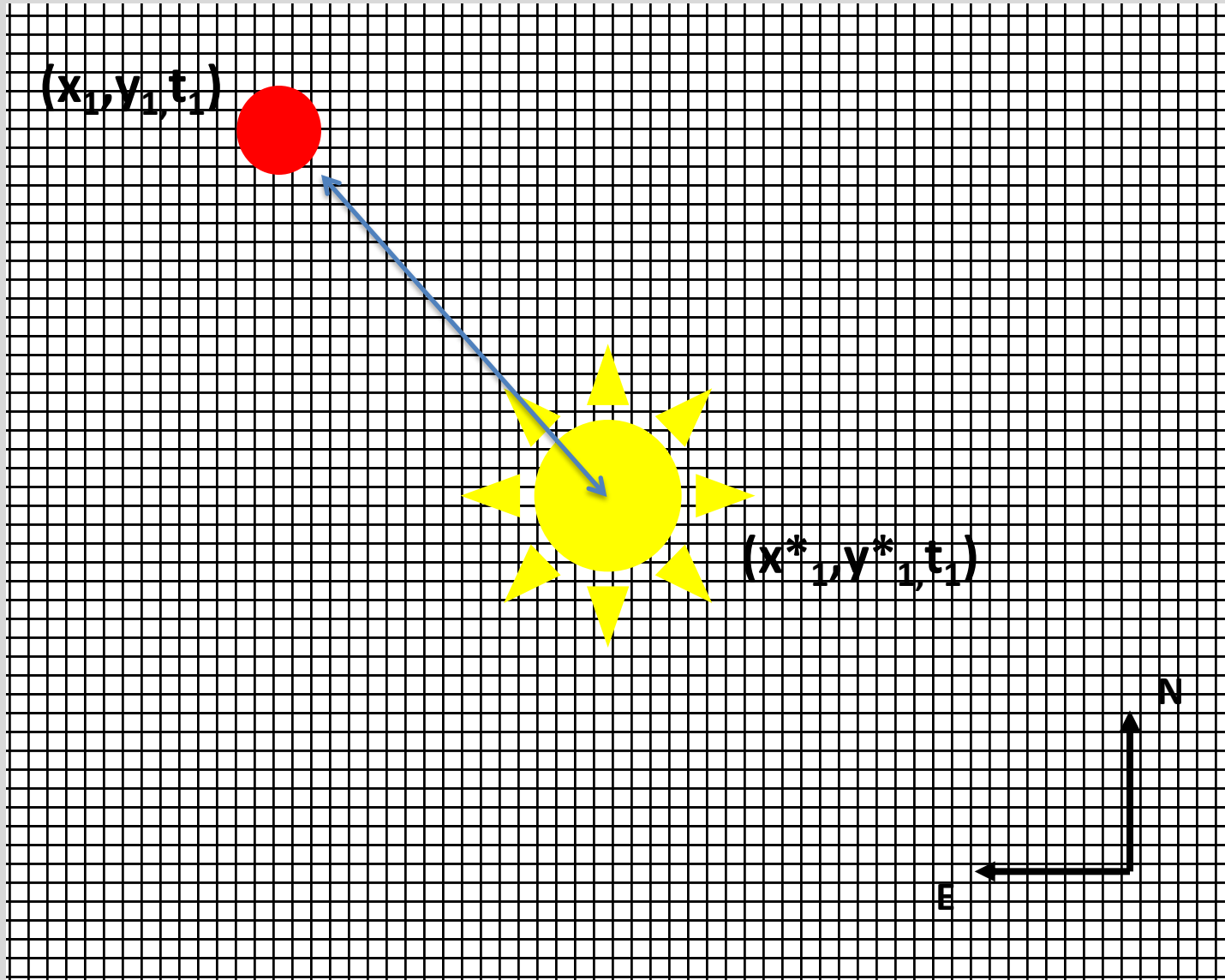


## What are the challenges/limitations of performing these measurements?

As with visual binaries, we avoid reference frame requirements by performing *relative* astrometry.

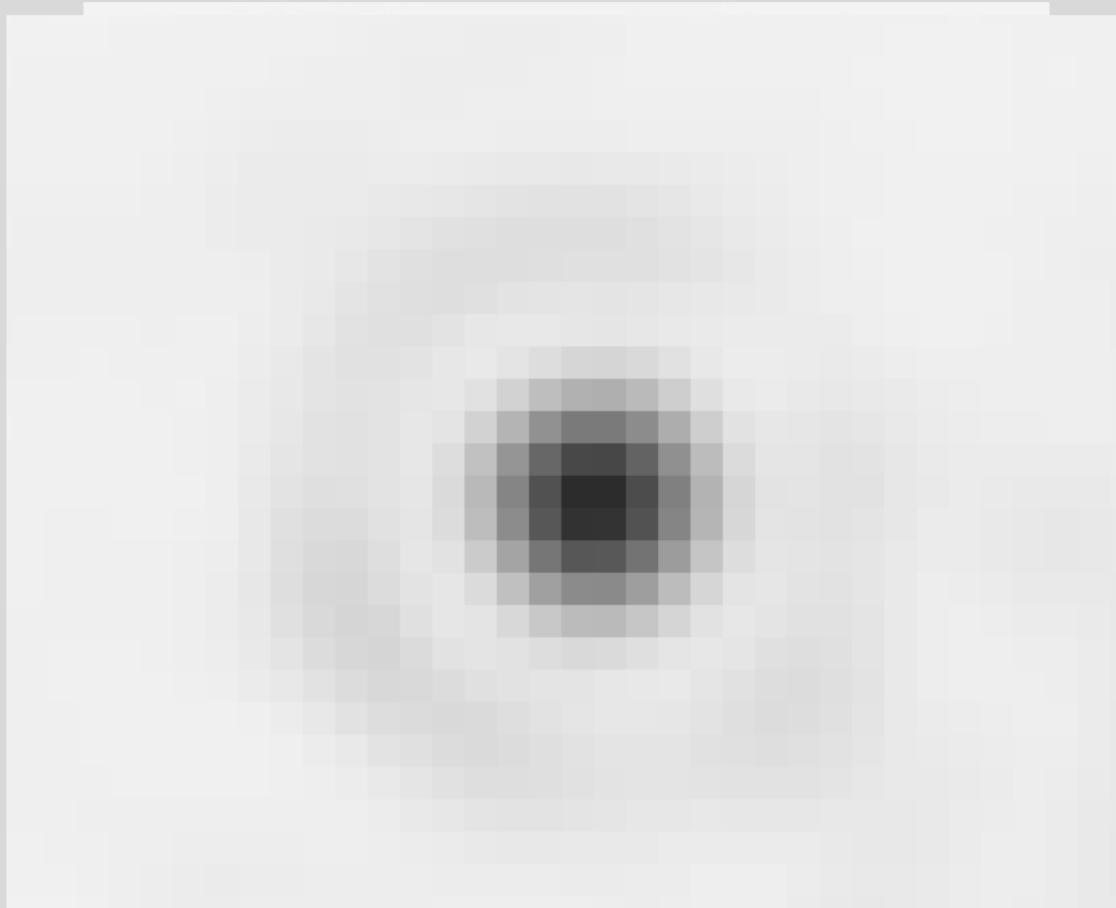


Positional measurements require accurate estimation of the exact center of the two objects.

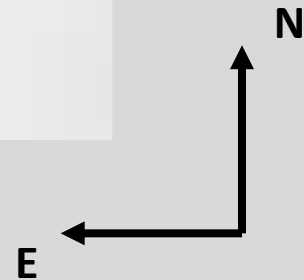




**Positional measurements require accurate estimation of the exact center of the two objects.**



Triple system HD 205545, Keck NIRC2

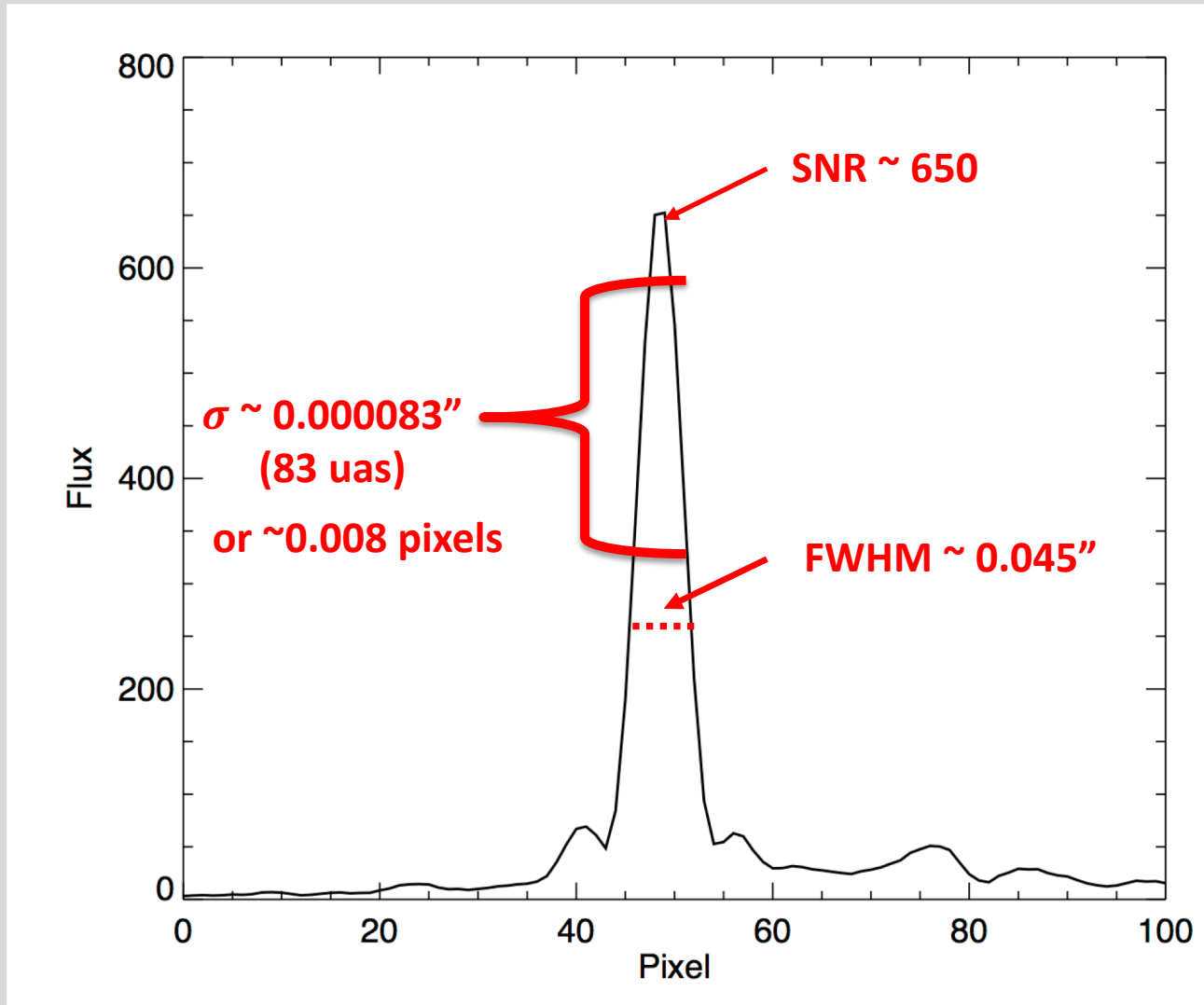


# There are theoretical predictions for astrometric precision.

$$\sigma \sim \frac{\textit{Full Width Half Max}}{\textit{Signal to Noise Ratio}}$$

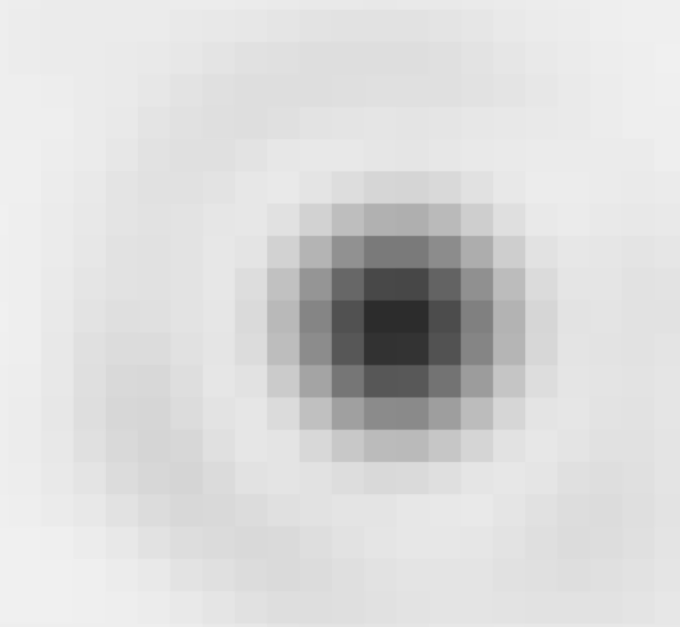
e.g., Lindegren (1978), King (1983), Kaiser et al. (2000)

