

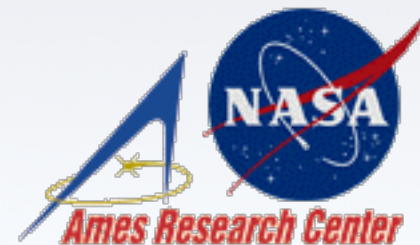
# The Demographics of Exoplanetary Companions to M Dwarfs and Free- Floating Planets

{ Synthesizing Results from Microlensing,  
Radial Velocity, and Direct Imaging Surveys

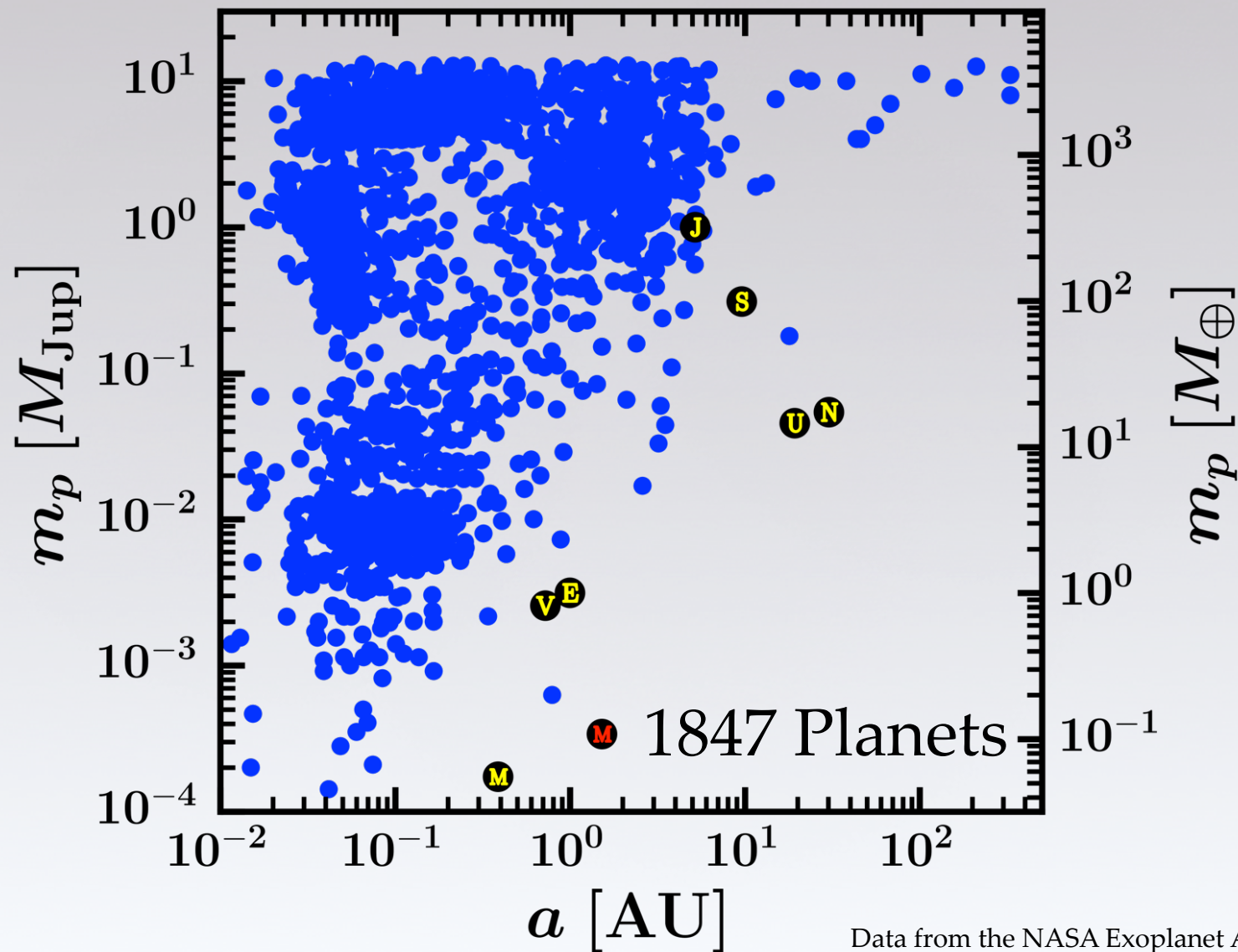
Sagan Exoplanet Summer Workshop 2016

**Christian Clanton**

NPP Fellow



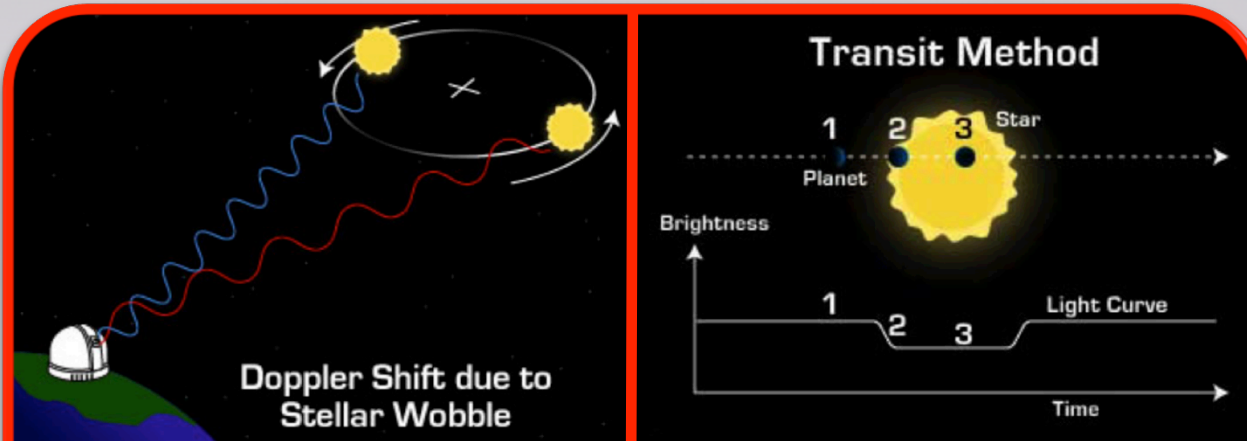
# Currently Known Planets (All Host Spectral Types)



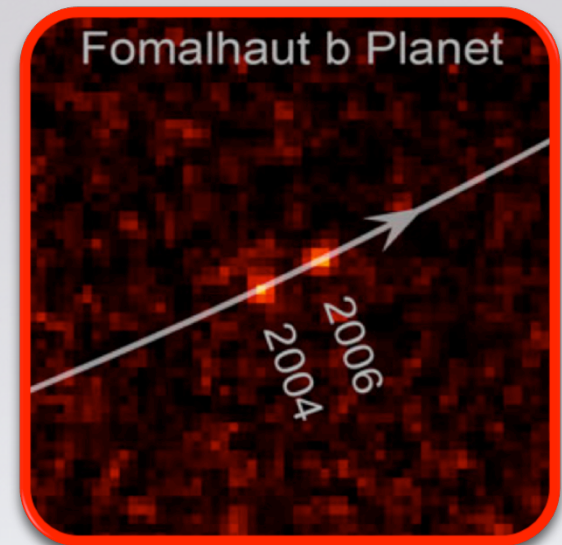


# Exoplanet Detection Methods

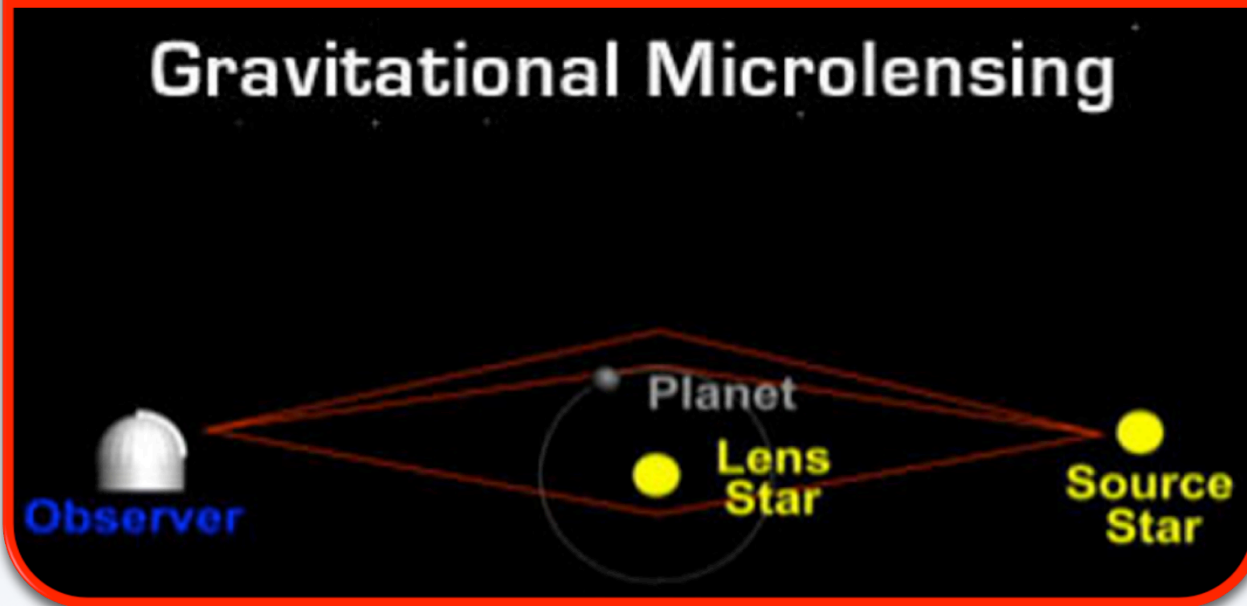
-Indirect-



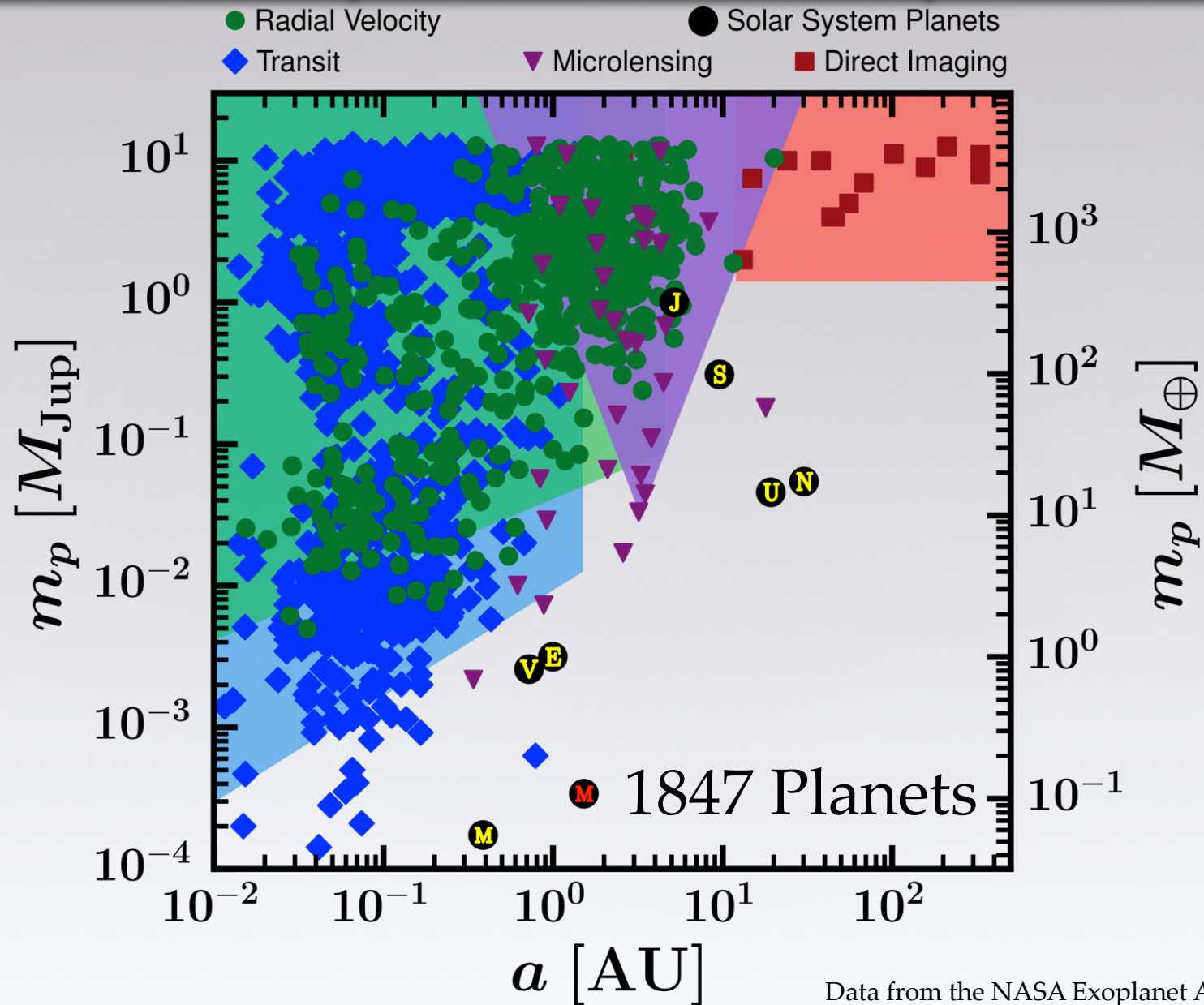
-Direct-



## Gravitational Microlensing



# Full Sample of Confirmed Exoplanets

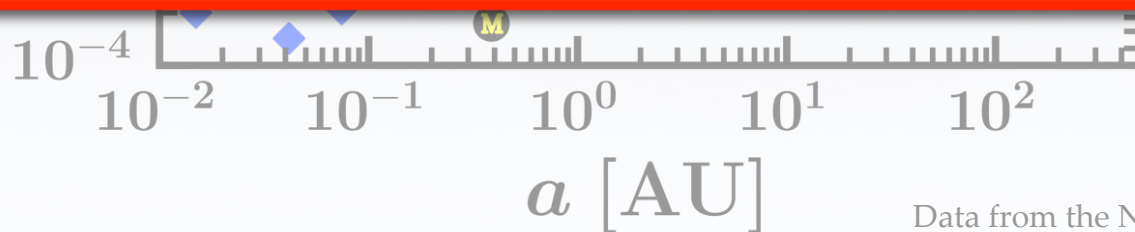


# Full Sample of Confirmed Exoplanets



## Primary Goal

Construct a statistically-complete census of exoplanets by synthesizing results from multiple detection techniques



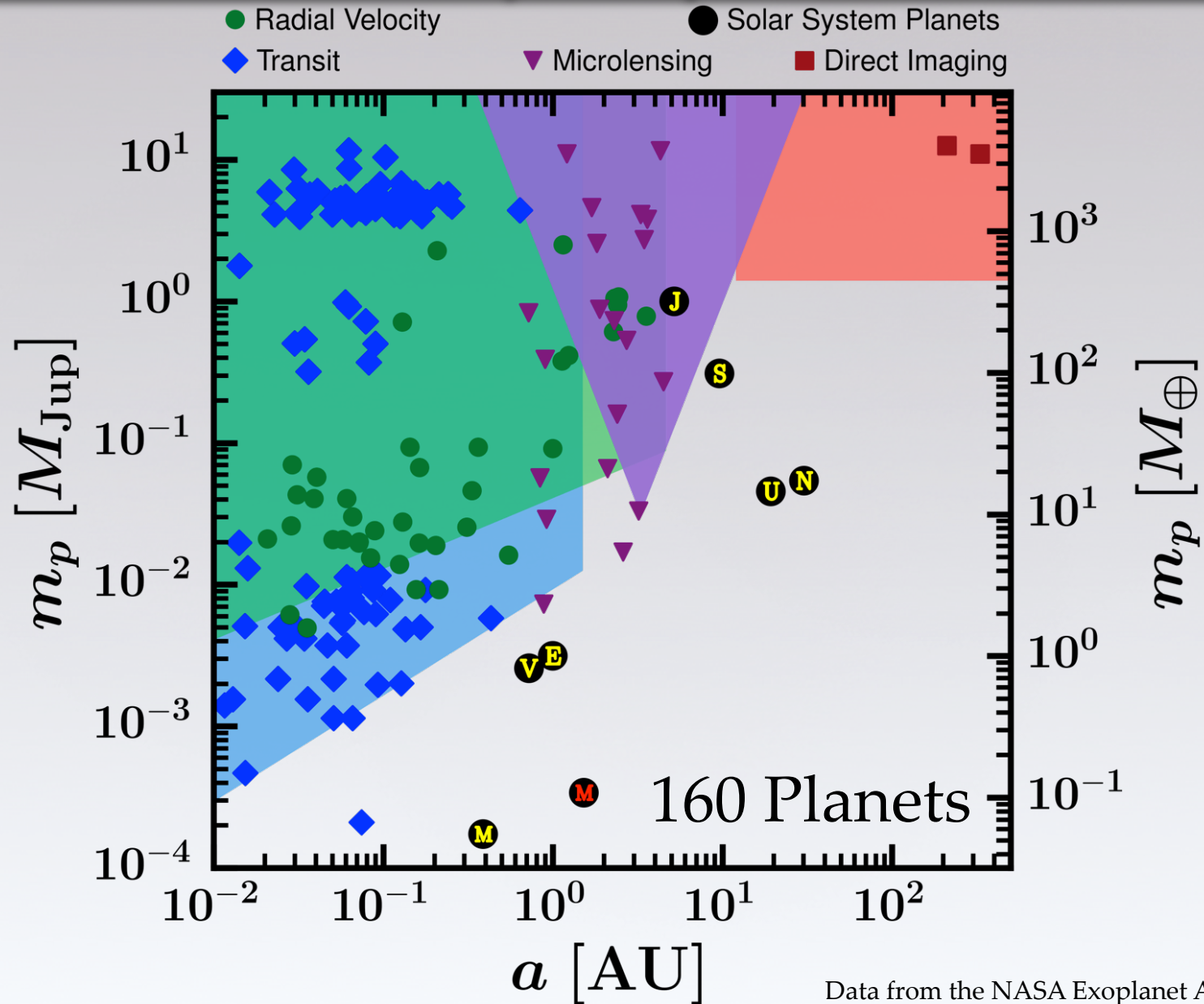
Part I.  
Demographics of Planets  
Around M Dwarfs



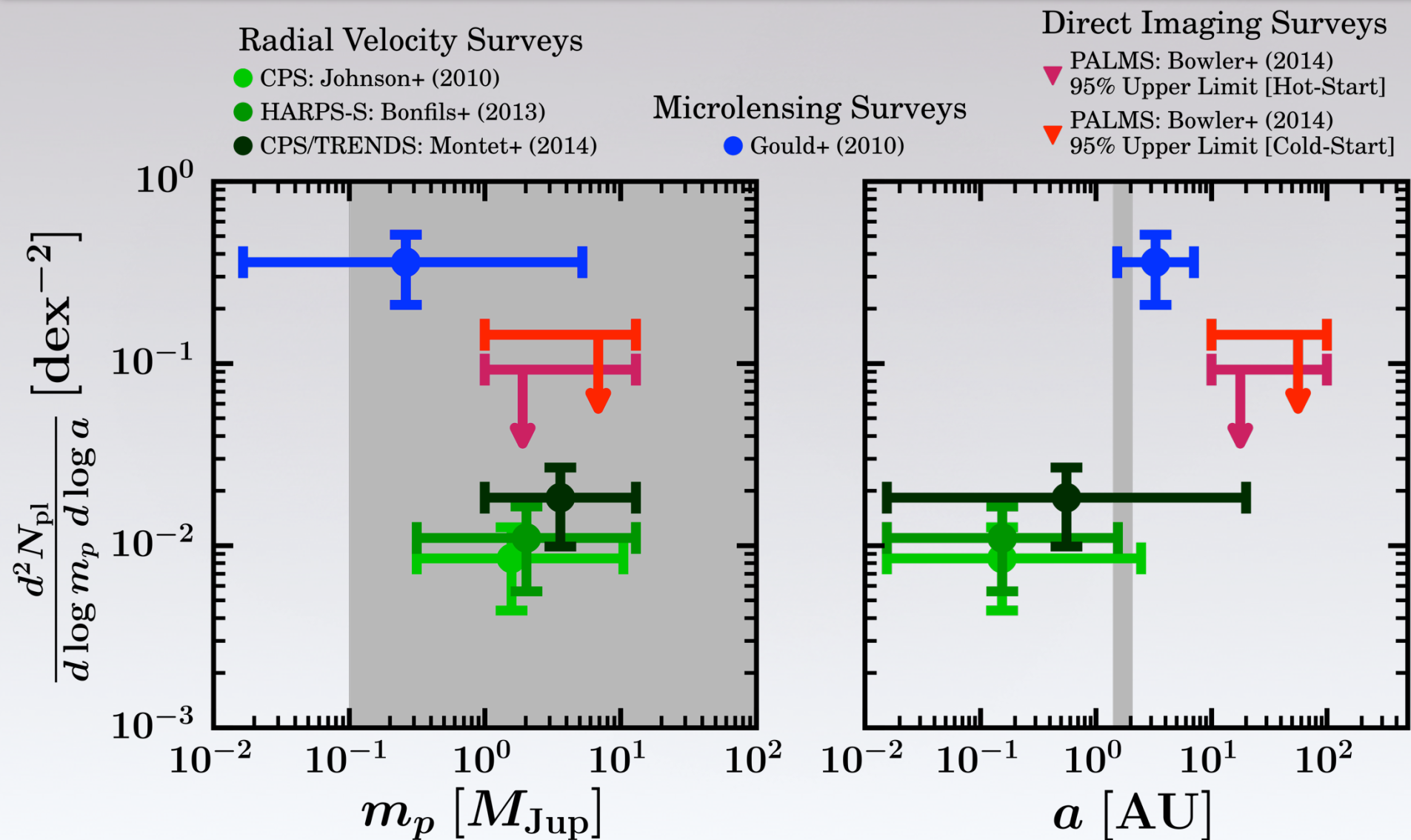
# M Dwarfs

Common  
Well-Characterized Demographics

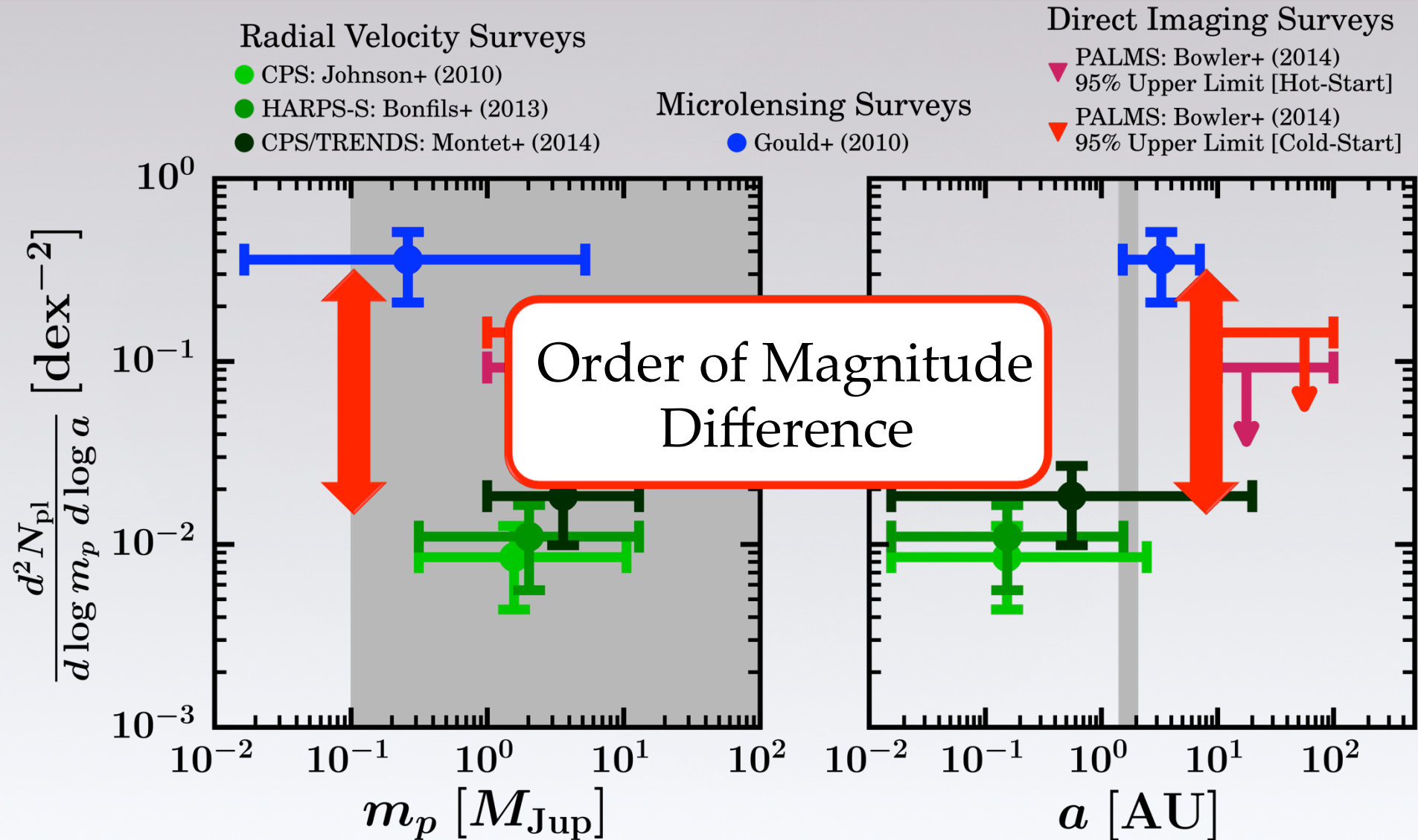
# Confirmed Planetary Companions to M Dwarfs



