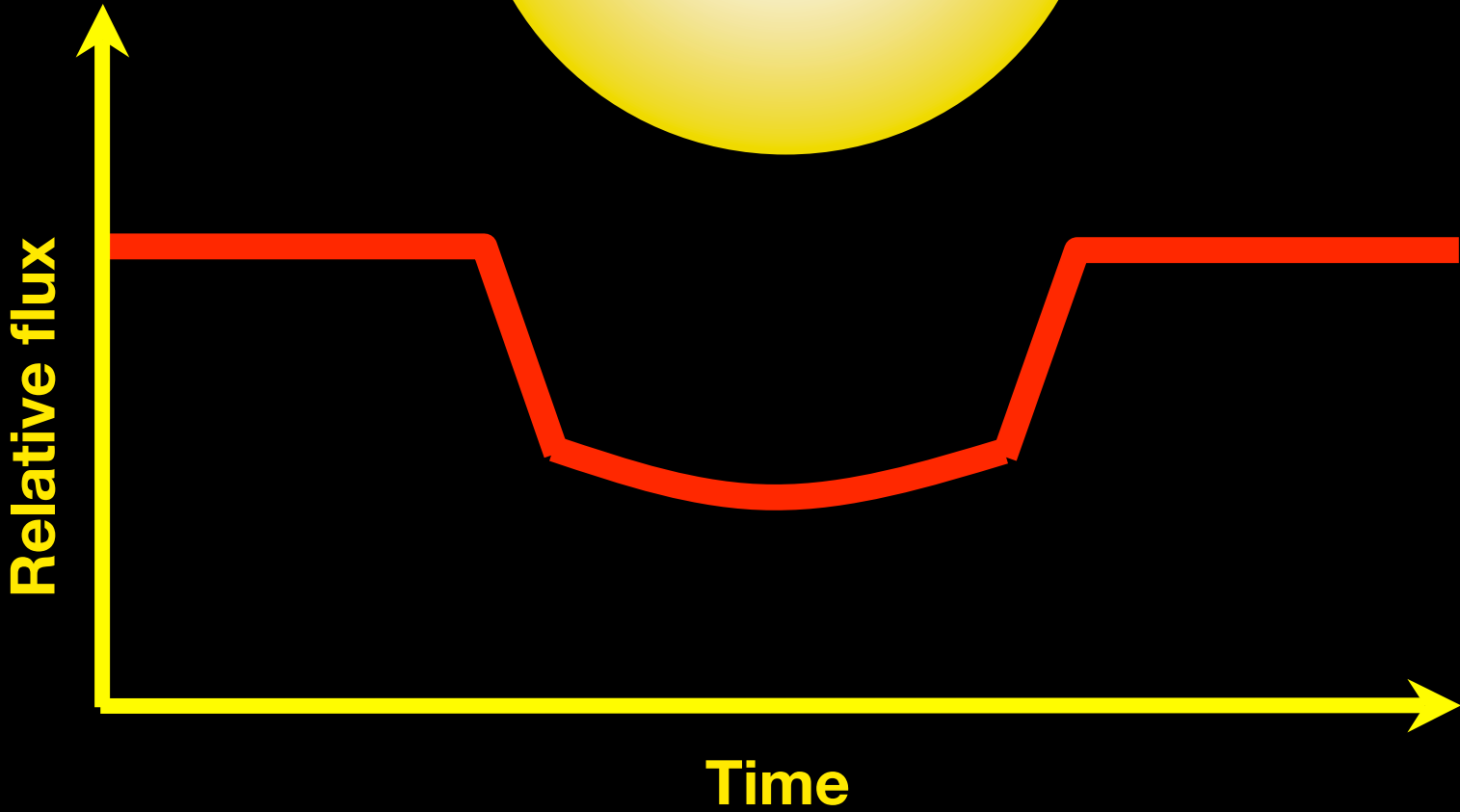
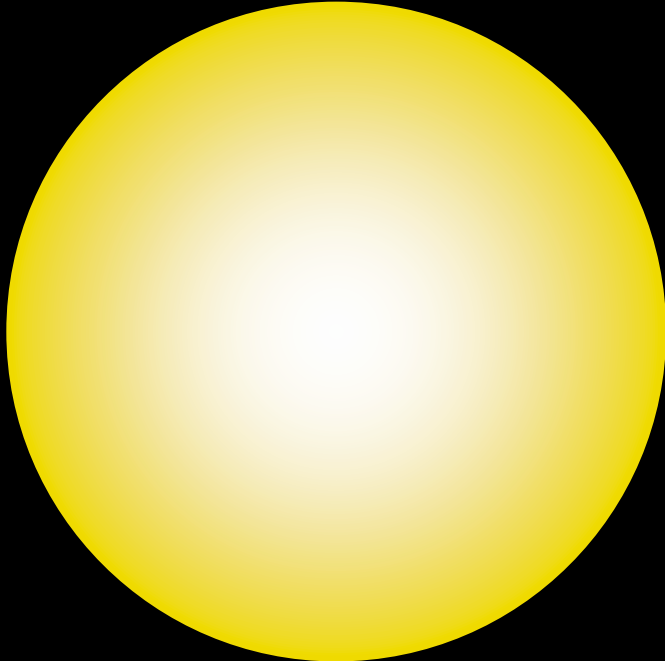


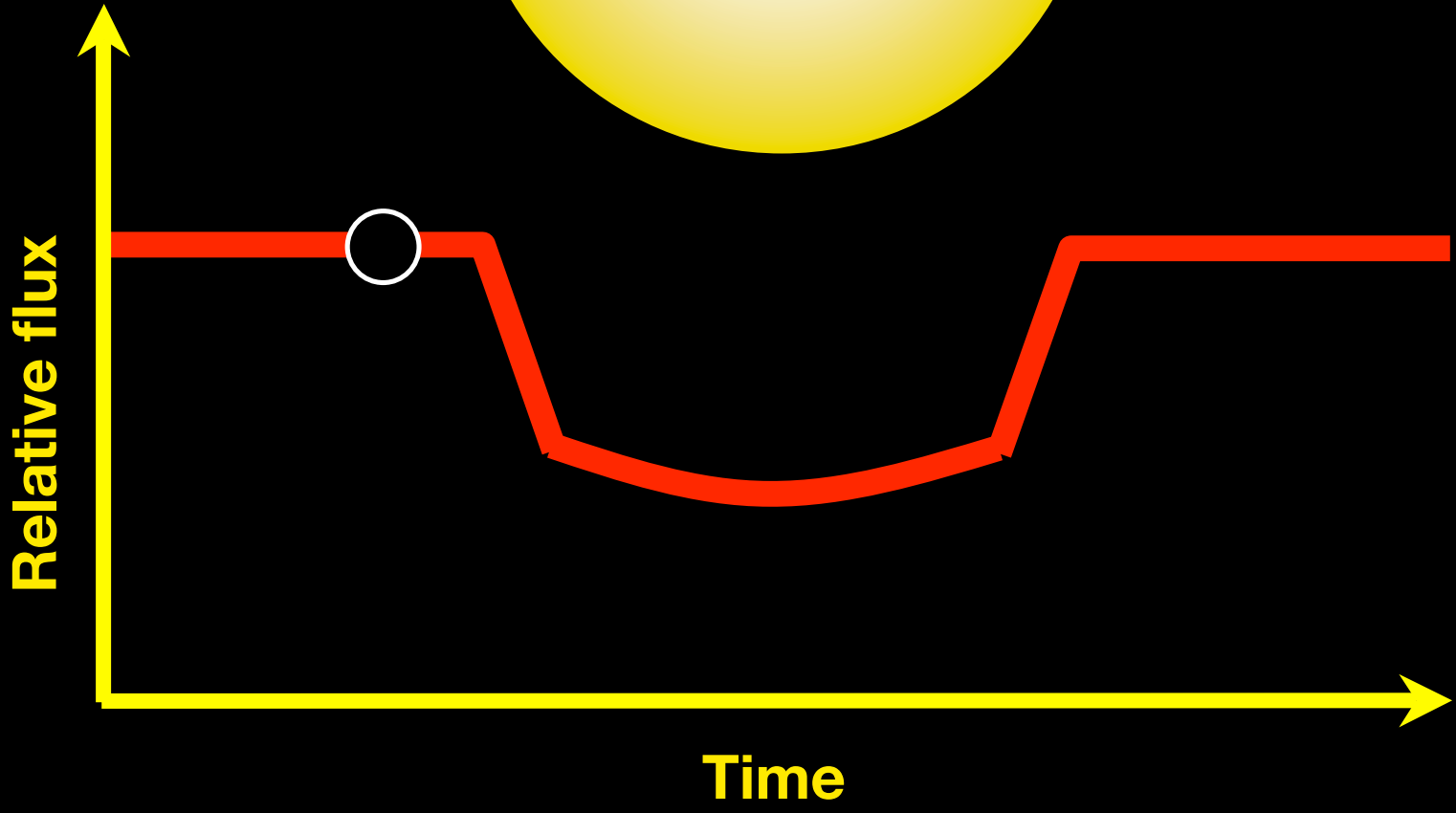
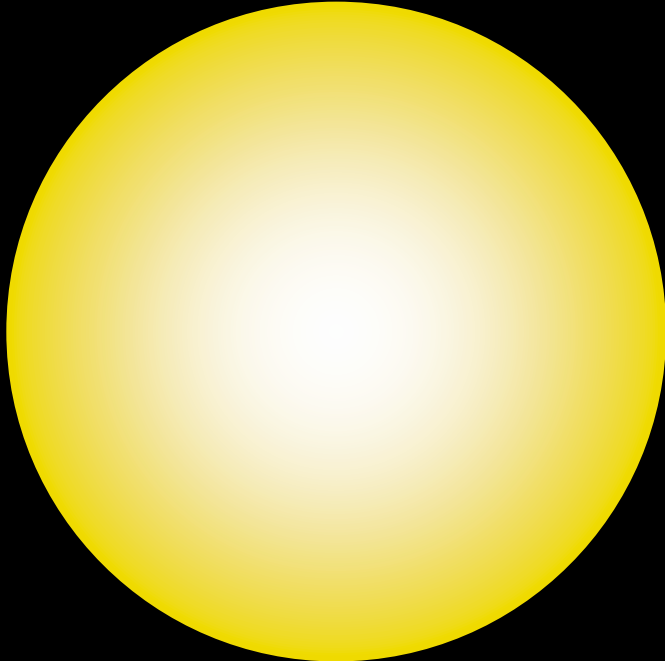
The Rossiter- McLaughlin Effect

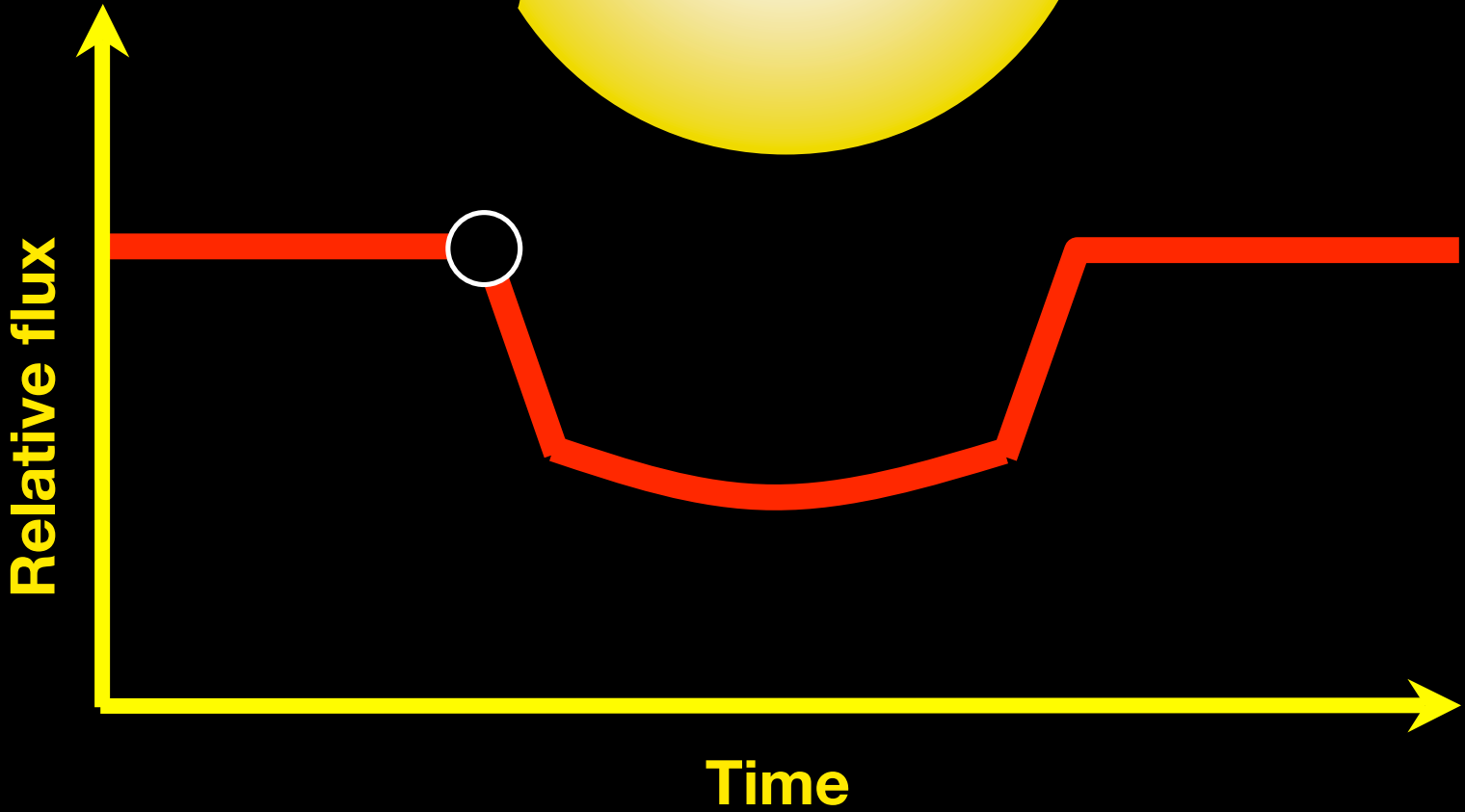
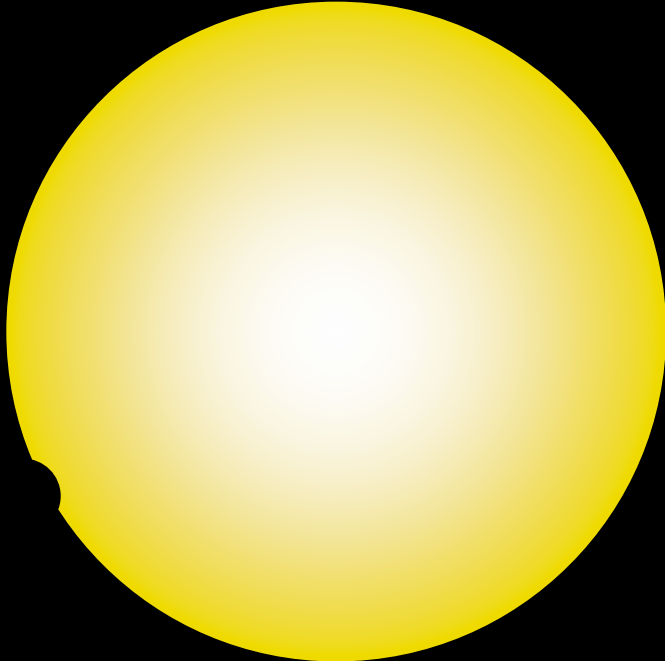
B. Scott Gaudi

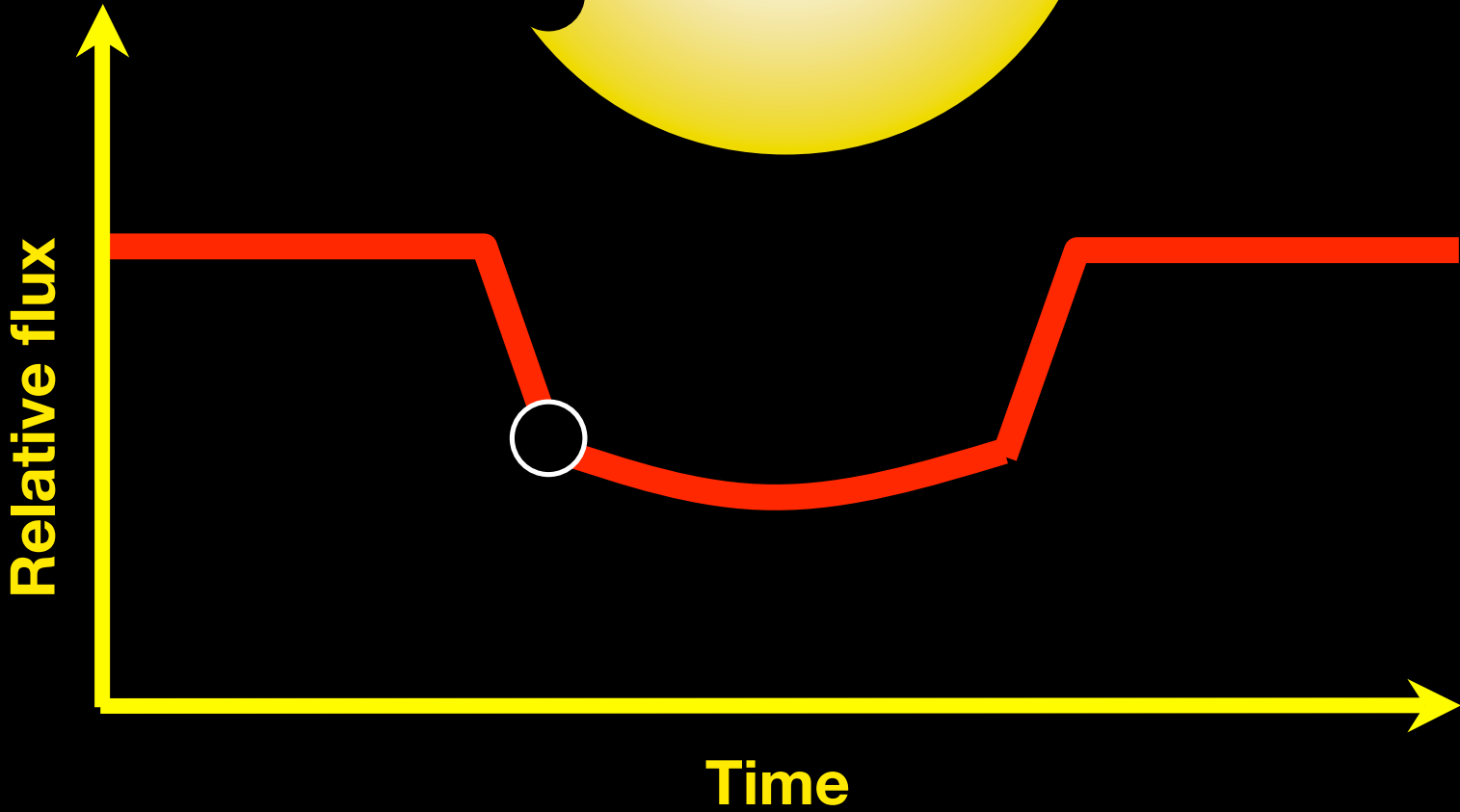
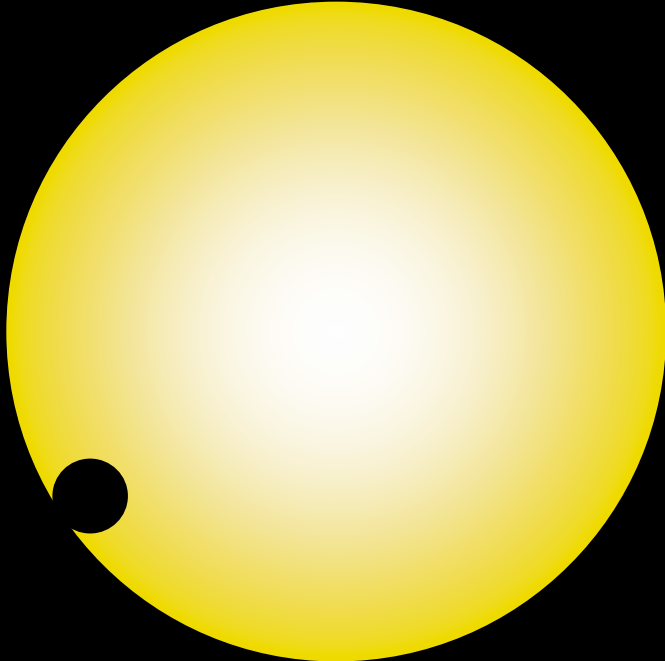
The Ohio State University