# There are theoretical predictions for astrometric precision.



# There are theoretical predictions for astrometric precision.

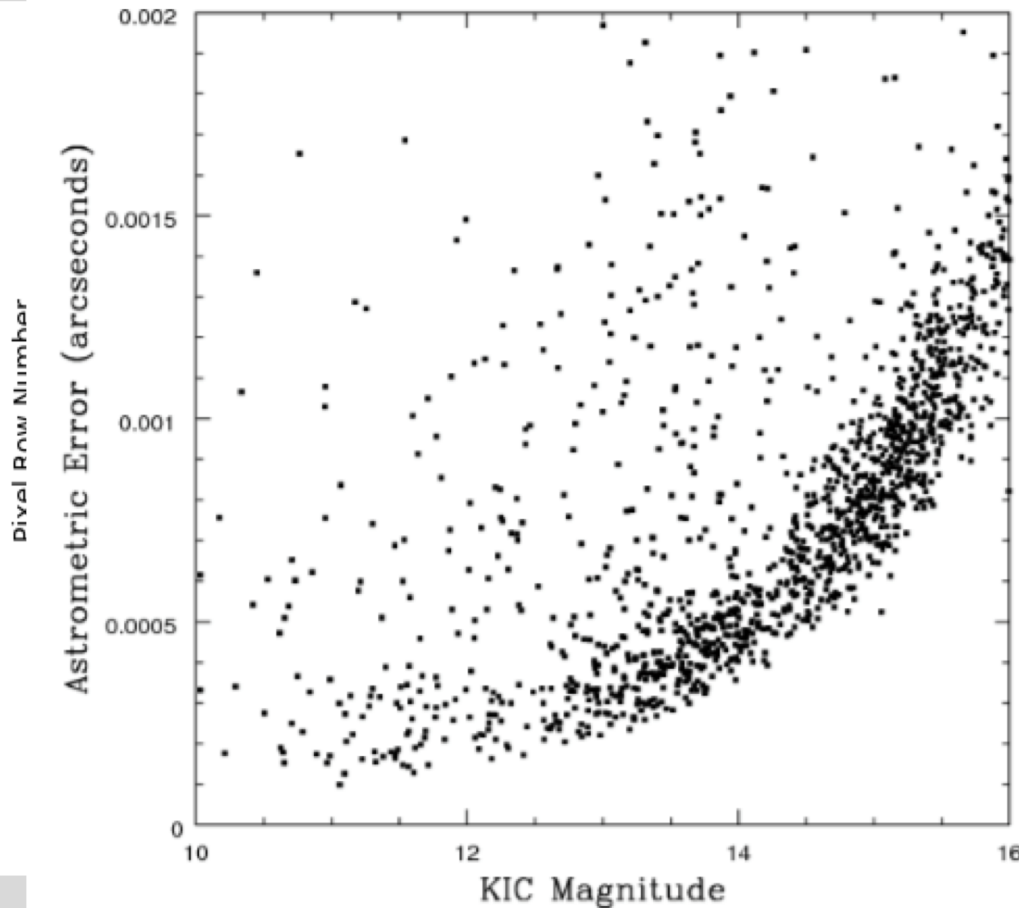
Actual precision of this measurement  $\sim 200 \mu\text{as}$



In practice, the theoretical limit is challenging to reach.

**Side note – the dependence of precision on SNR generated some excitement about using Kepler data for astrometry.**

lightcurve.keplerscience.org

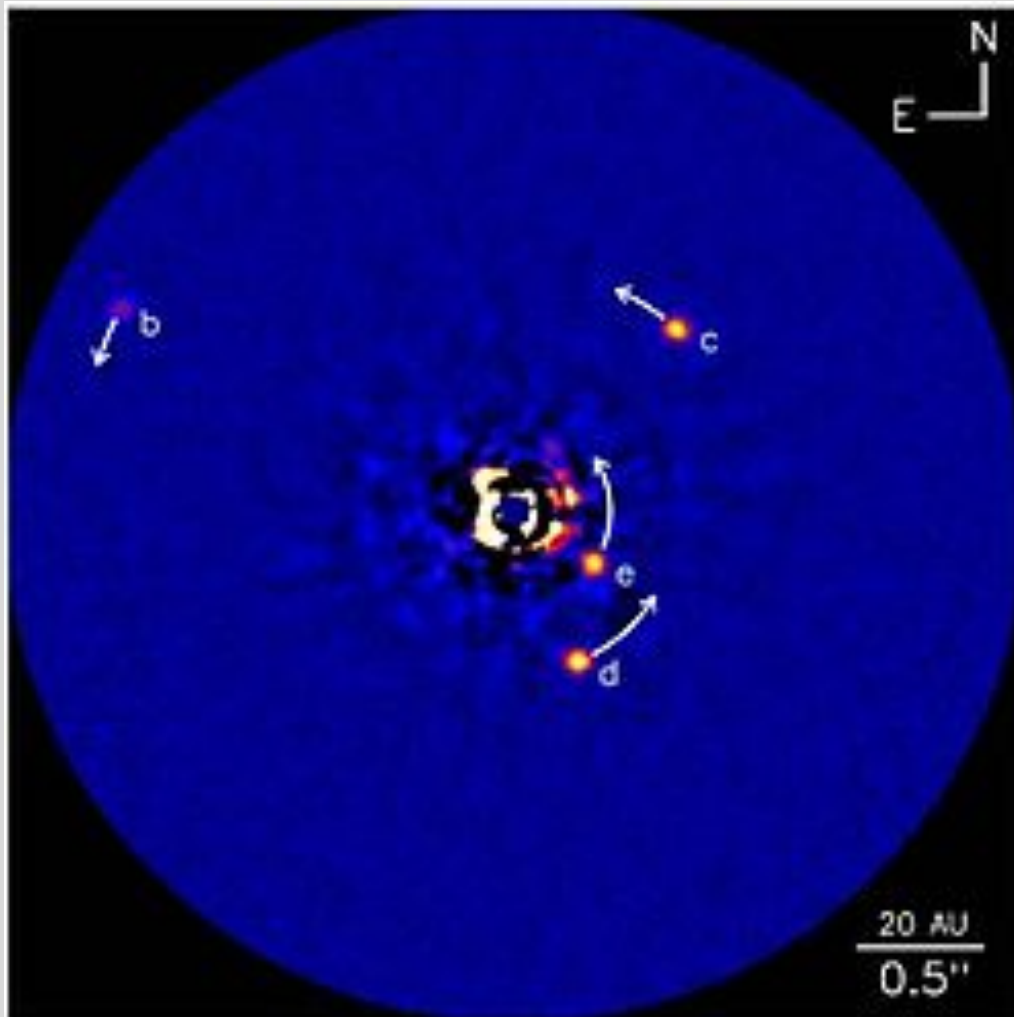


Undersampled pixels (3.98"), large FWHM (5-6") but very high SNR (>10,000)

Precision as good as 0.0001 pixels implied

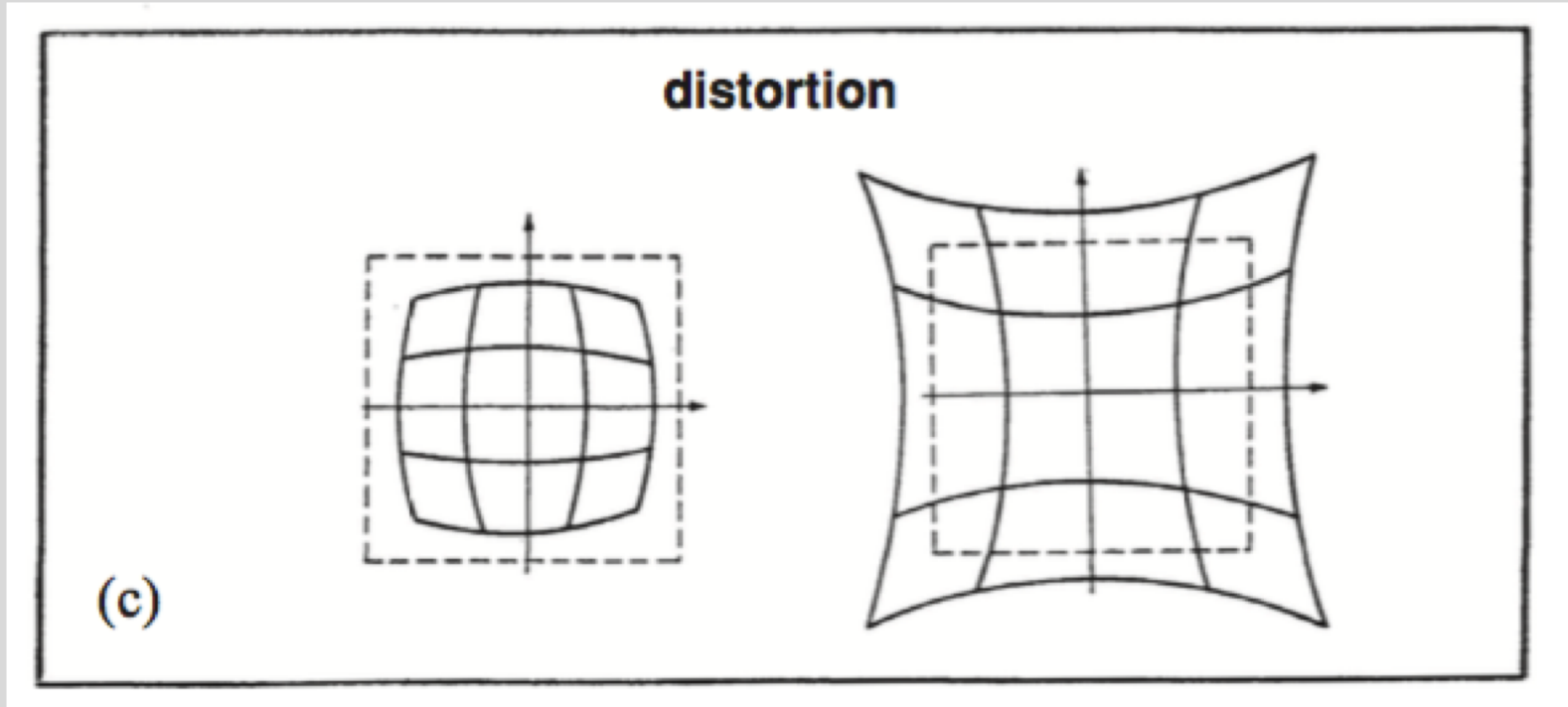
Monet et al. 2010

# Let's go through some of the sources of astrometric error for direct imaging.



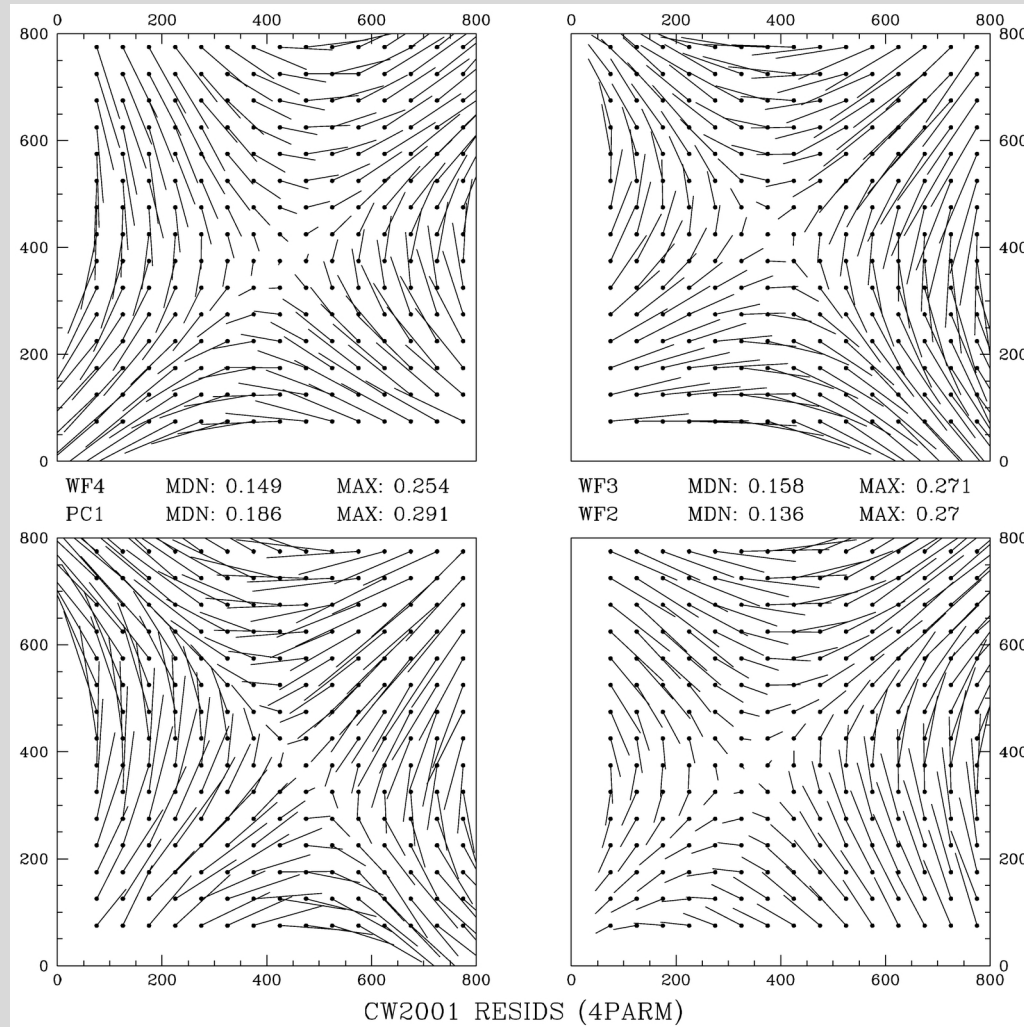
HR 8799  
Marois et al. 2010

# One of the first sources of uncertainty to deal with is distortion.



Resource: [Astronomical Optics](#) by Schroeder

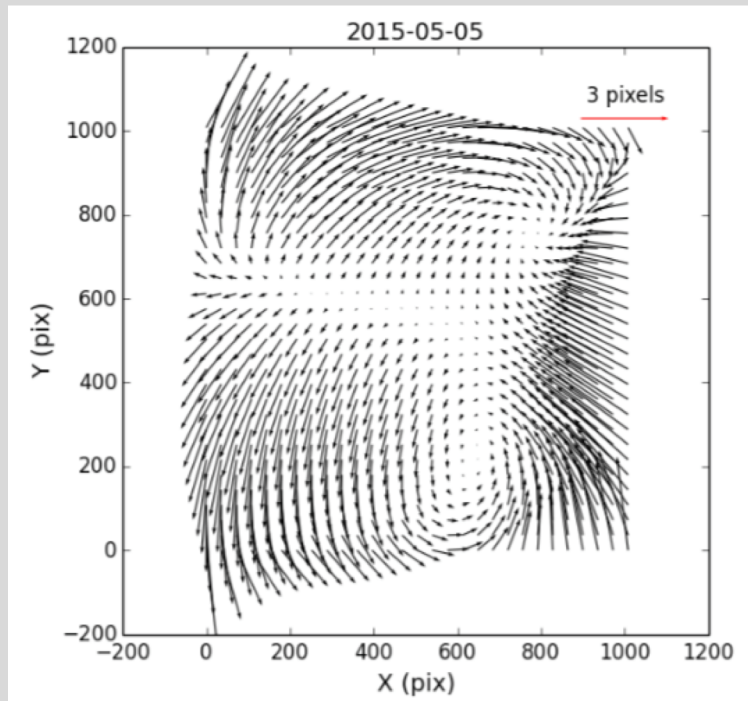
# Optical aberrations in a telescope/camera can “move” the centroid of a star by a small amount up to 10s of milliarcseconds.