# Exoplanet Censuses of M Dwarfs from Individual Methods

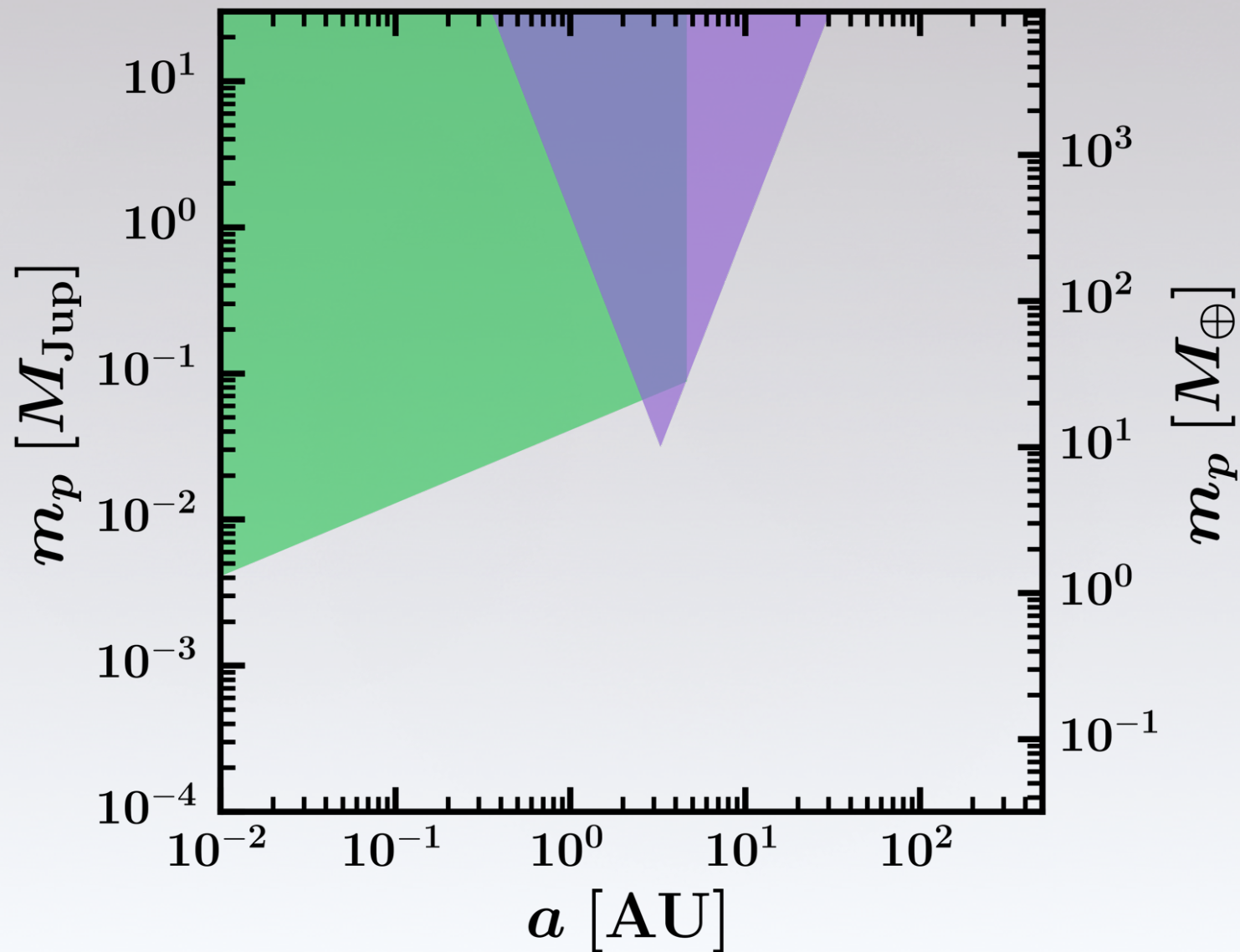


# Exoplanet Censuses of M Dwarfs from Individual Methods





# Sensitivities of Microlensing and RV Surveys



# “Microlensing Planets”

$$\frac{d^2 N_{\text{pl}}}{d \log q d \log s} = (0.23 \pm 0.10) \left( \frac{q}{5 \times 10^{-4}} \right)^{-0.68 \pm 0.20}$$

# “Microlensing Planets”

Sumi+ (2010) & Gould+ (2010)

Sumi+ (2010)

$$\frac{d^2 N_{\text{pl}}}{d \log q d \log s} = (0.23 \pm 0.10) \left( \frac{q}{5 \times 10^{-4}} \right)^{-0.68 \pm 0.20}$$

# “Microlensing Planets”

Sumi+ (2010) & Gould+ (2010)

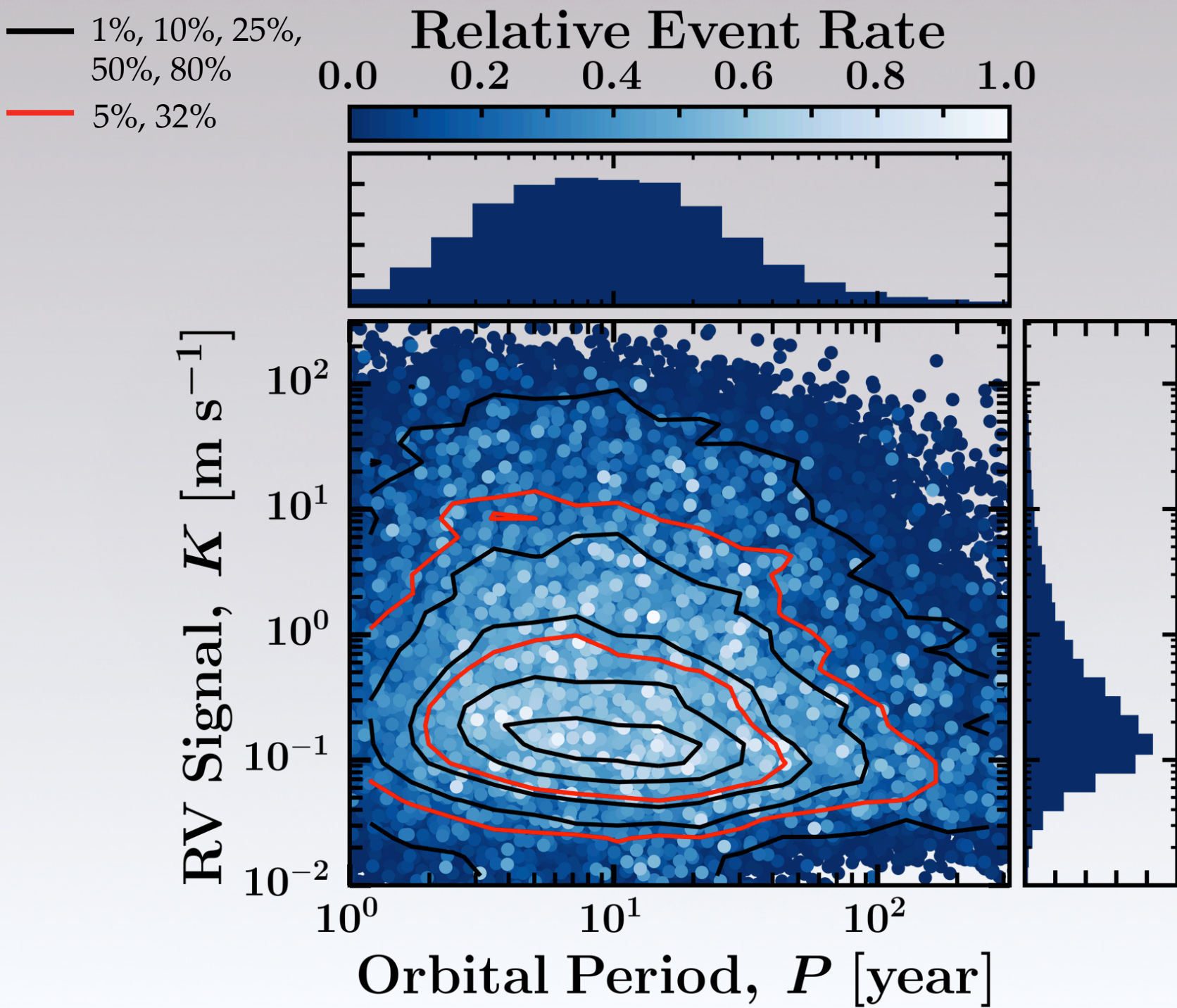
Sumi+ (2010)

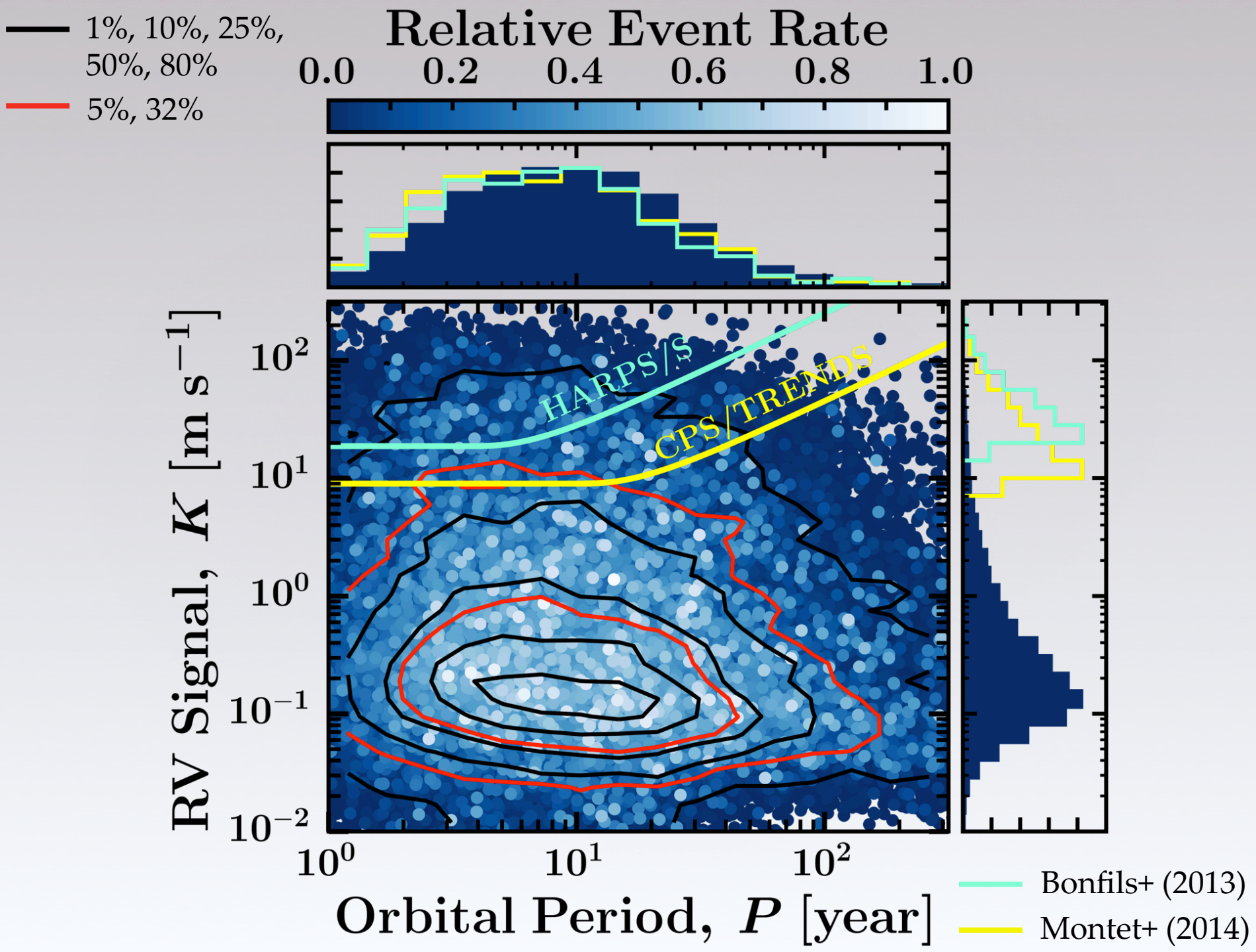
$$\frac{d^2 N_{\text{pl}}}{d \log q d \log s} = (0.23 \pm 0.10) \left( \frac{q}{5 \times 10^{-4}} \right)^{-0.68 \pm 0.20}$$

Map the properties of such planets  
into the space of RV observables:

$$(q, s) \rightarrow (K, P)$$







# Comparison with HARPS-S (Bonfils+ 2013)

Expected:

**1.1 ± 0.8**

Actual:

**1**

$$1 \lesssim m_p/M_{\text{Jup}} \lesssim 13 \quad ; \quad 3 \lesssim P/\text{years} \lesssim 10$$

# Comparison with CPS/TRENDS (Montet+ 2014)

Expected Number:

**$4.7 \pm 2.7$**

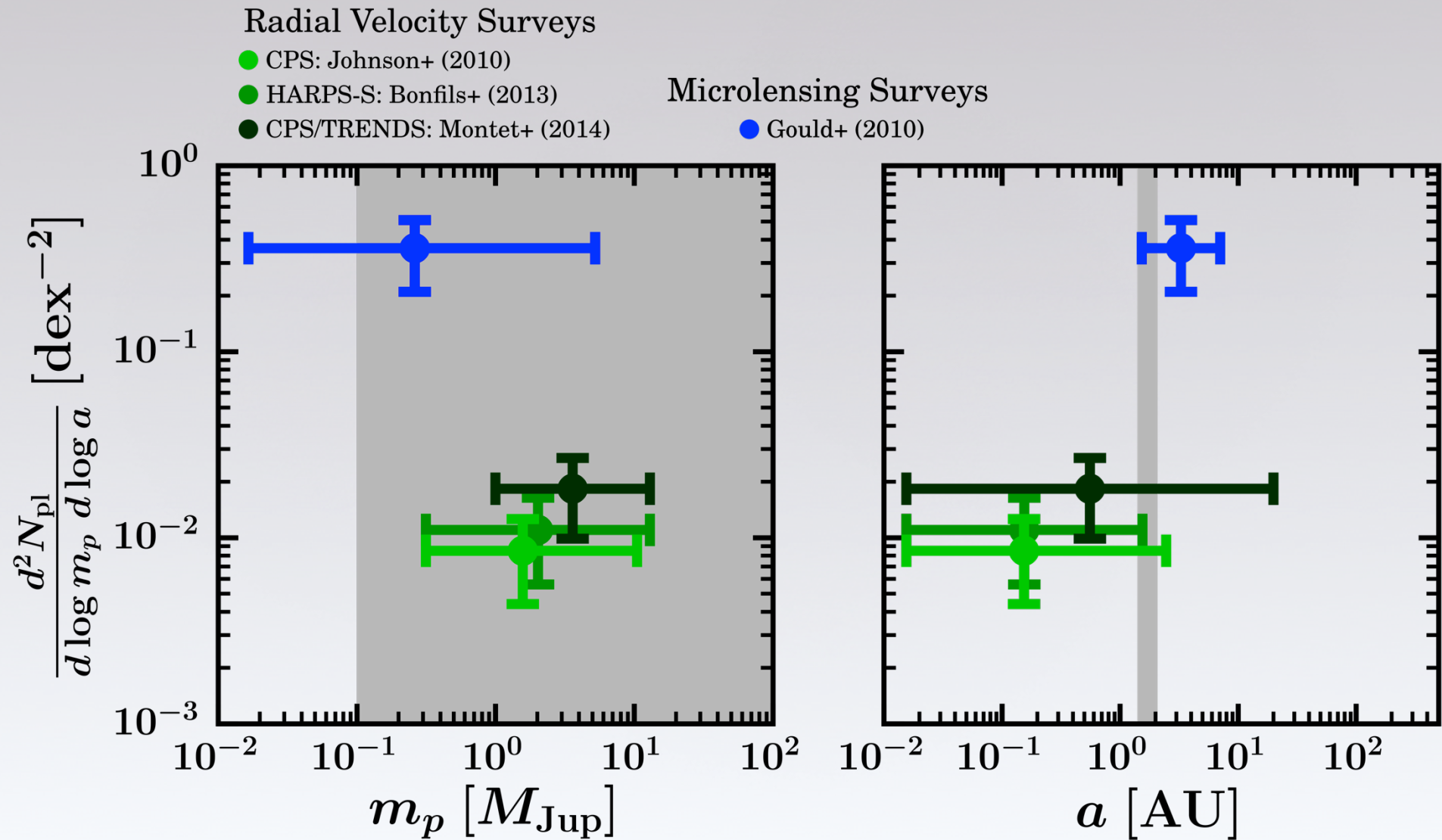
Actual Number:

**4**

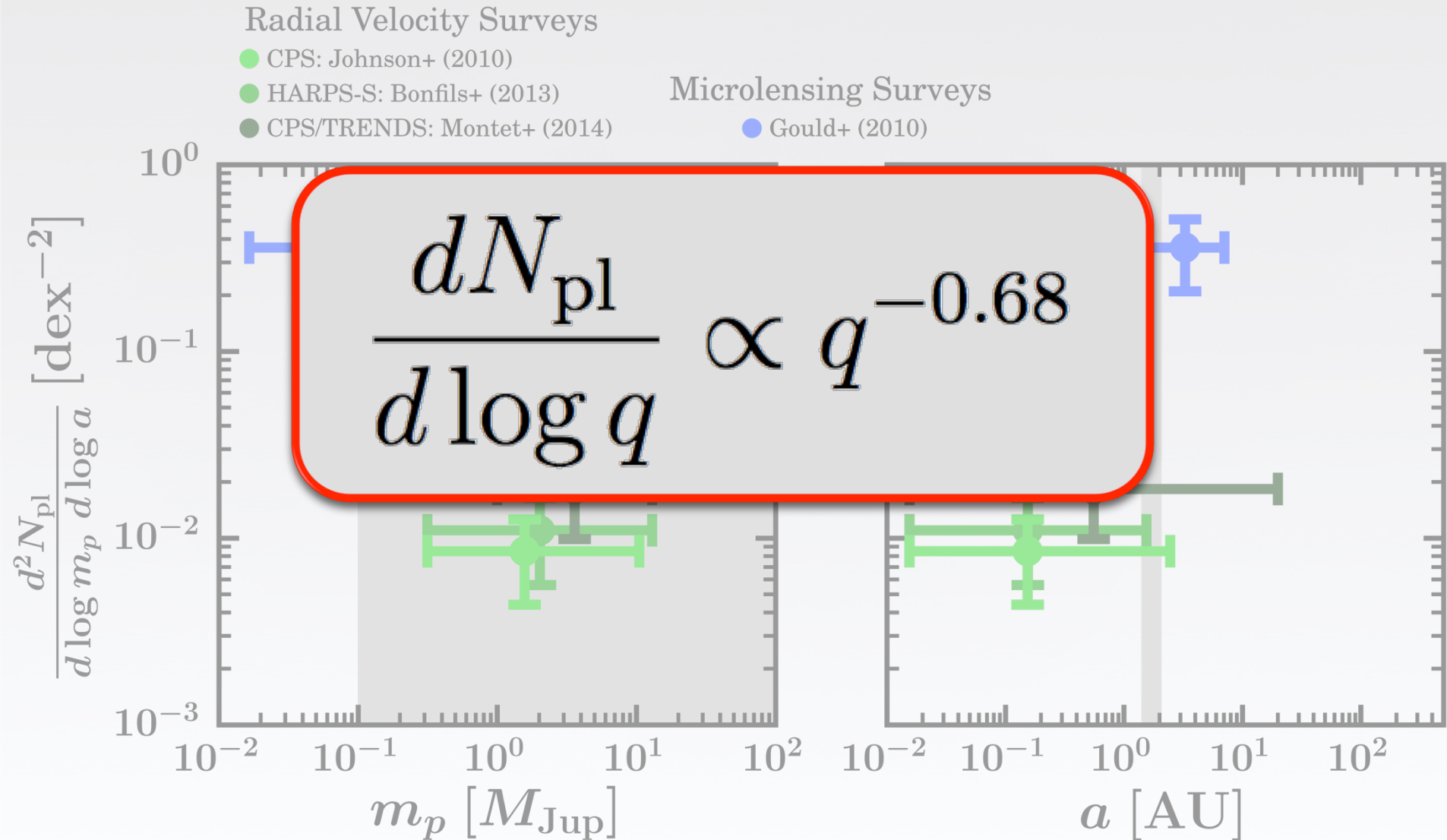
Similar Masses and Orbital Periods



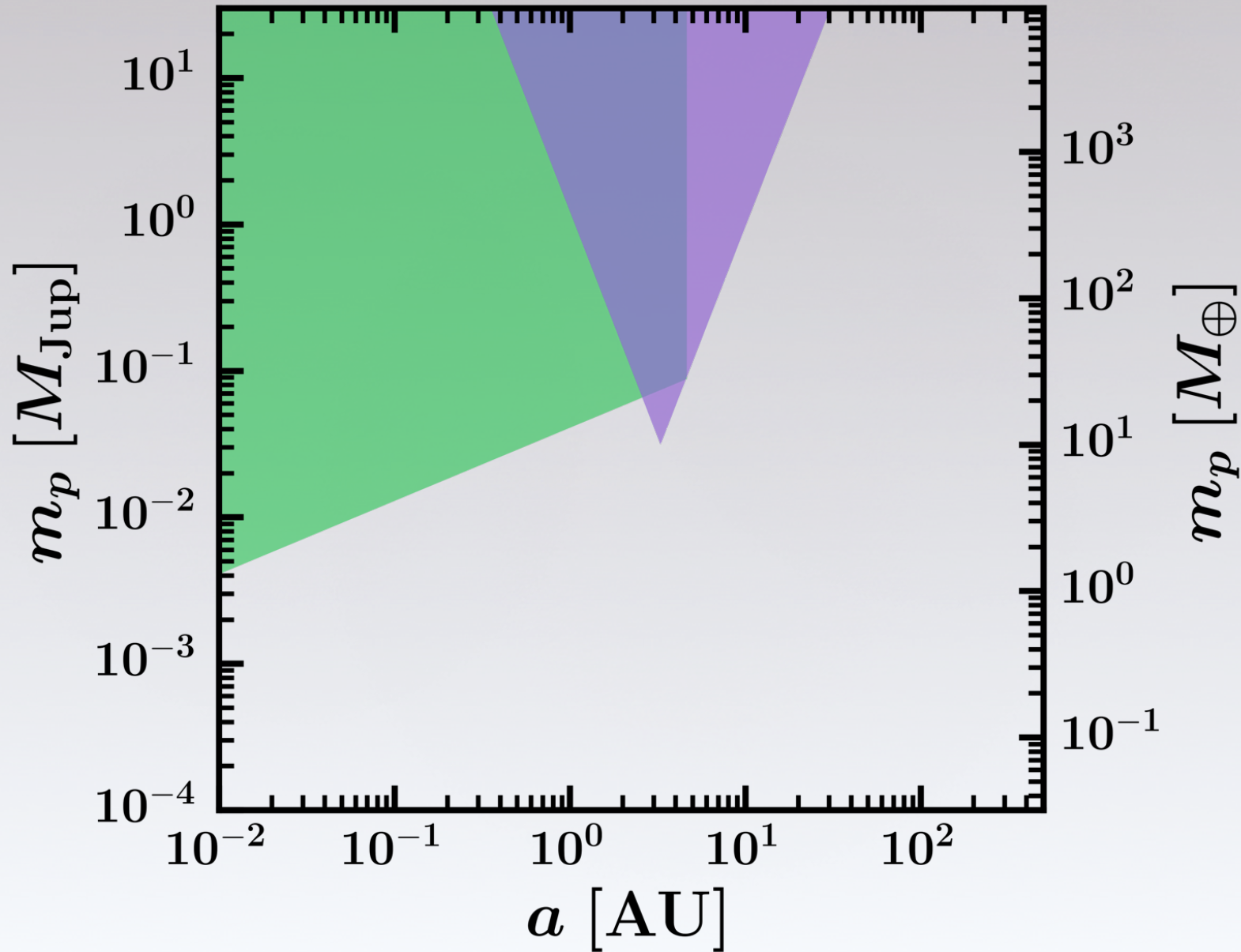
# Consistency Between Microlensing and RV Results