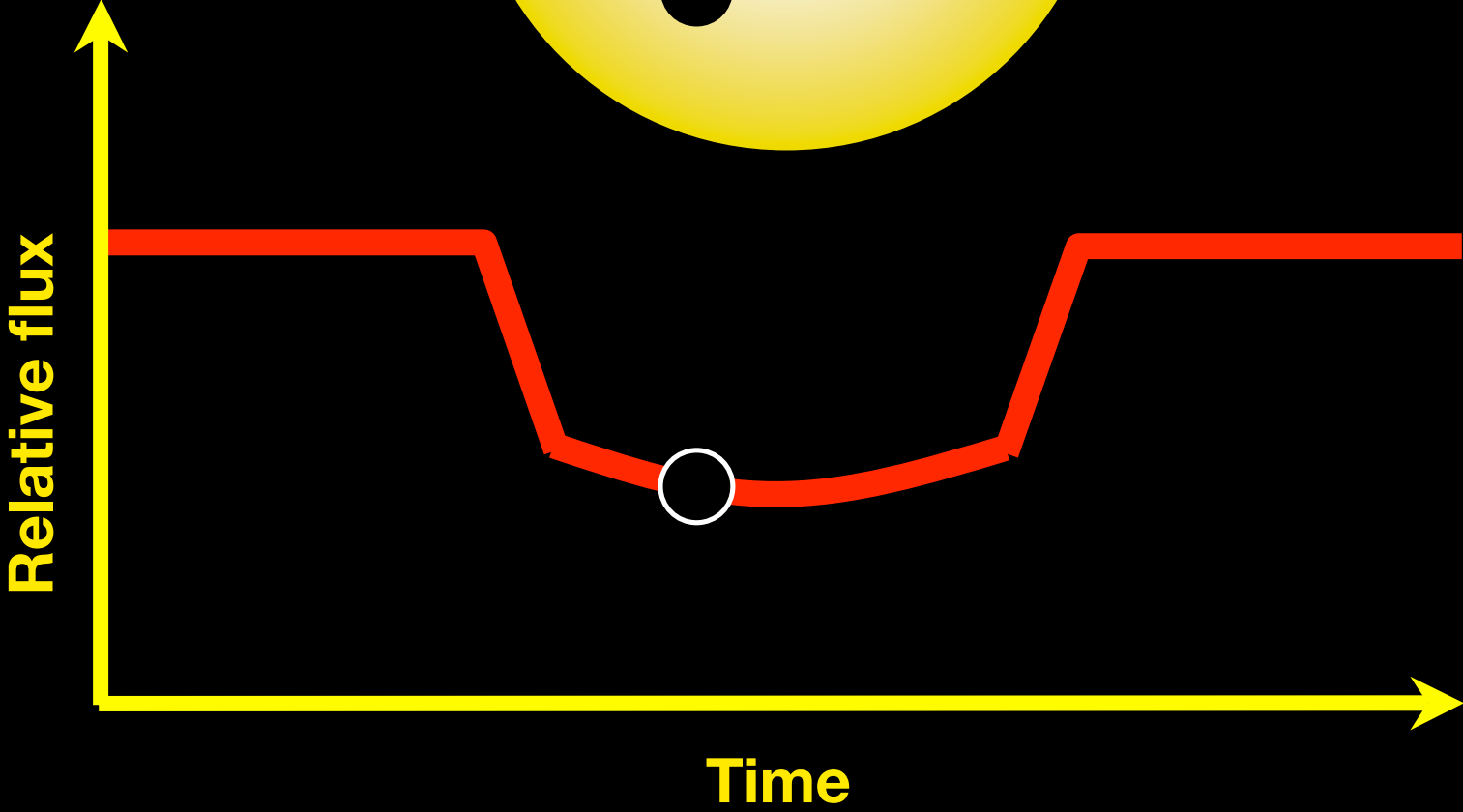
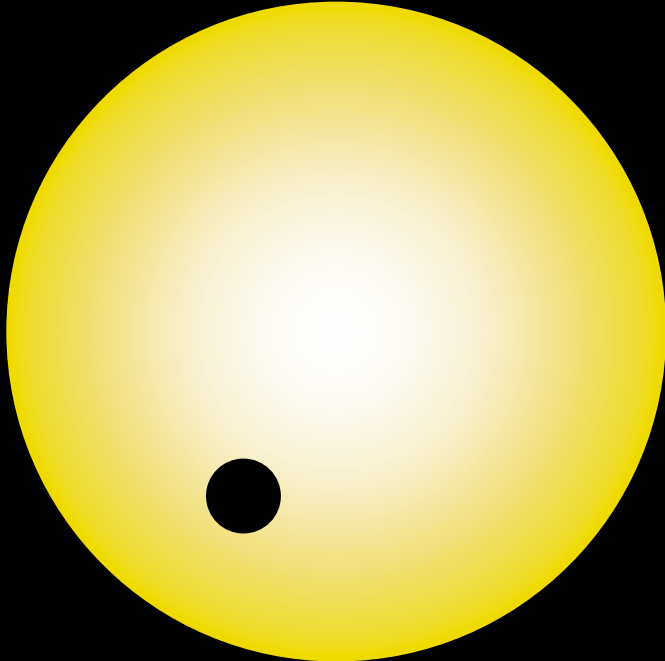
(special thanks to Josh Winn)

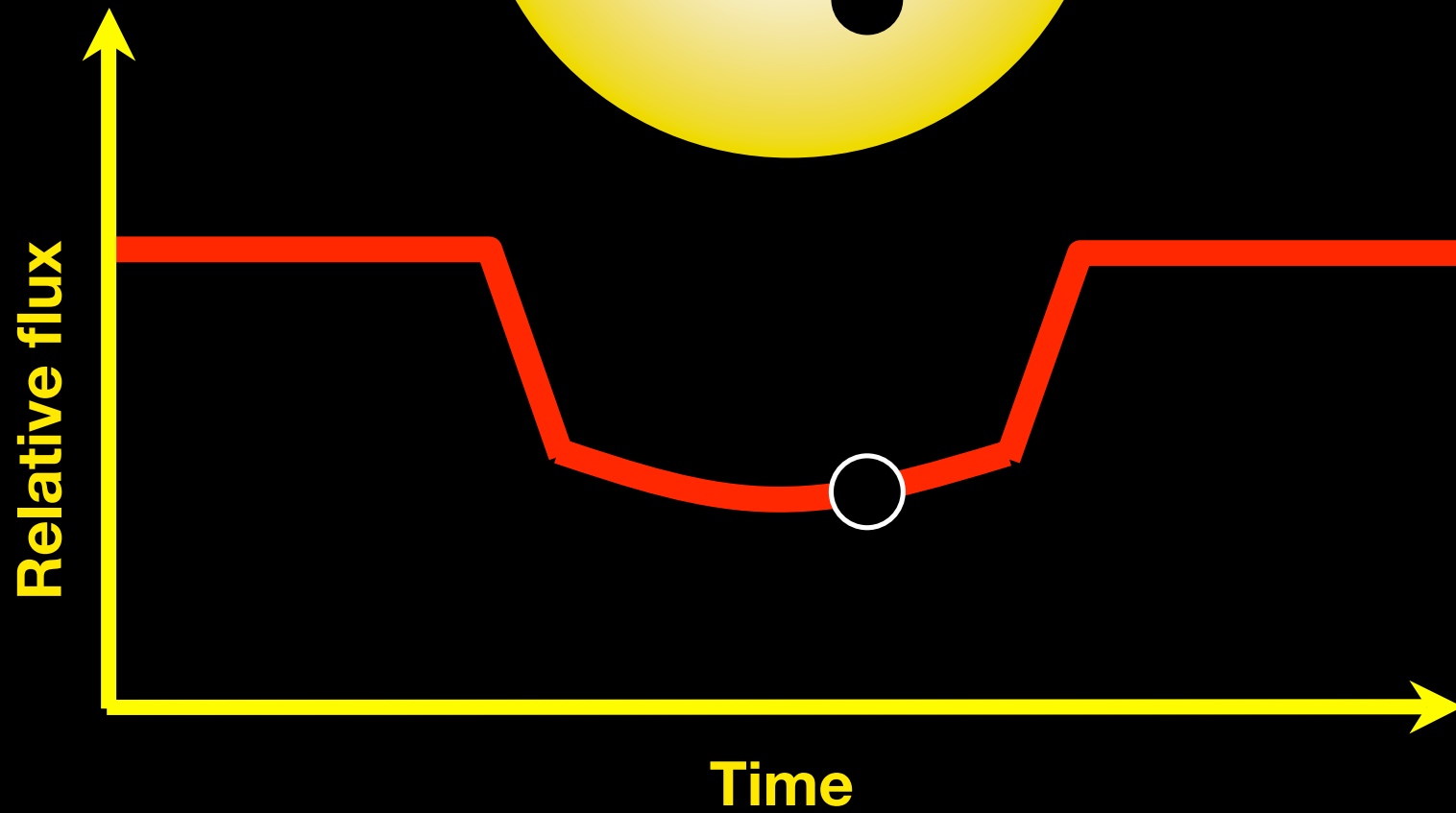
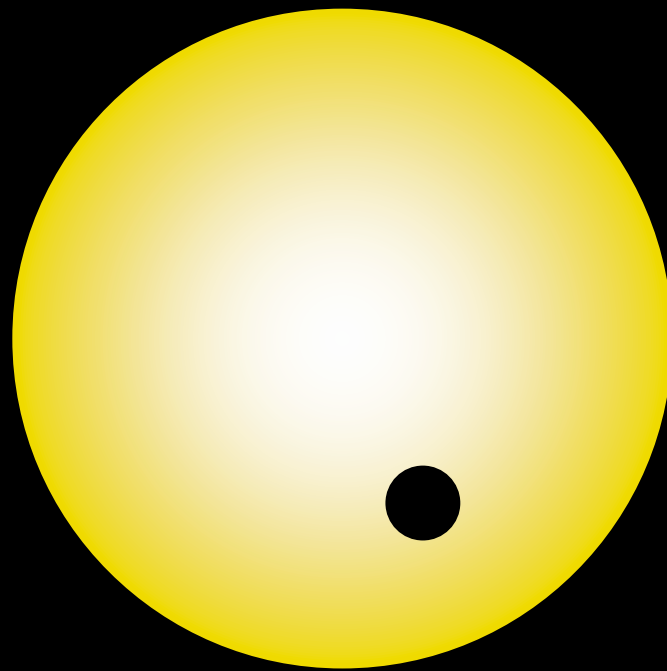


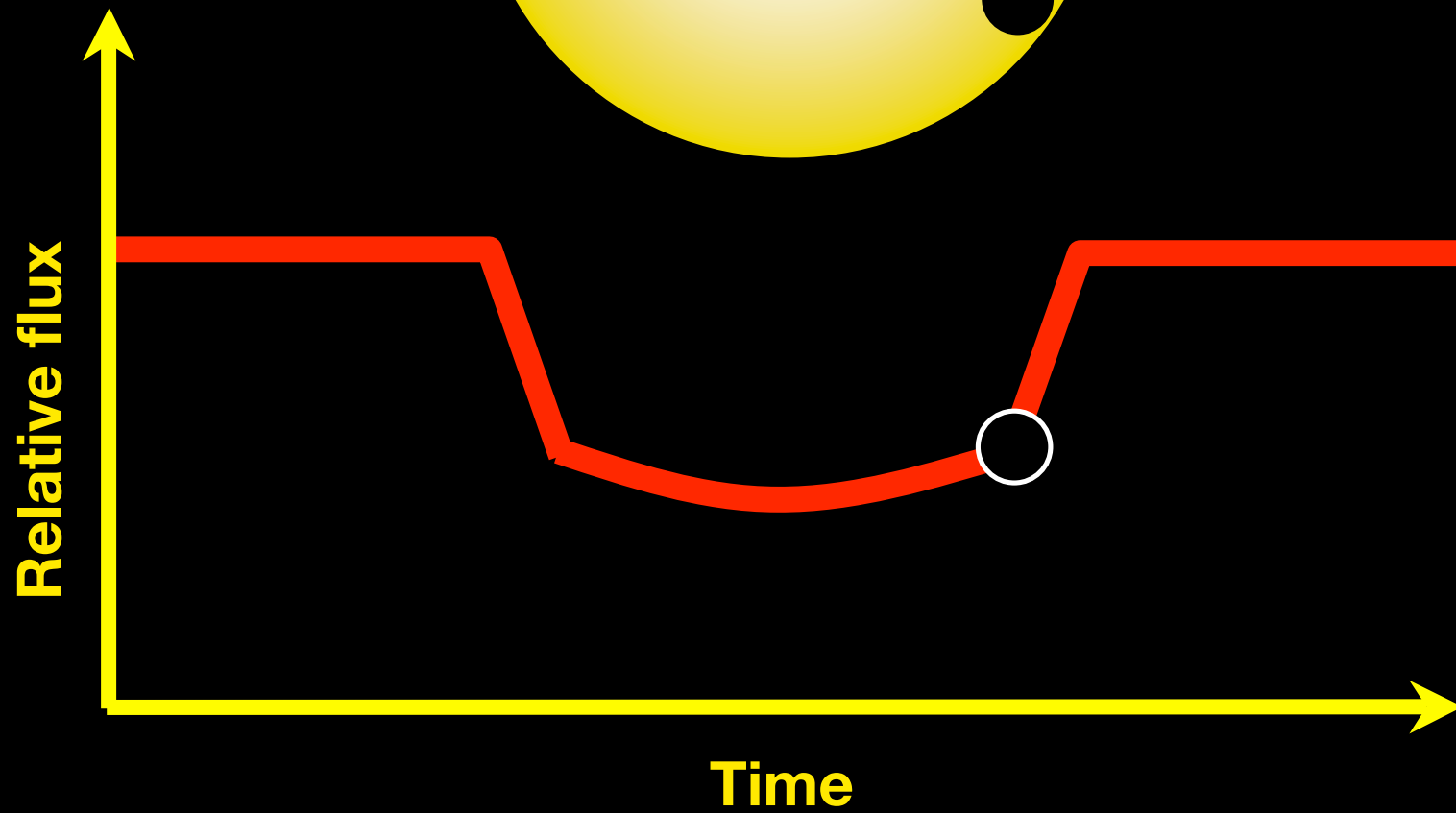
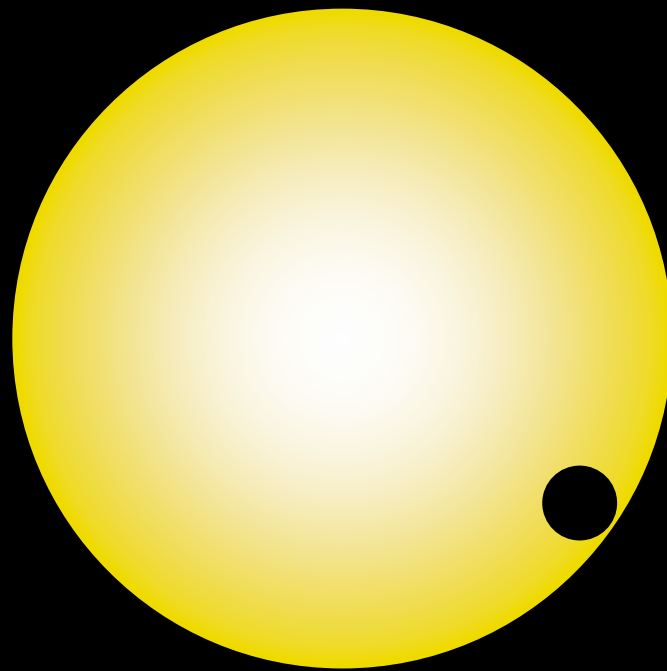


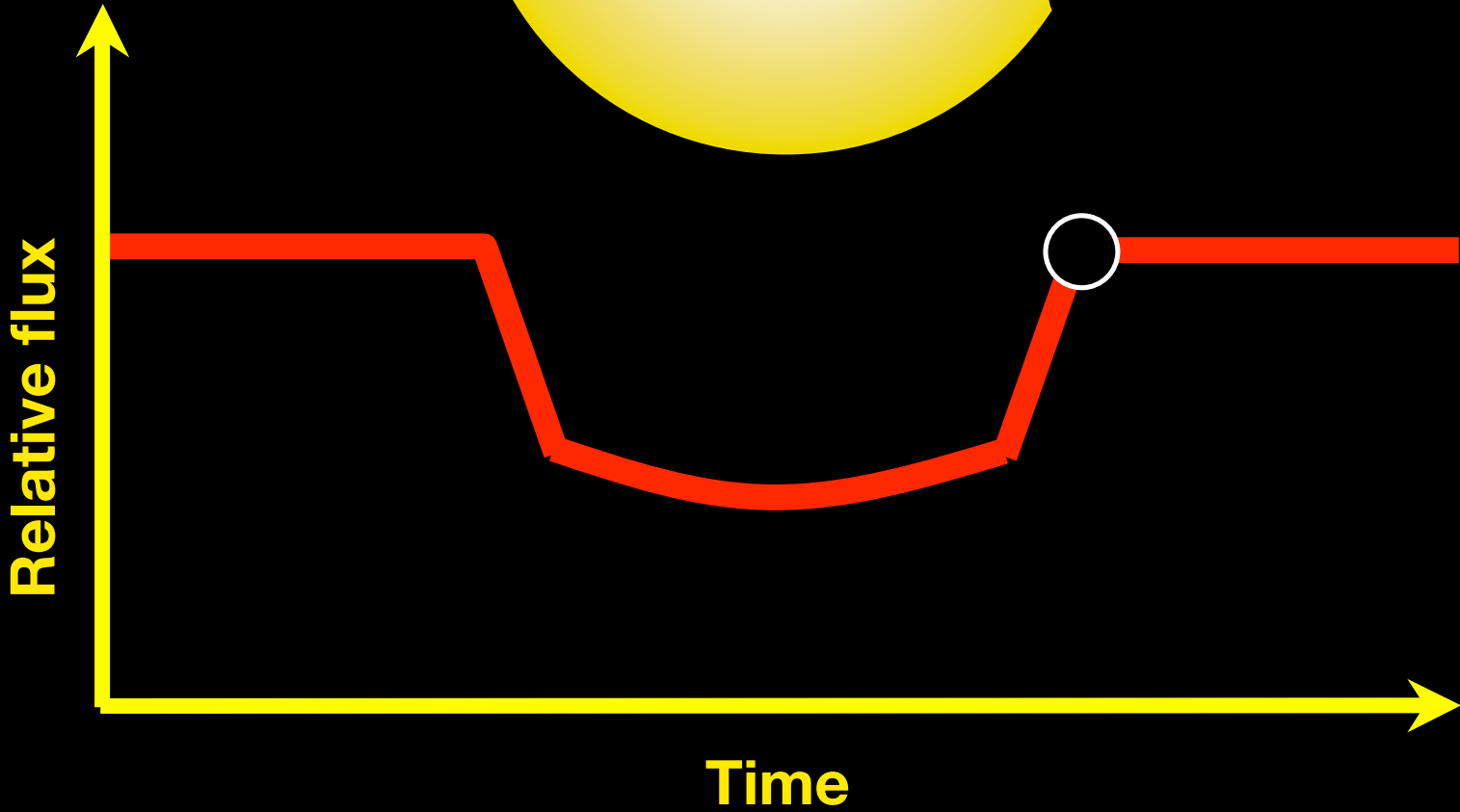
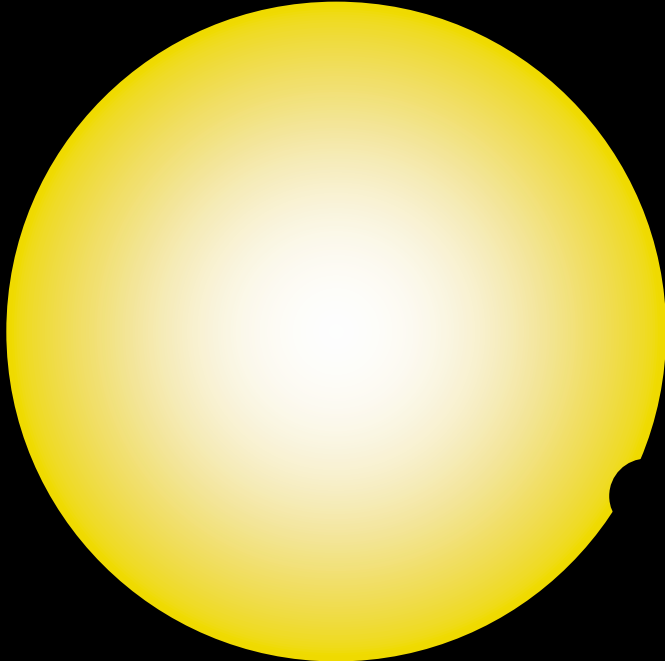