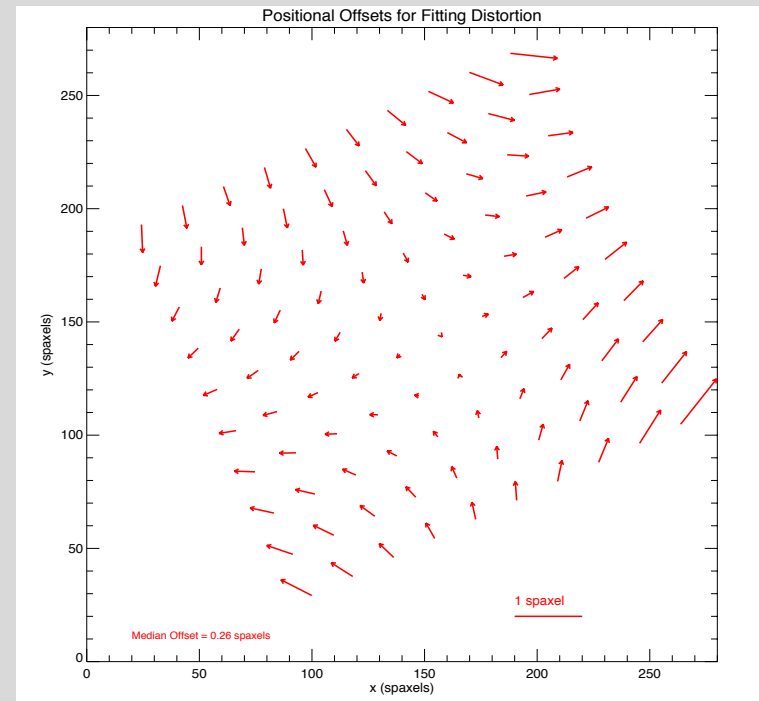
HST WFPC2,  
Anderson &  
King 2003



# Optical aberrations in a telescope/camera can “move” the centroid of a star by a small amount up to 10s of milliarcseconds.

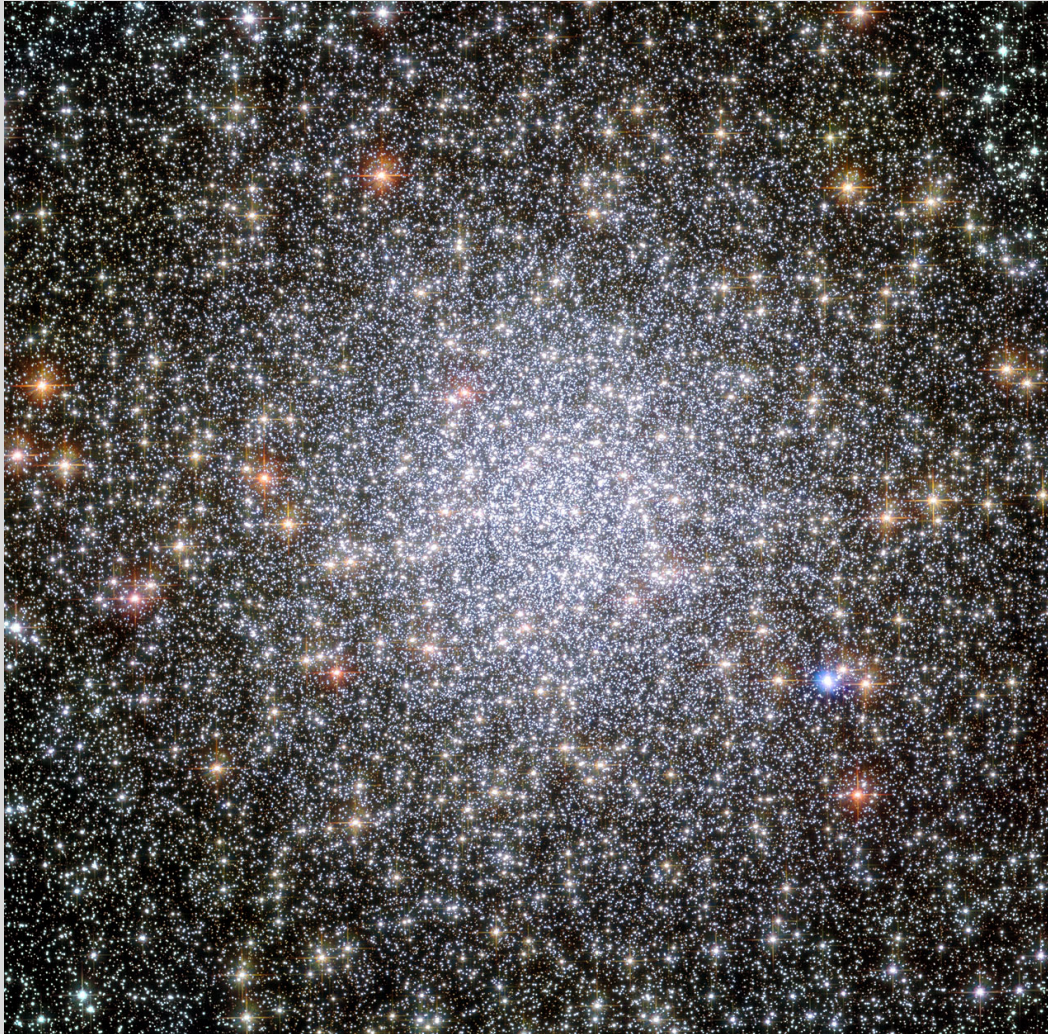


NIRC2, Service et al. 2016



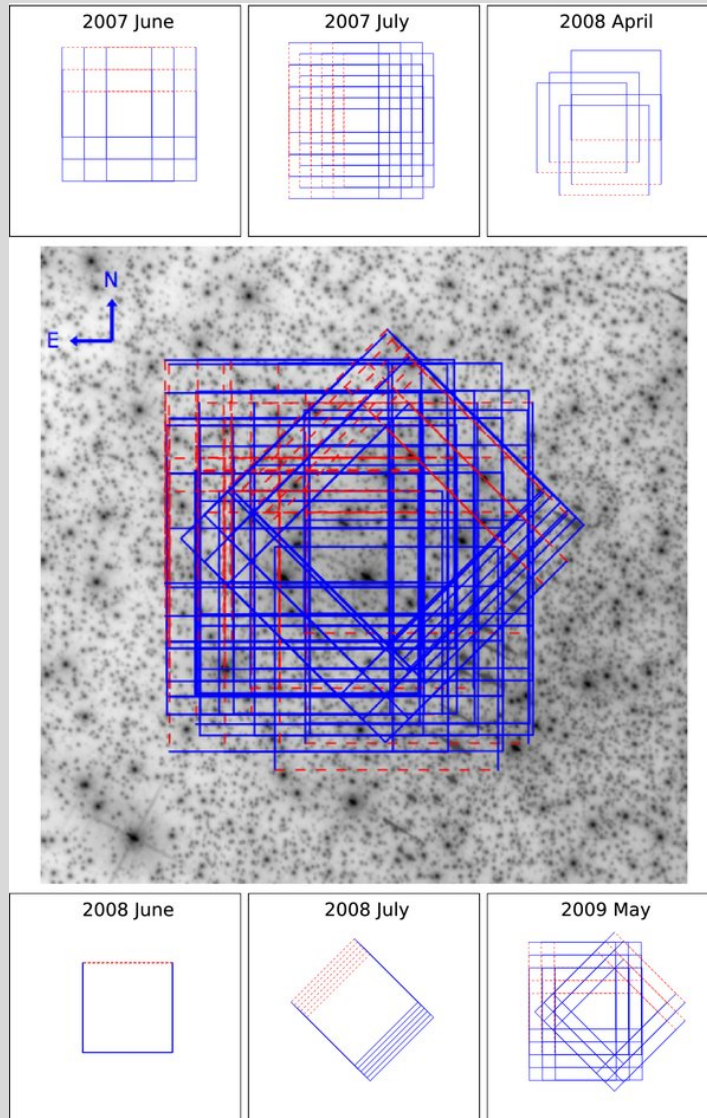
GPI, Konopacky et al. 2014

# Distortion pattern is typically measured using a dense field of stars (or simulated stars).



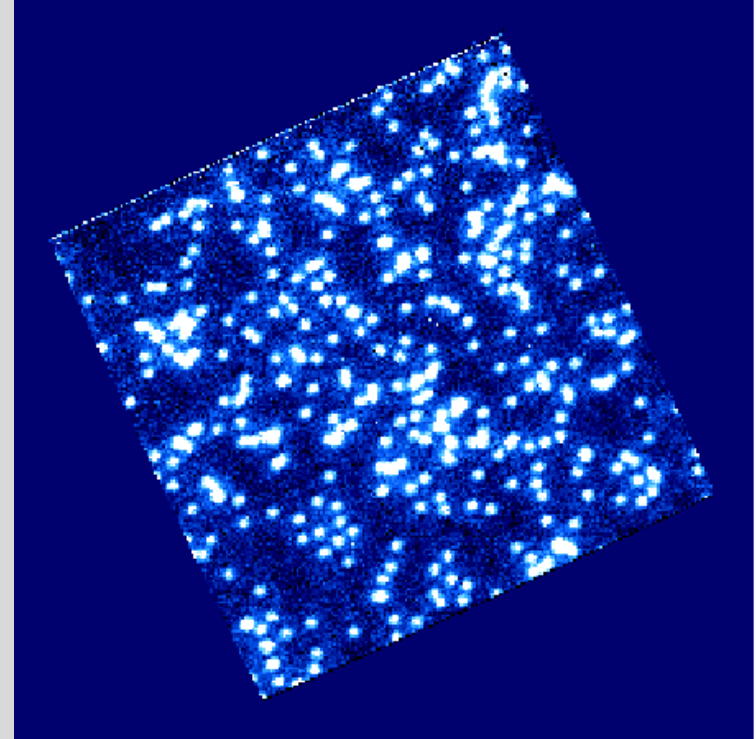
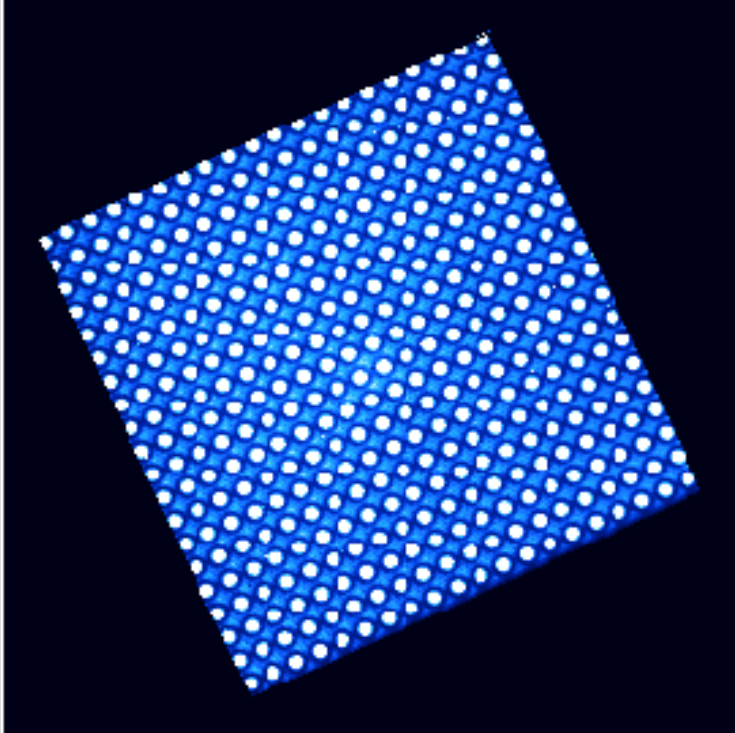
For HST solutions,  
use a globular  
cluster like 47  
Tucanae (Anderson  
& King 2003)