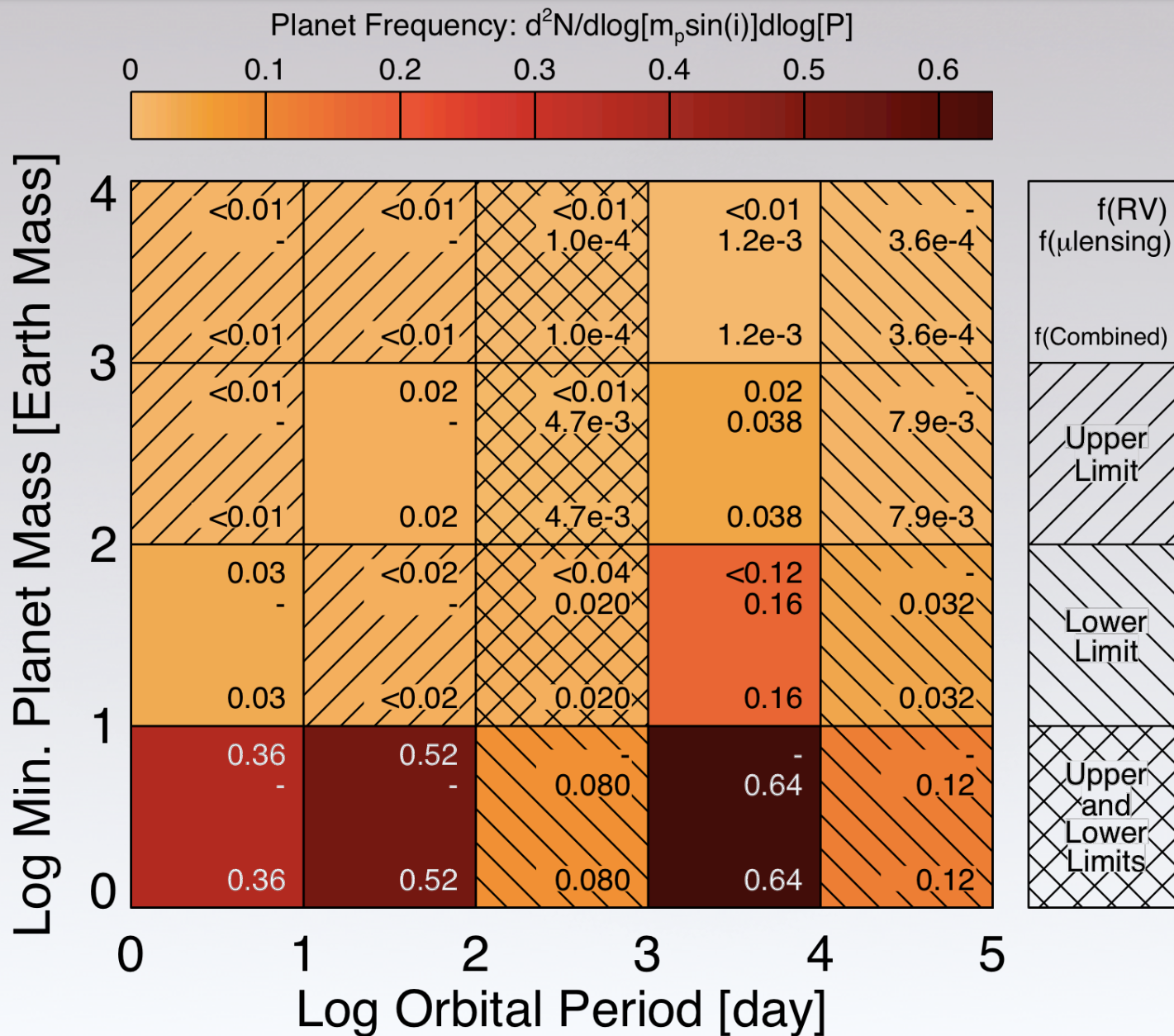
# Consistency Between Microlensing and RV Results



# Synthesizing Microlensing and RV Results

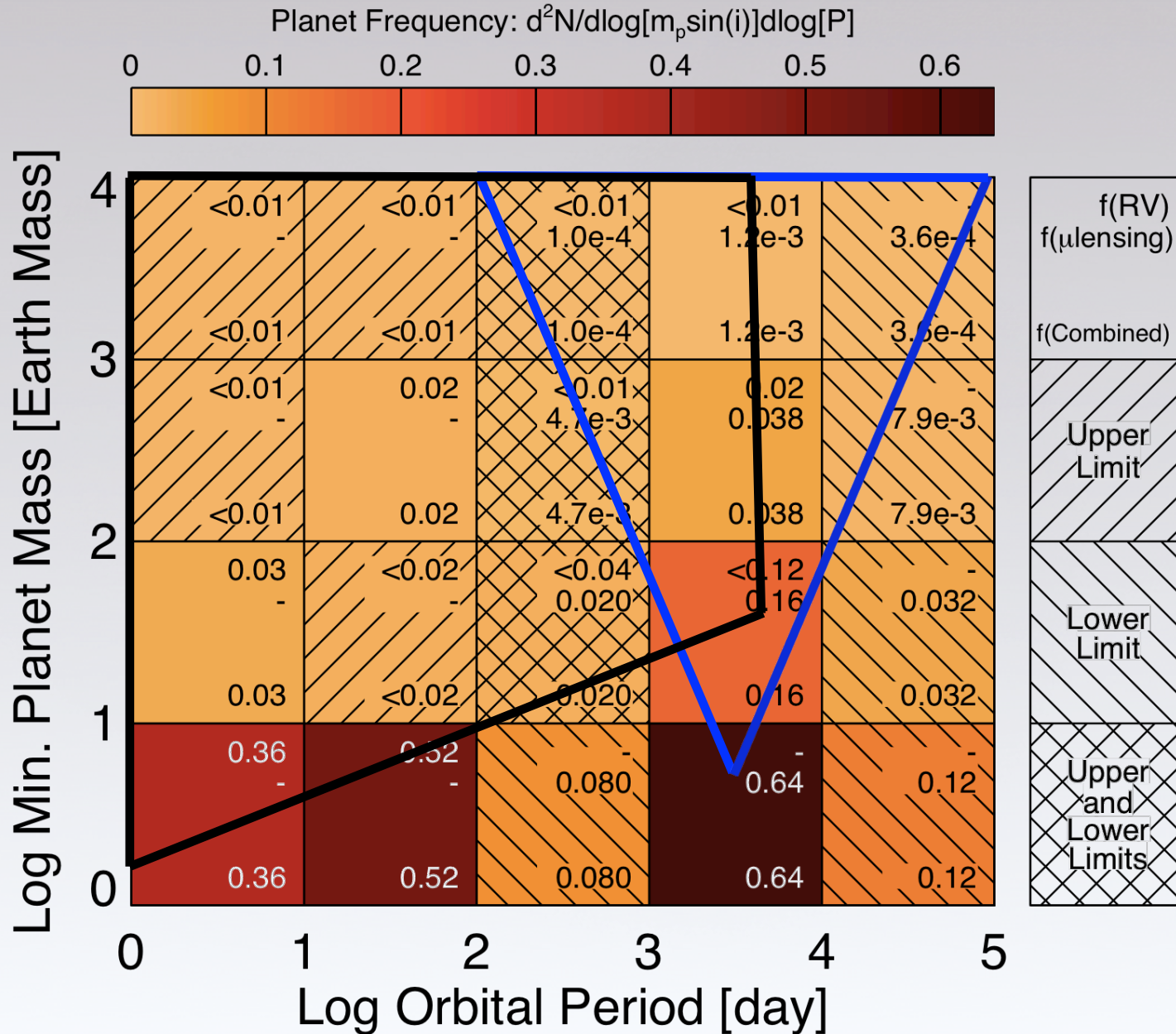


# Synthesized Constraints

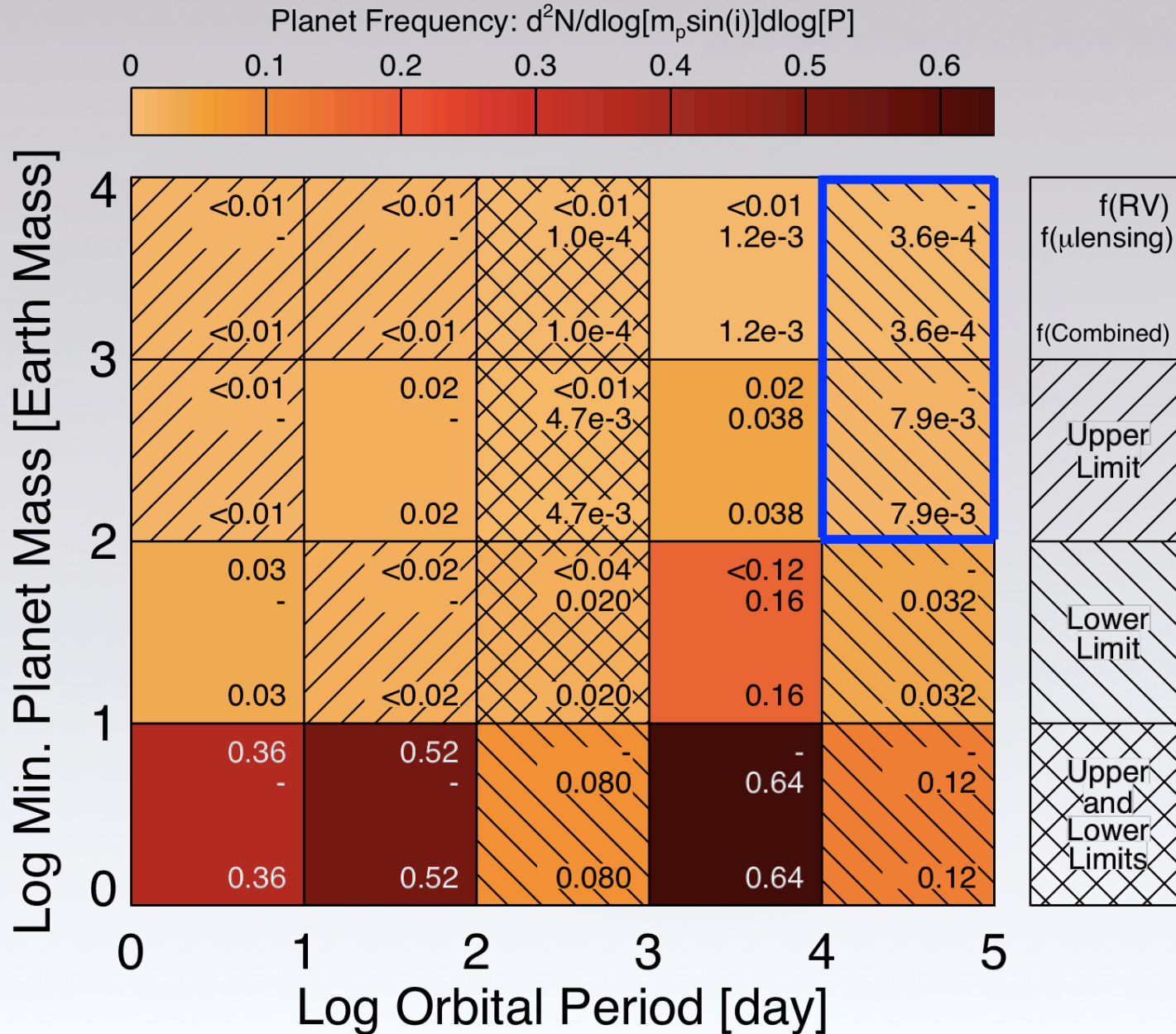




# Synthesized Constraints



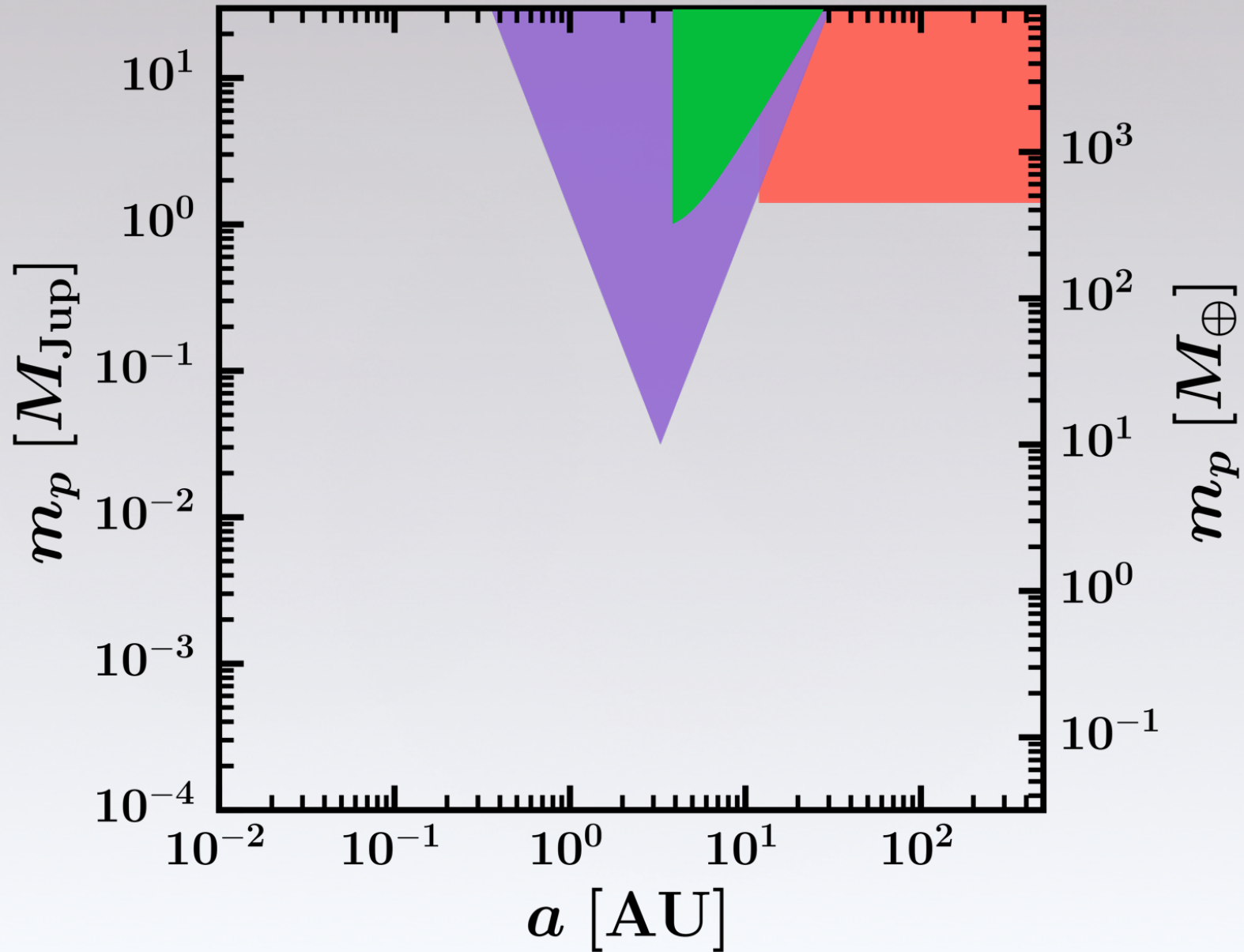
# Improving Constraints on Long-Period Planets



## Part II.

# Long-Period Planets: Synthesizing Results from Microlensing, Radial Velocity, and Direct Imaging Surveys

# Direct Imaging + Microlensing + RV Trends





# Constraints on Long-Period Planetary Companions to M Dwarfs

## Microlensing Surveys

Gould+ (2010)

Sumi+ (2010)

## Radial Velocity Surveys

Montet+ (2014)

## Direct Imaging Surveys

Bowler+ (2014)

Lafrenière+ (2007)

# Constraints on Long-Period Planetary Companions to M Dwarfs

## Primary Question

Is there a single planet  
population that is consistent  
with the results of these  
surveys?

# Model

---

$$\frac{d^2 N_{\text{pl}}}{d \log m_p d \log a} = \mathcal{A} \left( \frac{m_p}{M_{\text{Sat}}} \right)^\alpha \left( \frac{a}{2.5 \text{ AU}} \right)^\beta$$

$$\{ \alpha, \beta, \mathcal{A}, a_{\text{out}} \}$$

# Methodology

$$(m_p, a)$$

Gravitational Microlensing	Radial Velocity (RV)	Direct Imaging
$(q, s)$	$(\dot{v}, P)$	$(\Delta\text{mag}, \rho)$



# Microlensing

$$(m_p, a) \rightarrow (q, s)$$

$$q(m_p, M_L)$$

$$s(a, i, e, \omega, E, M_L, D_L, D_S)$$

# Methodology

$$(m_p, a)$$

Gravitational Microlensing	RV	Direct Imaging
$(q, s)$	$(\dot{v}, P)$	$(\Delta\text{mag}, \rho)$
<ul style="list-style-type: none"><li>- Orbital Parameters</li><li>- Lens Distances</li><li>- Lens Mass Function</li><li>- Galactic Model</li></ul>		

## RV Trends

---

$$(m_p, a) \rightarrow (\dot{v}, P)$$

$$\dot{v}(m_p, a, M_L, i, e, M_0)$$

$$P(a, M_L)$$

# Methodology

$$(m_p, a)$$

Gravitational Microlensing	Radial Velocity (RV)	Direct Imaging
$(q, s)$	$(\dot{v}, P)$	$(\Delta\text{mag}, \rho)$
<ul style="list-style-type: none"><li>- Orbital Parameters</li><li>- Lens Distances</li><li>- Lens Mass Function</li><li>- Galactic Model</li></ul>	<ul style="list-style-type: none"><li>- Orbital Parameters</li><li>- Host masses</li></ul>	



# Direct Imaging

$$(m_p, a) \rightarrow (\Delta\text{mag}, \rho)$$

$$\Delta\text{mag}(M_{H,\text{pl}}, D_L, H_L)$$

$$\rho(a, i, e, \omega, M_0, D_L)$$

# Direct Imaging

$$(m_p, a) \rightarrow (\Delta\text{mag}, \rho)$$

$$\Delta\text{mag}(M_{H,\text{pl}}, D_L, H_L)$$

$$\rho(a, i, e, \omega, M_0, D_L)$$

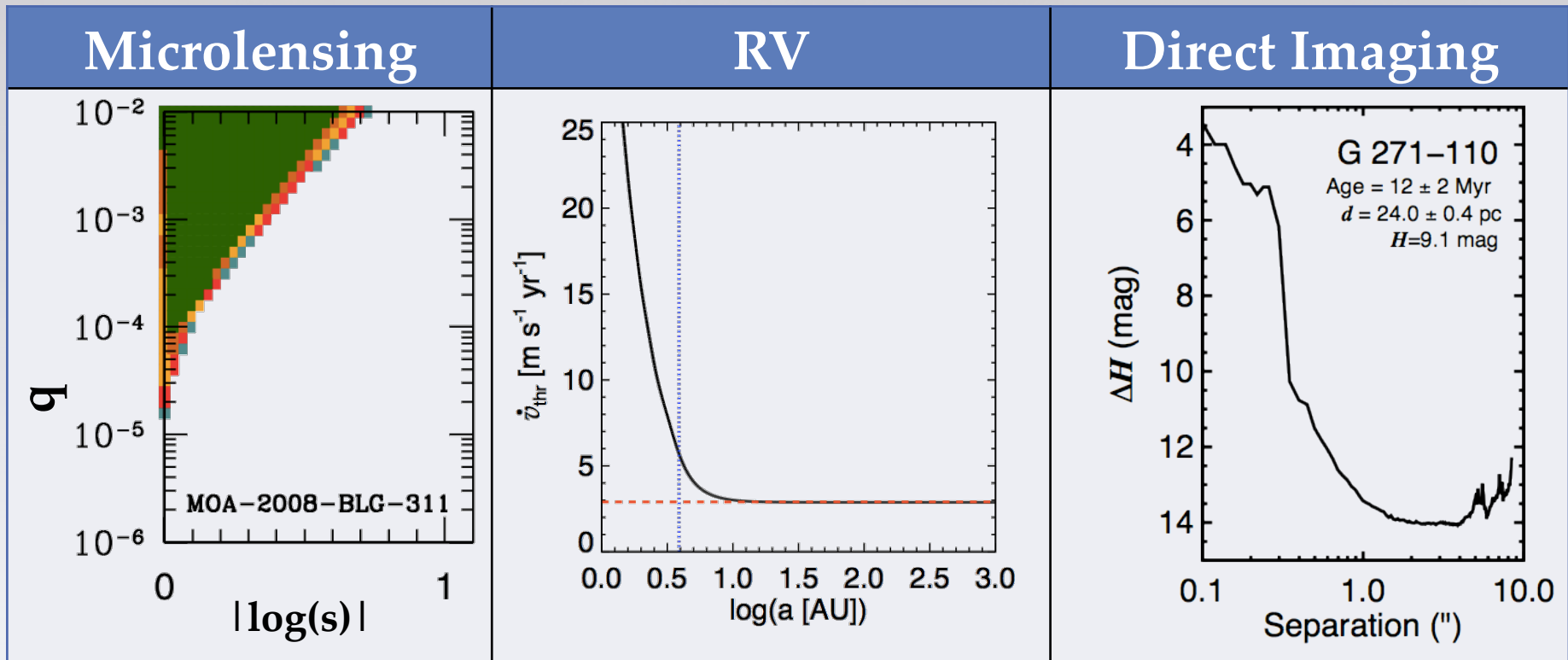


# Methodology

$$(m_p, a)$$

Gravitational Microlensing	Radial Velocity (RV)	Direct Imaging
$(q, s)$	$(\dot{v}, P)$	$(\Delta\text{mag}, \rho)$
<ul style="list-style-type: none"><li>- Orbital Parameters</li><li>- Lens Distances</li><li>- Lens Mass Function</li><li>- Galactic Model</li></ul>	<ul style="list-style-type: none"><li>- Orbital Parameters</li><li>- Host masses</li></ul>	<ul style="list-style-type: none"><li>- Orbital Parameters</li><li>- Ages and Distances</li><li>- Planet Evolution Models (Hot-/Cold-Start)</li></ul>