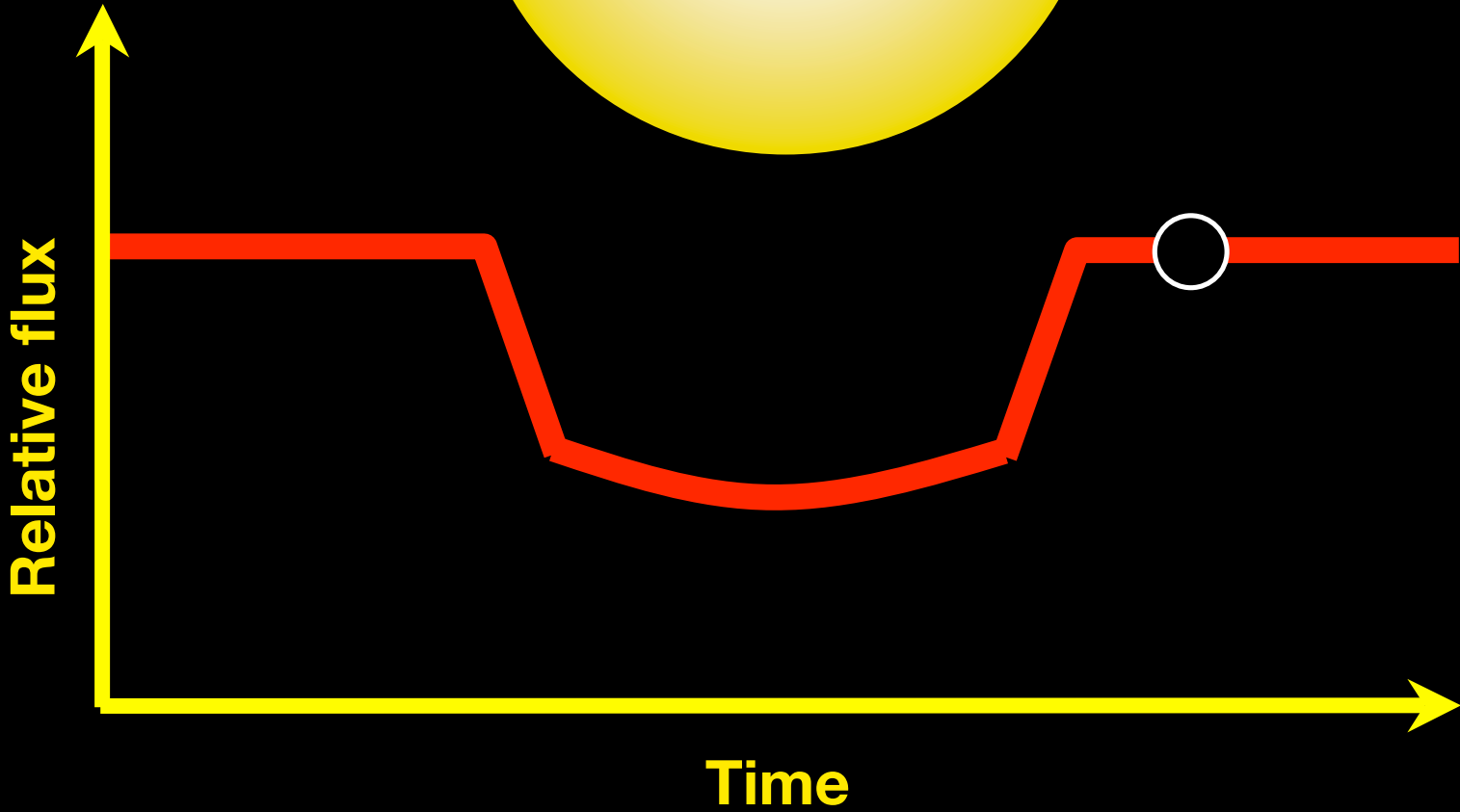
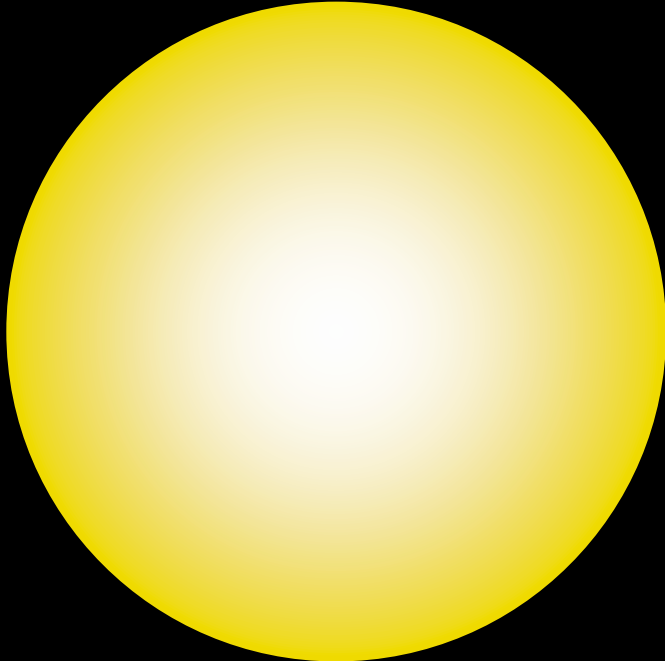


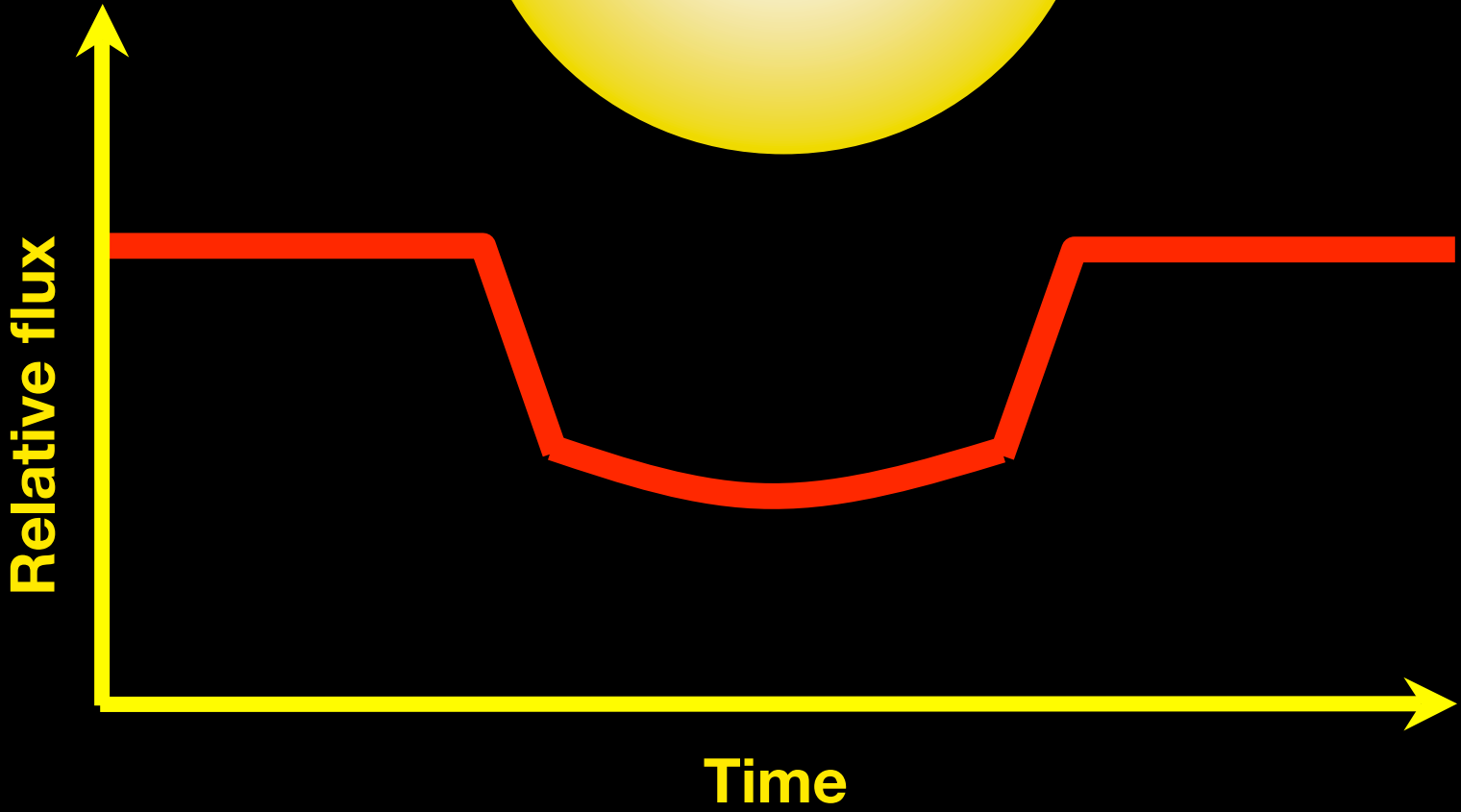
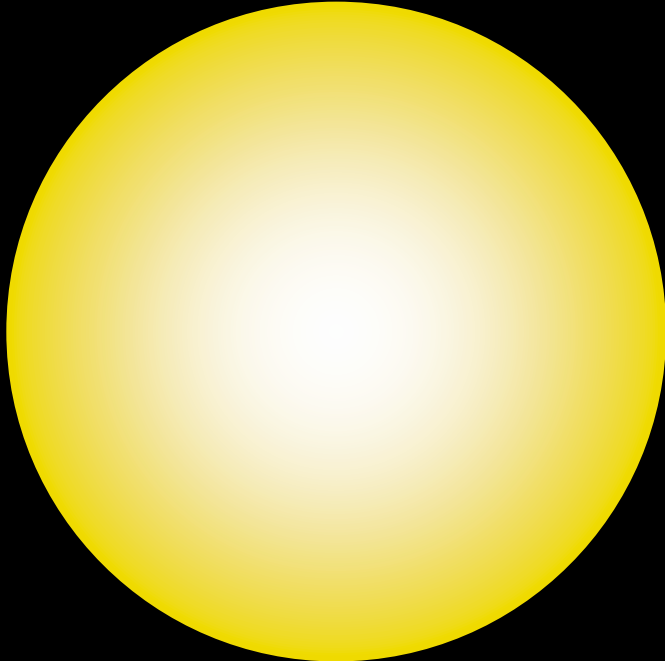