# Distortion pattern is typically measured using a dense field of stars (or simulated stars).



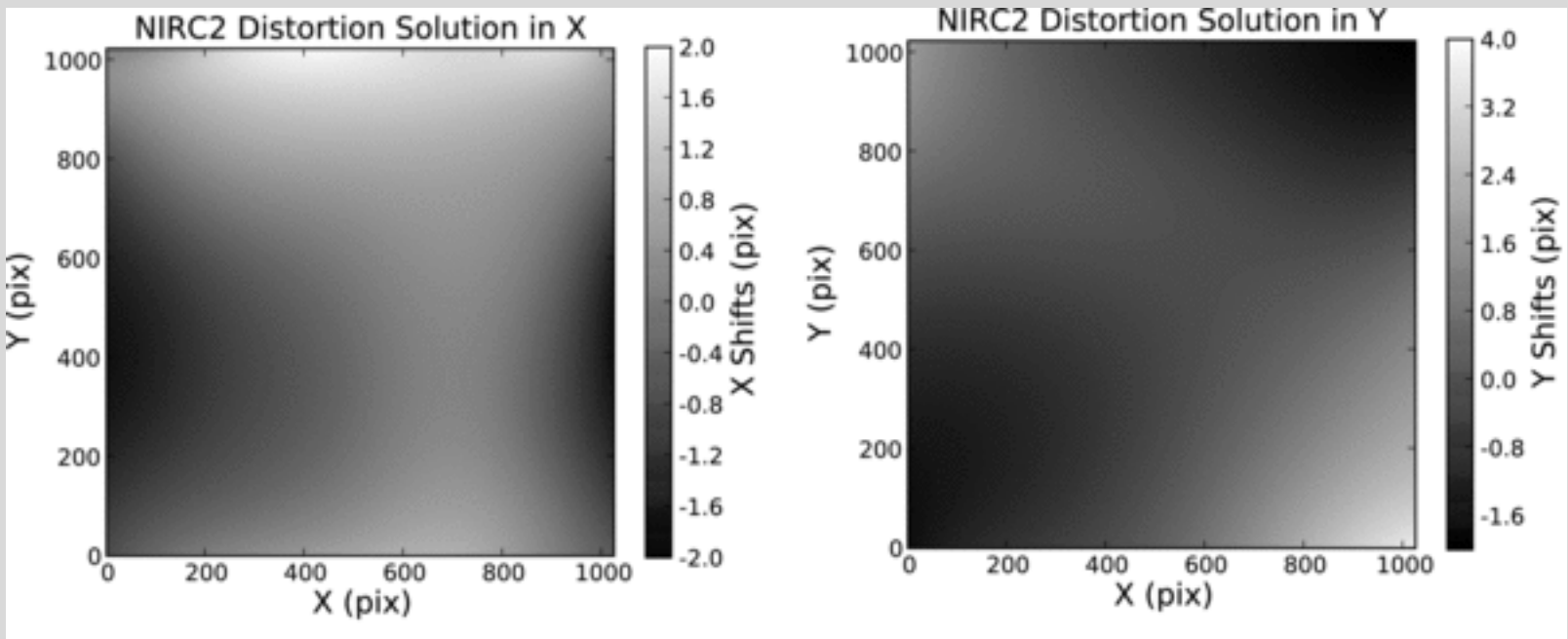
For NIRC2 solutions, use a globular cluster M92 (Yelda et al. 2010)

**Distortion pattern is typically measured using a dense field of stars (or simulated stars).**



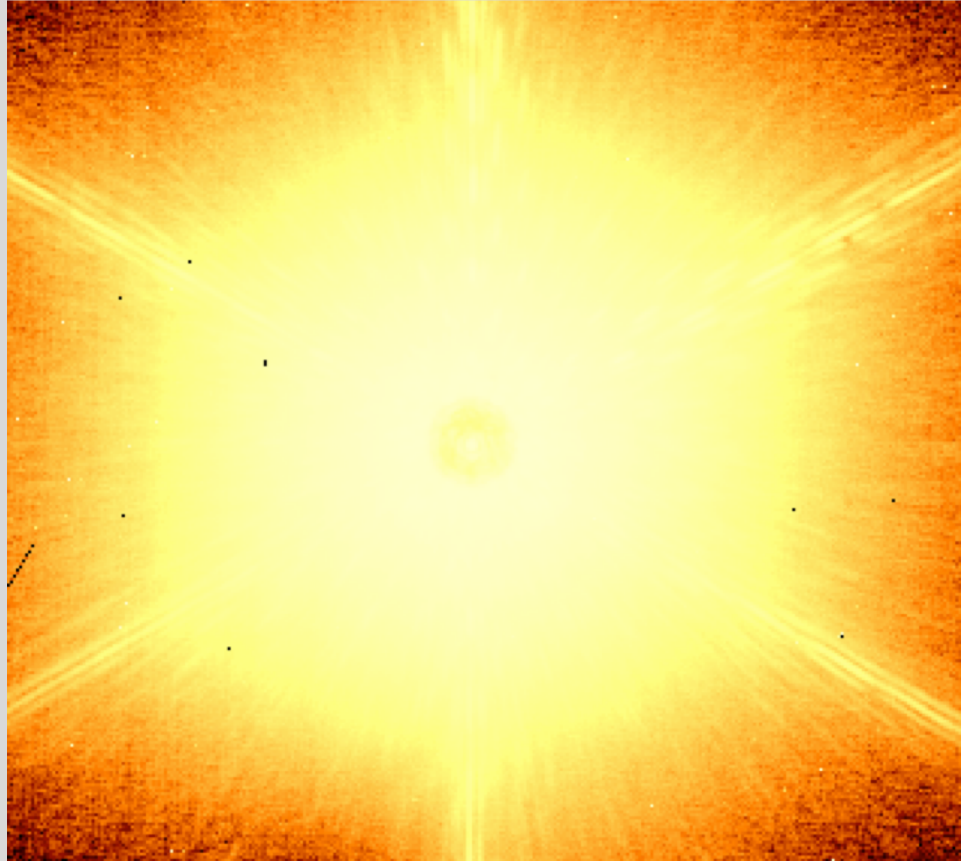
For GPI solutions, use a pinhole mask (Konopacky et al. 2014)

# Fitting residual maps with polynomial or spline surfaces allow you to correct for shifted pixels.



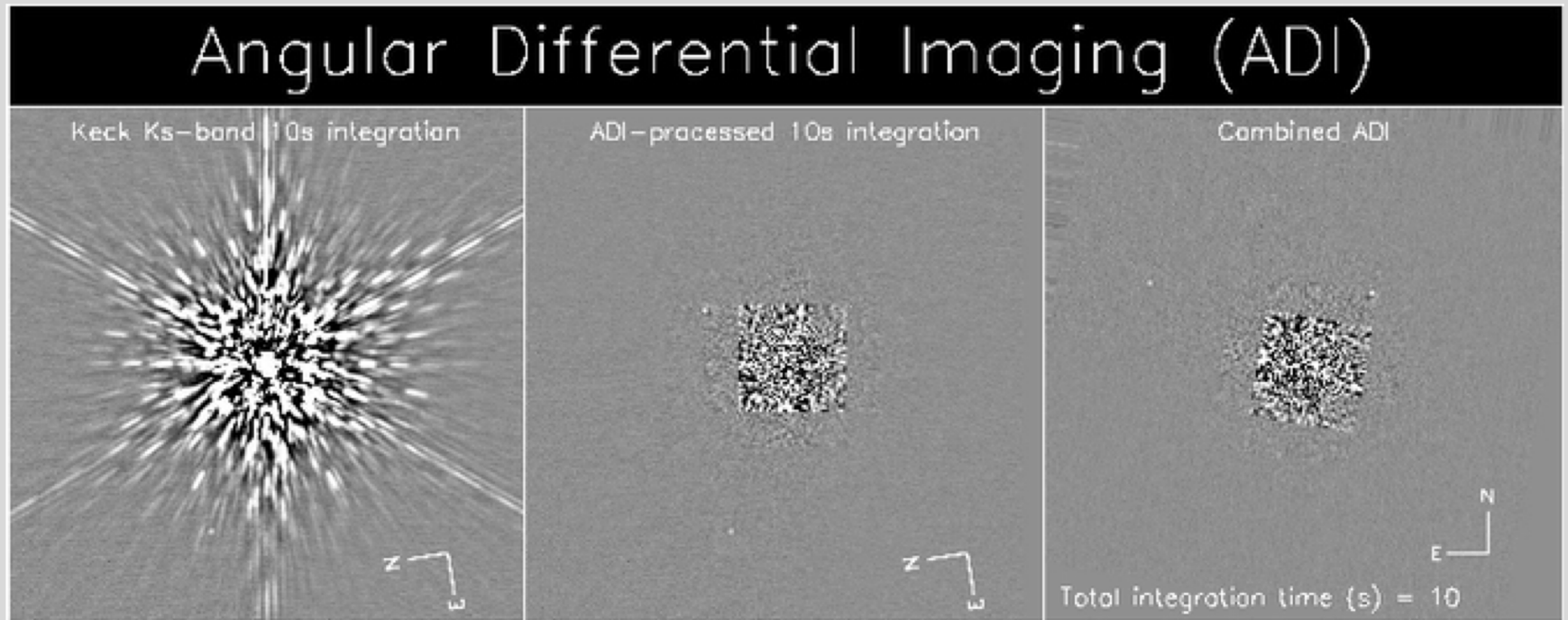
Bivariate B-spline, NIRC2, Yelda et al. 2010

**So now your data is reduced and corrected for distortion – next comes starlight removal (PSF subtraction).**

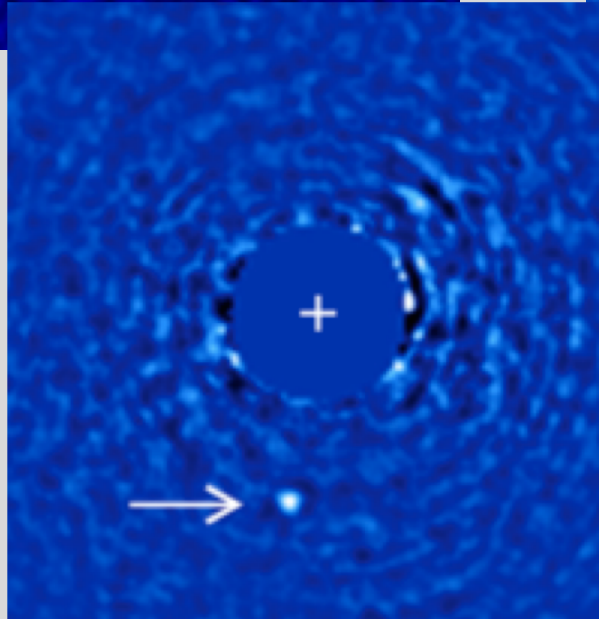
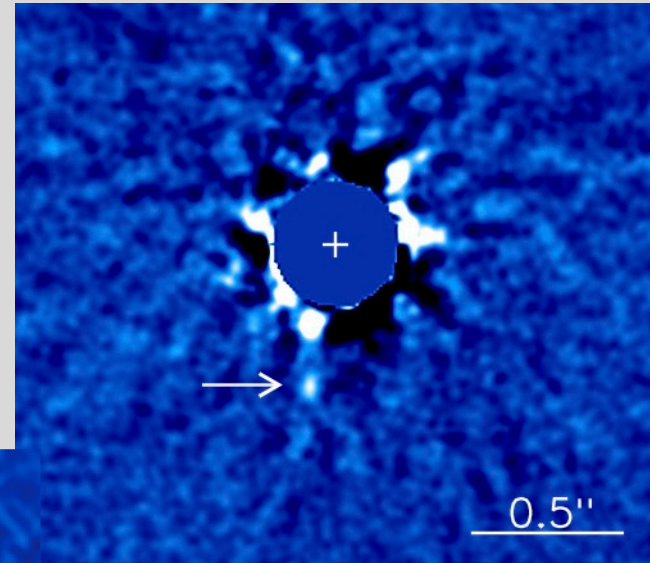
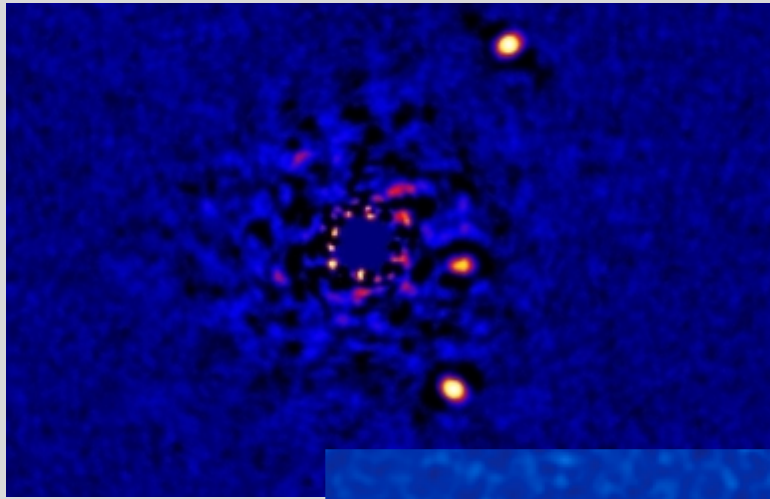


**Unprocessed data on HR 8799 from NIRC2 –  
600 mas coronagraphic spot used**

**Angular differential imaging and LOCI/KLIP PSF subtraction are powerful techniques, but can introduce astrometric biases.**

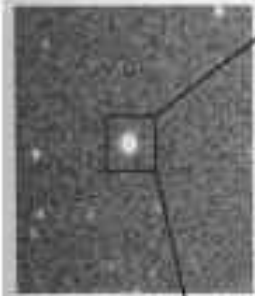


Depending on choice of subtraction techniques, the planet PSF can be strongly impacted.