# Methodology



Above figure from Gould+ (2010)

Above figure from Bowler+ (2015)



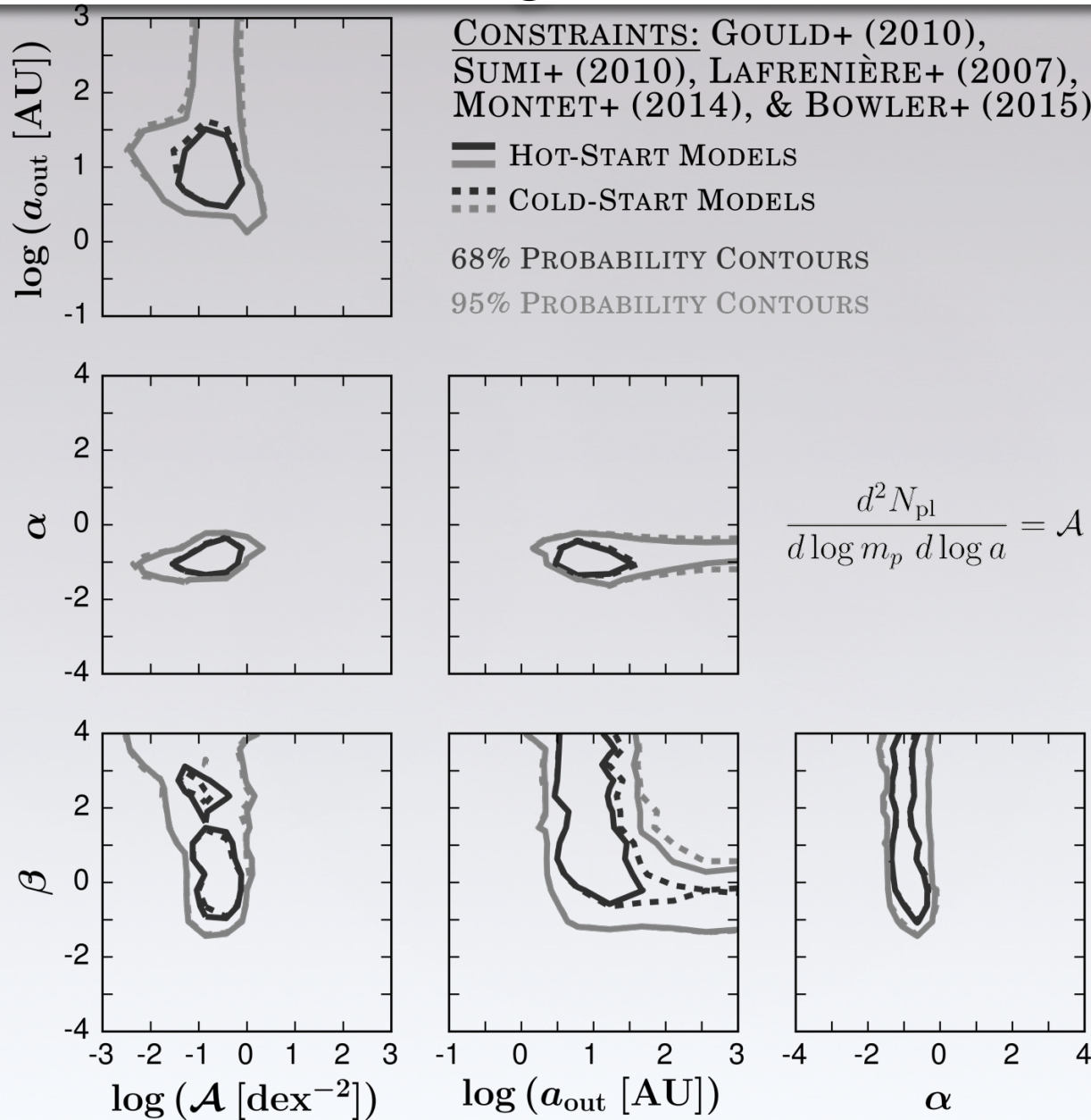
# Model

---

$$\frac{d^2 N_{\text{pl}}}{d \log m_p d \log a} = \mathcal{A} \left( \frac{m_p}{M_{\text{Sat}}} \right)^\alpha \left( \frac{a}{2.5 \text{ AU}} \right)^\beta$$

$$\{ \alpha, \beta, \mathcal{A}, a_{\text{out}} \}$$

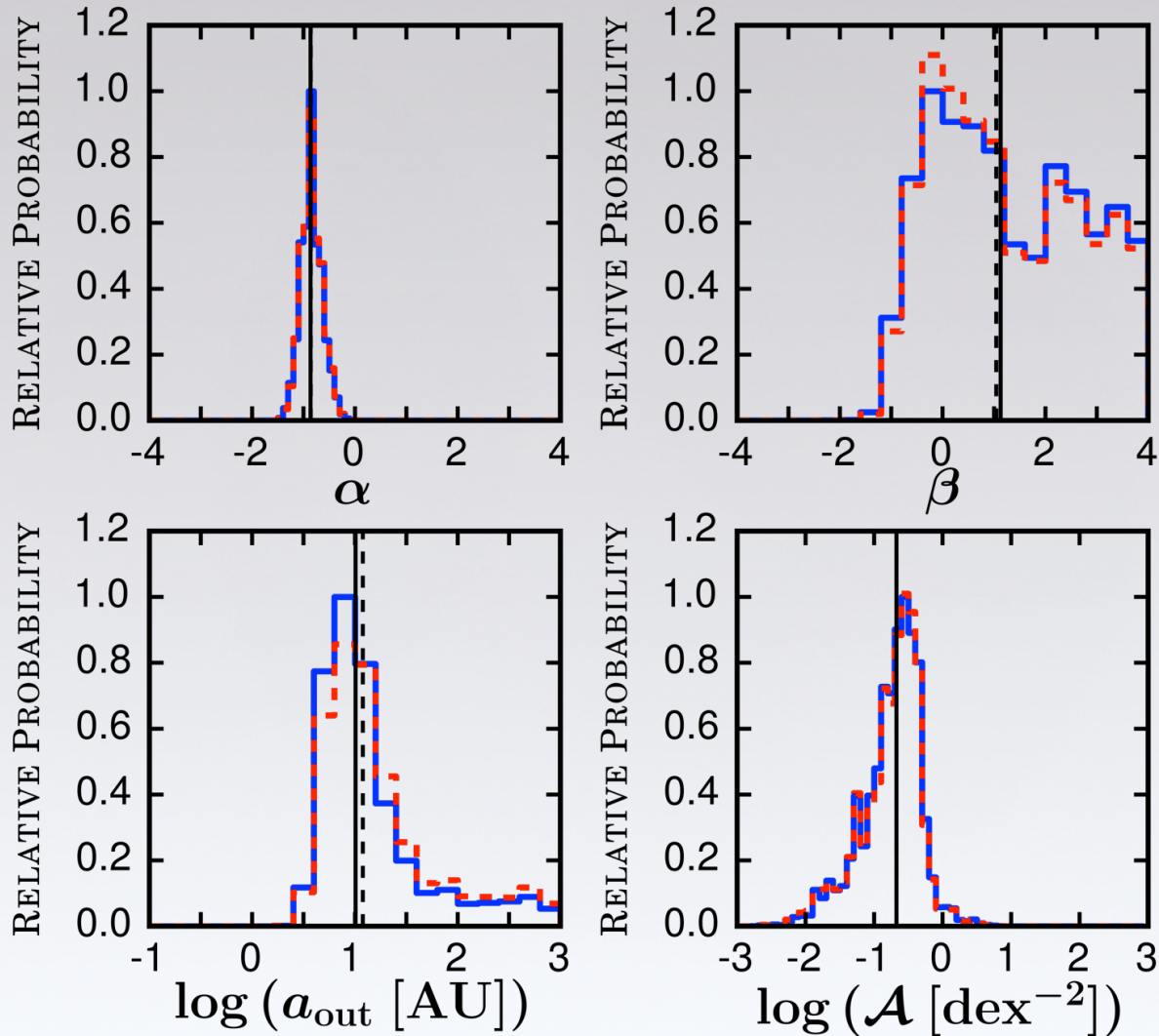
# Results: Microlensing + RV Trends + Imaging



# Results: Marginal Distributions

CONSTRAINTS: GOULD+ (2010),  
SUMI+ (2010), LAFRENIÈRE+ (2007),  
MONTET+ (2014), & BOWLER+ (2015)

— HOT-START  
- - - COLD-START  
- - - MEDIAN VALUES



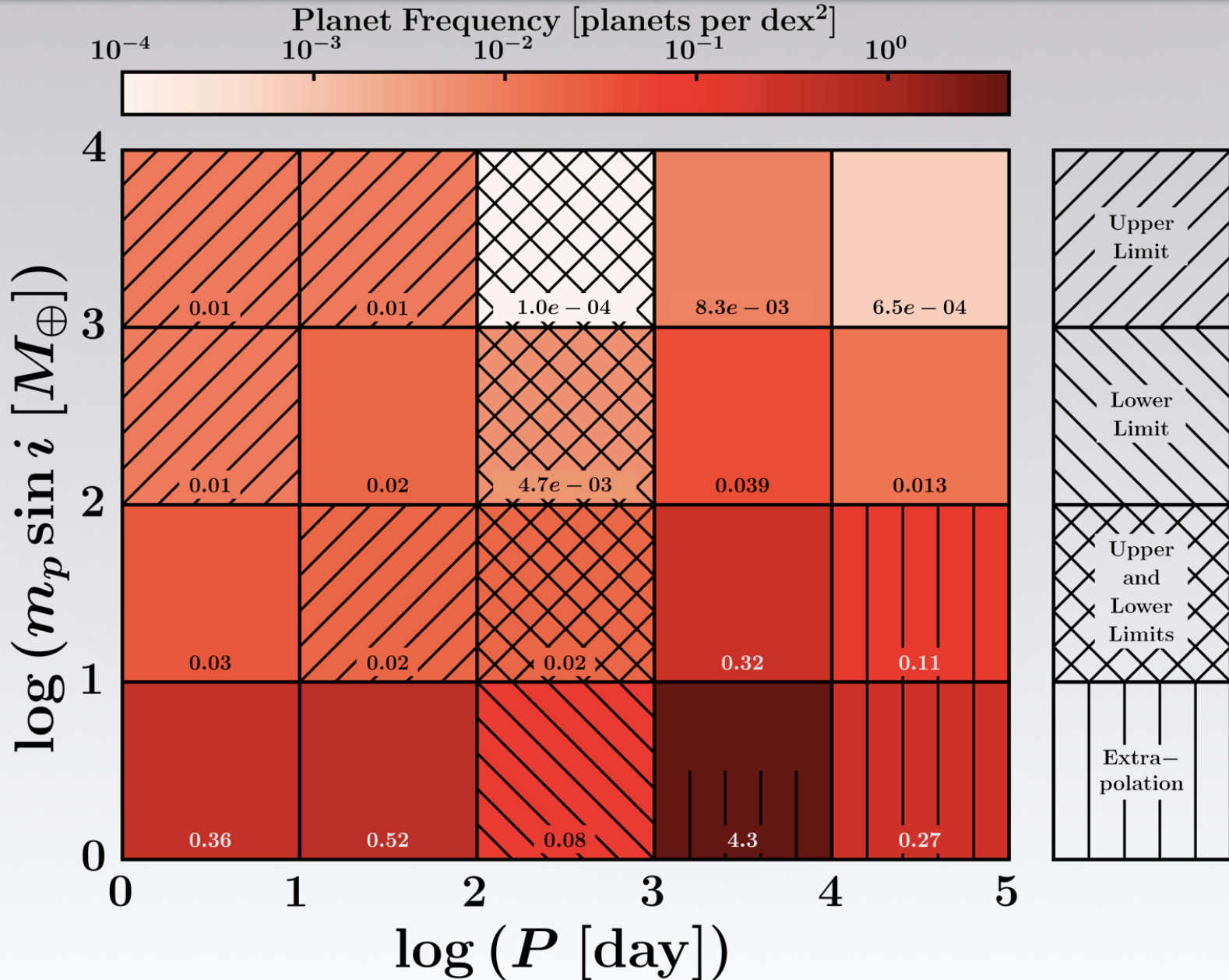
# Results: Final Parameter Constraints

Planet Evolutionary Models	Median Values and 68% Uncertainties			
	$\alpha$	$\beta$	$\mathcal{A}$ [dex <sup>-2</sup> ]	$a_{\text{out}}$ [AU]
“Hot-Start” (Baraffe et al. 2003)	$-0.86^{+0.21}_{-0.19}$	$1.1^{+1.9}_{-1.4}$	$0.21^{+0.20}_{-0.15}$	$10^{+26}_{-4.7}$
“Cold-Start” (Fortney et al. 2008)	$-0.85^{+0.21}_{-0.19}$	$1.1^{+1.9}_{-1.3}$	$0.21^{+0.20}_{-0.15}$	$12^{+50}_{-6.2}$

$$\frac{d^2 N_{\text{pl}}}{d \log m_p d \log a} = \mathcal{A} \left( \frac{m_p}{M_{\text{Sat}}} \right)^\alpha \left( \frac{a}{2.5 \text{ AU}} \right)^\beta$$