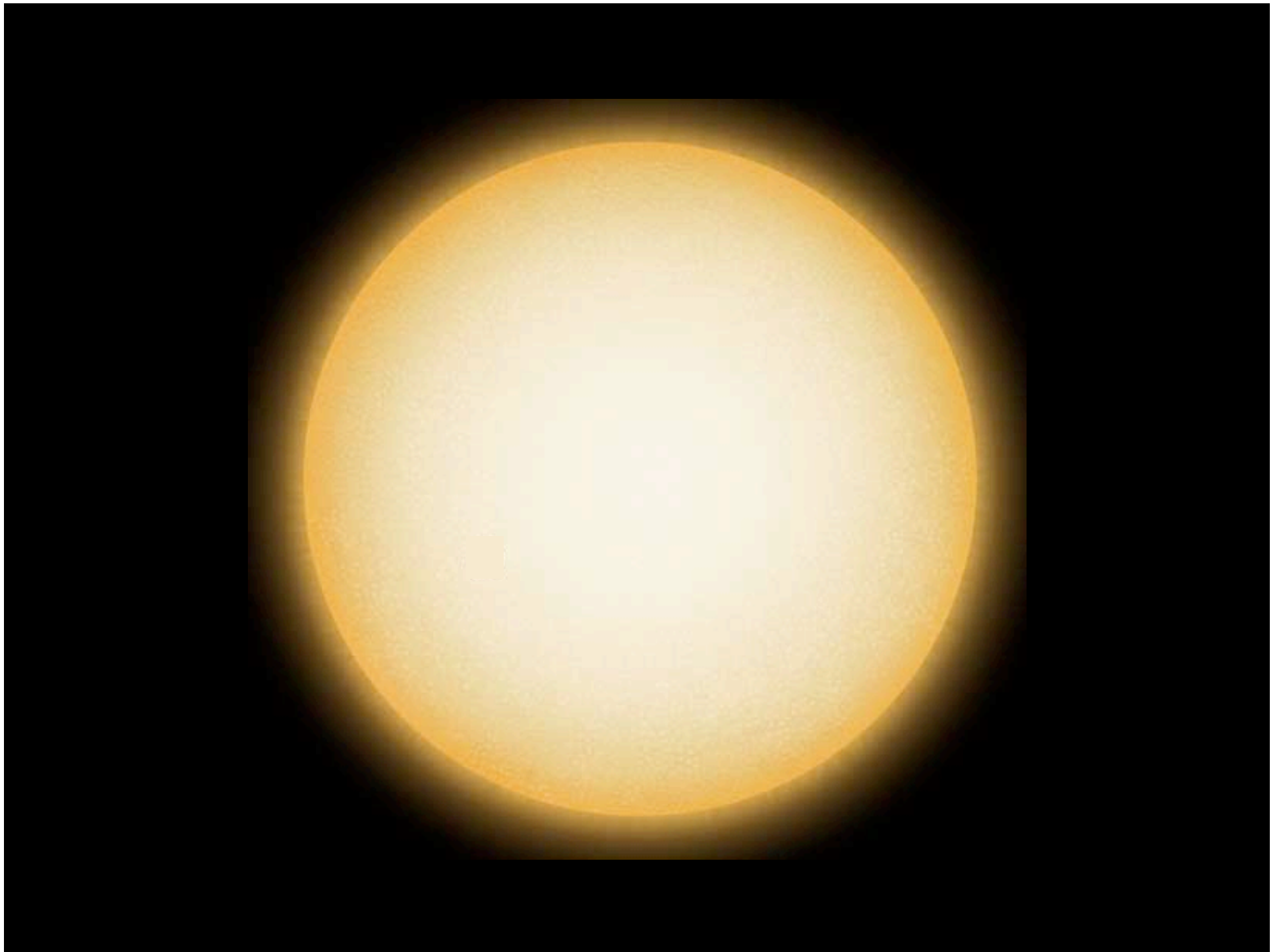


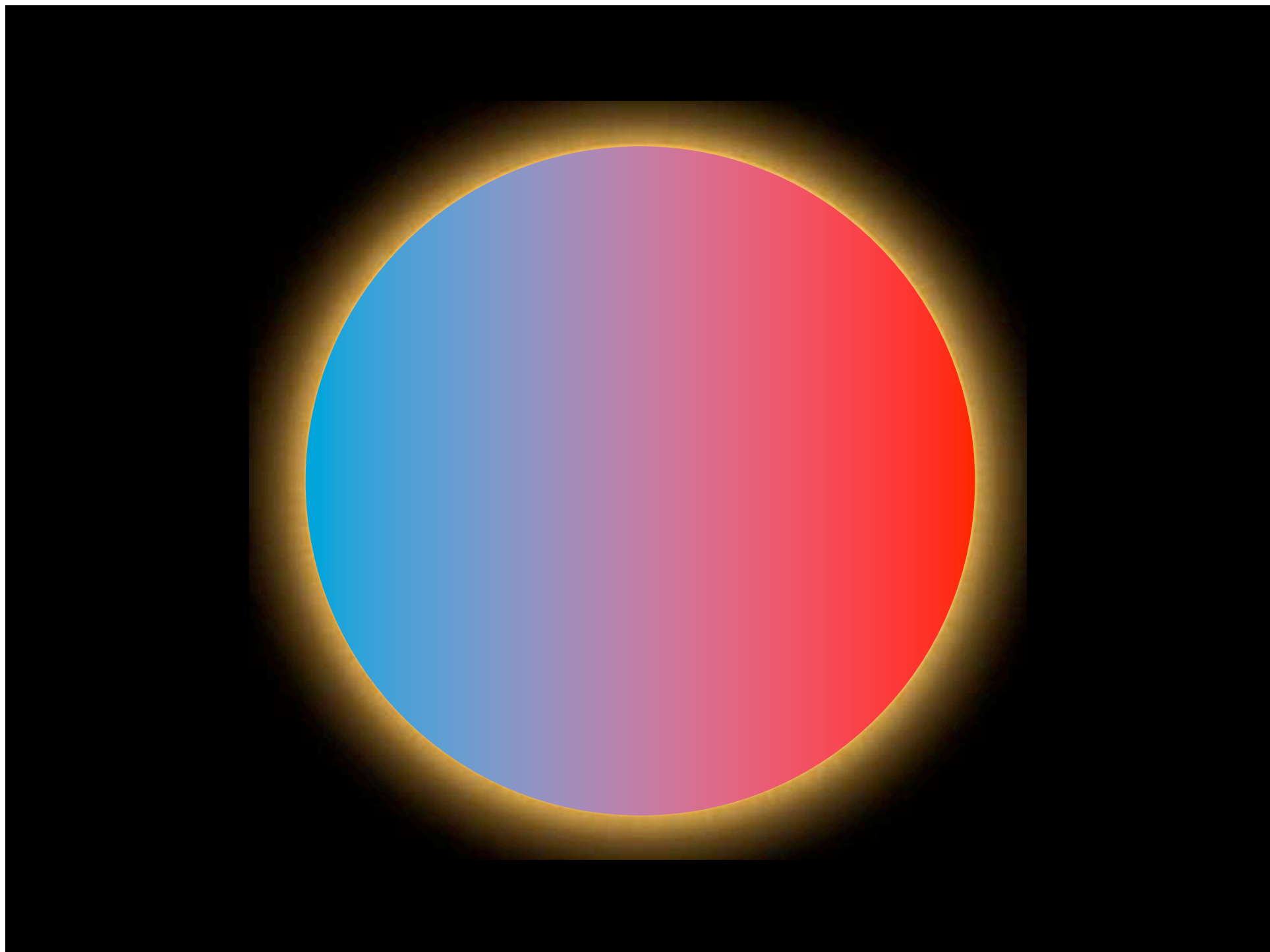


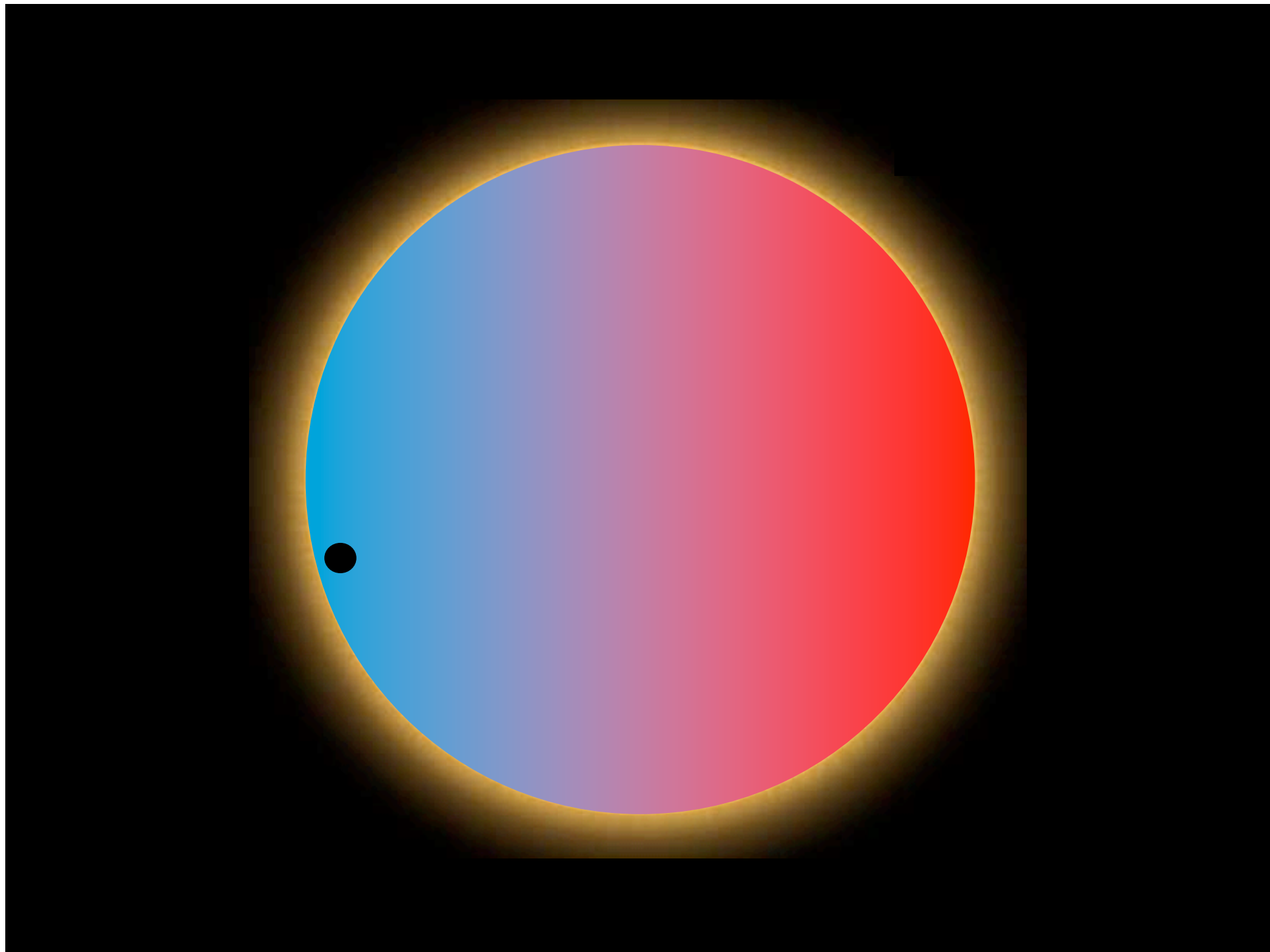


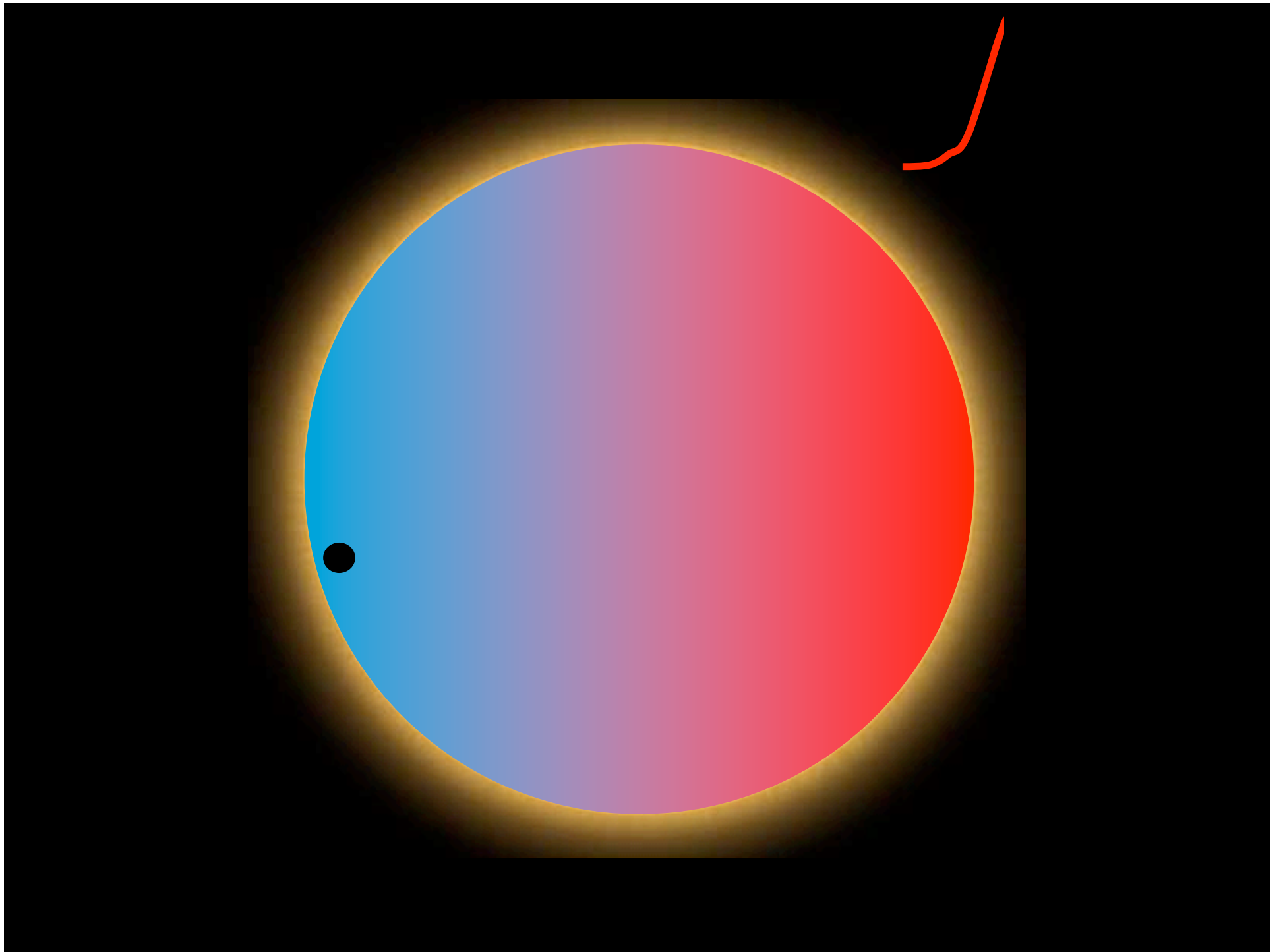


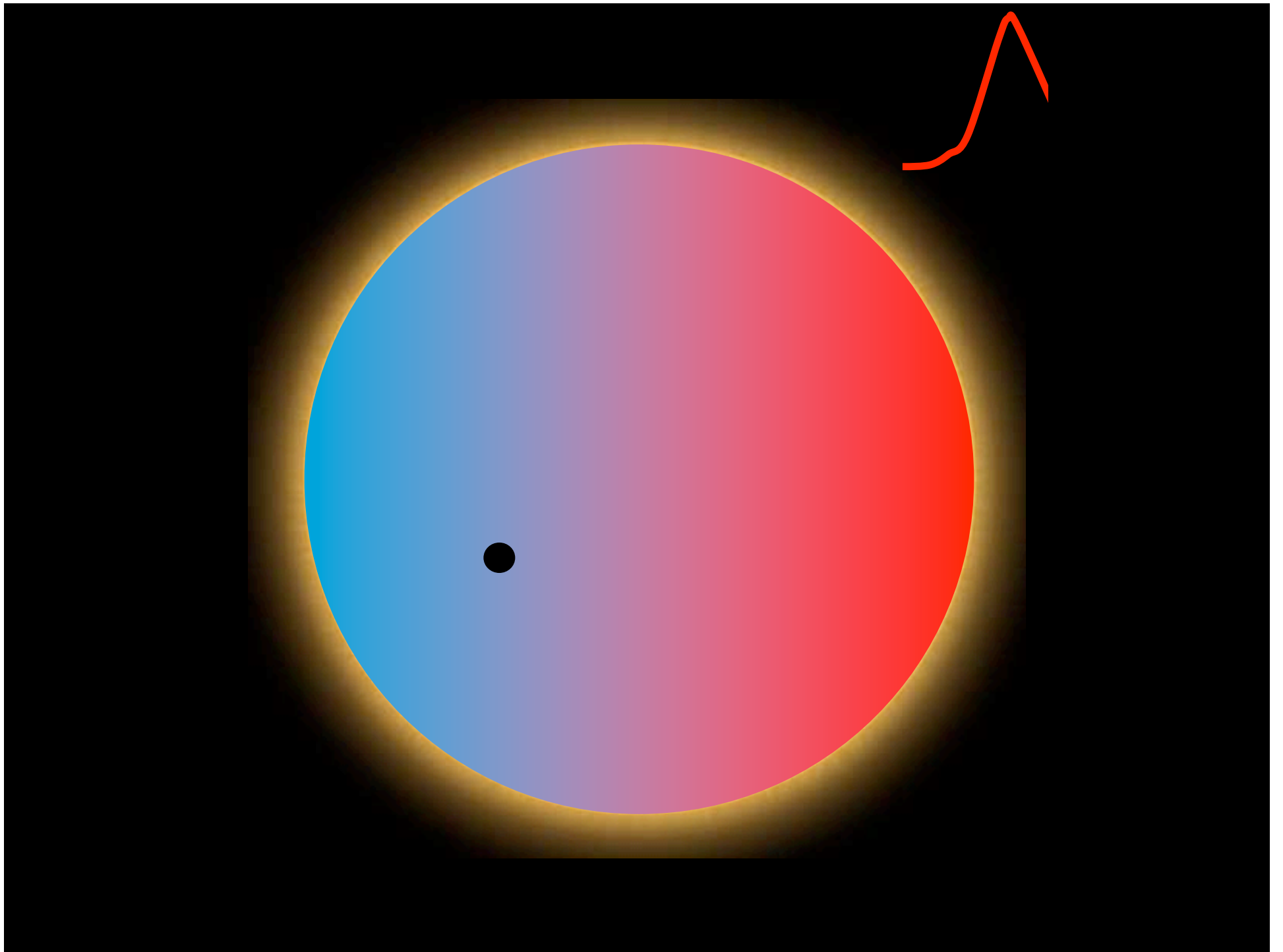


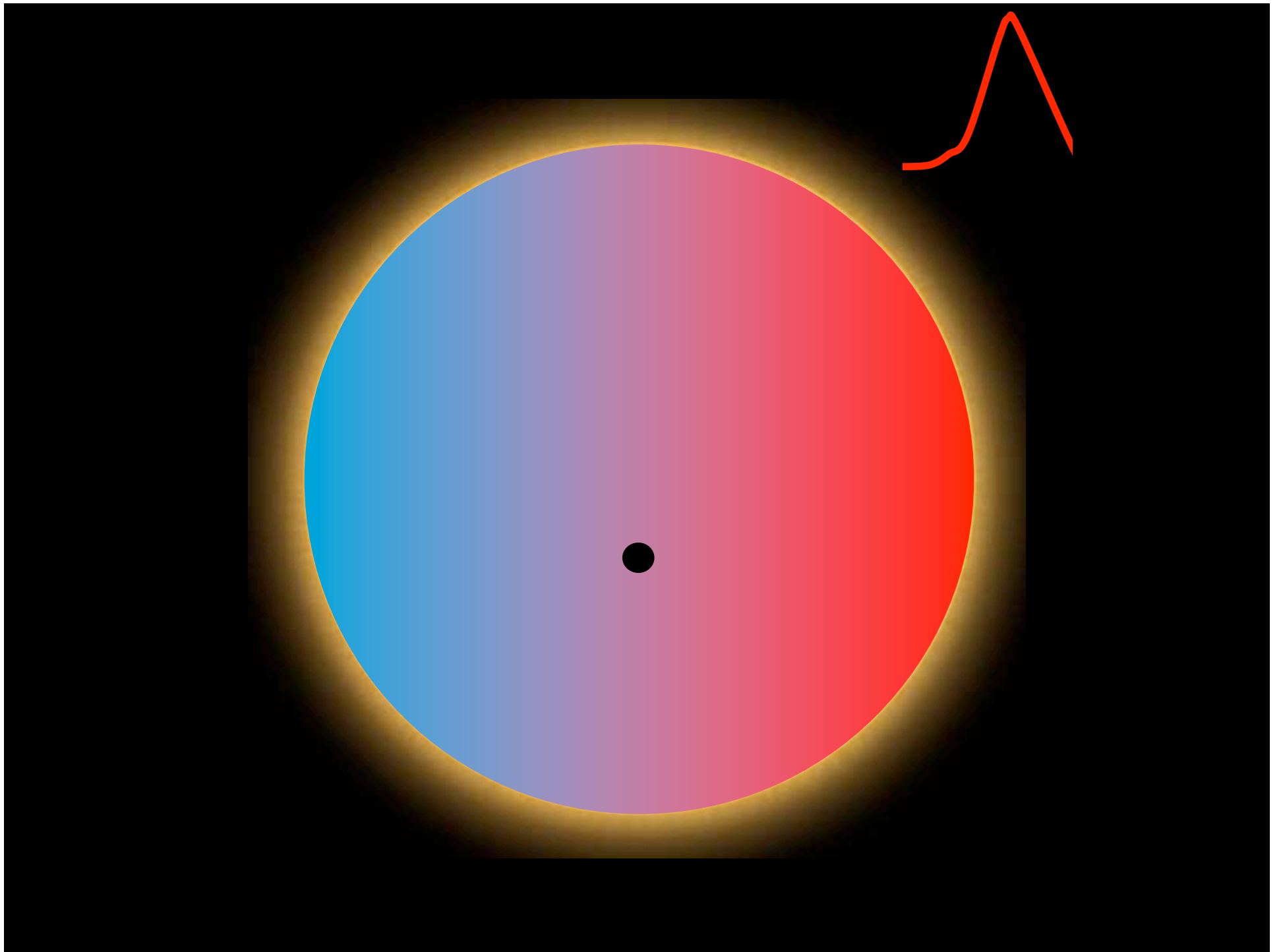


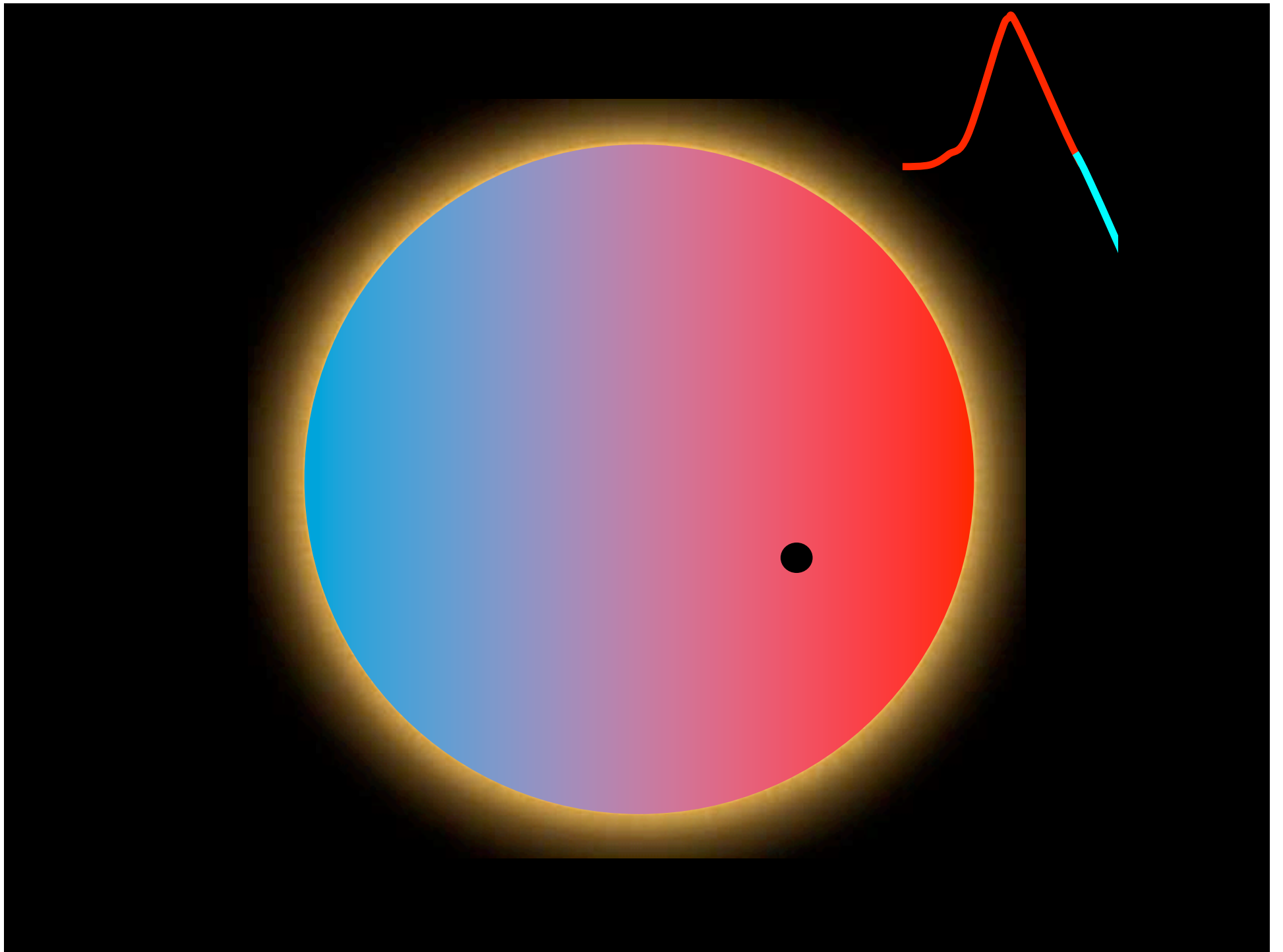


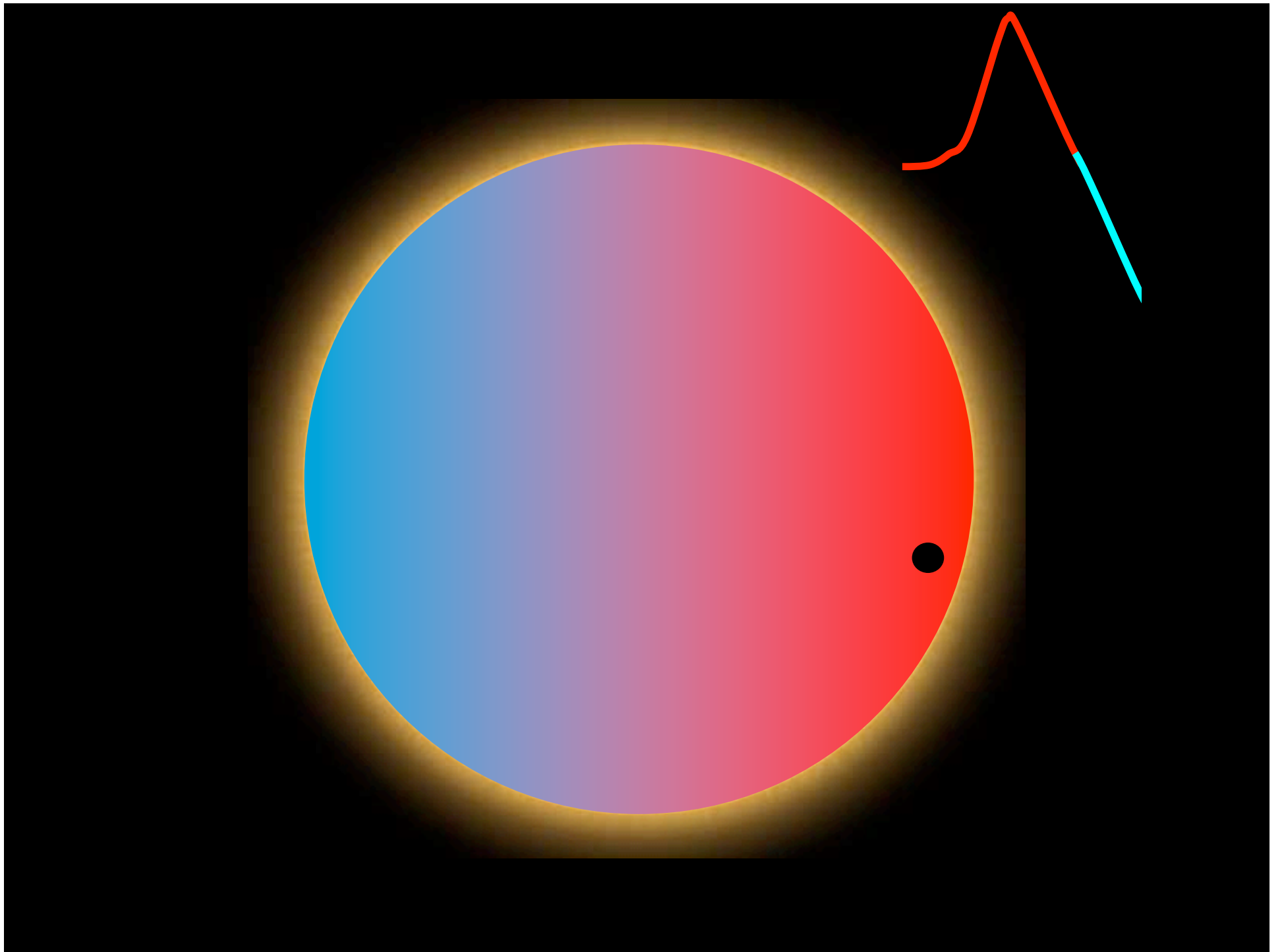


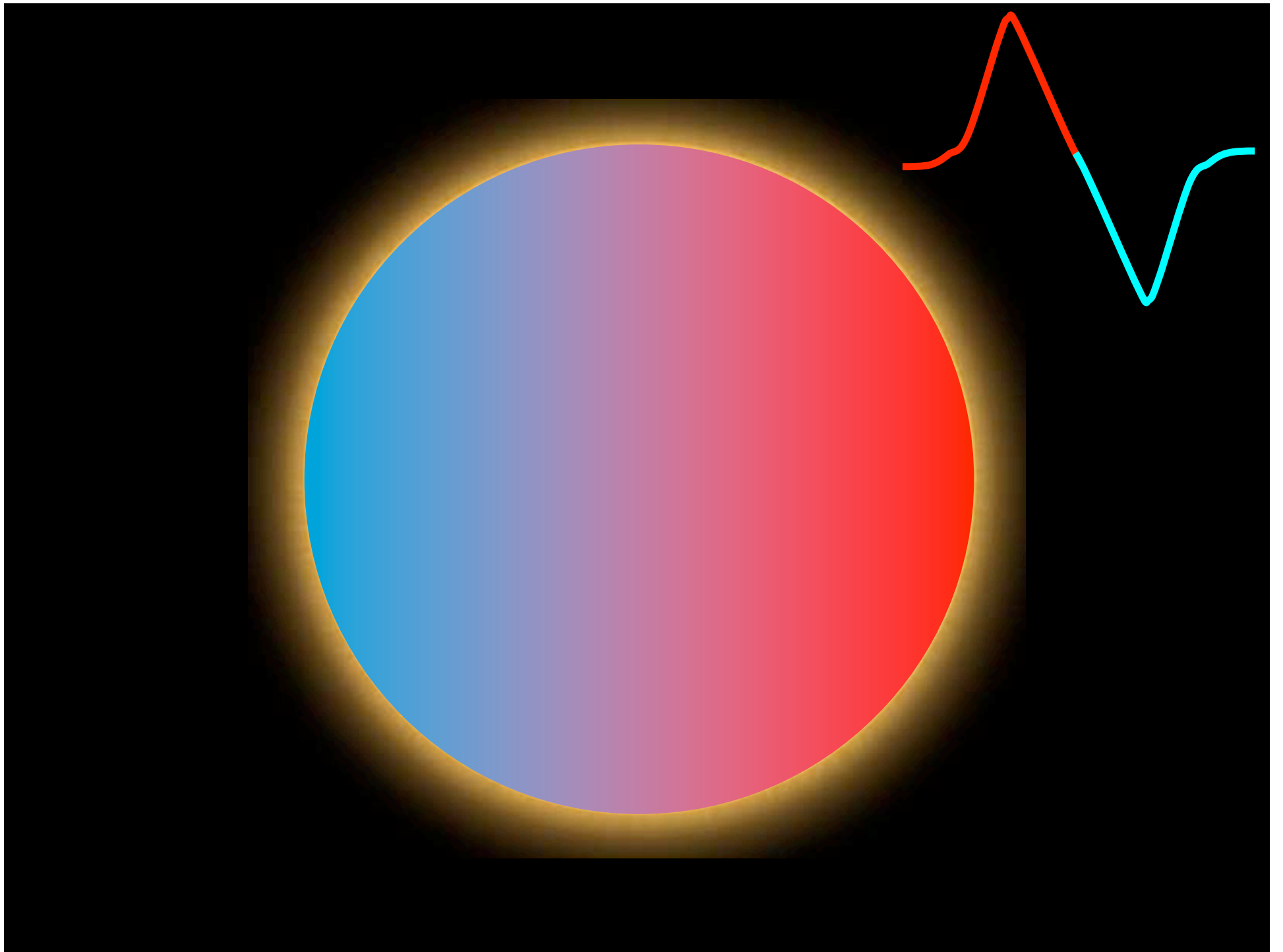


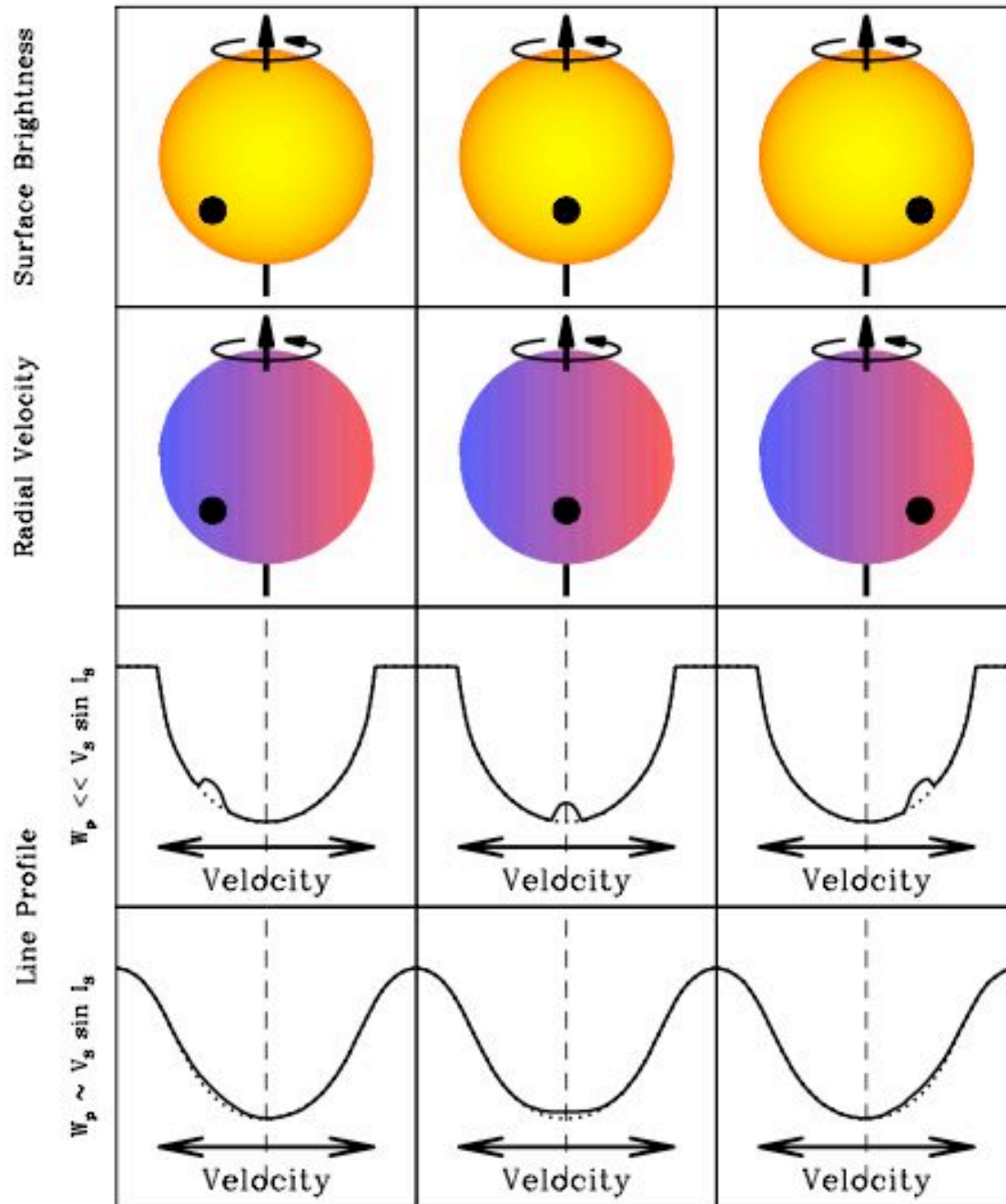








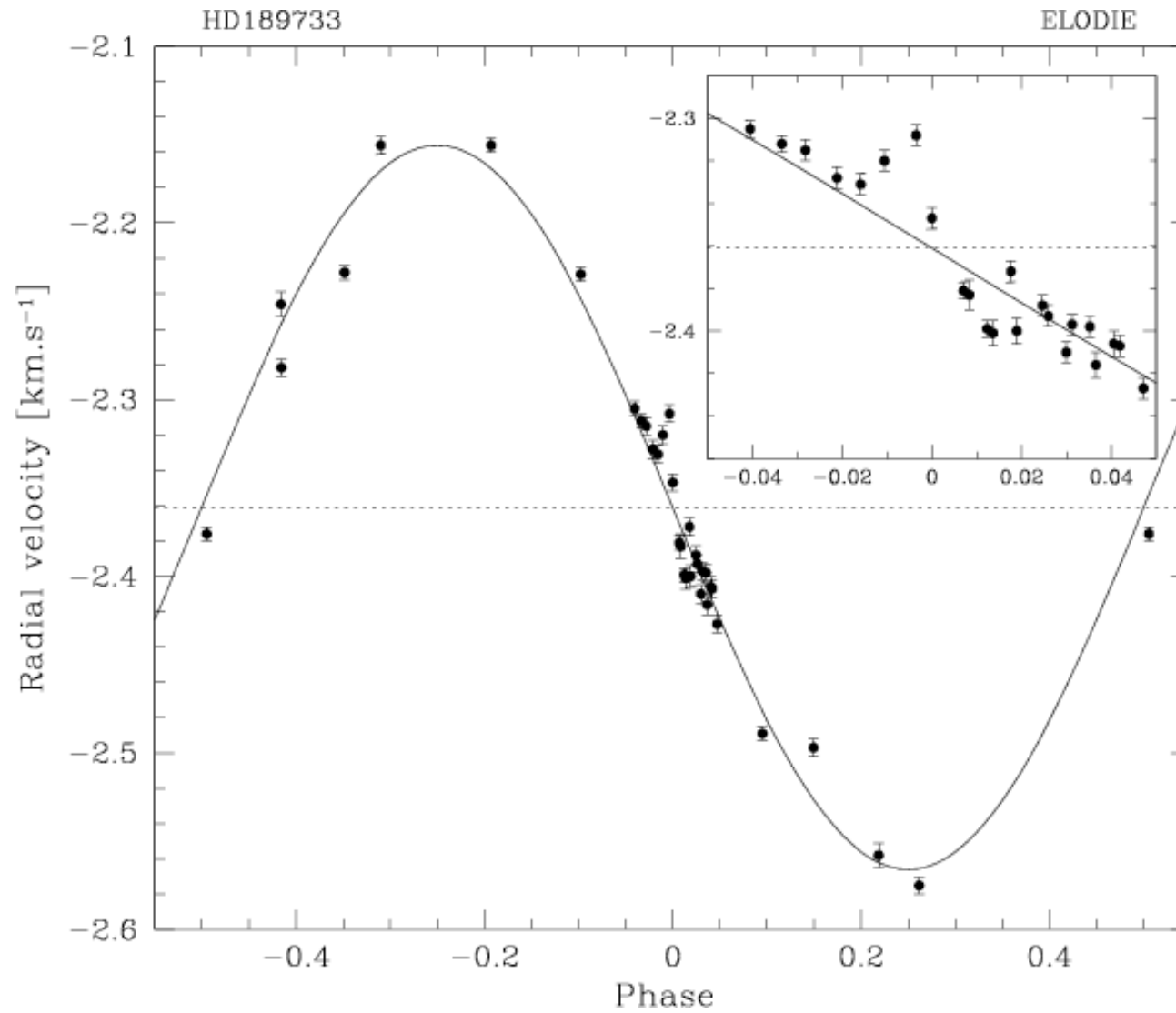




Gaudi &
Winn (2007)

What is the
Rossiter-McLaughlin
Effect?