# Straightforward centroid calculations can be biased by PSF structure.



Sky = 376.6 ± 4.6

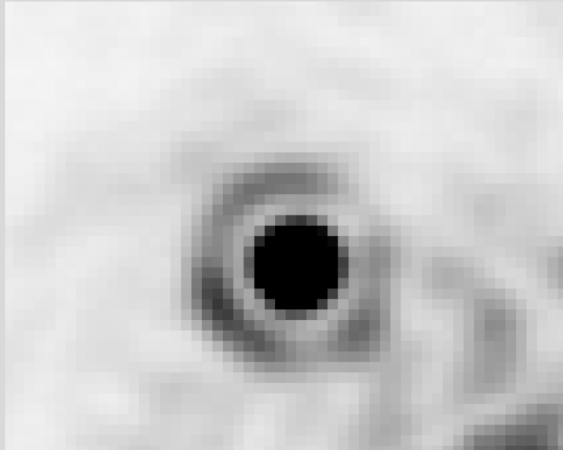
363	379	376	379	382	383	386	390	373
385	377	381	389	396	392	388	386	378
376	375	392	430	469	446	394	381	384
381	393	404	558	1105	863	431	376	378
380	396	418	668	2204	1787	467	390	392
380	386	398	539	1470	1189	434	394	376
379	383	384	413	541	491	389	379	381
387	377	380	388	400	402	381	379	379
369	374	384	380	378	378	372	376	374

astronomyclub.xyz

$$\hat{x} = \frac{\sum x I_{x,y}}{\sum I_{x,y}}$$

$$\hat{y} = \frac{\sum y I_{x,y}}{\sum I_{x,y}}$$

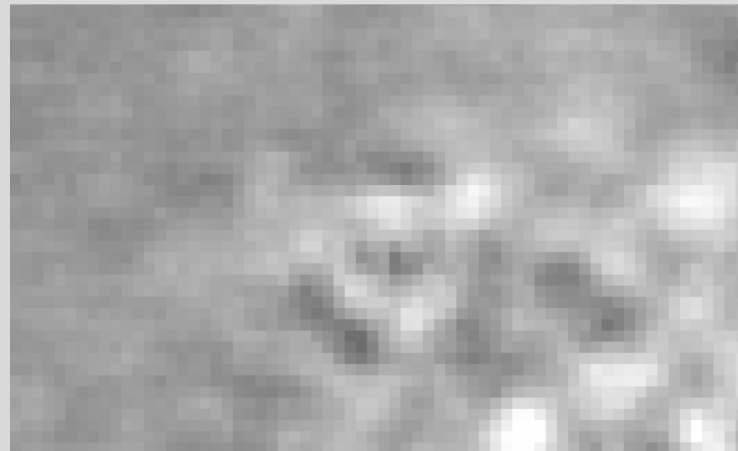
# PSF fitting tends to give the most precise results.



Data



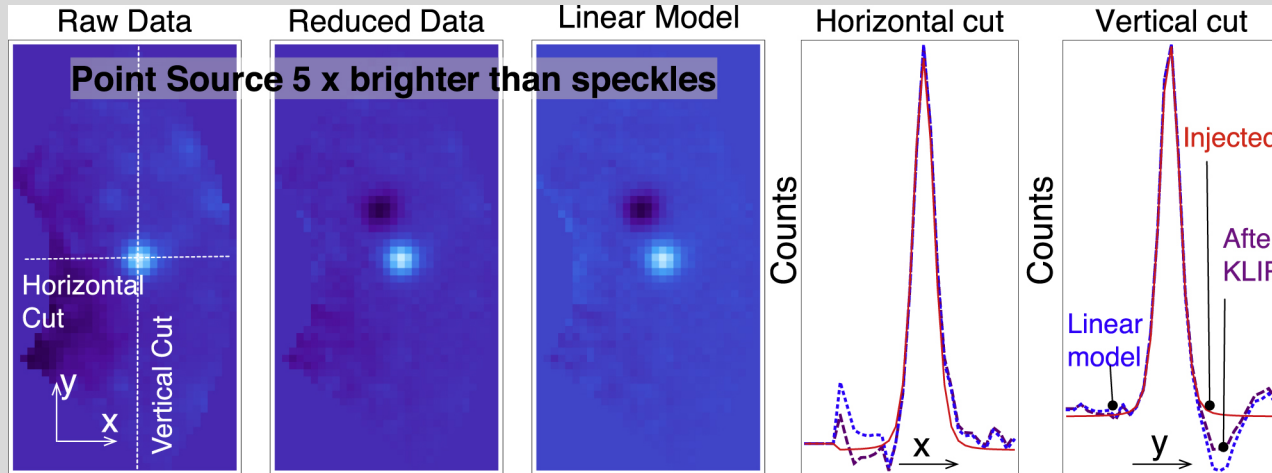
Model (measured PSF)



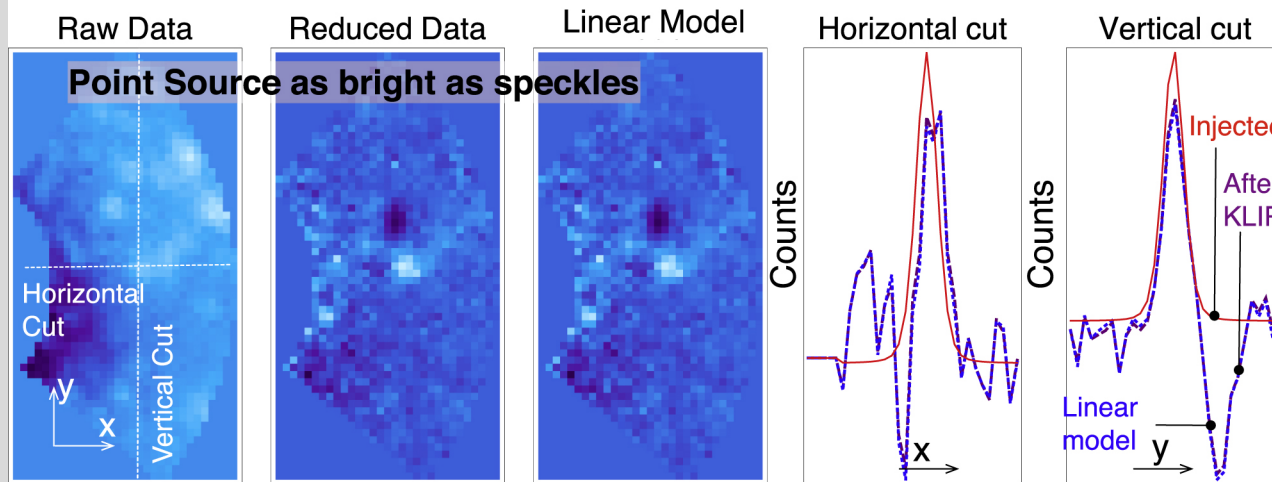
Data – Model (residuals)

Keck NIRC2

# Providing an accurate PSF model for a “speckle subtracted” image is yielding excellent results.

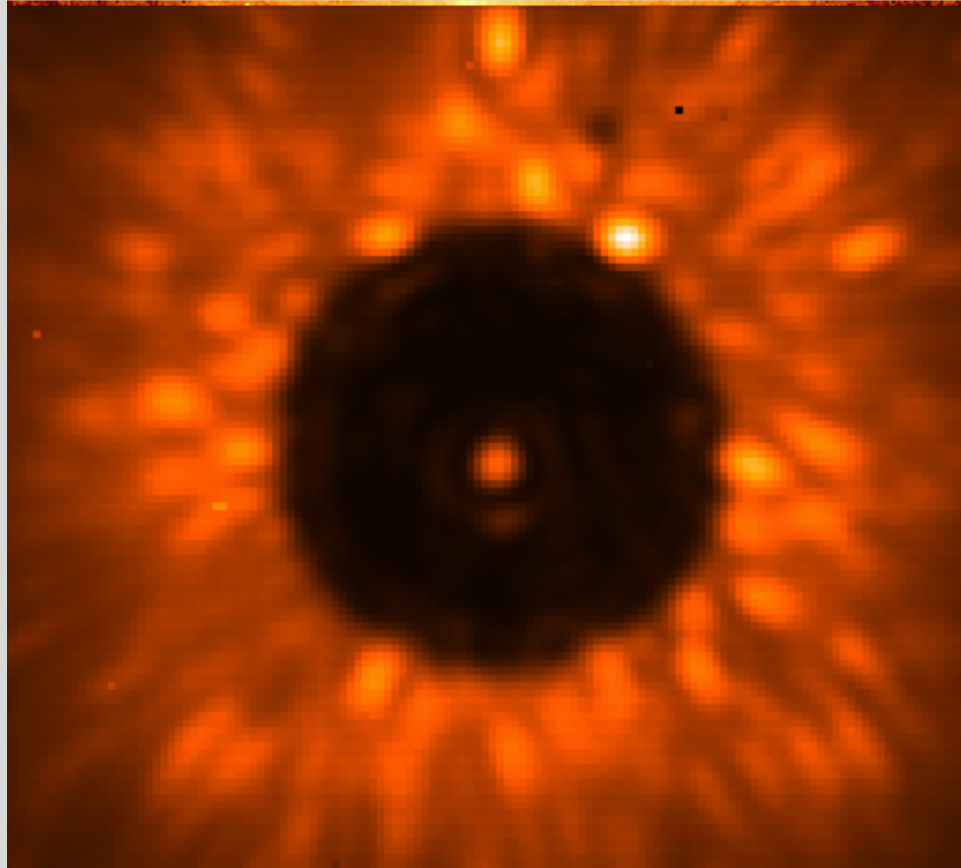


Non aggressive reduction:  $N_r = 5$ ,  $N_\phi = 4$ ,  $N_{\text{Corr}} = 20$ ,  $K_{\text{Klip}} = 2$ ,  $N_\delta = 1.5$ .

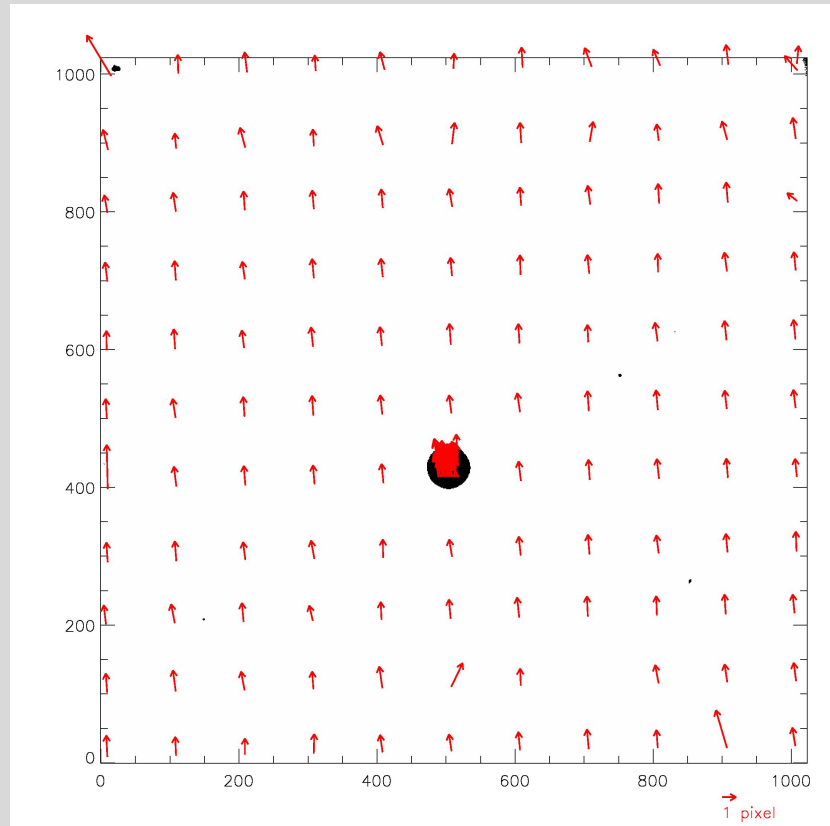


Non aggressive reduction:  $N_r = 5$ ,  $N_\phi = 4$ ,  $N_{\text{Corr}} = 30$ ,  $K_{\text{Klip}} = 30$ ,  $N_\delta = 0.8$ .

**So now we can find the positions of our planets  
– but what about the star??**

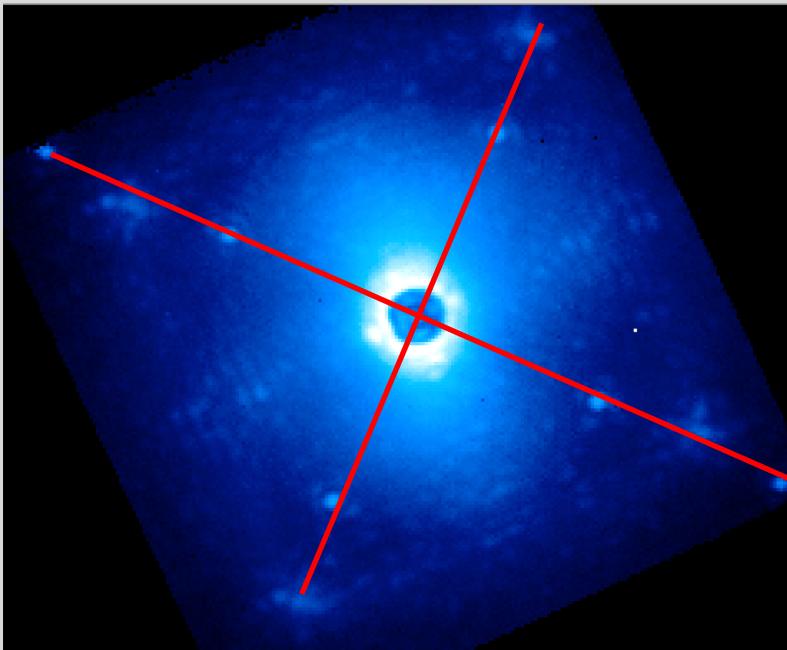


# Sometimes your good fortune isn't as good as you thought it was...

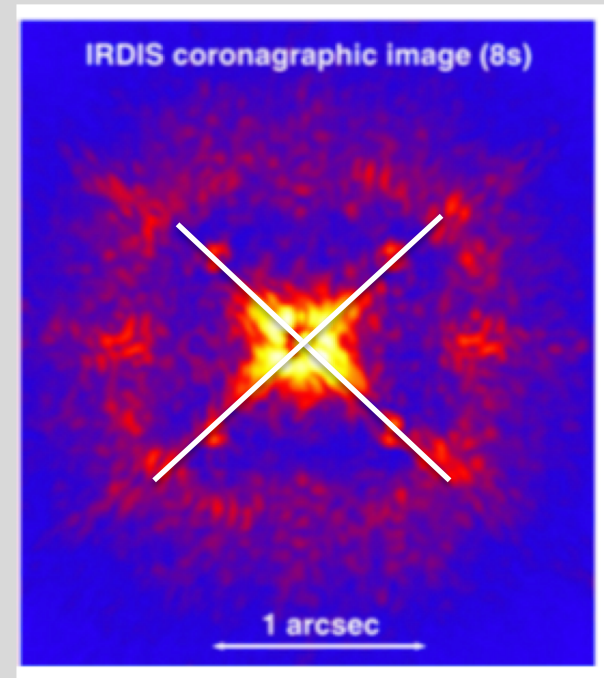


Calibration map showing the direction of the “flow” caused by the NIRC2 focal plane mask. Arrow size is different under the spot.