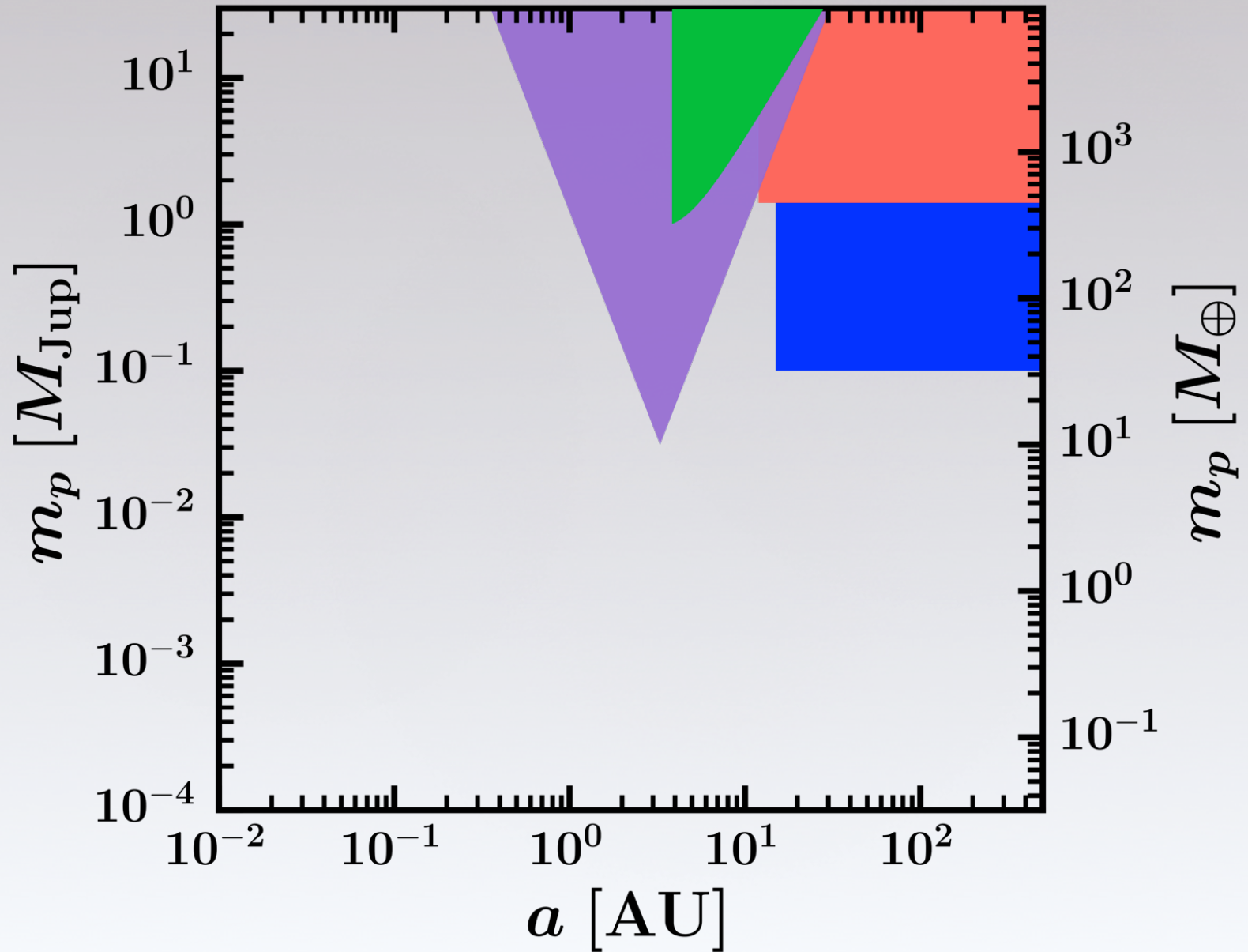
# Updated Demographic Constraints



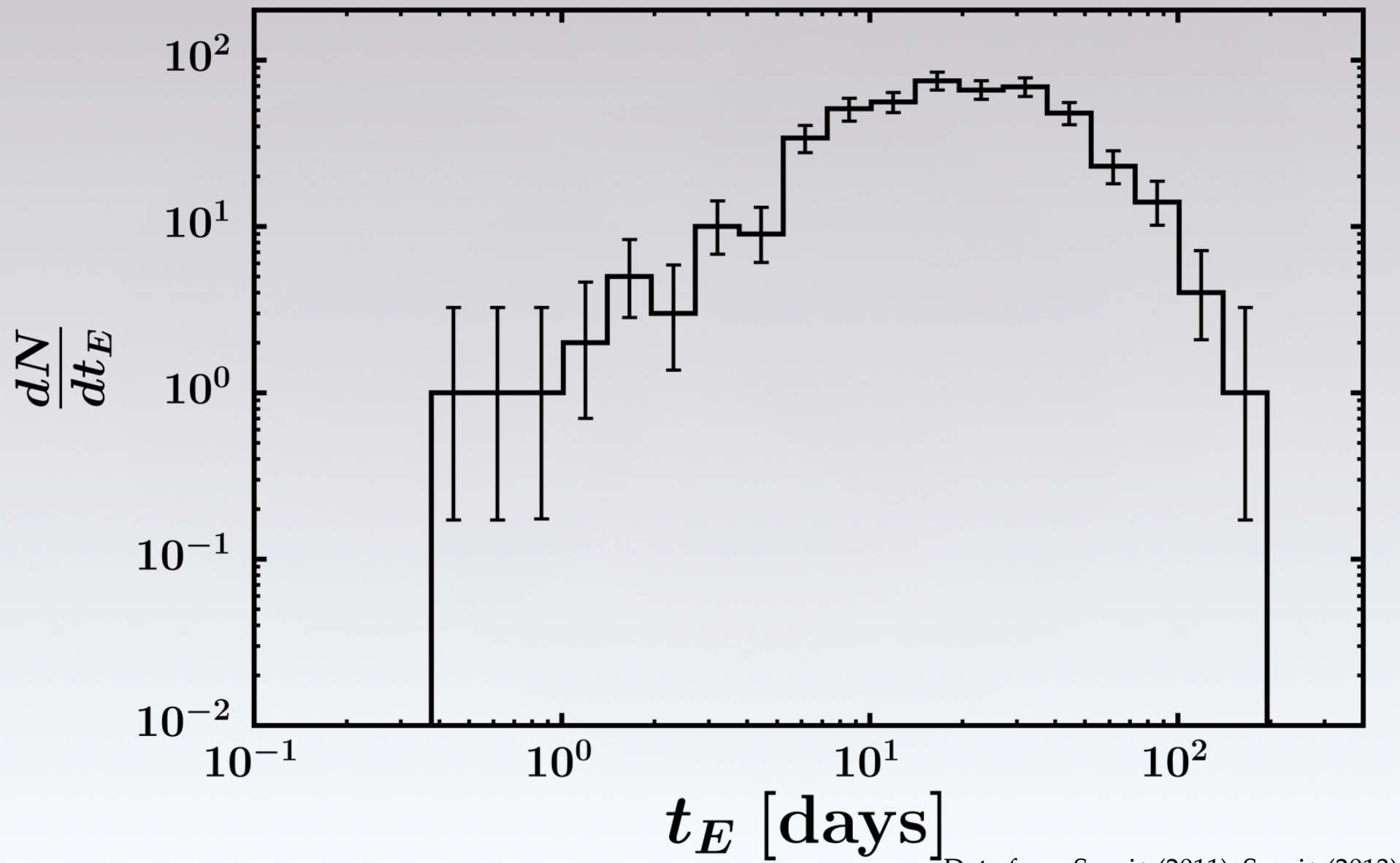


Part III.  
Constraining the Galactic  
Population of Free-Floating  
Planets

# Short-Timescale Microlensing Events

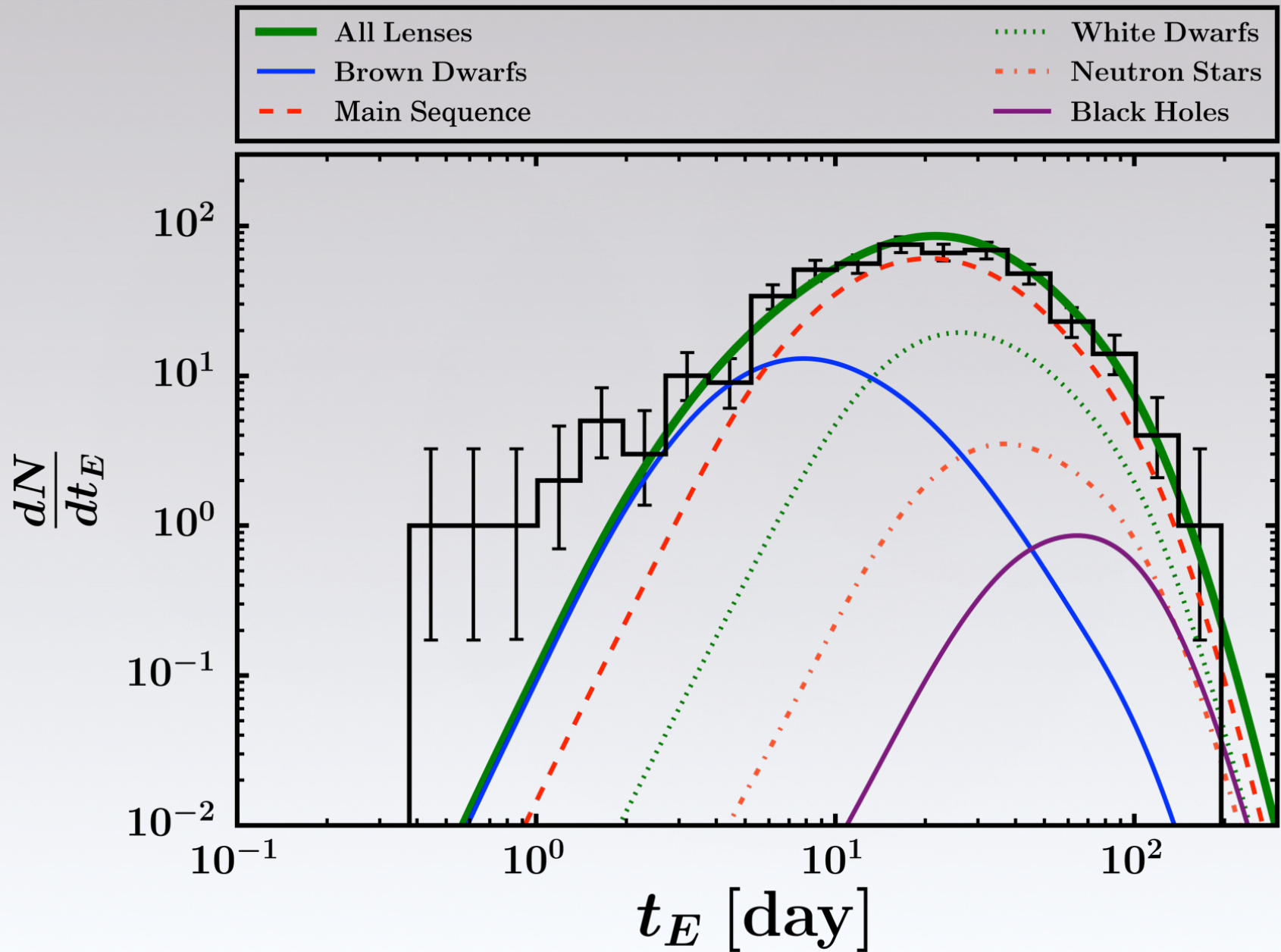


# MOA-II Data (2006-2007)



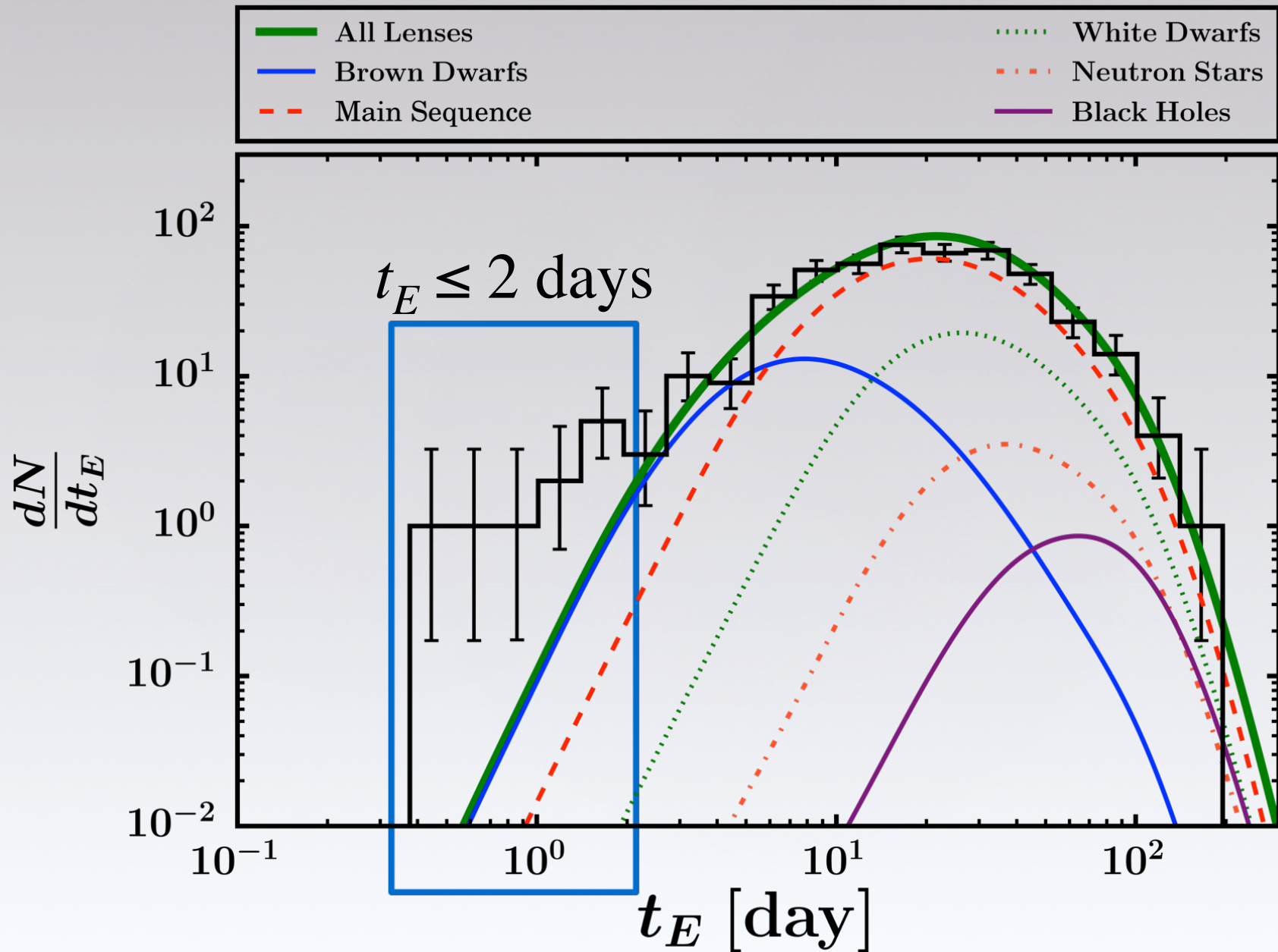
Data from Sumi+ (2011); Sumi+ (2013)

# Explaining the Observed Timescale Distribution





# Explaining the Observed Timescale Distribution





# Free-Floating Planets?

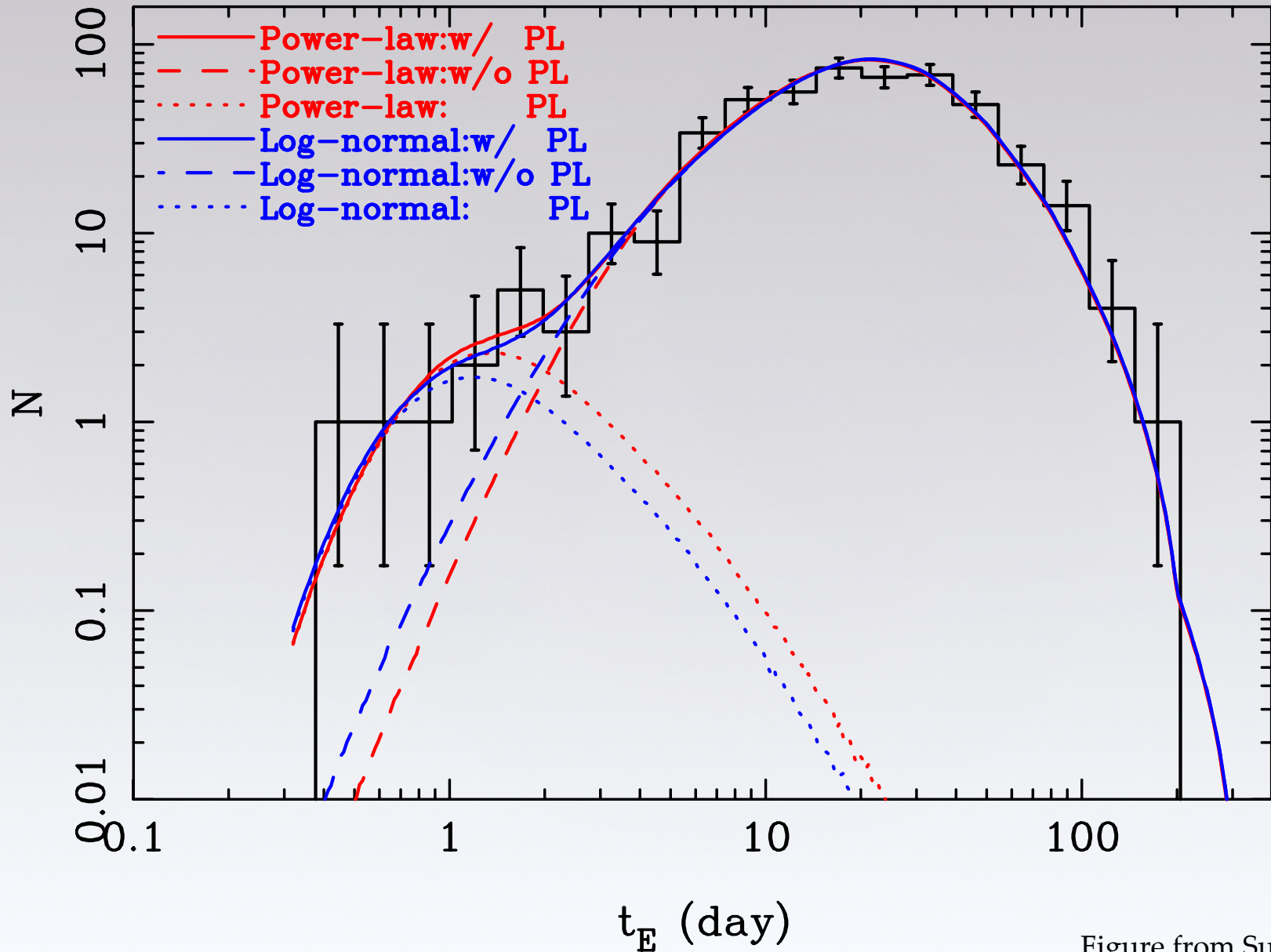
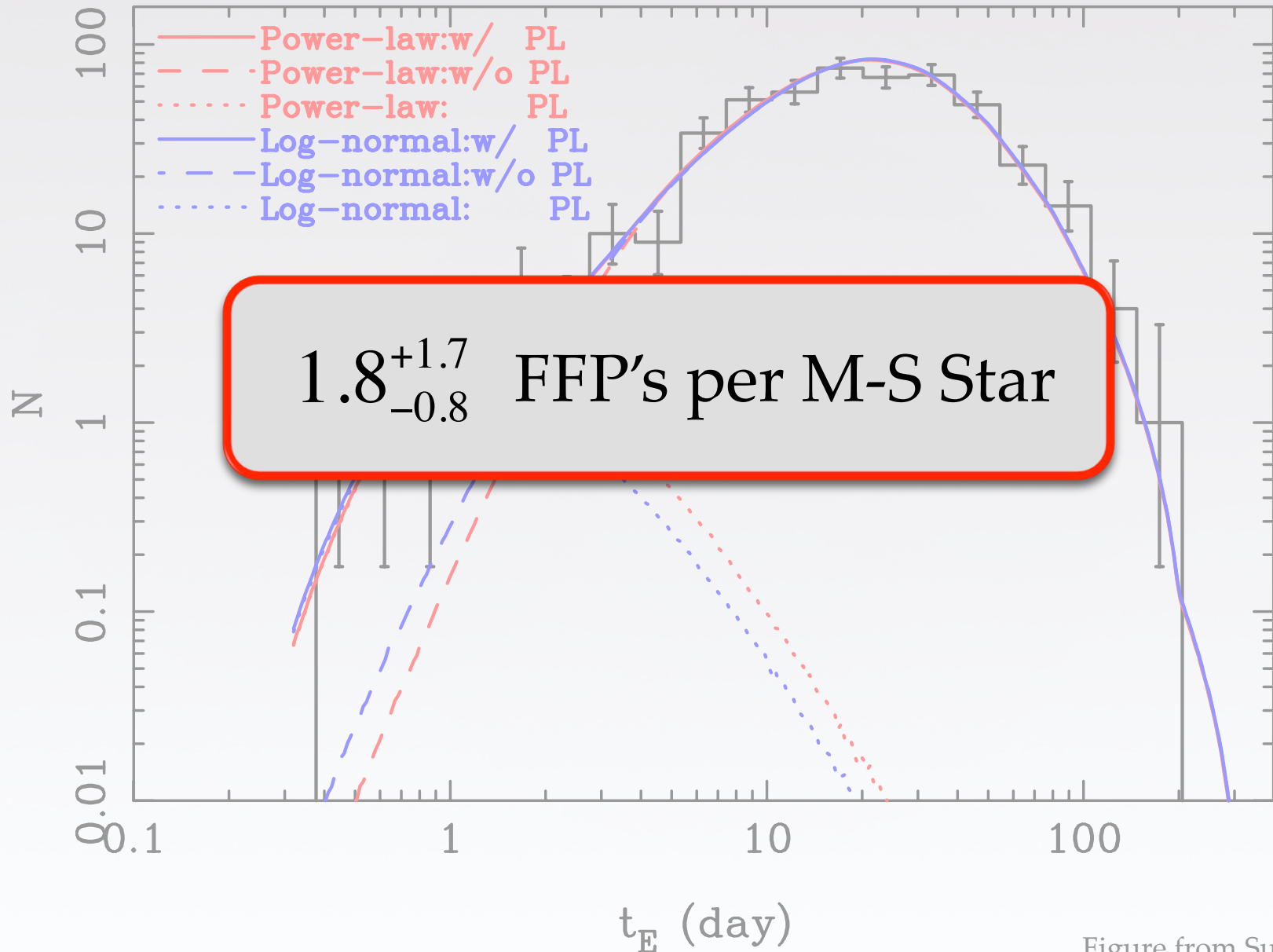
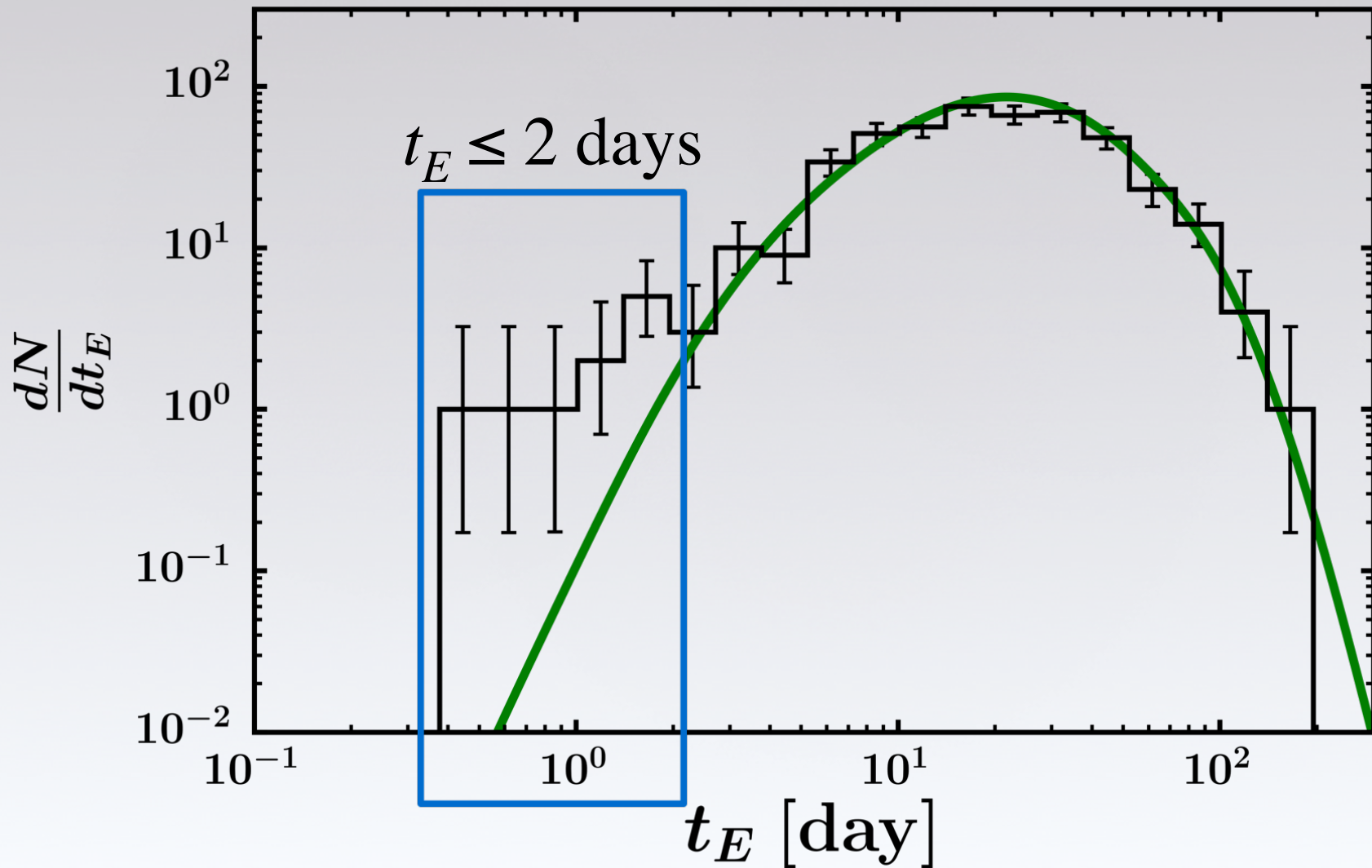


Figure from Sumi+ (2011)

# Free-Floating Planets?



# Shorttimescale Events Show No Evidence of a Primary



# Distinguishing Wide-Separation from Free-Floating Planets

1. Low-Magnification Primary “Bump”
2. Planetary Caustic Events

# Distinguishing Wide-Separation from Free-Floating Planets

Planet



Primary Lens





# Distinguishing Wide-Separation from Free-Floating Planets

$$s = r_{\perp} / R_E$$
$$q = m_p / M_L$$

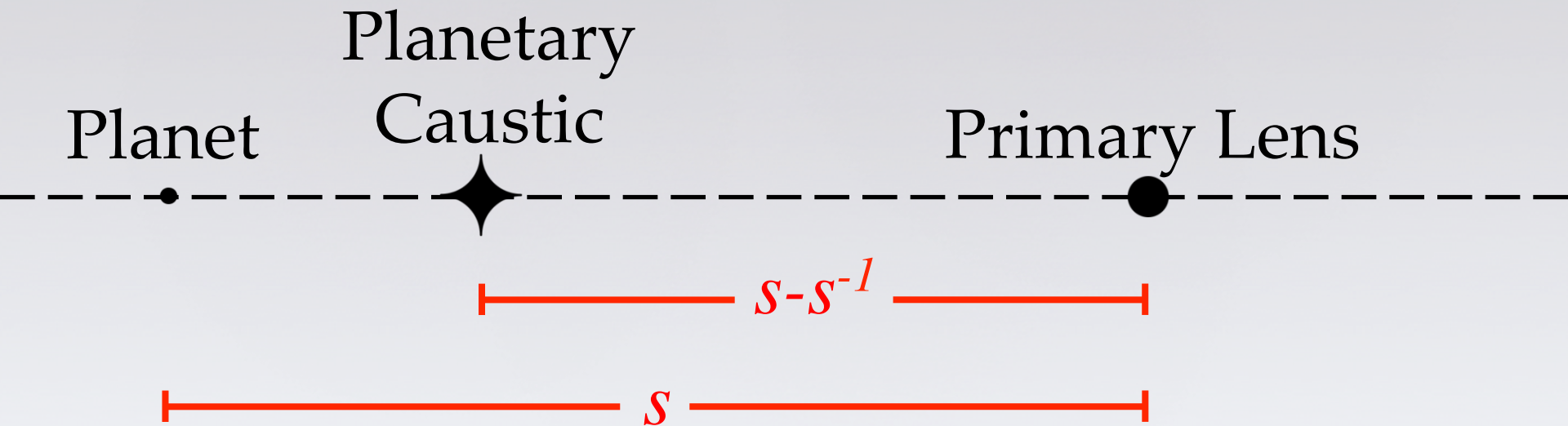
Planet

Primary Lens

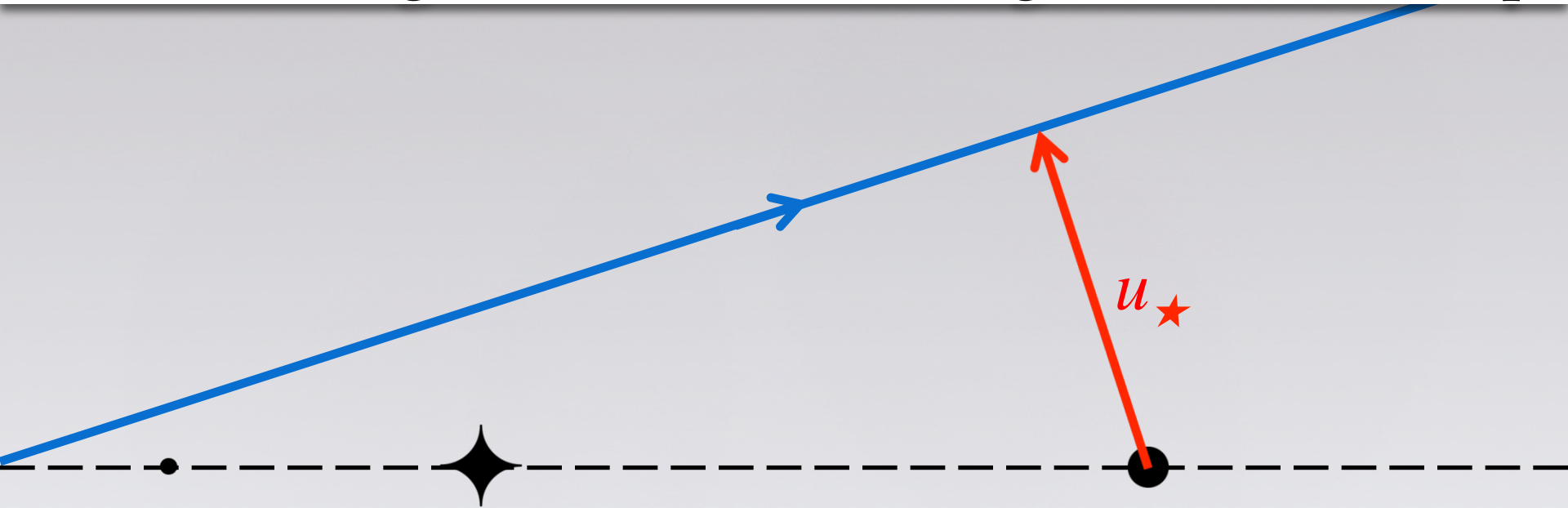


# Distinguishing Wide-Separation from Free-Floating Planets

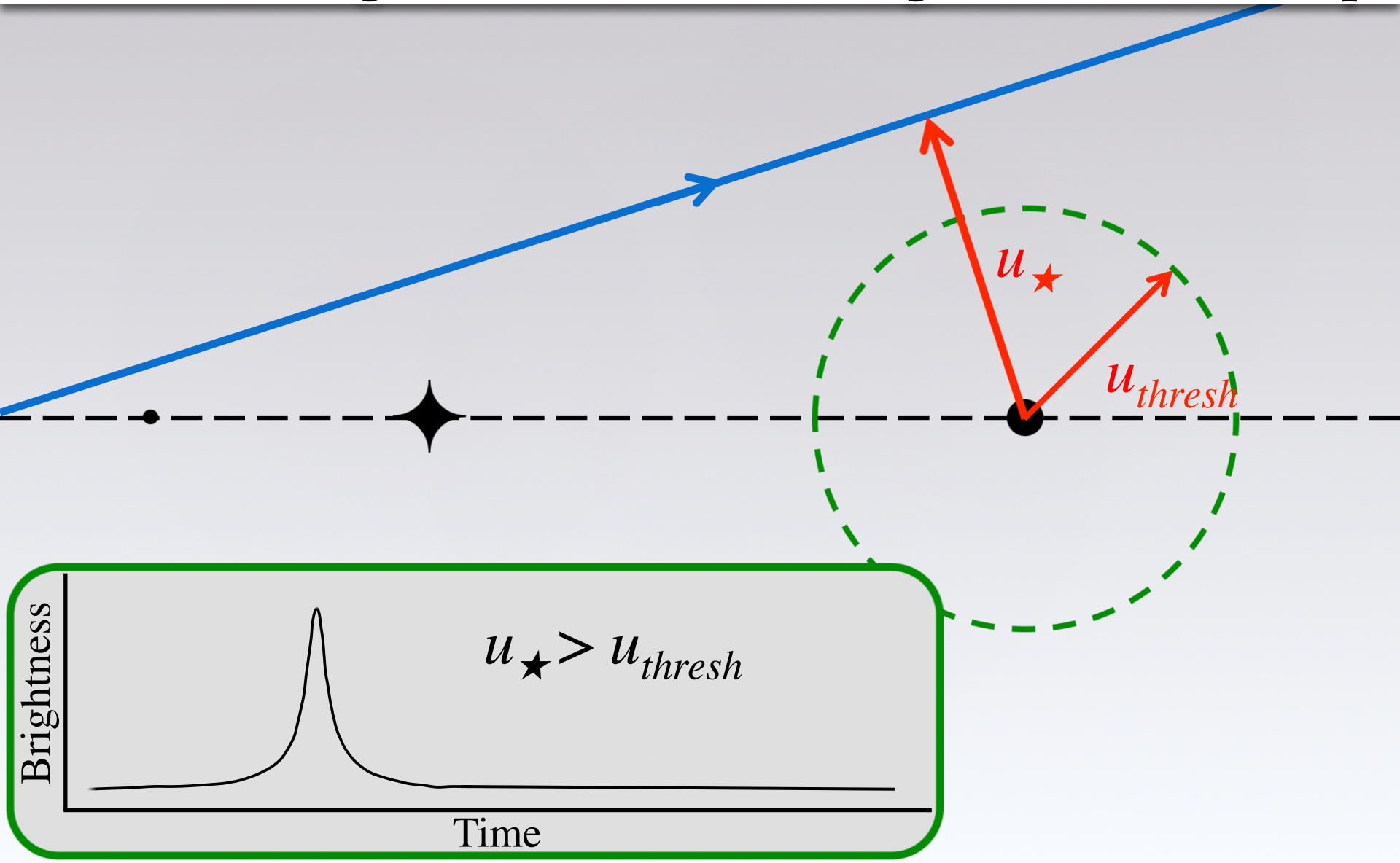
$$s = r_{\perp} / R_E$$
$$q = m_p / M_L$$