What do we measure?



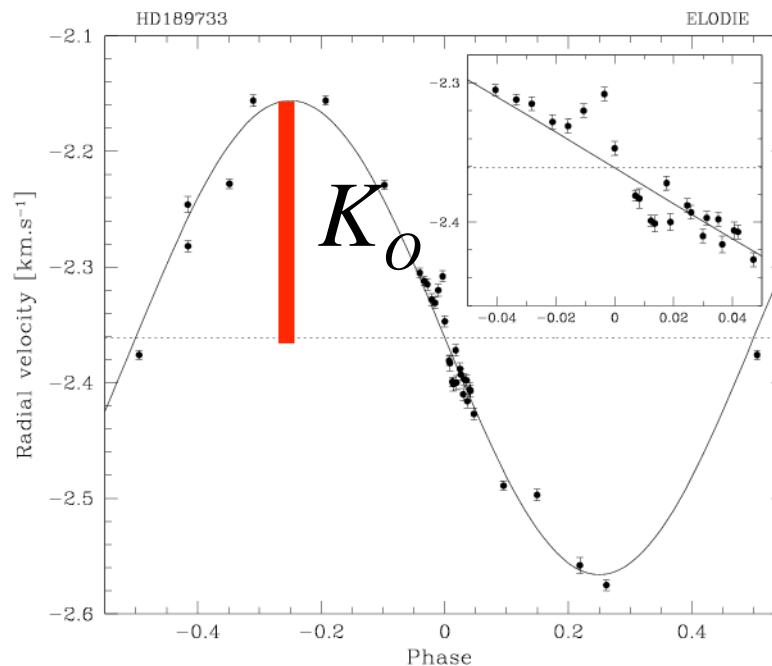
What do we measure?

$$V(t) = V_o(t) + V_R(t) + V_0$$

Doppler

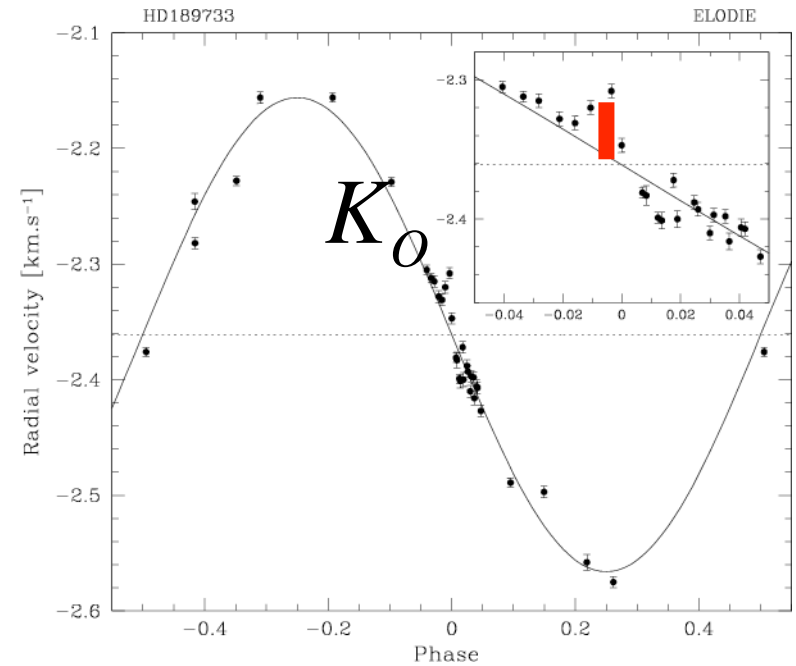
$$V_o(t) = K_o \{ \cos[f(t) + \omega] + e \cos \omega \}$$

$$K_o = \left(\frac{2\pi G}{P} \right)^{1/3} \frac{m \sin i}{(M + m)^{2/3}} (1 - e^2)^{-1/2}$$

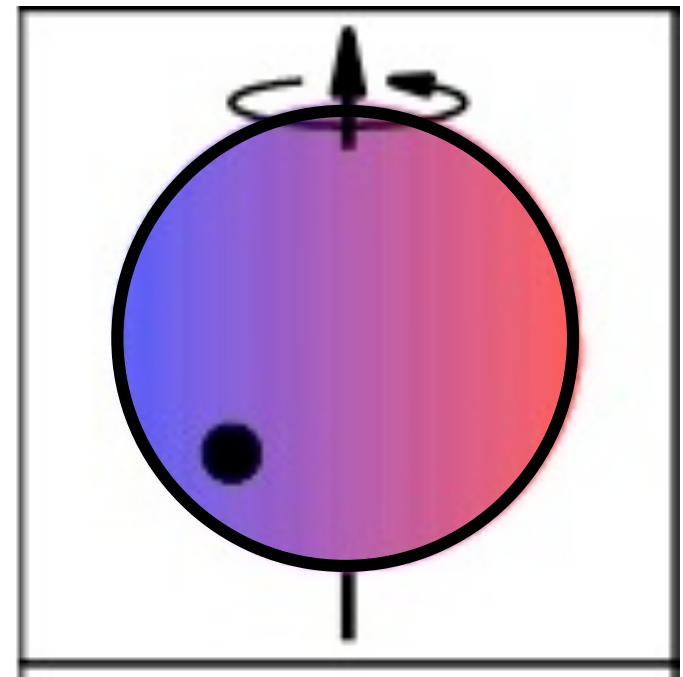


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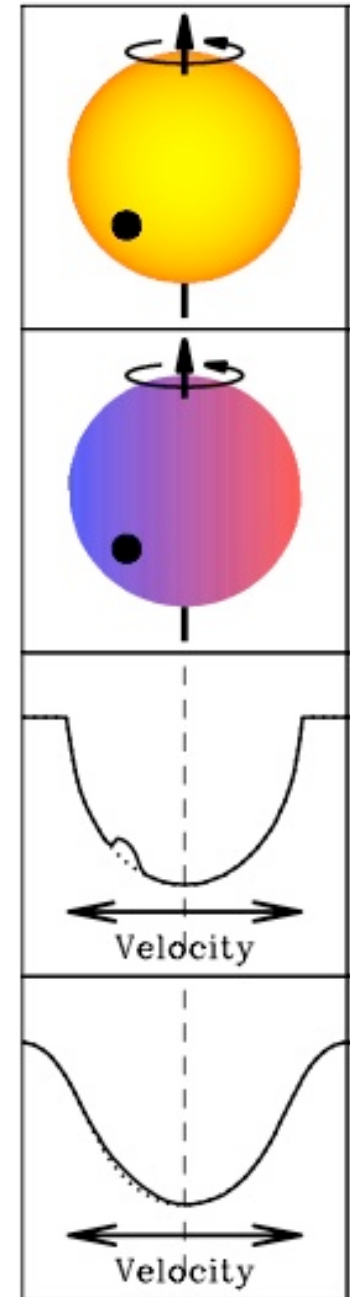


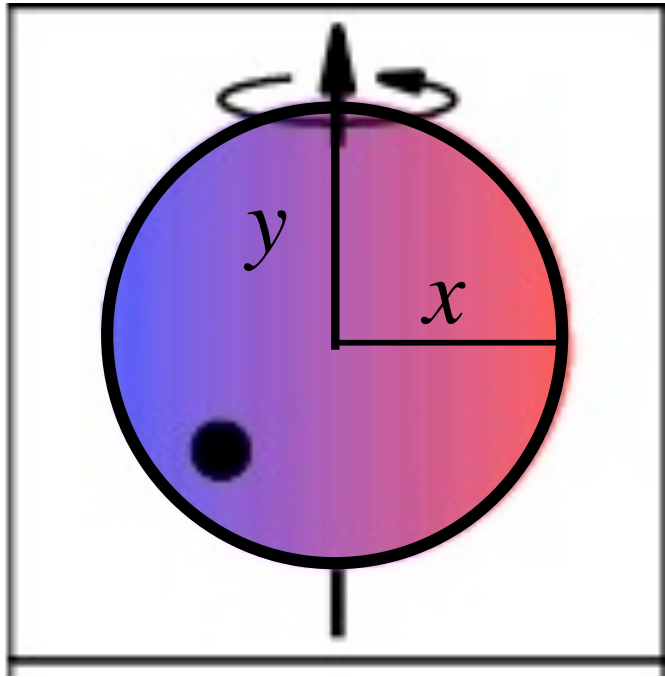
“Anomalous RV”



What exactly is the RM effect?