# Newer instruments have other methods for locating the star.



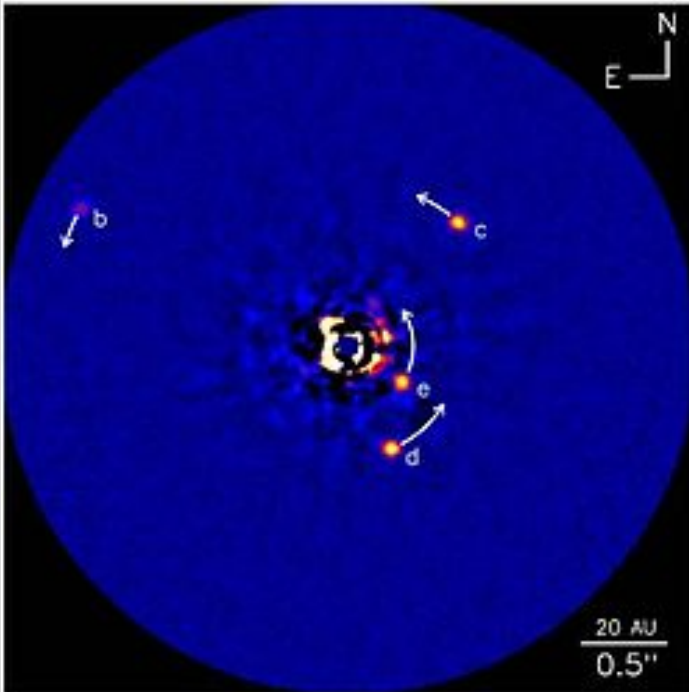
GPI "Satellite Spots" from  
apodizer grid  
Macintosh et al. 2014



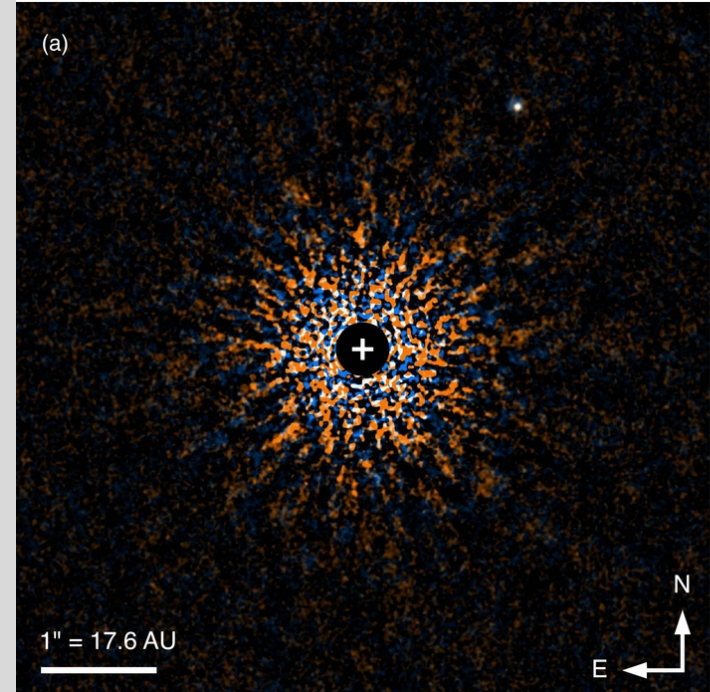
SPHERE DM Waffle Pattern  
Milli et al. 2018

**So what is the current astrometric precision for directly imaged planets?**

# Direct imaging precision is still at the milliarcsecond level.



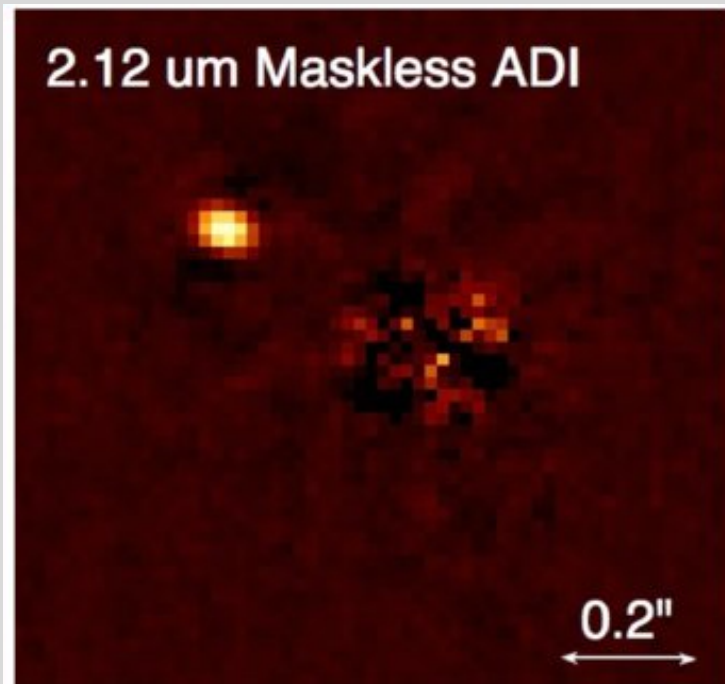
HR8799 with NIRC2,  $\sim 3 - 20$  mas,  
Marois et al. 2010,  
Konopacky et al. 2016



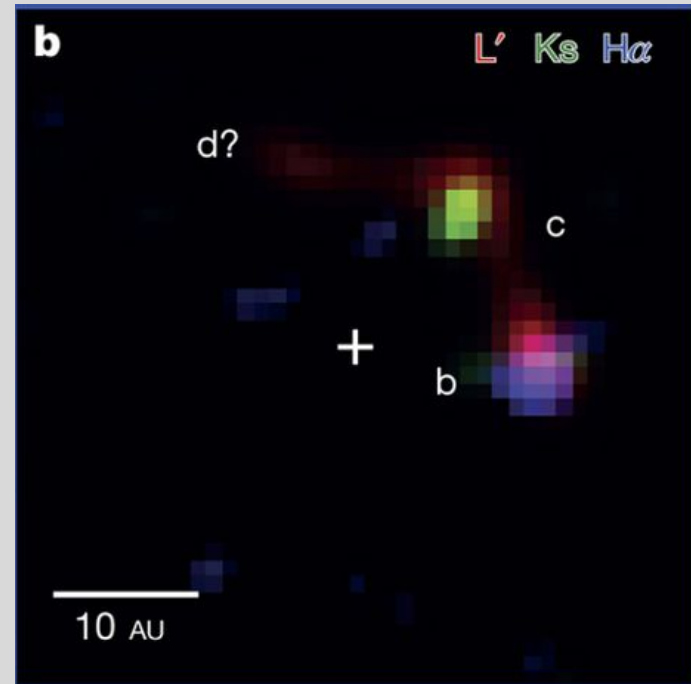
GJ 504b with Subaru/HiCIAO,  $\sim 8 - 20$  mas,  
Kuzuhara et al. 2013