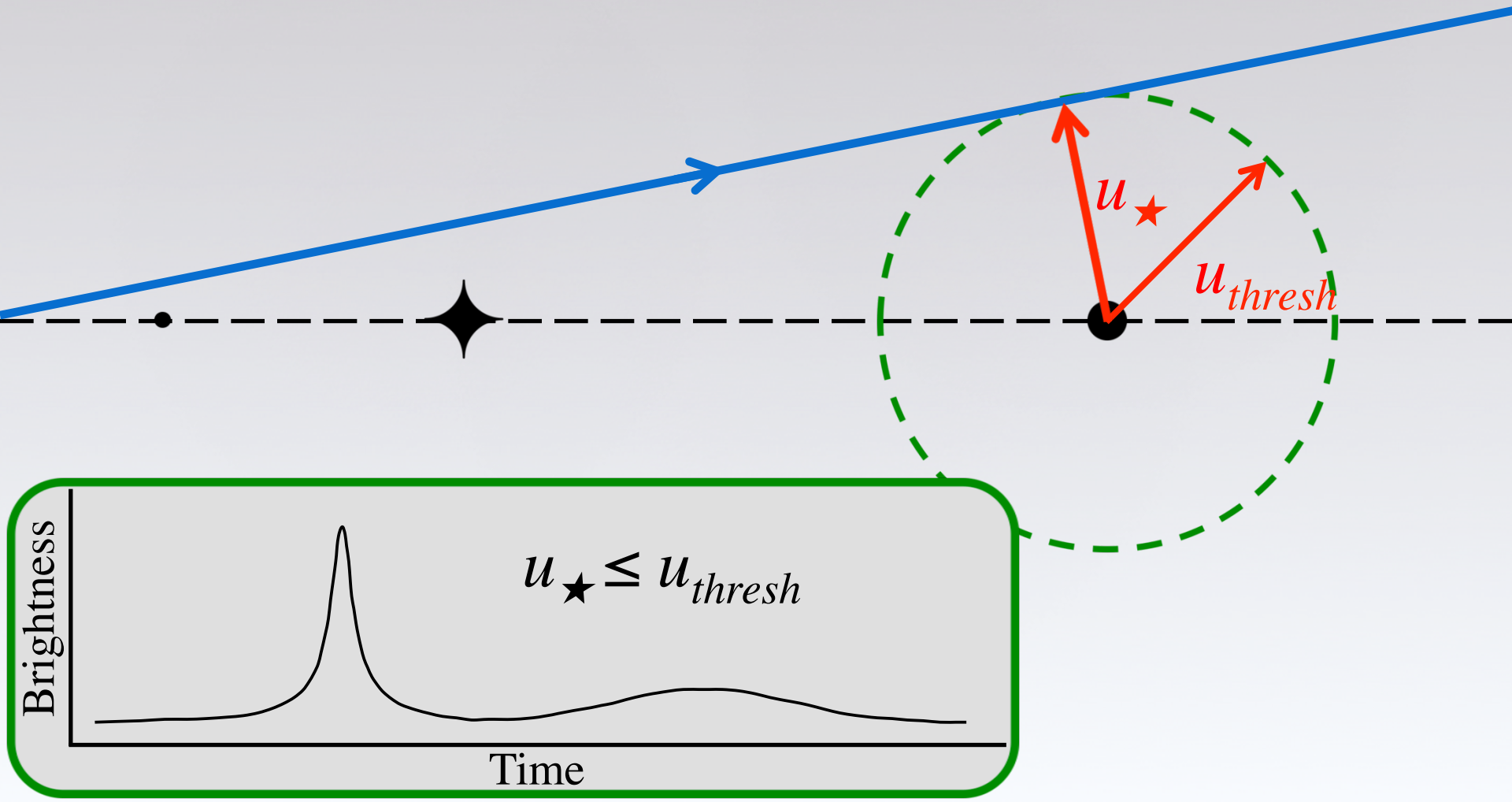
# Distinguishing Wide-Separation from Free-Floating Planets – Low-Magnification Bump



# Distinguishing Wide-Separation from Free-Floating Planets – Low-Magnification Bump



# Distinguishing Wide-Separation from Free-Floating Planets – Low-Magnification Bump

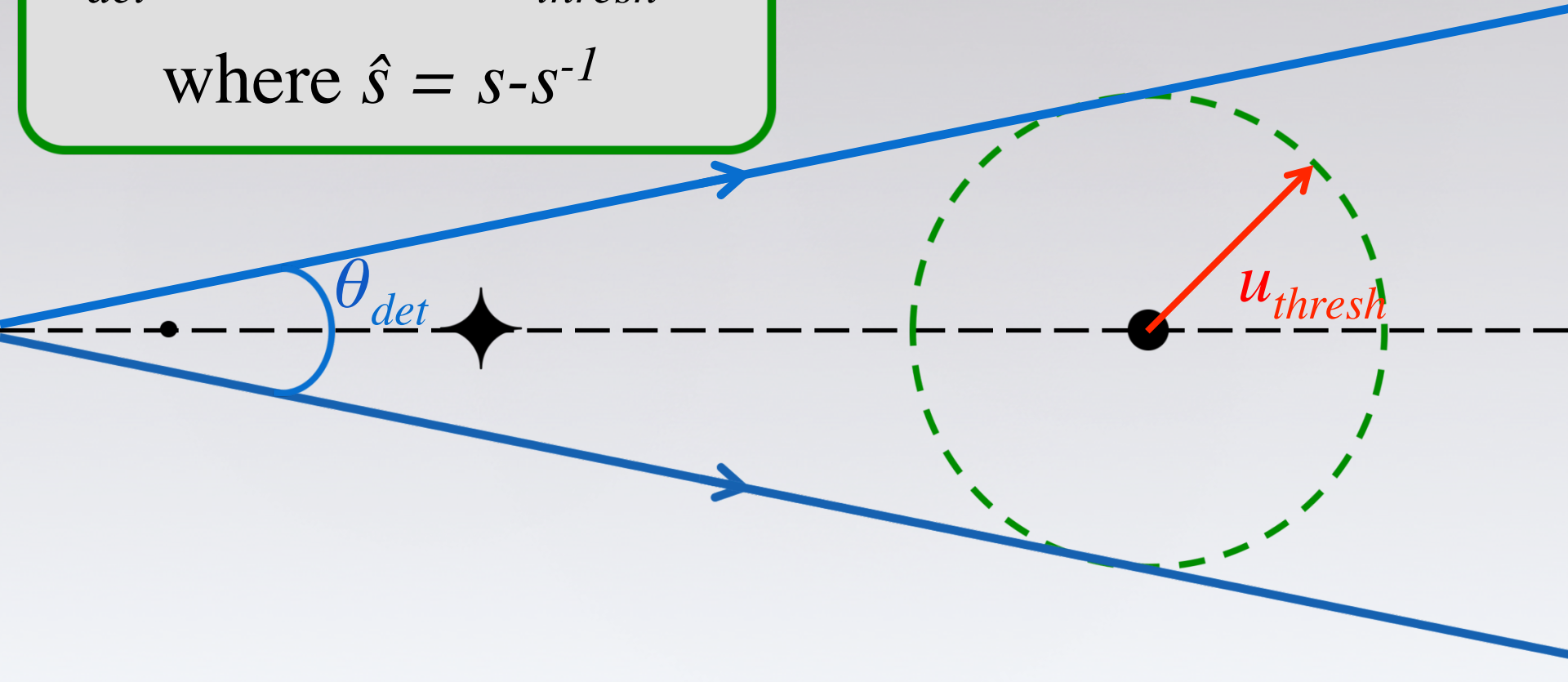




# Distinguishing Wide-Separation from Free-Floating Planets – Low-Magnification Bump

$$\theta_{det}(s) = 2\sin^{-1}(u_{thresh}/\hat{s}),$$

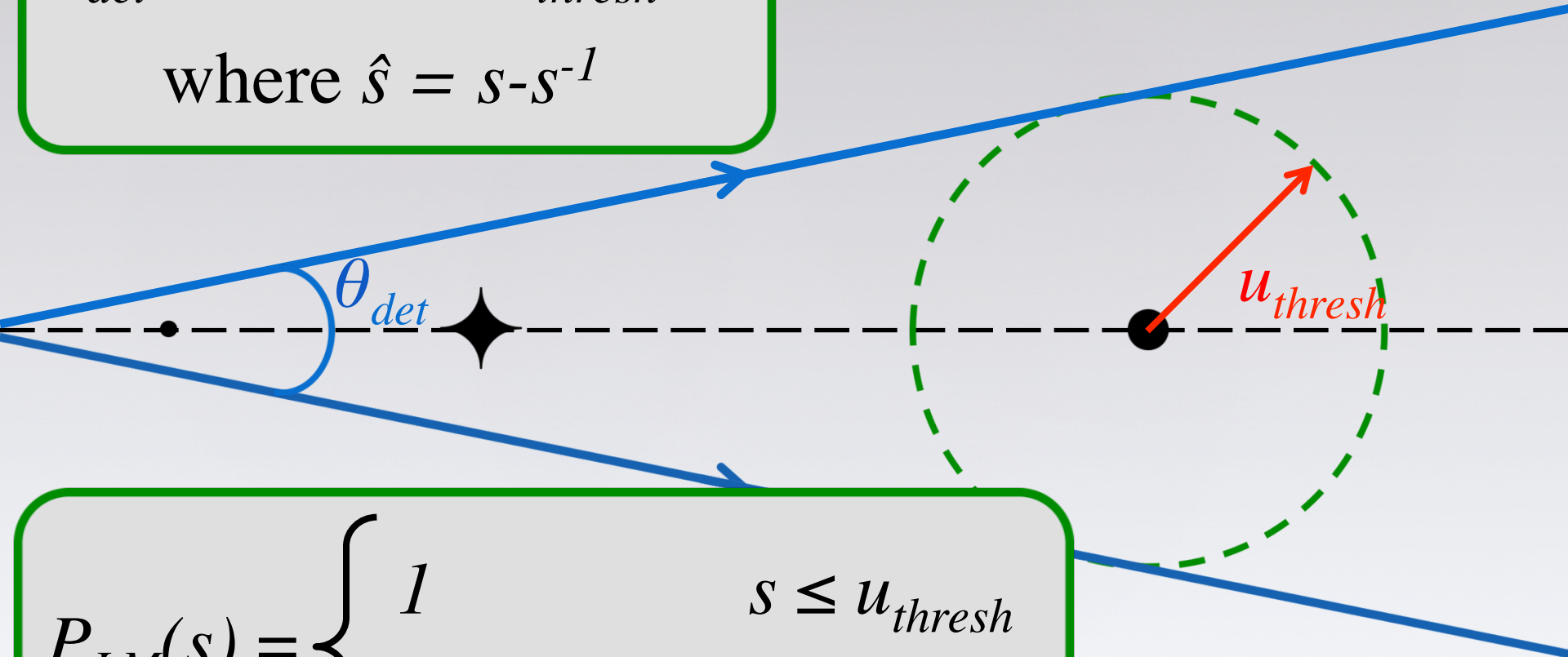
$$\text{where } \hat{s} = s - s^{-1}$$



# Distinguishing Wide-Separation from Free-Floating Planets – Low-Magnification Bump

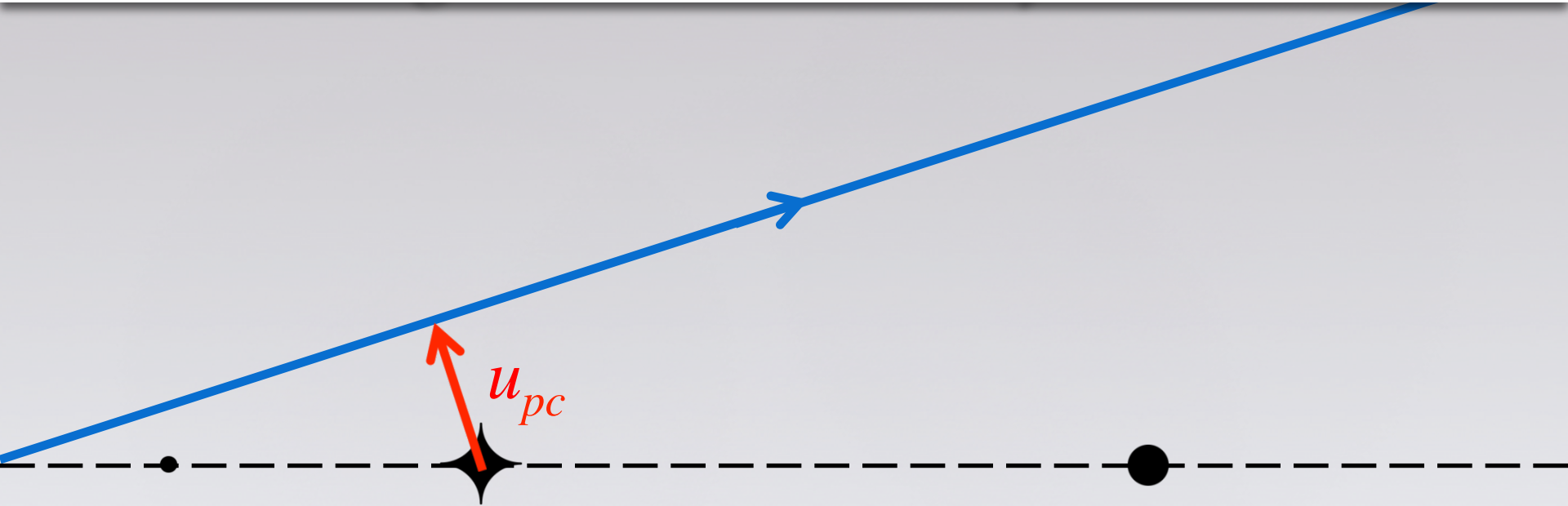
$$\theta_{det}(s) = 2\sin^{-1}(u_{thresh}/\hat{s}),$$

where  $\hat{s} = s - s^{-1}$

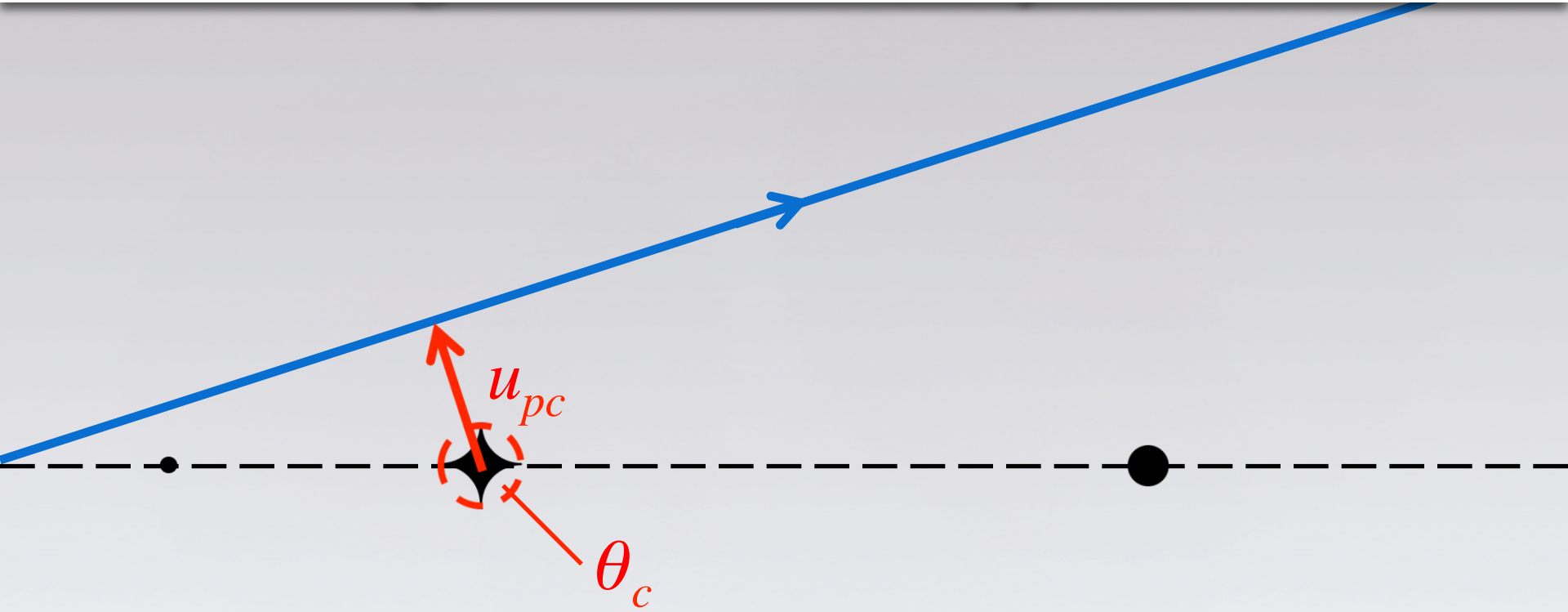


$$P_{LM}(s) = \begin{cases} 1 & s \leq u_{thresh} \\ \theta_{det}(s) / \pi & s > u_{thresh} \end{cases}$$

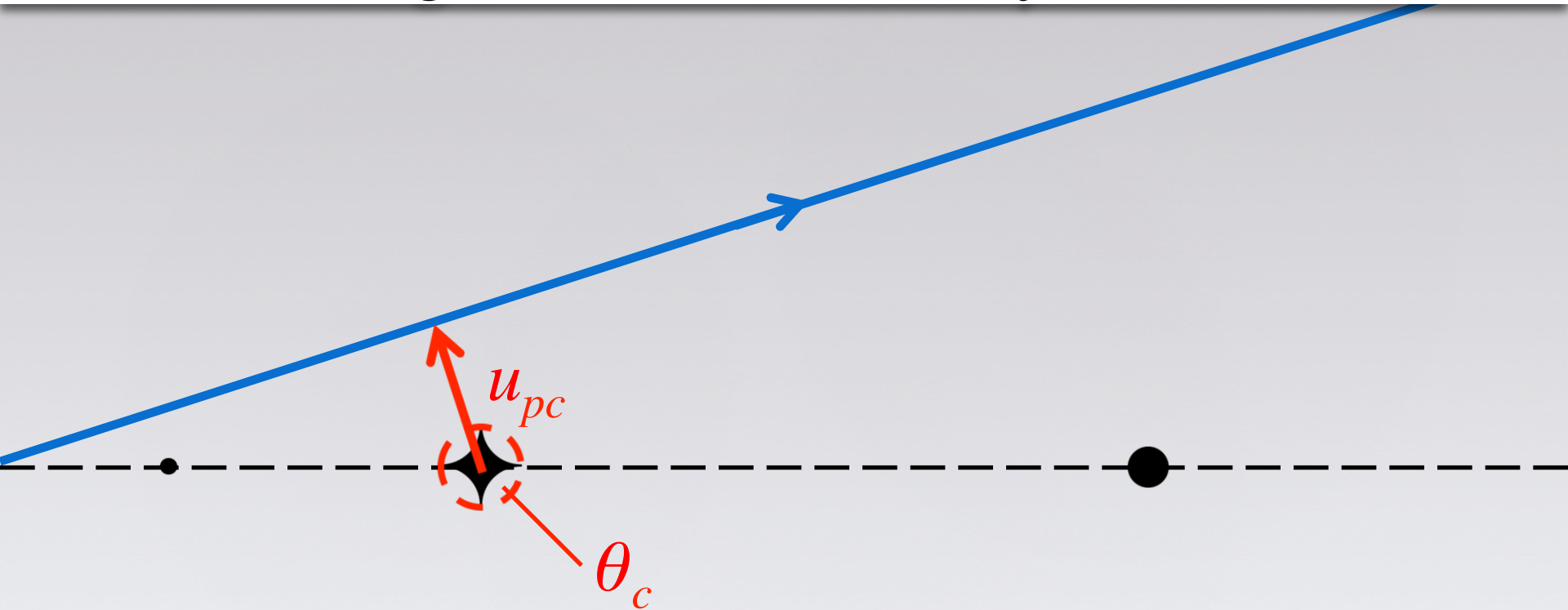
# Distinguishing Wide-Separation from Free-Floating Planets – Planetary Caustic Events



# Distinguishing Wide-Separation from Free-Floating Planets – Planetary Caustic Events



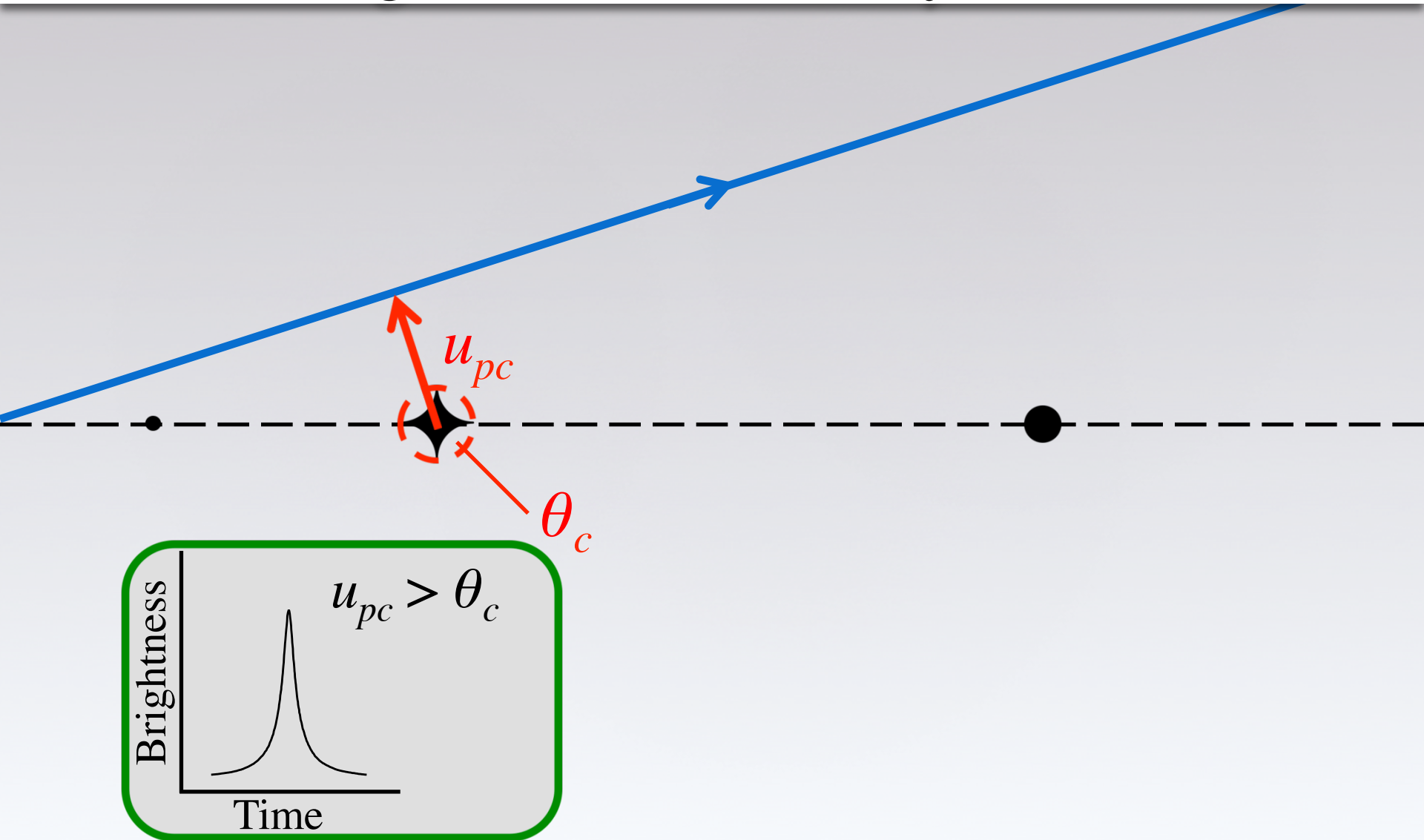
# Distinguishing Wide-Separation from Free-Floating Planets – Planetary Caustic Events