- Change in line shape
- *Not* a Doppler shift
- Cross-correlation measures line centroids
- Some methods attempt to correct for line shape variations





$$V(x, y) = xV_* \sin I$$

Centroid approximation

$$V_R = V_* \sin I \frac{\int \int xS(x, y) dx dy}{\int \int S(x, y) dx dy}$$

$$\gamma = \frac{r}{R}$$

$$V_R = V_* \sin I \frac{\gamma^2}{1 - \gamma^2} g(t; x_p, y_p, \gamma, u_1, \dots) \equiv K_R g(t)$$

Ohta et al 2005

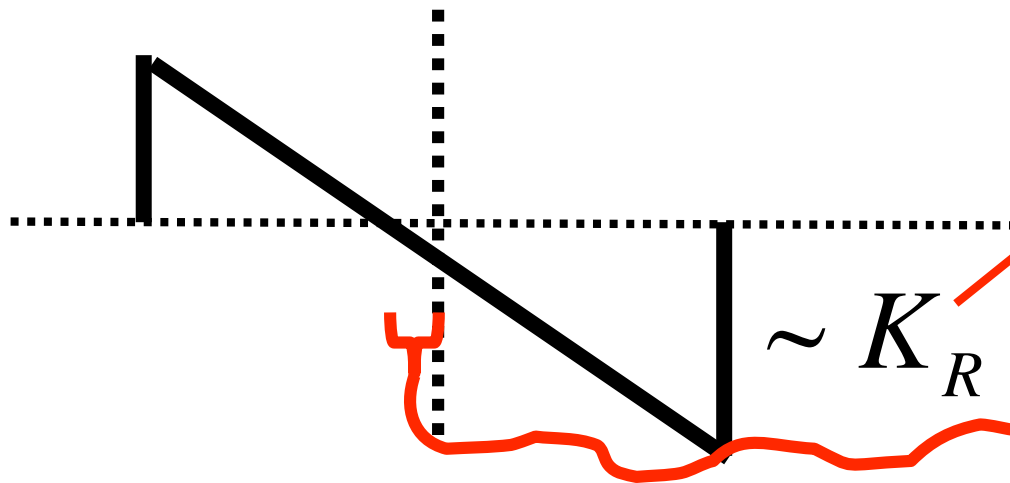
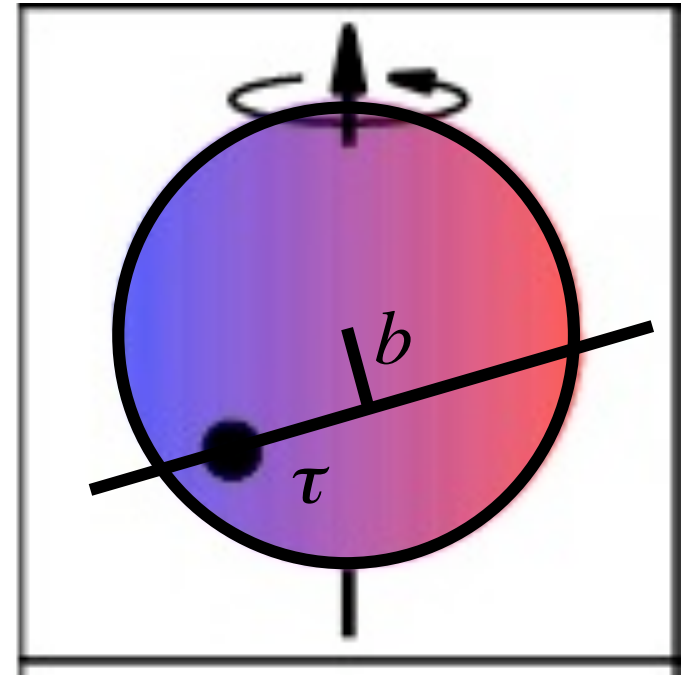
Gimenez 2006

No limb-darkening, complete transit

$$V_R = K_R g(t)$$

$$g(t) = x(t) = \tau \cos \lambda - b \sin \lambda$$

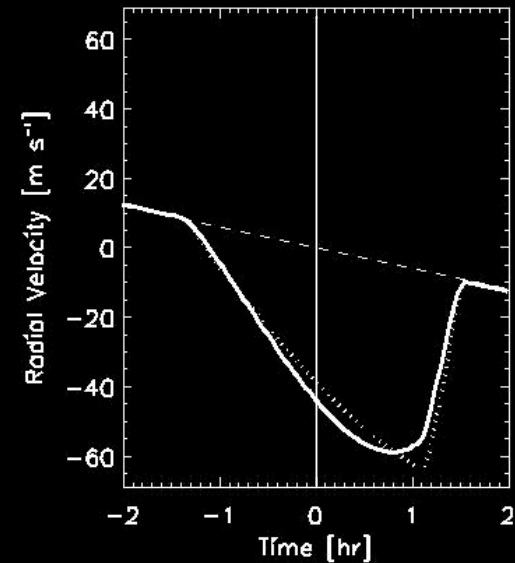
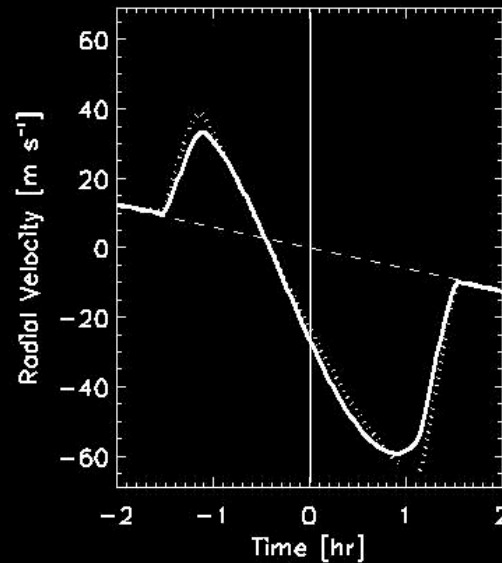
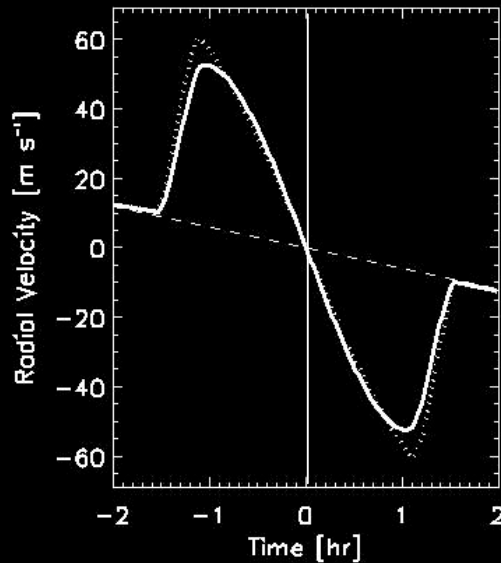
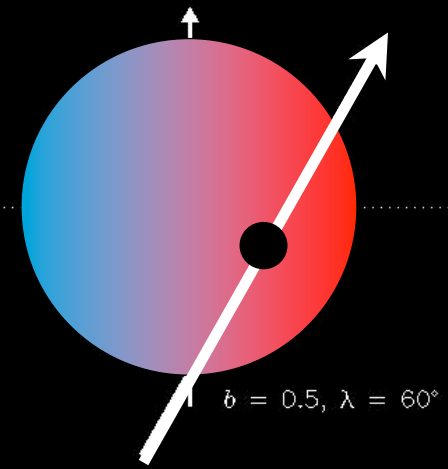
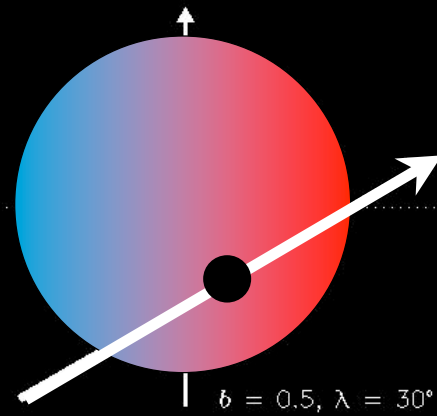
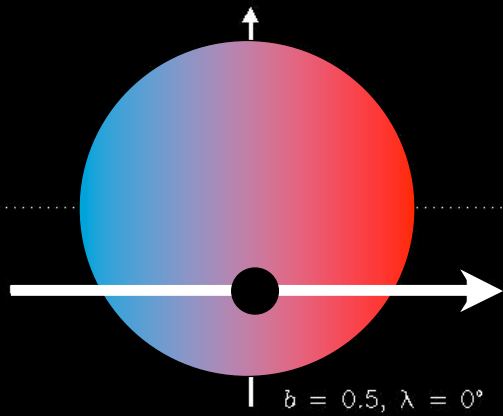
where $\tau = \frac{t - t_{tra}}{T}$



$$K_R = V_* \sin I \frac{\gamma^2}{1 - \gamma^2}$$

$$\frac{t_{rot} - t_{tra}}{T} \sim b \tan \lambda$$

Measuring spin-orbit alignment



Ohta, Taruya, & Suto 2005; Gaudi & Winn 2007

Parameters

Specified by the photometric transit:

- Duration
- Ingress/Egress Time
- Impact Parameter
- Limb Darkening
- Planet/Star Radius Ratio

Additional Parameters Required for RM Effect

- λ (Spin-Orbit alignment)
- $V_* \sin I$ (can also be constrained from spectrum)

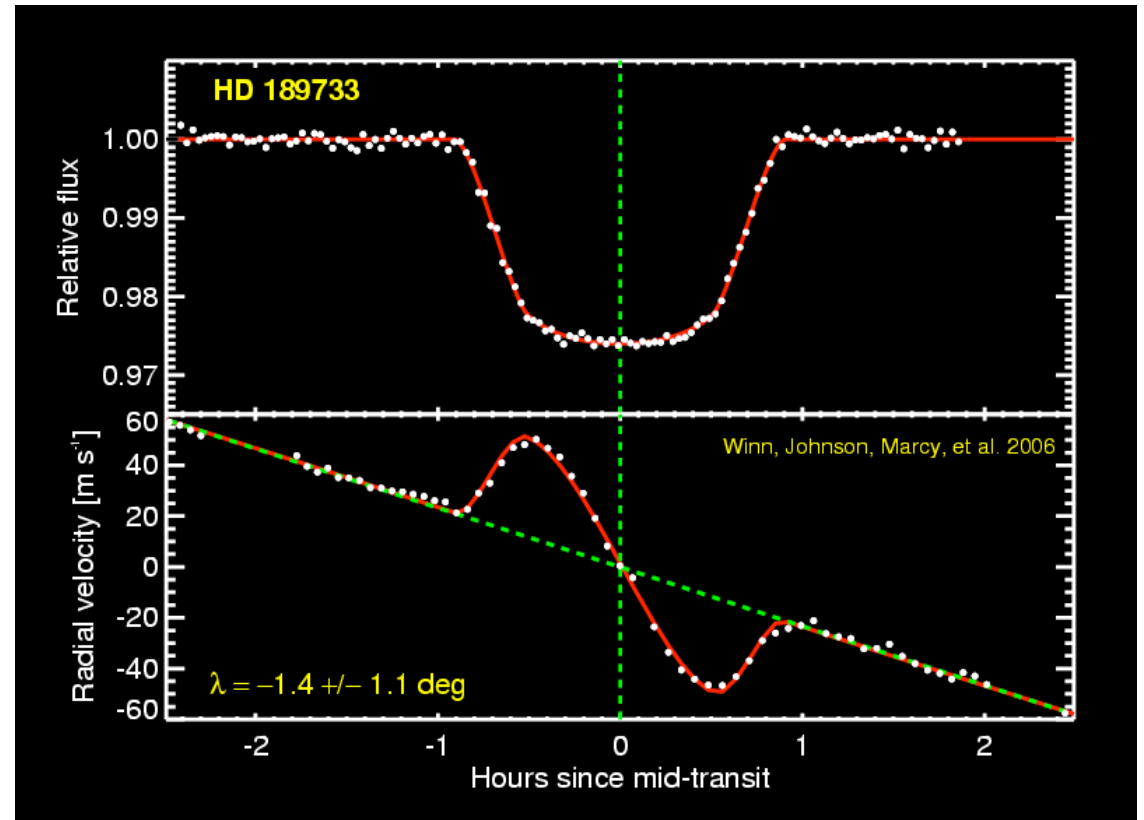
Total S/N

$$\frac{S}{N} \approx Q_R \left[\frac{1}{3} (1 - 4b^2) \cos^2 \lambda + b^2 \right]^{1/2}$$

where

$$Q_R = \frac{\sqrt{N}}{\sigma} K_R$$

$$\frac{S}{N} \approx 50$$



Measurement Uncertainties

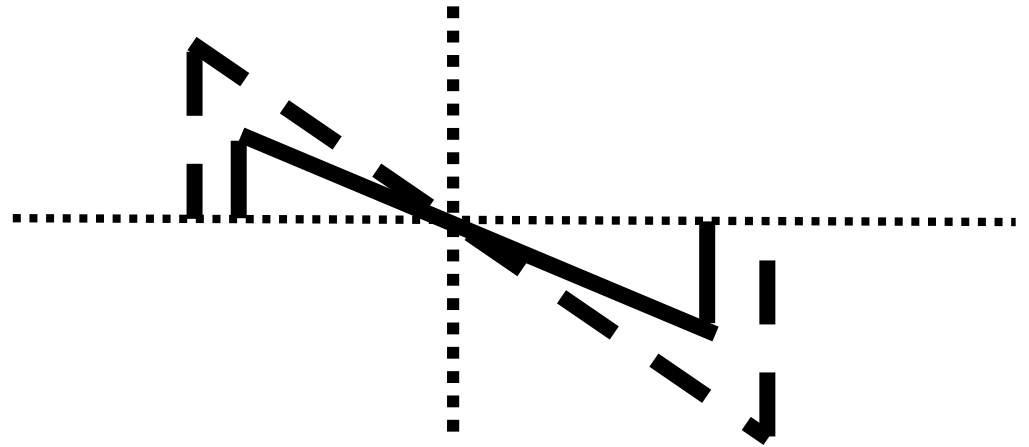
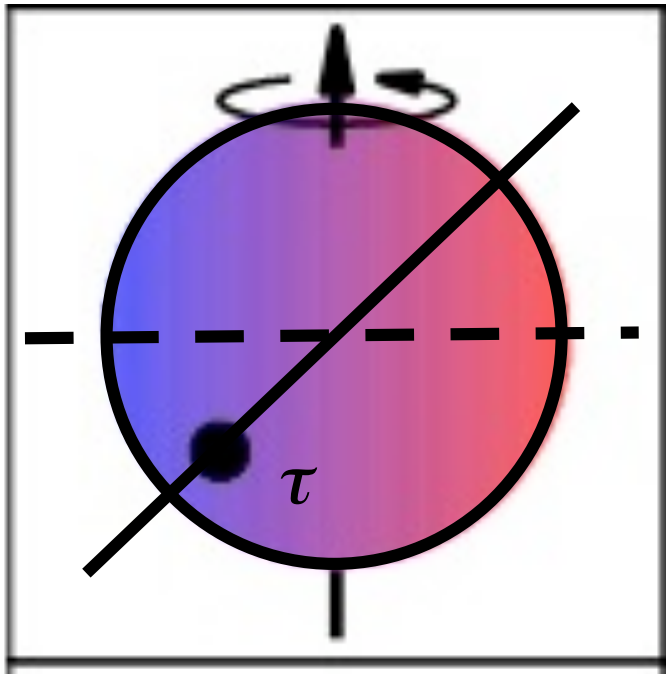
$$\sigma_{\lambda} \approx Q_R^{-1} \left[\frac{(1 - b^2) \cos^2 \lambda + 3b^2 \sin^2 \lambda}{b^2 (1 - b^2)} \right]^{1/2}$$

Gaudi &
Winn (2007)

$$\frac{\sigma_{V_* \sin I}}{V_* \sin I} \approx Q_R^{-1} \left[\frac{(1 - b^2) \sin^2 \lambda + 3b^2 \cos^2 \lambda}{b^2 (1 - b^2)} \right]^{1/2}$$

Useful for estimating expected uncertainties

Central Transits are bad:



$$V_R = K_R (\tau \cos \lambda - b \sin \lambda) \rightarrow [K_R \cos \lambda] \tau$$

λ is degenerate with $V_* \sin I$

Why Measure the
Rossiter-McLaughlin
Effect?

Spin-orbit alignment for exoplanets

Spin-orbit alignment for exoplanets

- Solar system: alignment is within $\sim 10^\circ$

Spin-orbit alignment for exoplanets

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- How common or unusual is this?

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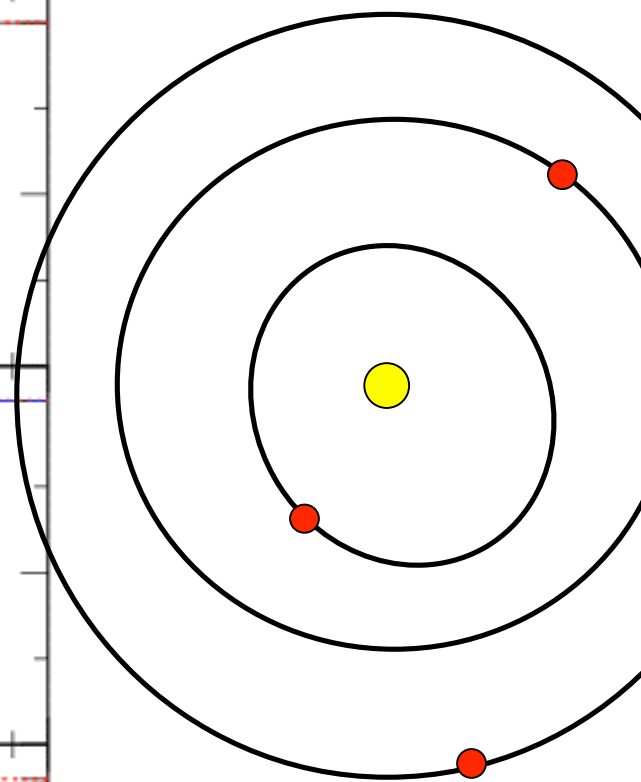
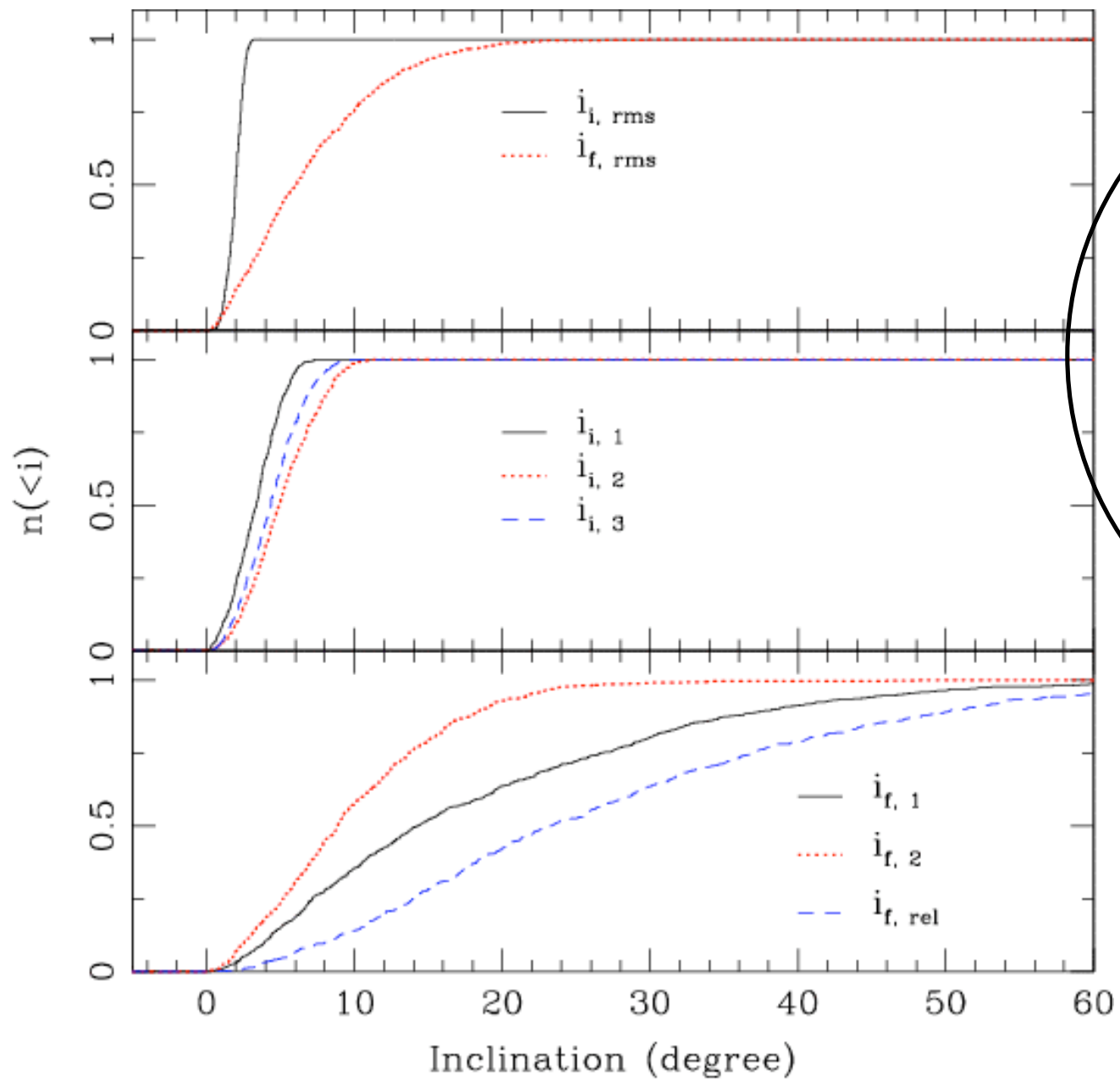
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Spin-orbit alignment for exoplanets