# Direct imaging precision is still at the milliarcsecond level.

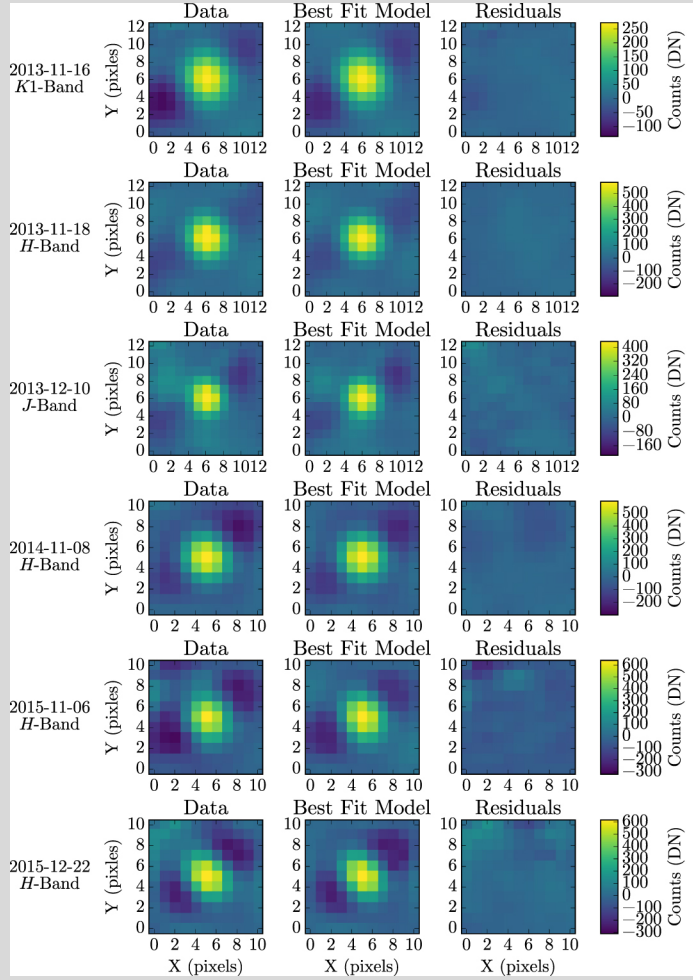


PZ Tel with NICI, 3-10 mas,  
Biller et al. 2010

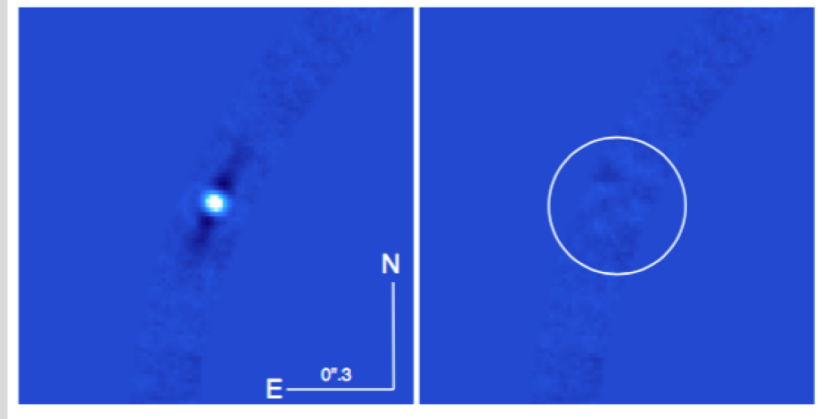


LkCA 15 with MagAO, 8mas,  
Sallum et al. 2015

# Some studies have approached the 1 mas precision mark.

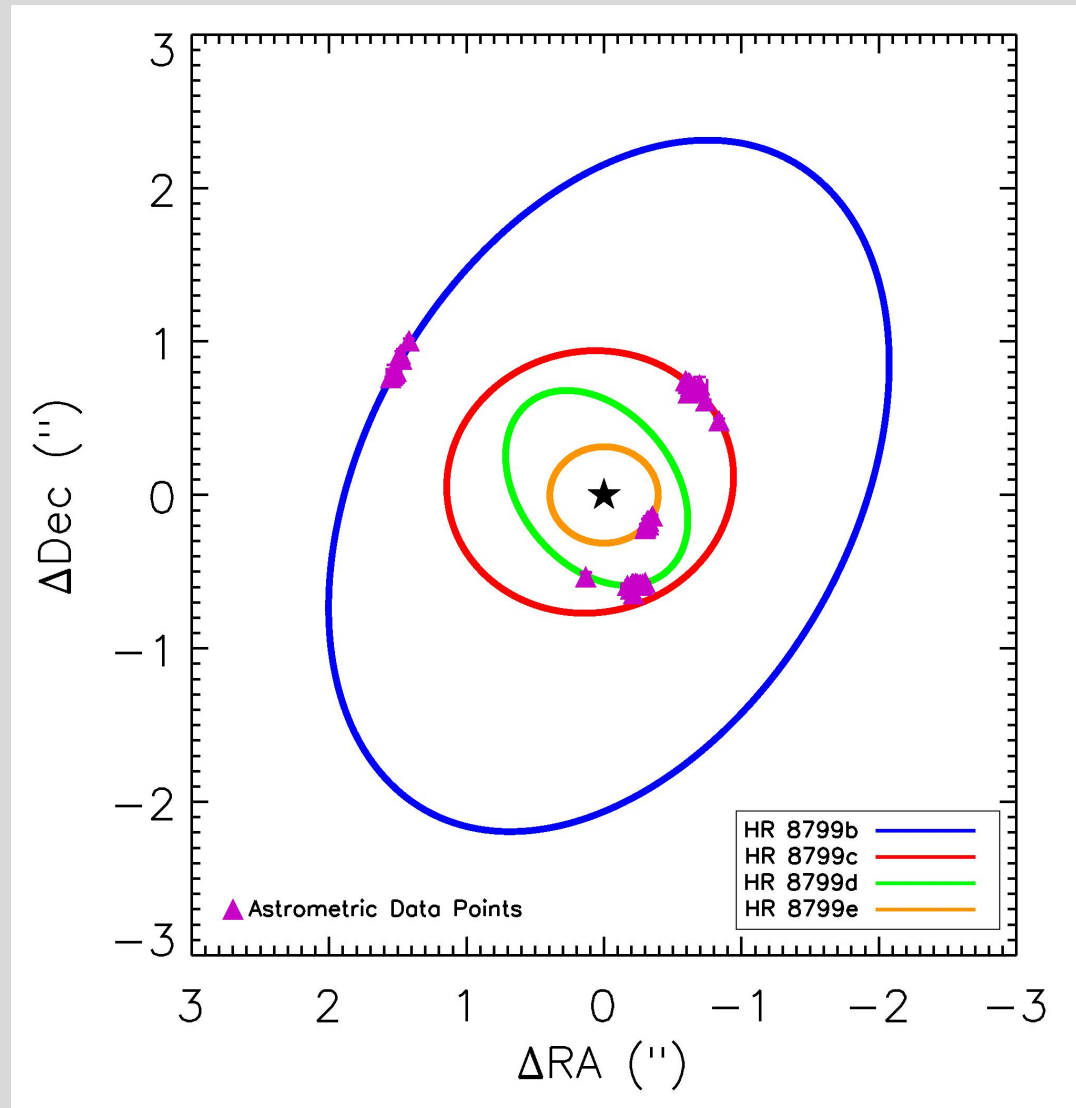


**$\beta$ Pic b with GPI, ~1 mas**  
Wang et al. 2016



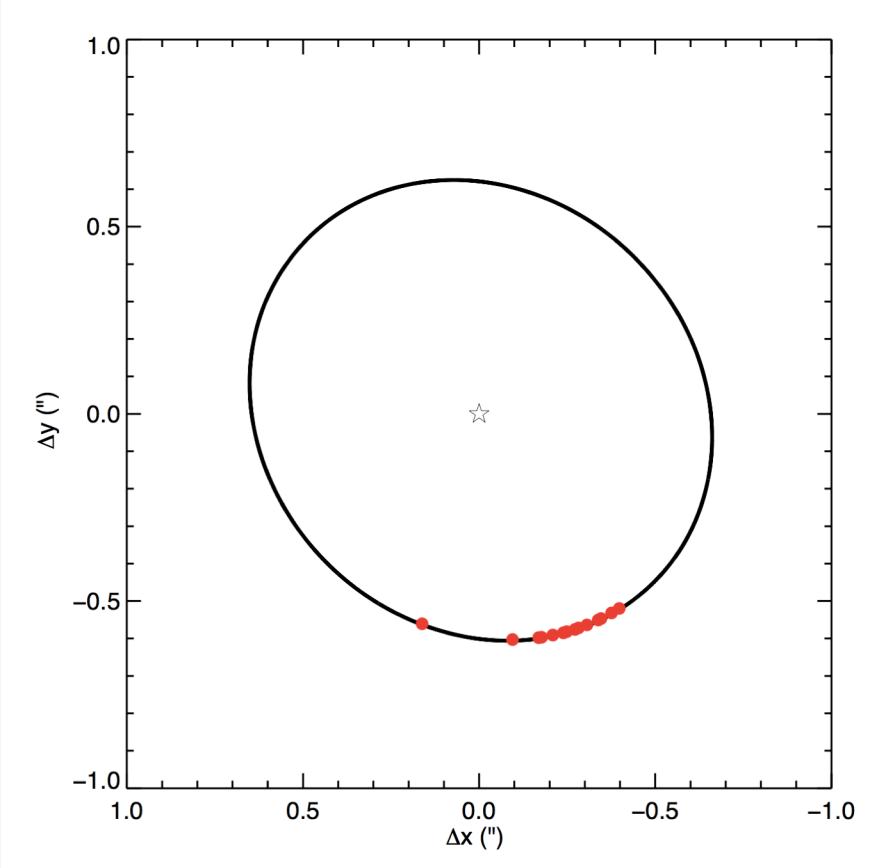
HR 8799bcde with SPHERE, ~2 mas  
Wertz et al. 2016

Once we get better precision on our astrometry, we need to think carefully about how we combine datasets.

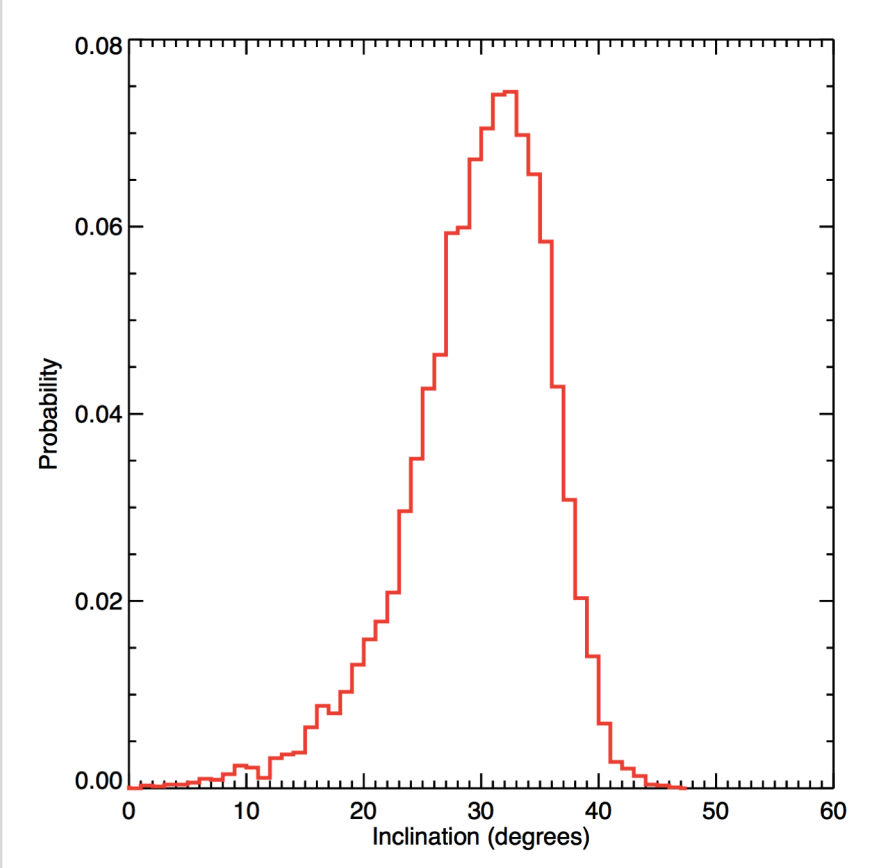
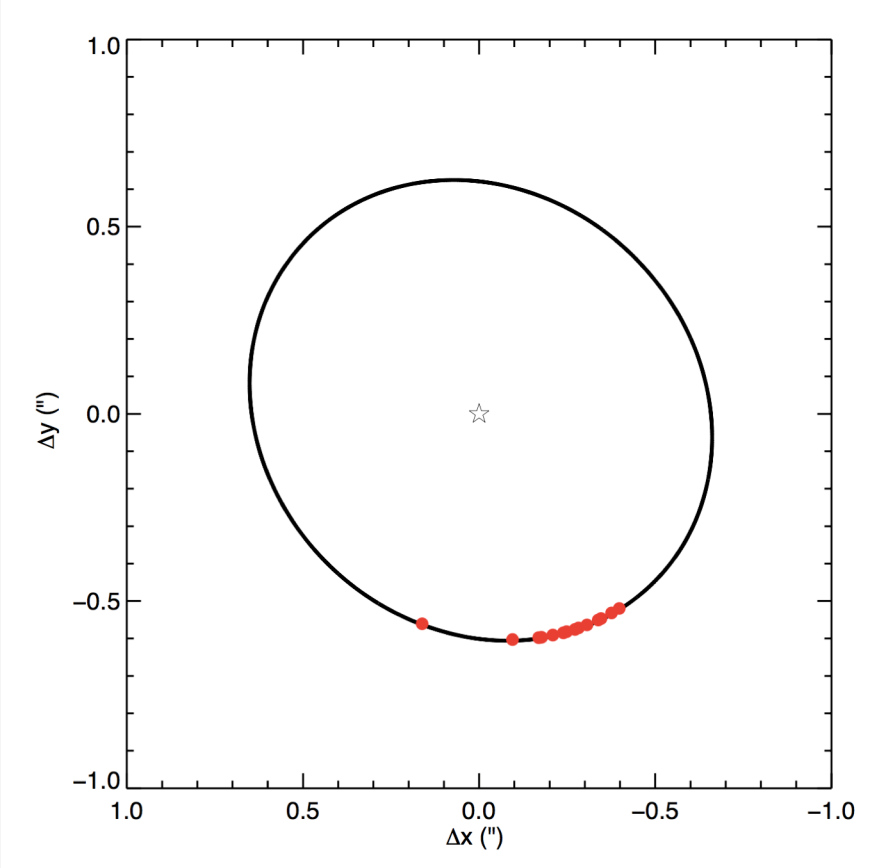


Zurlo et al. 2016

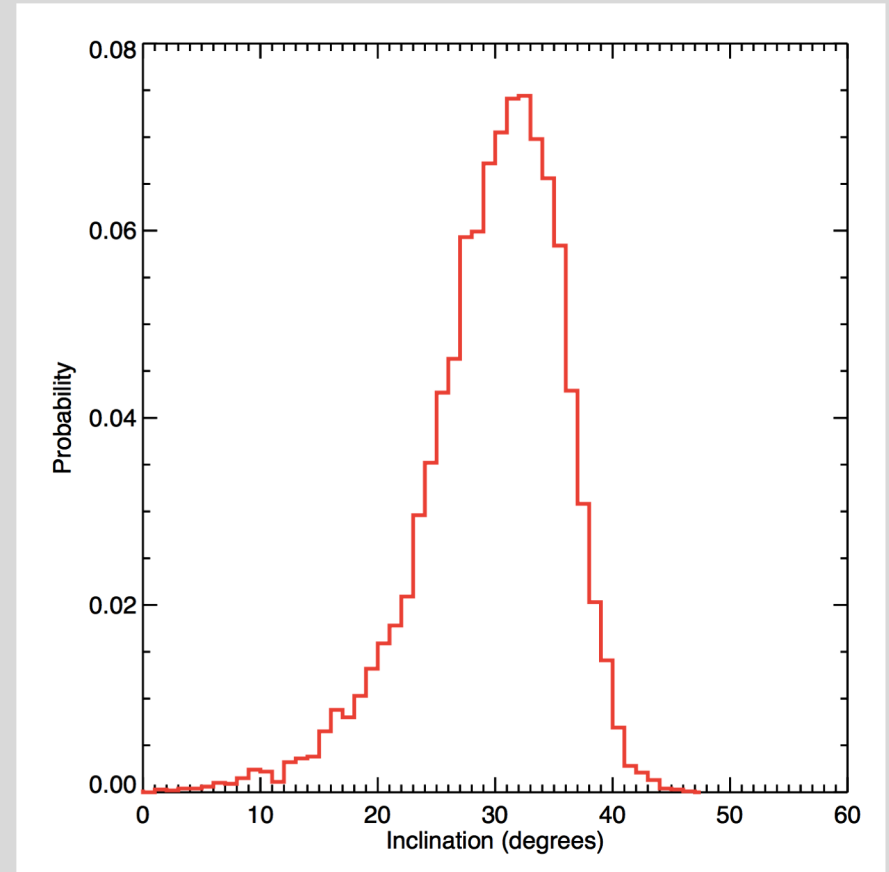
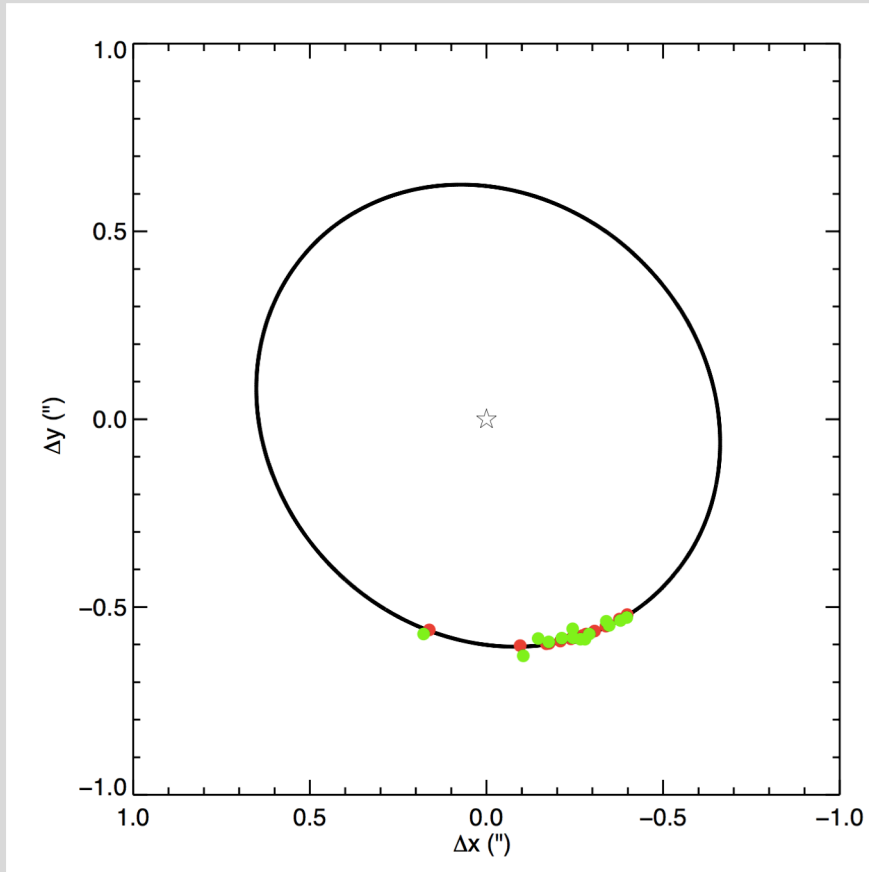
# Fitting undersampled orbits with systematics in astrometry can lead to biased results.