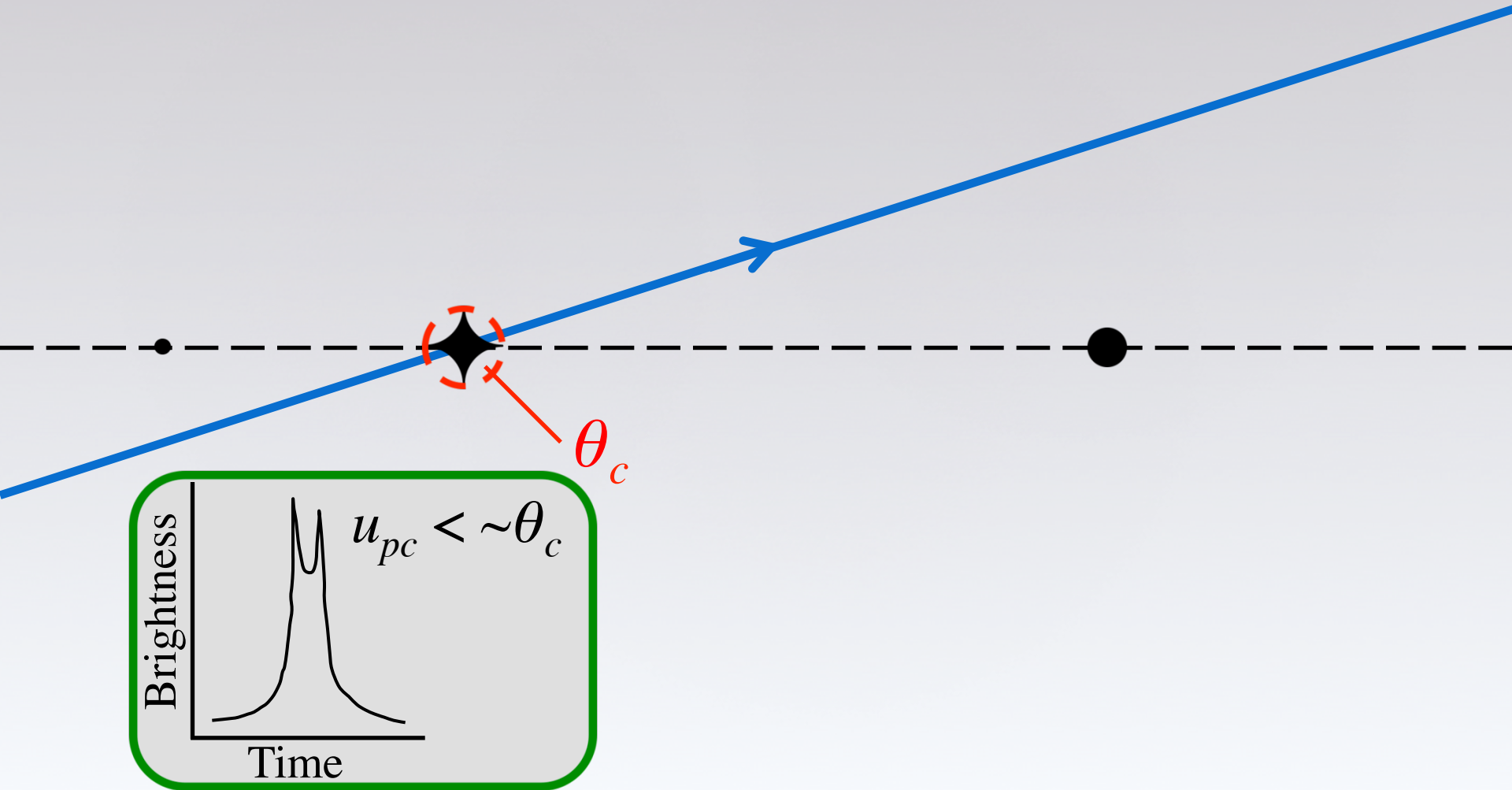
$$\theta_c(q, s) = 2q^{1/2} / s\sqrt{s^2 + 1}$$



# Distinguishing Wide-Separation from Free-Floating Planets – Planetary Caustic Events

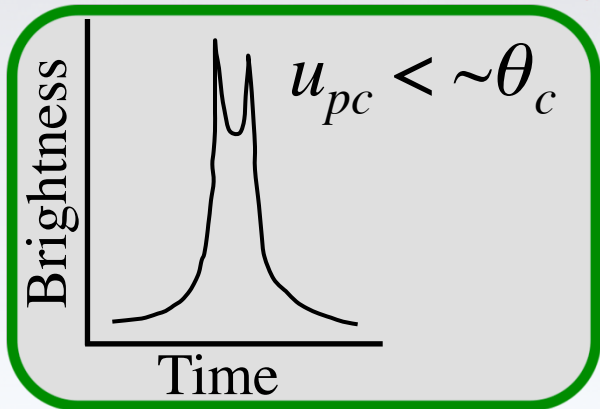
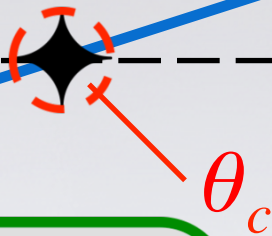


# Distinguishing Wide-Separation from Free-Floating Planets – Planetary Caustic Events

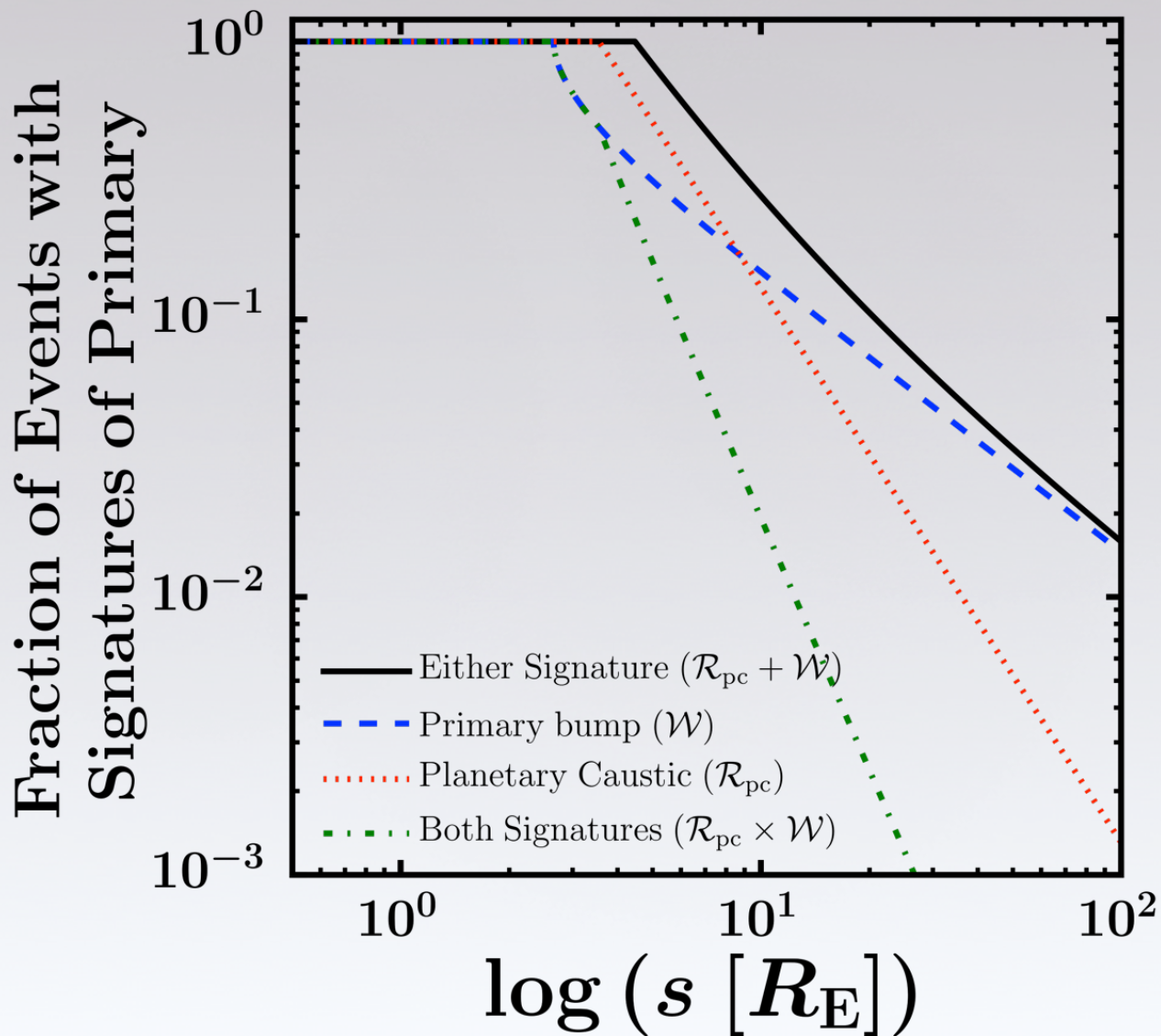


# Distinguishing Wide-Separation from Free-Floating Planets – Planetary Caustic Events

$$R_{pc}(q,s) = \begin{cases} 1 & s \leq s_c \\ \theta_c(q,s)/const. & s > s_c \end{cases}$$

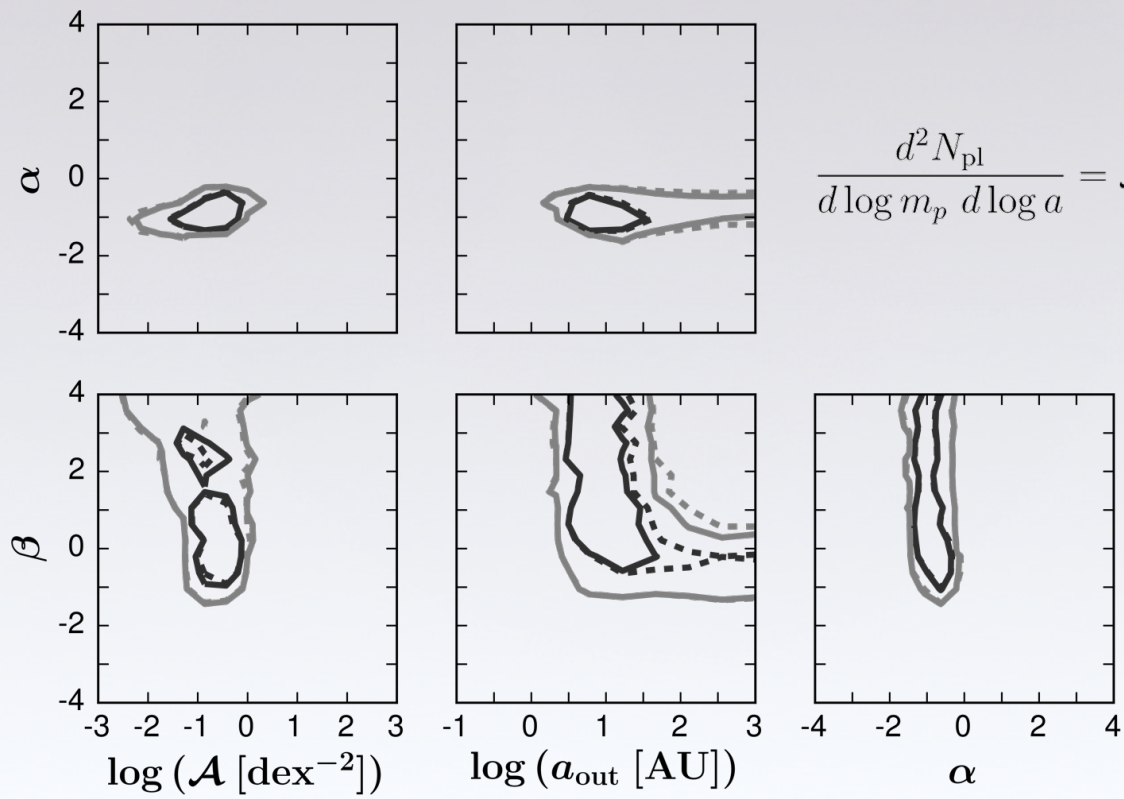
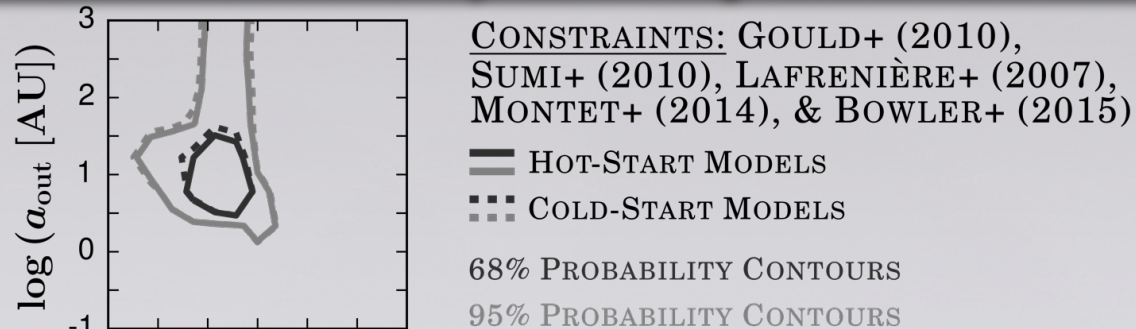


# Distinguishing Wide-Separation from Free-Floating Planets





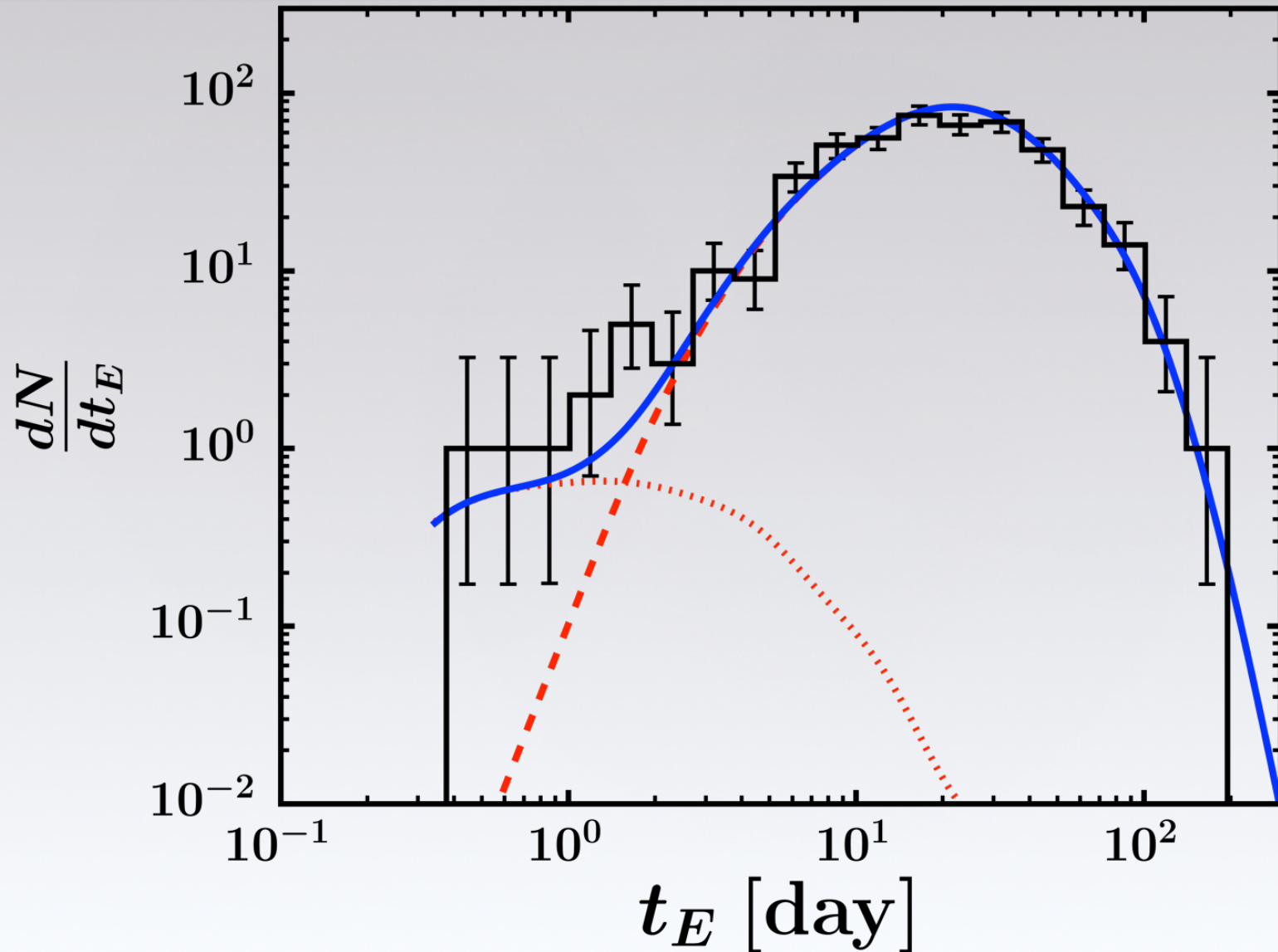
# Constructing the Timescale Distribution of Bound Planetary Companions



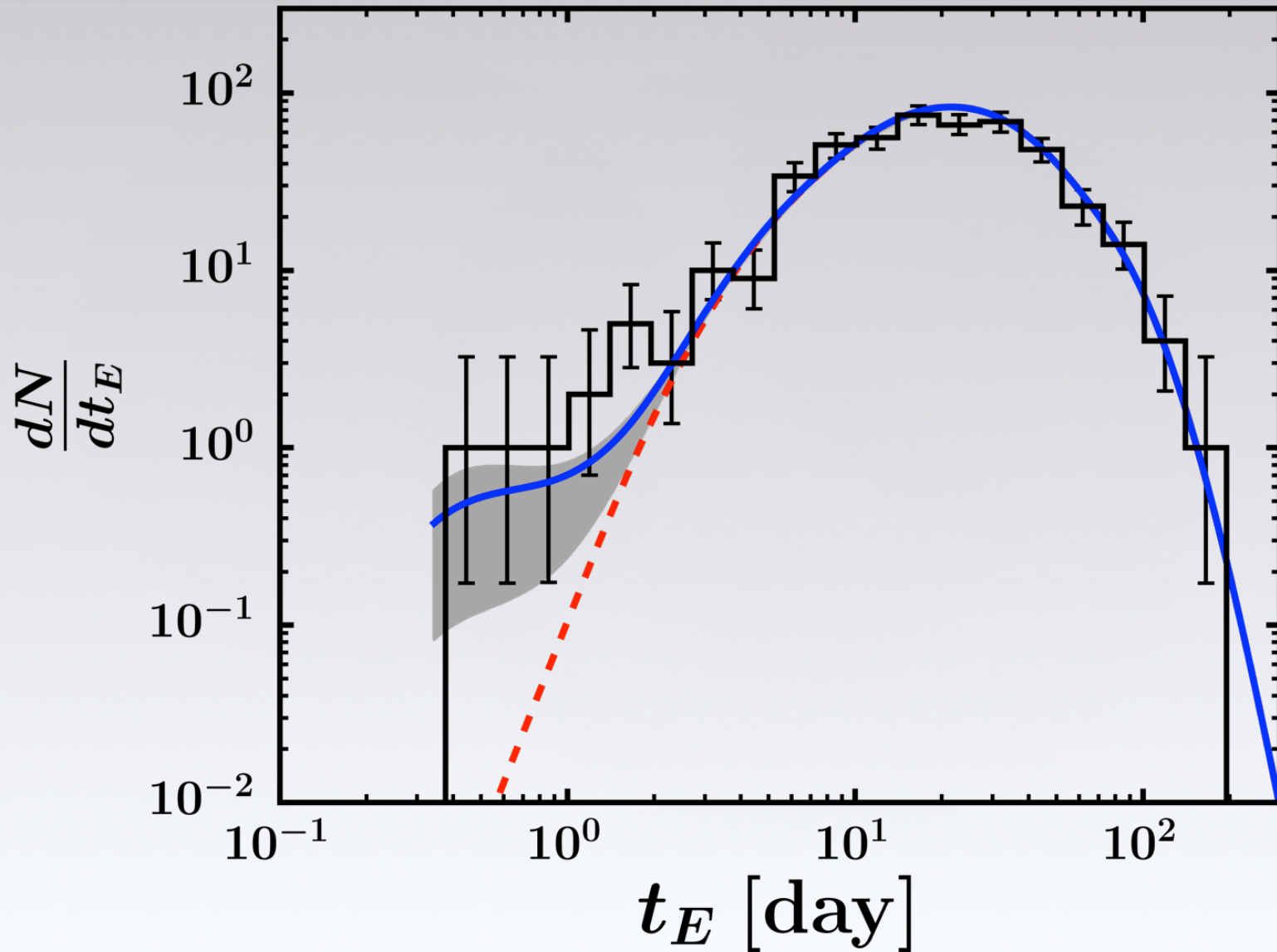
$$\frac{d^2 N_{\text{pl}}}{d \log m_p d \log a} = \mathcal{A} \left( \frac{m_p}{M_{\text{Sat}}} \right)^\alpha \left( \frac{a}{2.5 \text{ AU}} \right)^\beta$$