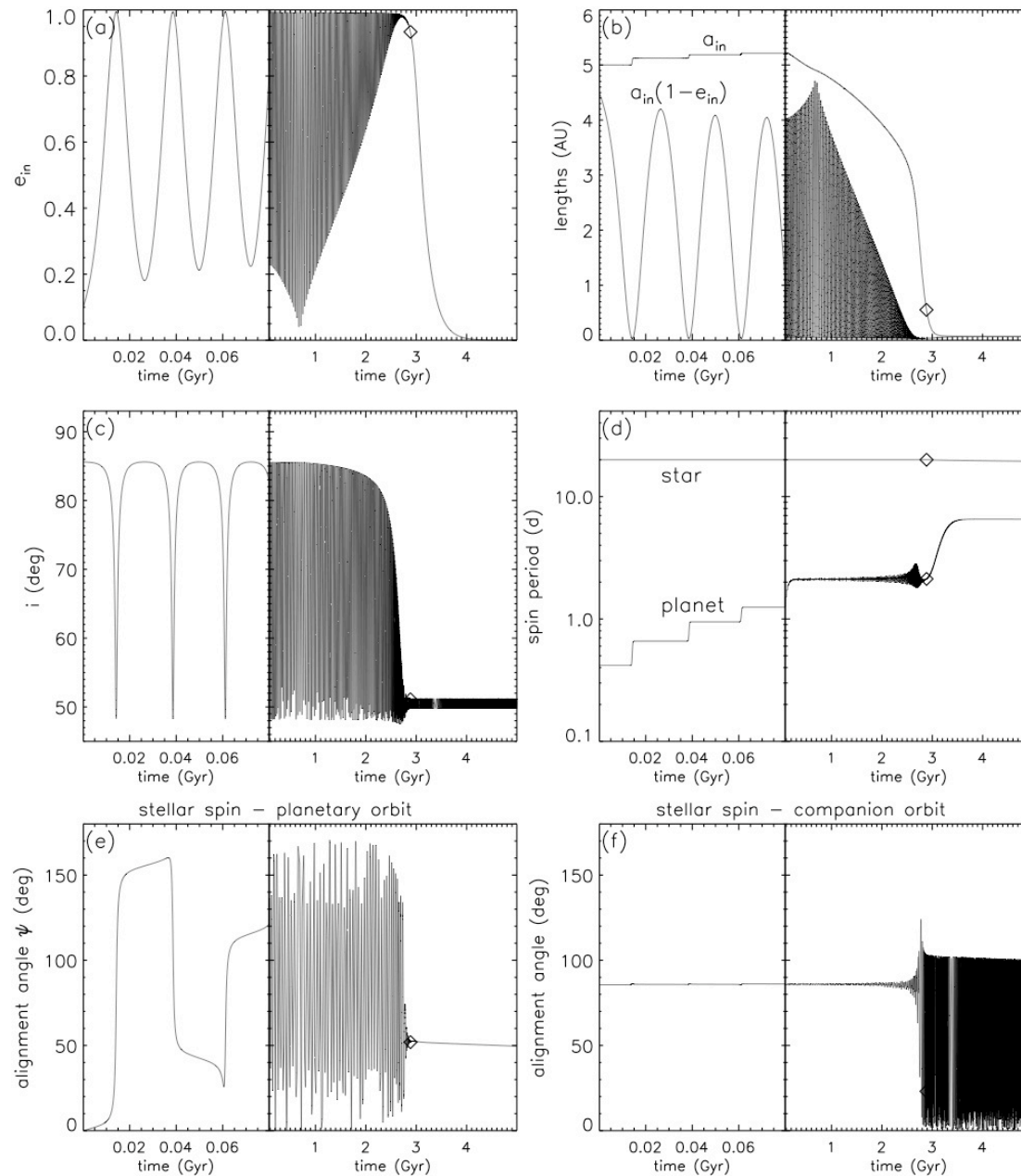
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 - Migration (disk interaction *v.* scattering, Kozai)

Planet-Planet Scattering



Chatterjee, Ford,
& Rasio (2007)

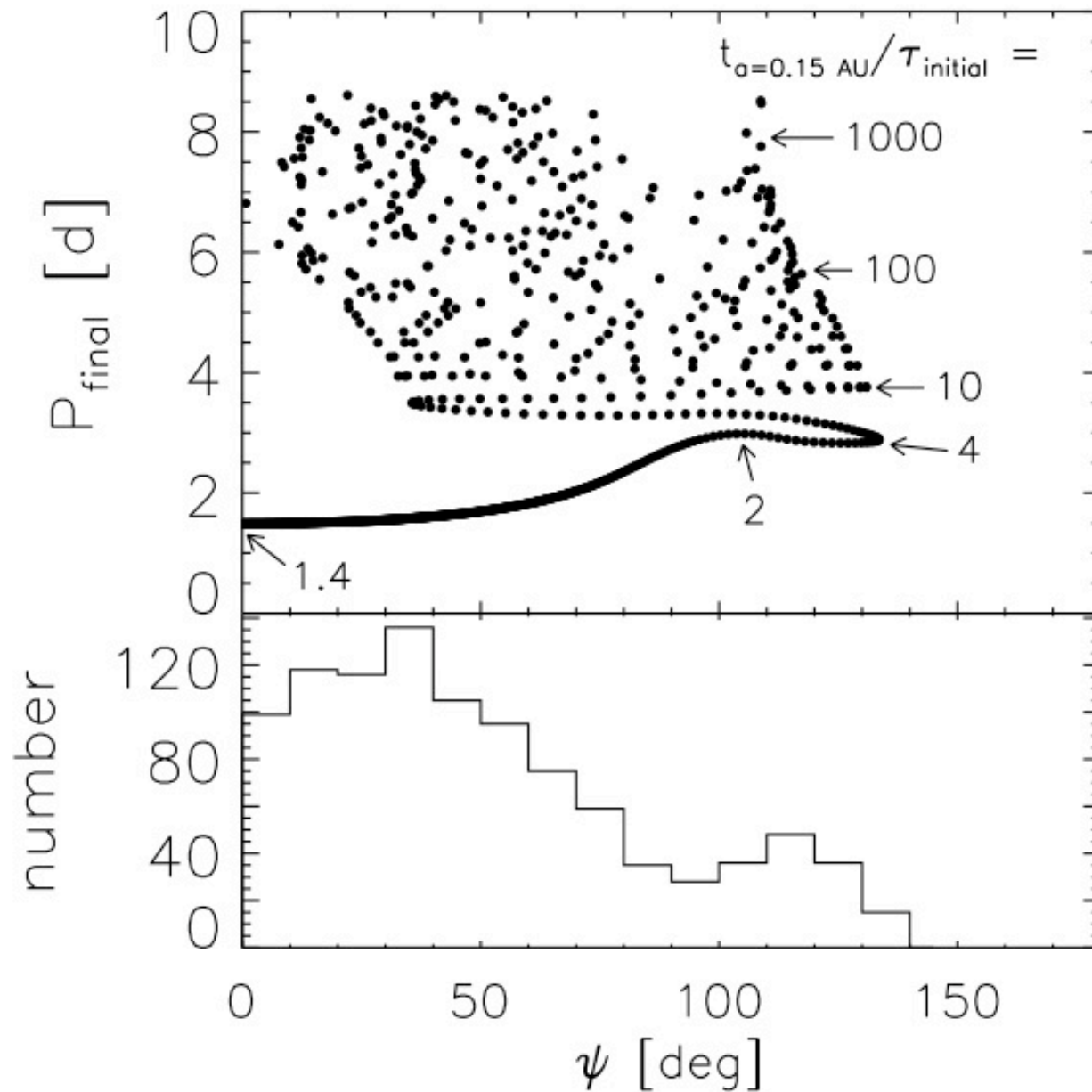
Kozai Oscillations with Tides



Fabrycky
& Tremaine (2007)

Wu et al (2007)

Kozai Oscillations with Tides



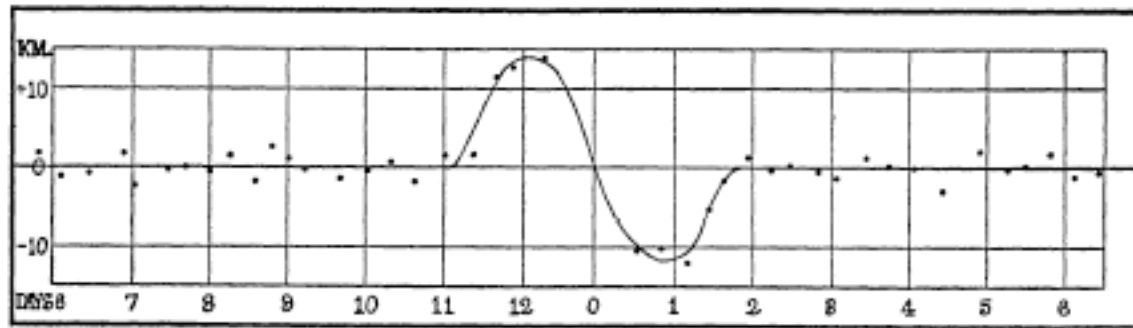
Spin-orbit alignment for exoplanets

- Solar system: alignment is within $\sim 10^\circ$
- How common or unusual is this?
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 - Migration (disk interaction v. scattering, Kozai)
- Fundamental measurement

Measurements of the
Rossiter-McLaughlin
Effect



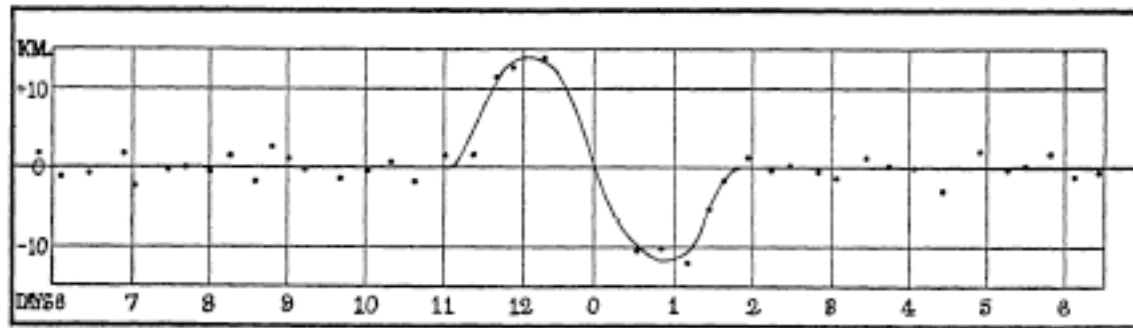
R. A. Rossiter
(1896-1977)



β Lyrae: Rossiter 1924, ApJ, 60, 15



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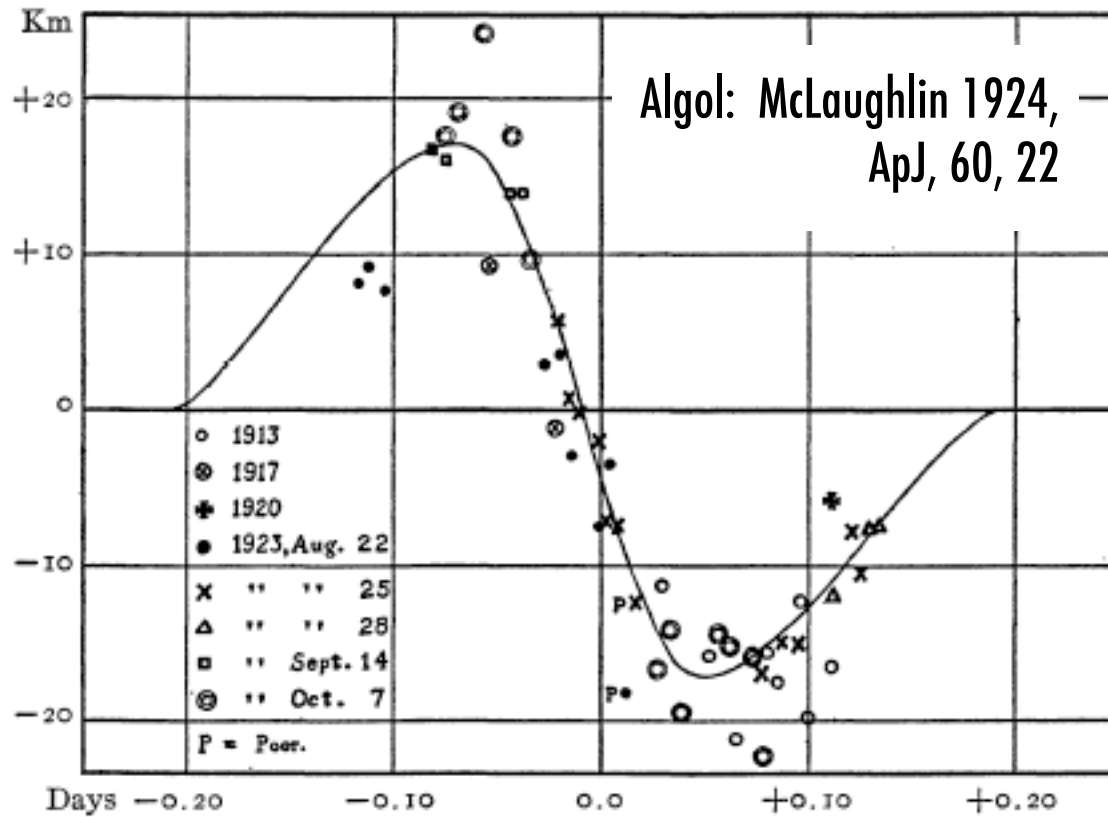
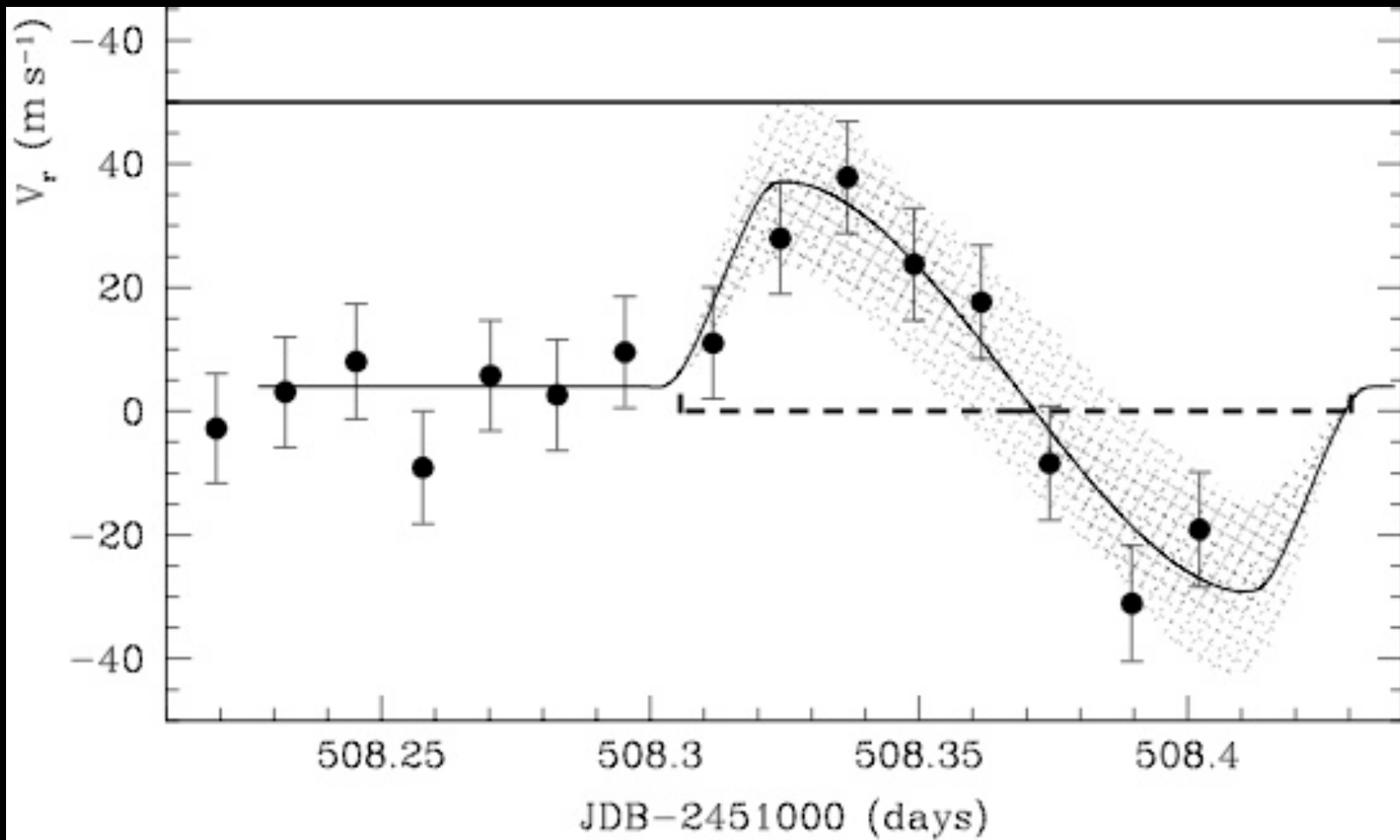


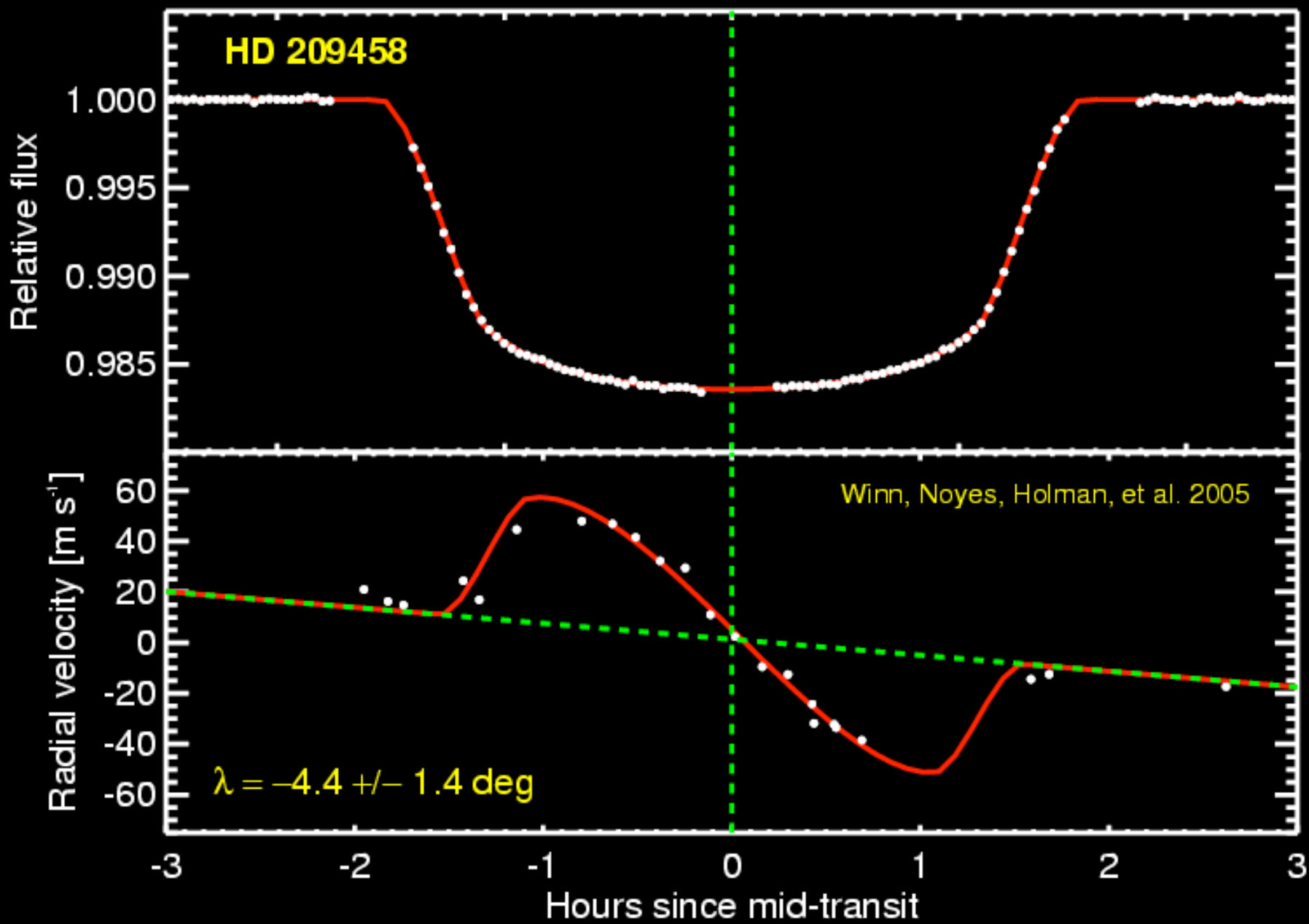
FIG. 1.—Curve of the rotational effect in Algol