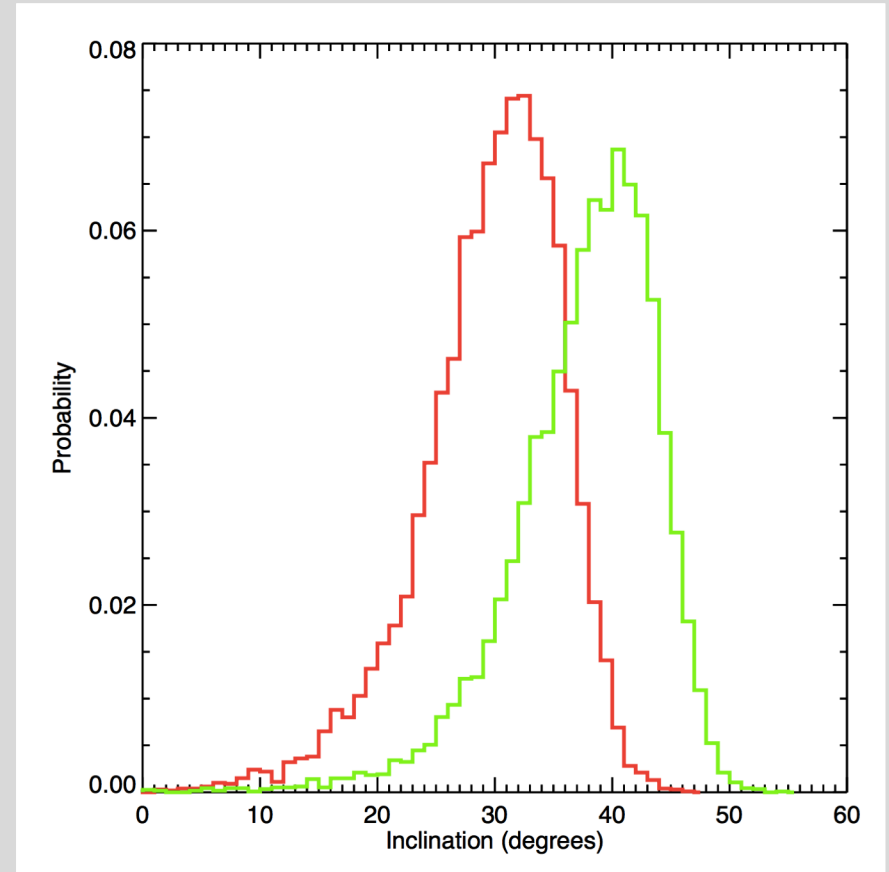
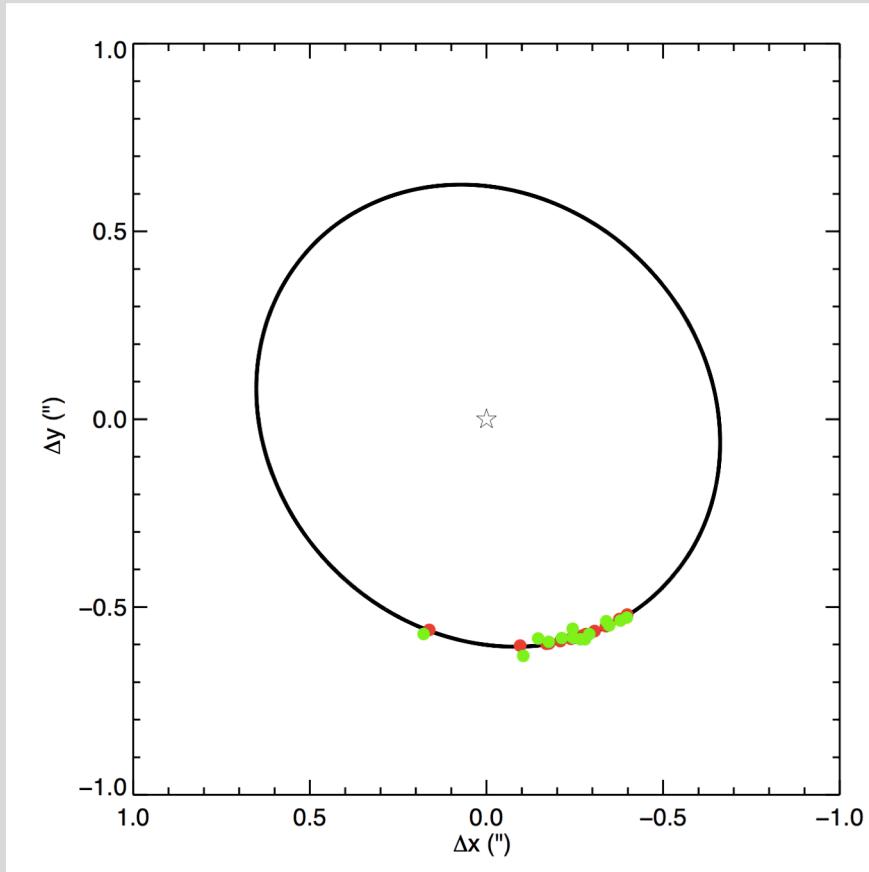
# Fitting undersampled orbits with systematics in astrometry can lead to biased results.



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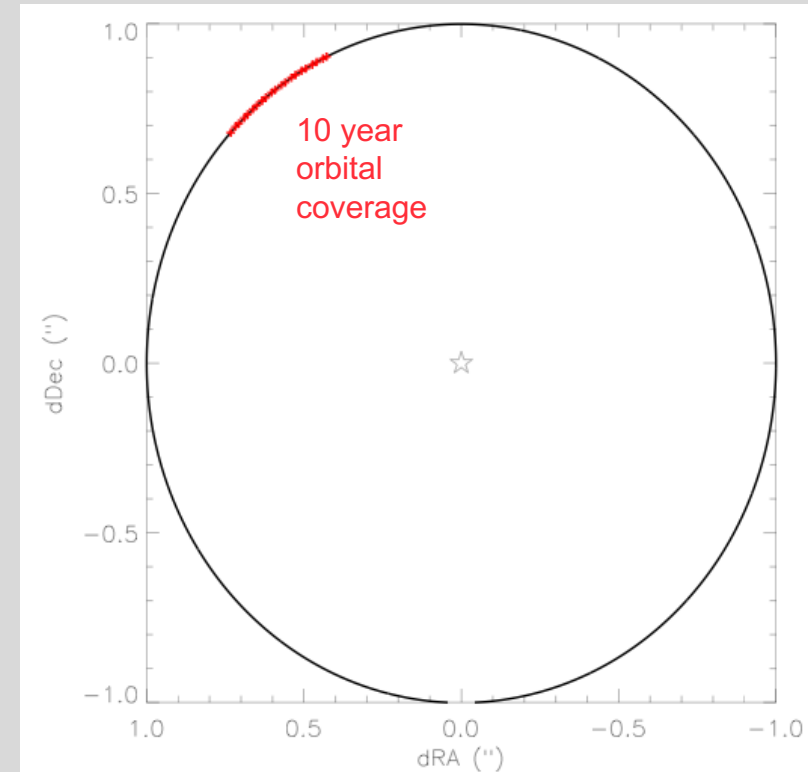
# Fitting undersampled orbits with systematics in astrometry can lead to biased results.



Konopacky et al. 2016a

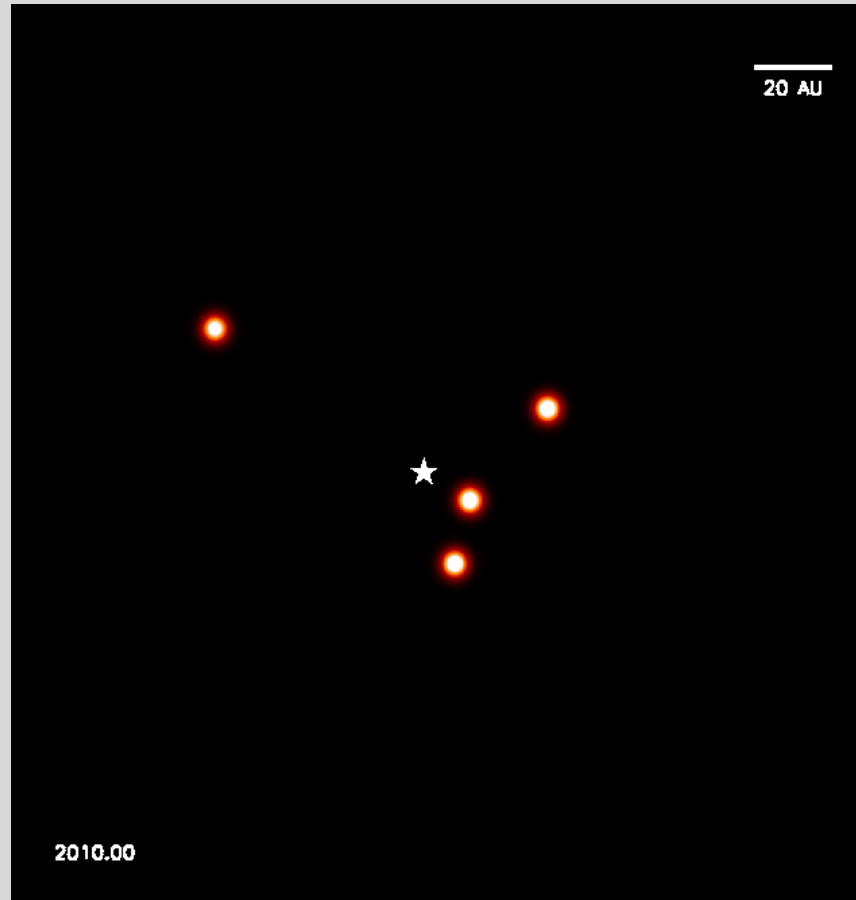
# But if we can control systematics and continue to push our precision, the results will be very rewarding!

- Over 10 years of monitoring, improving precision by a factor of  $\sim 2$  results in:
  - 30% better constraints on eccentricity
  - 60% better constraints on period
  - 40% better constraints on semimajor axis
  - 20% better constraints on inclination



**Circular, face on orbit with  $a=30$  AU and distance=30 pc**

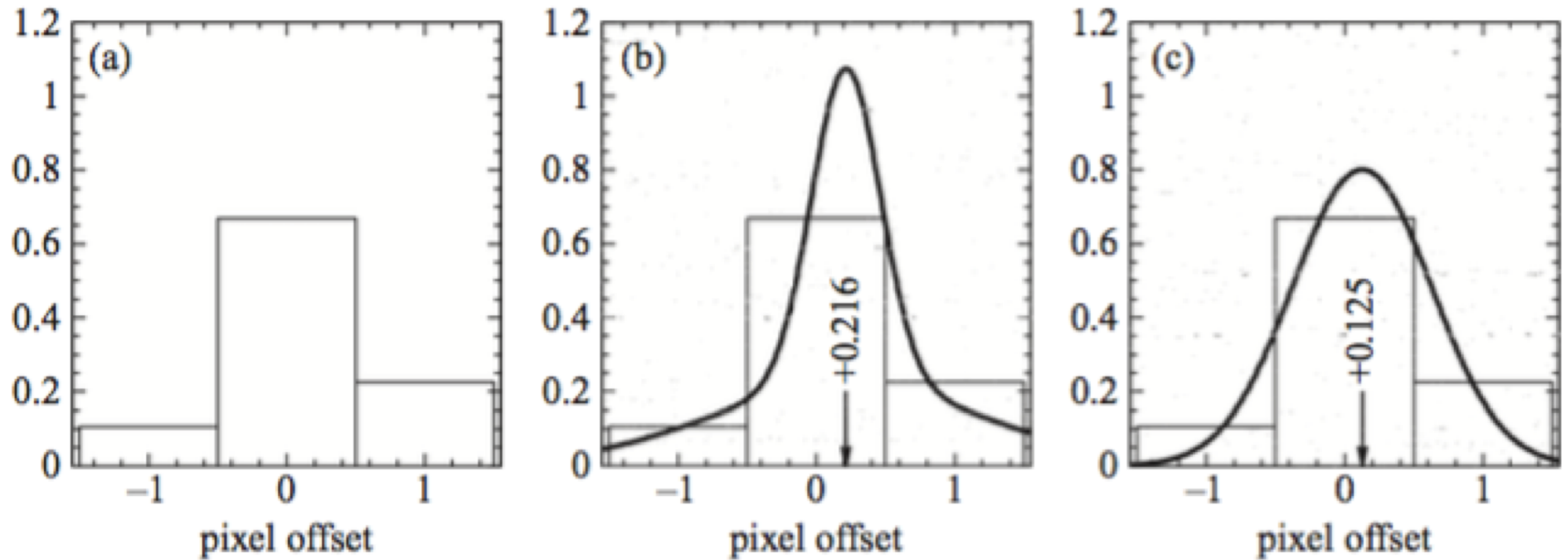




**Thanks! Hope everyone learned a lot this week!**

Good Reference Text: [Astrometry for Astrophysics: Methods, Models, and Applications](#),  
Ed. William van Altena

# Obtaining the exact center of light can be a challenging problem with an impacted PSF.



Anderson 2012 (undersampled PSF)