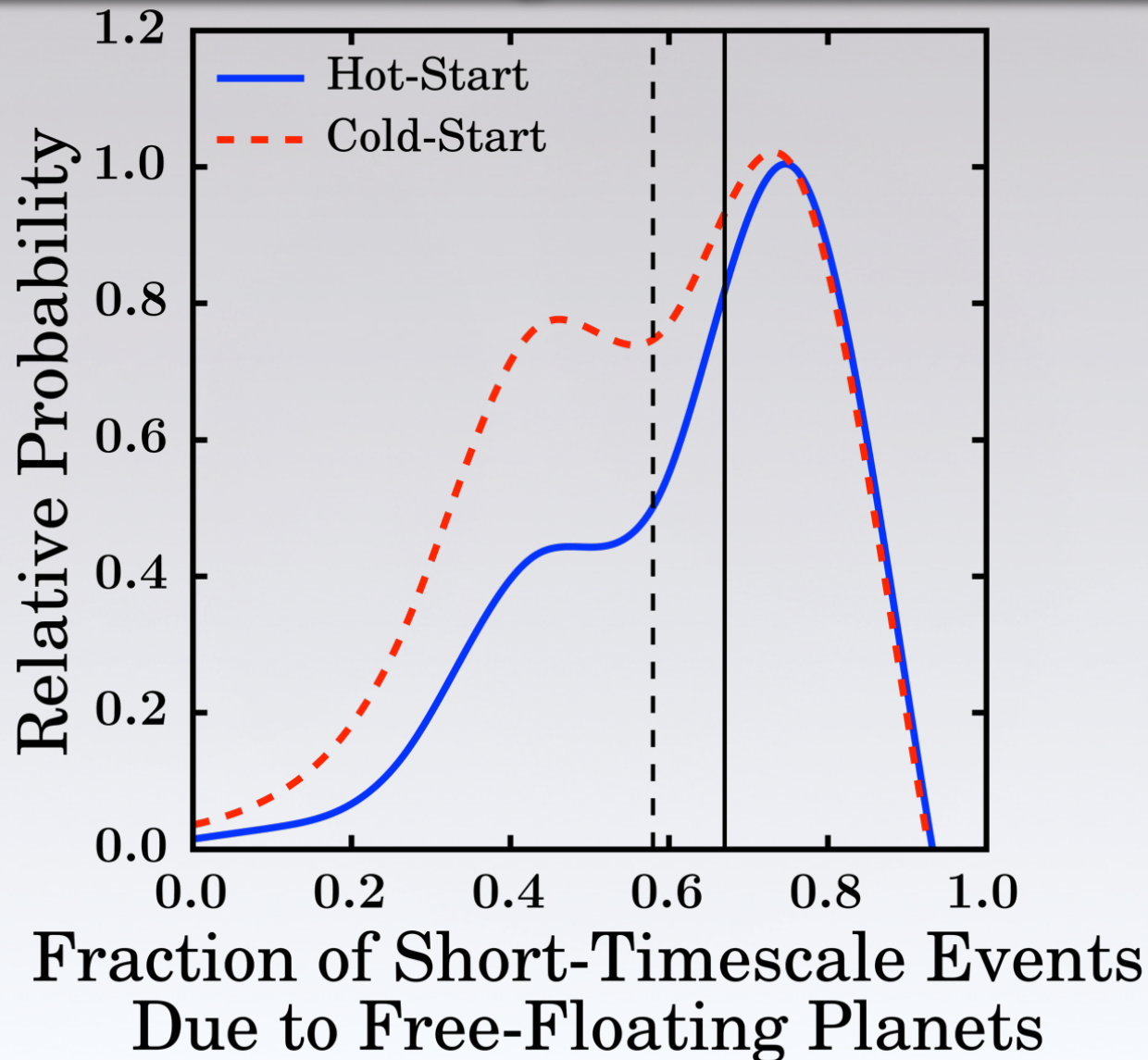
# Maximum Likelihood Estimation: Bound Planets + LMF Fit to Observed Timescale Distribution



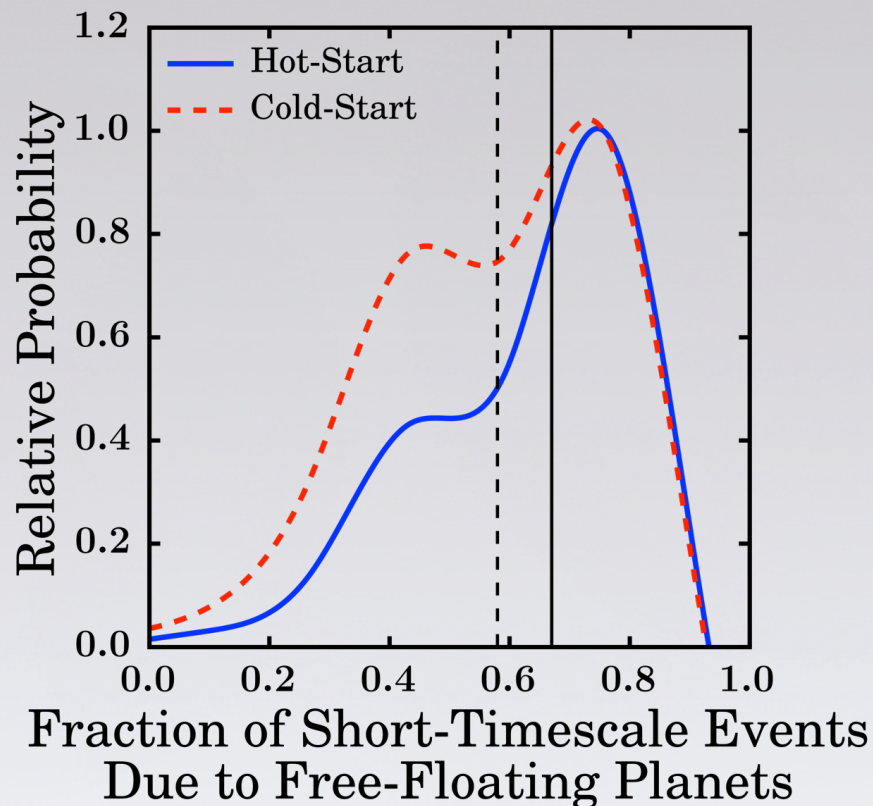
# Maximum Likelihood Estimation: Bound Planets + LMF Fit to Observed Timescale Distribution



# Constraints on the Galactic Population of Free-Floating Planets



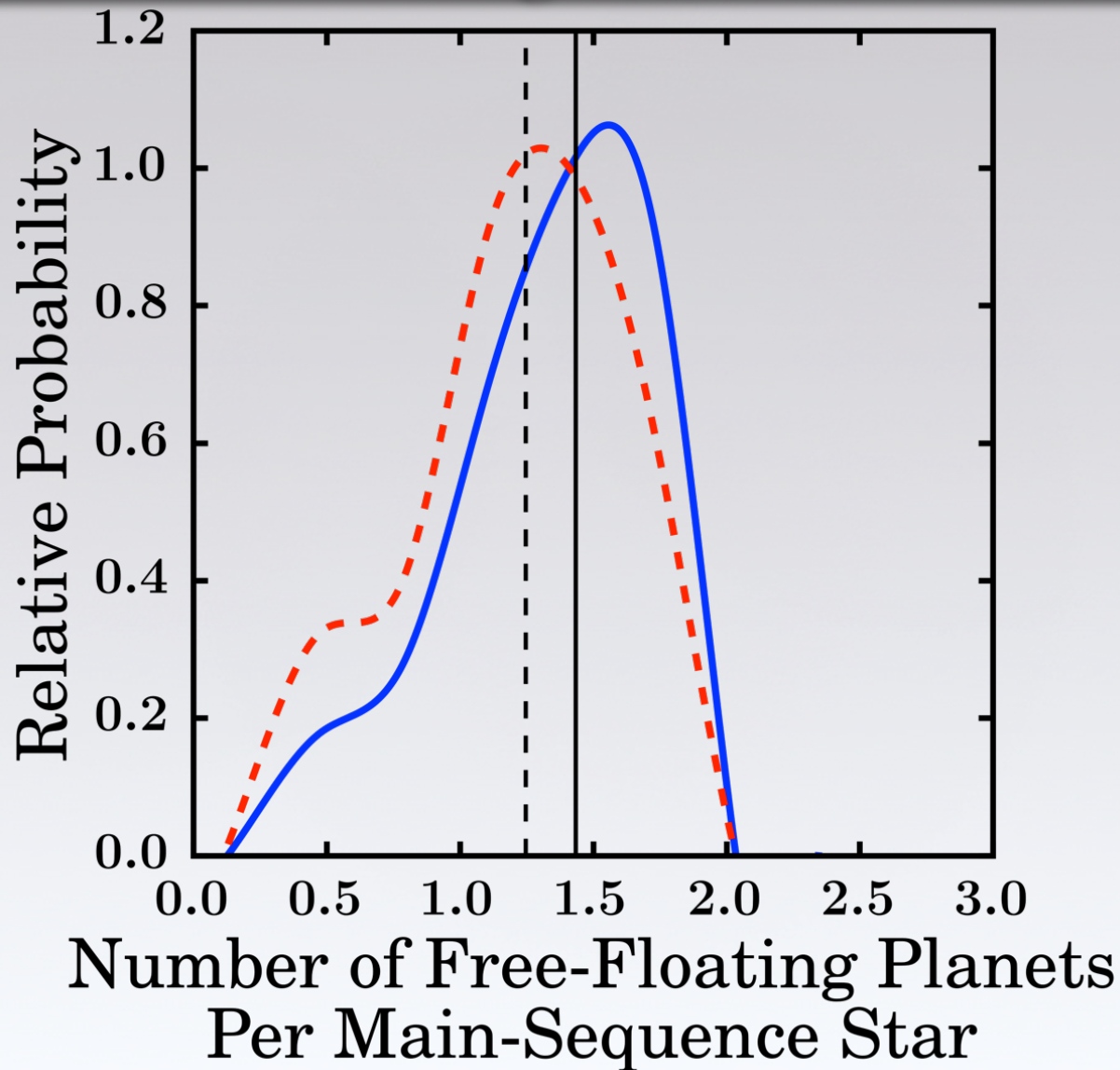
# Constraints on the Galactic Population of Free-Floating Planets



	Median	68% Credibility	95% Credibility
Hot—Start	0.67	0.44—0.78	0.23—0.85
Cold—Start	0.58	0.40—0.74	0.14—0.83

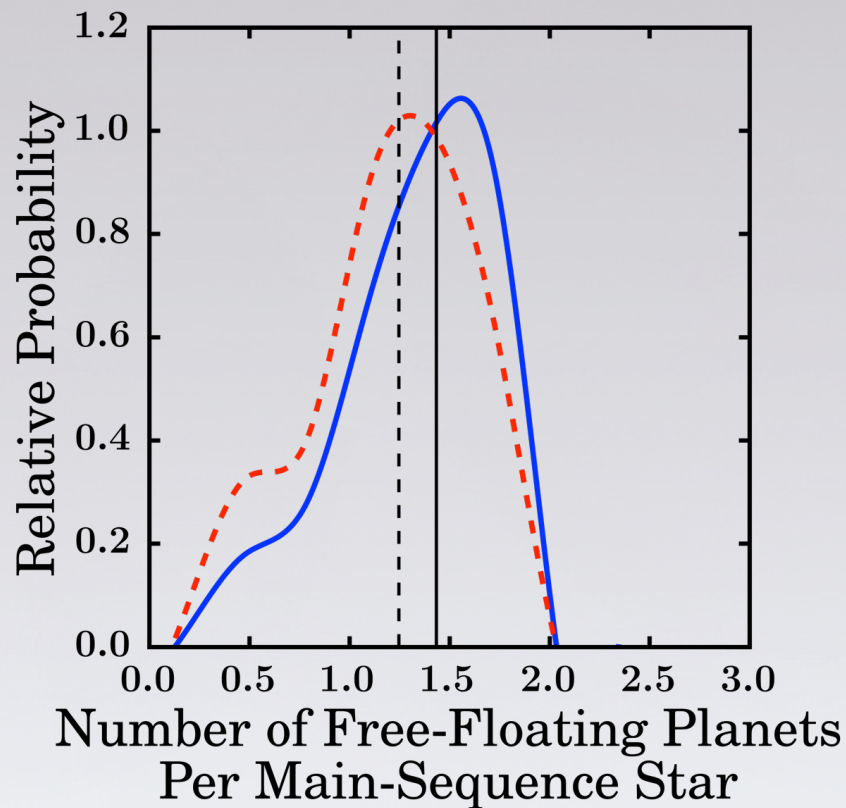


# Constraints on the Galactic Population of Free-Floating Planets





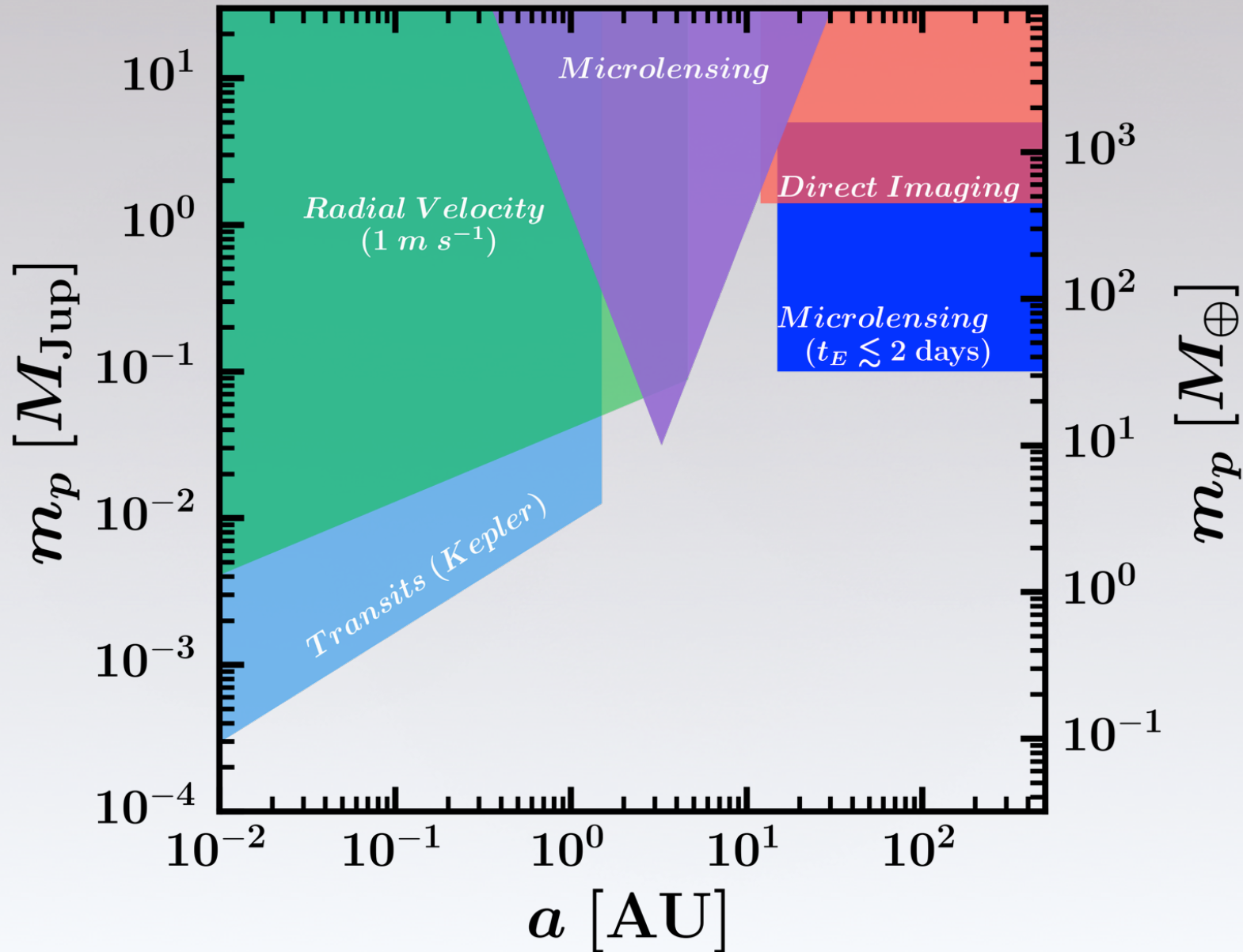
# Constraints on the Galactic Population of Free-Floating Planets



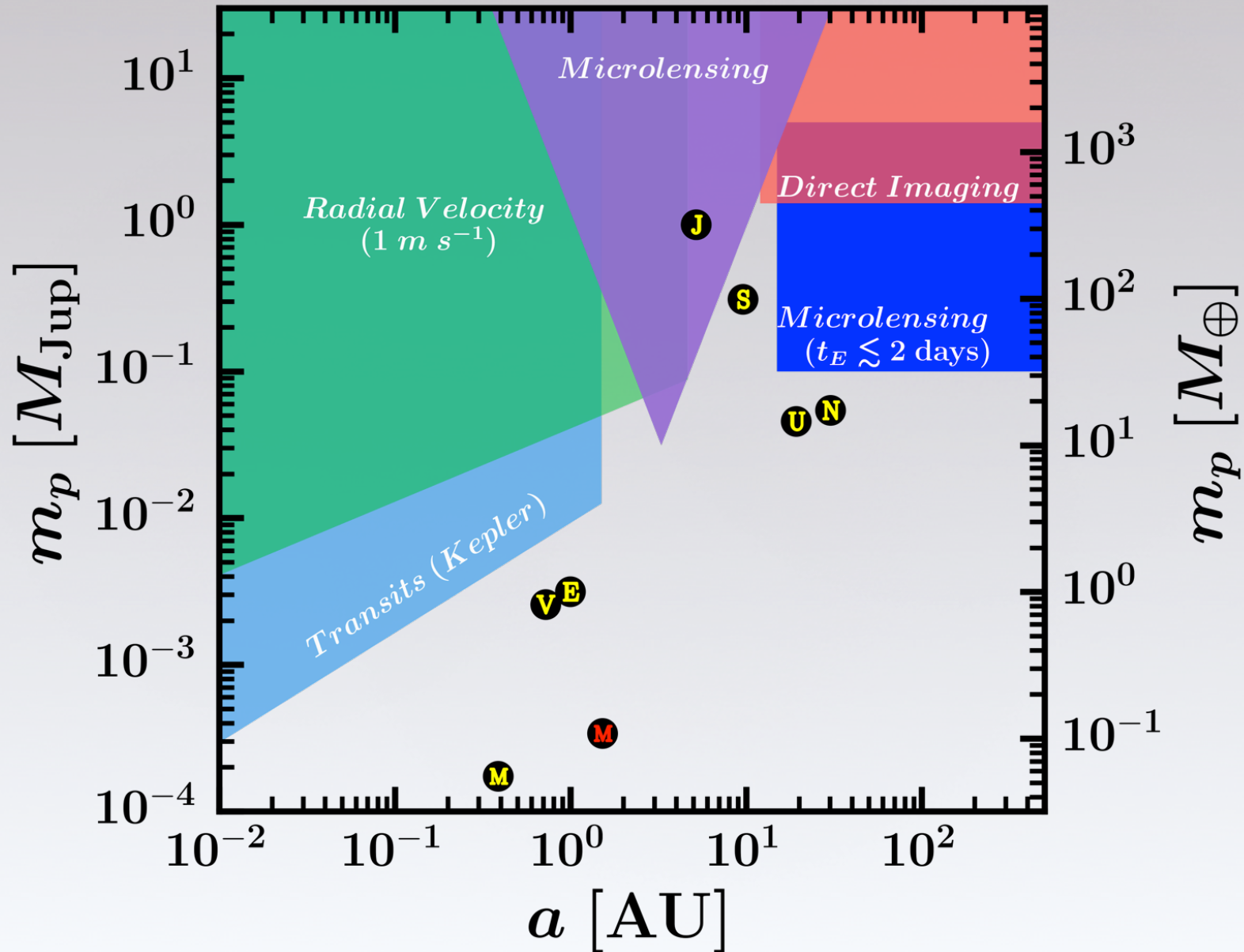
	<b>Median</b>	<b>68% Credibility</b>	<b>95% Credibility</b>
Hot—Start	1.4	0.95—1.7	0.48—1.8
Cold—Start	1.2	0.87—1.6	0.29—1.8

Part IV.  
Future Prospects

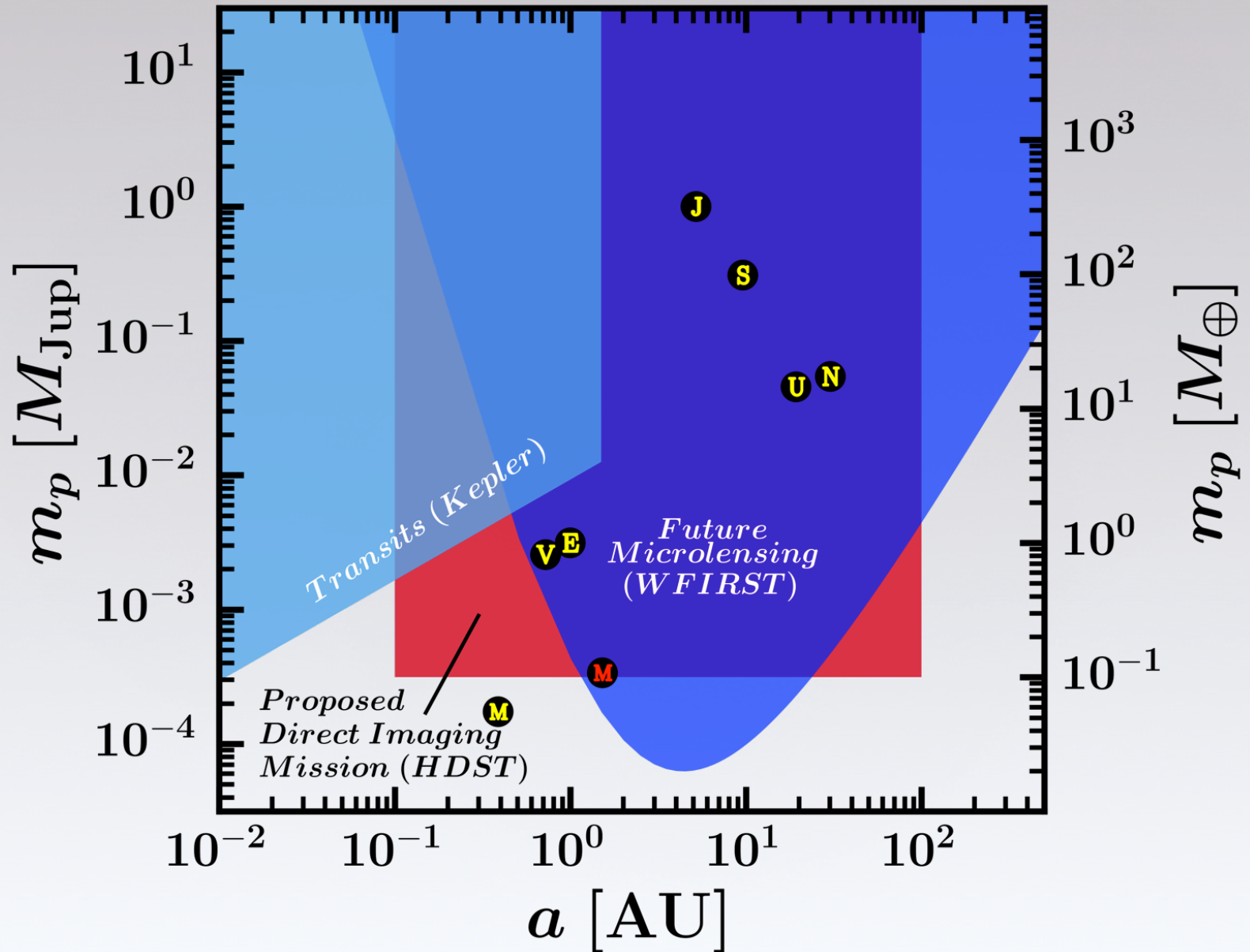
# Synthesis of “The Big Four”



# Synthesis of "The Big Four"



# Kepler + WFIRST (+ HDST)





# References

- RV +  $\mu$ lensing → Clanton, C. & Gaudi, B. S. 2014, ApJ, 791, 90  
→ Clanton, C. & Gaudi, B. S. 2014, ApJ, 791, 91
- RV +  $\mu$ lensing +  
Imaging → Clanton, C. & Gaudi, B. S. 2016, ApJ, 819, 125
- Free-Floating  
Planets → Clanton, C. & Gaudi, B. S. in prep.

End

[clantonastro.org](http://clantonastro.org)