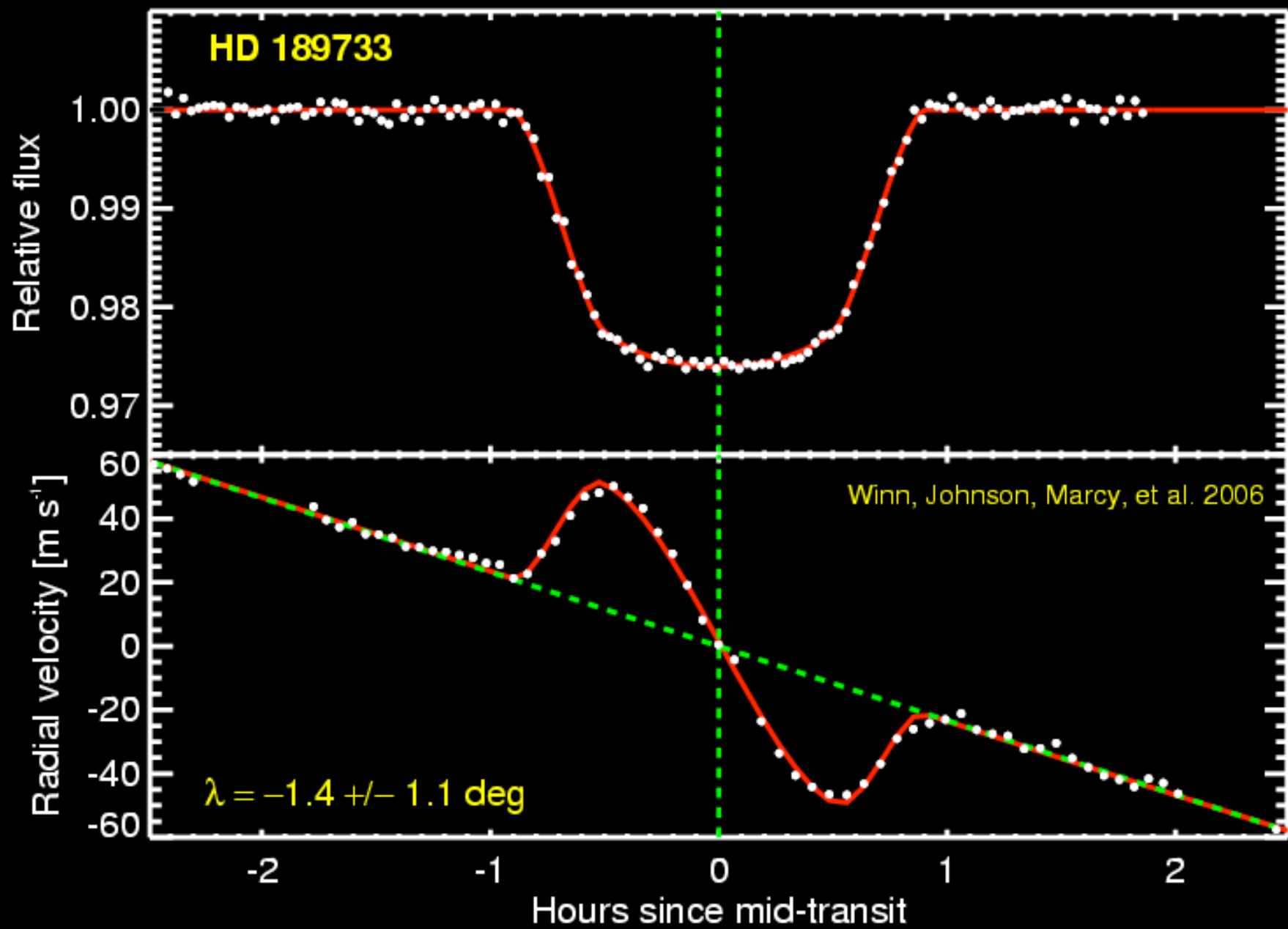


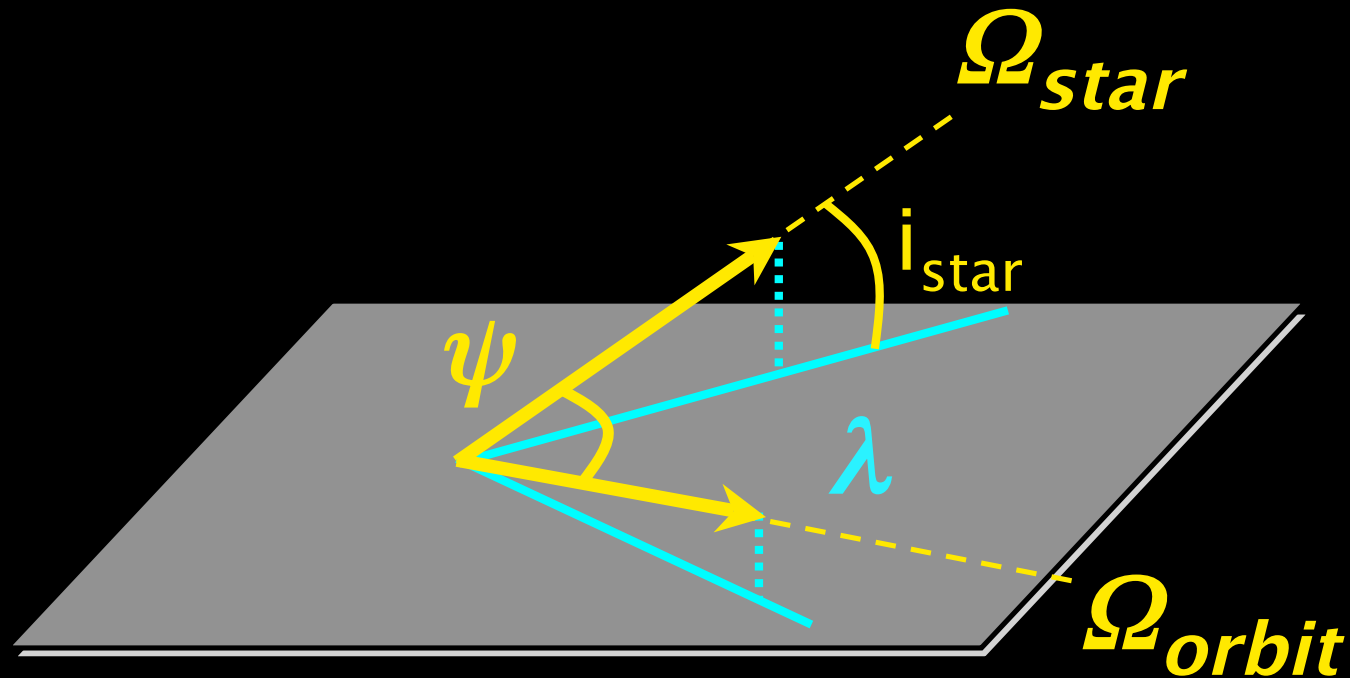
R. A. Rossiter
(1896-1977)



Queloz et al 2000







$$\lambda = -1.1 \pm 1.4 \text{ deg (RM effect)}$$

$$\sin i_{\text{star}} = [v \sin i_{\text{star}}] / (2\pi R/P)$$

$$\psi < 27 \text{ deg (95\% conf.)}$$

HD 147506 = HAT-P-2

Bakos et al. (2007)

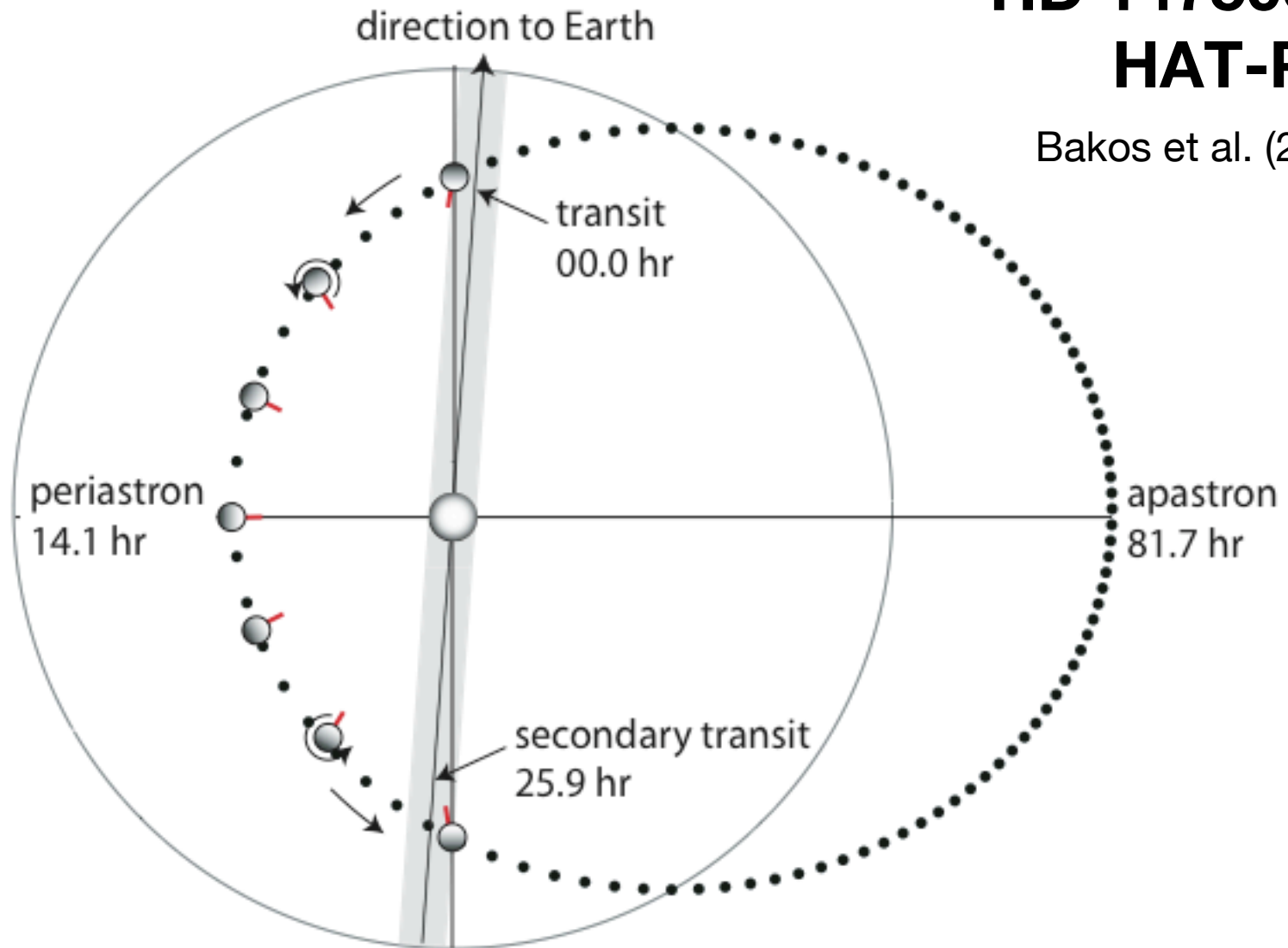
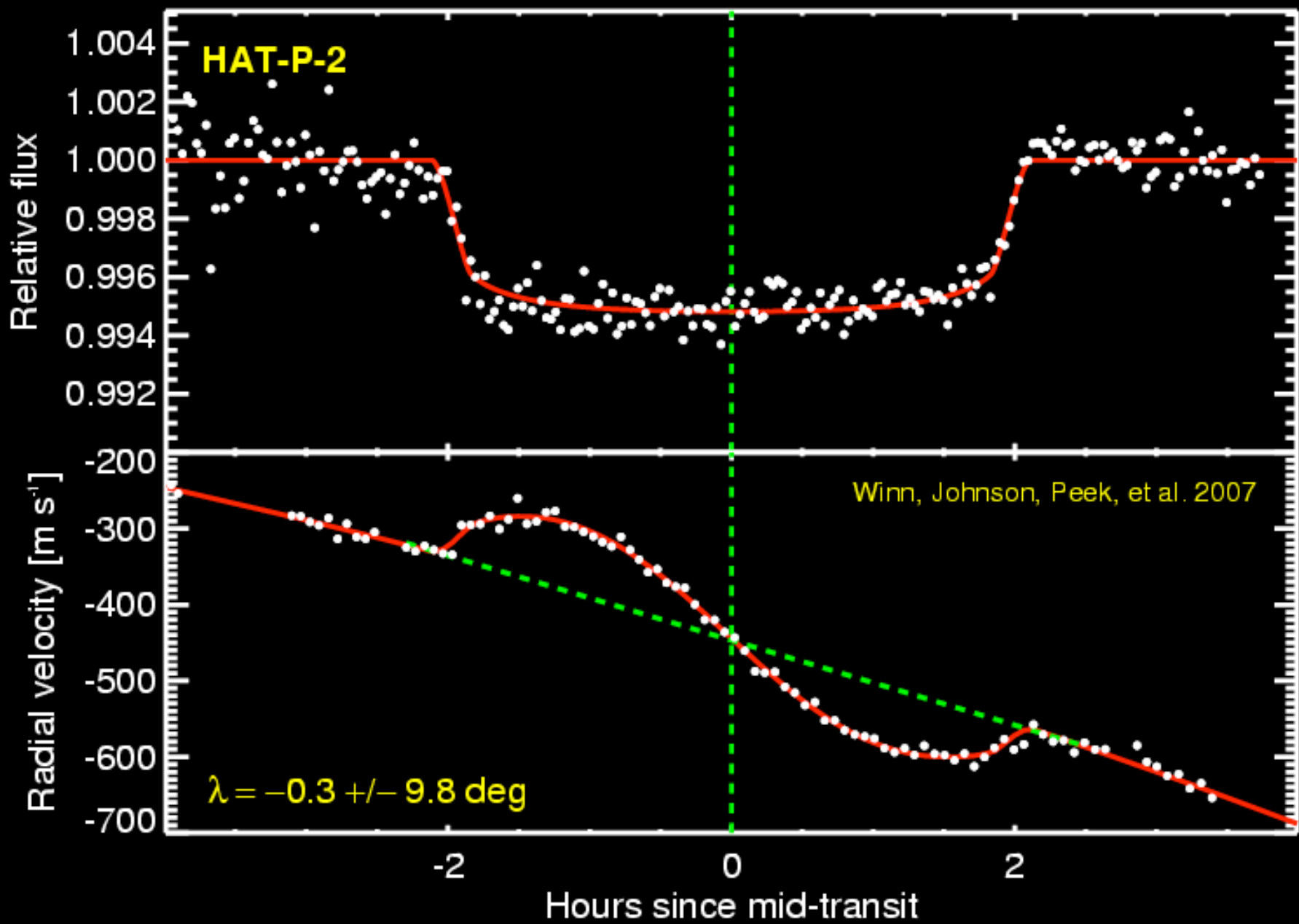
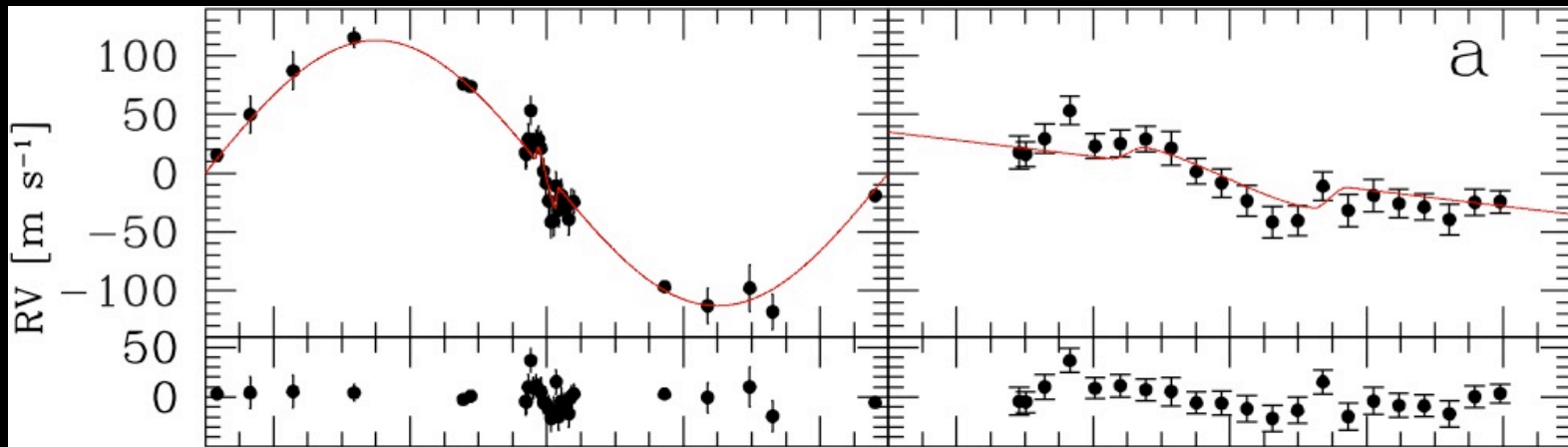
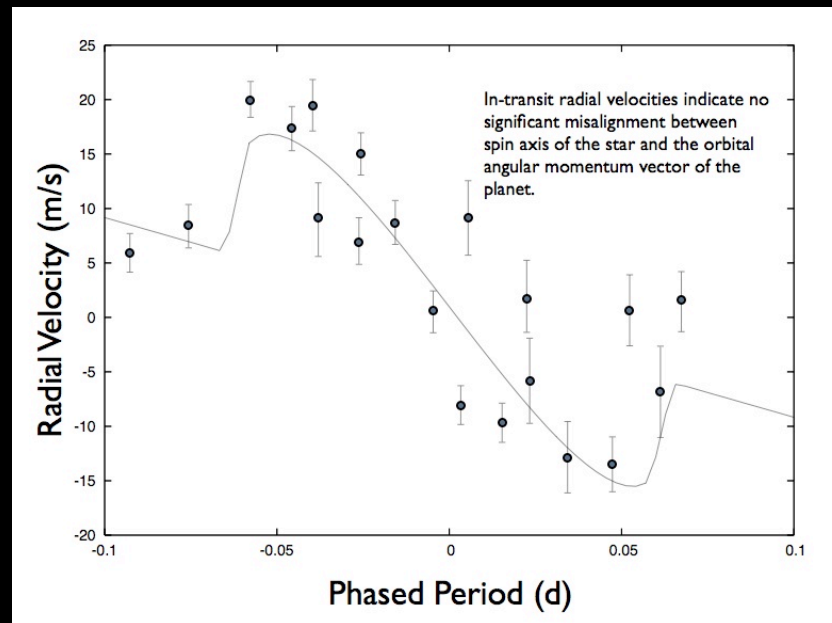


Diagram by G. Laughlin





TrES-I: $\lambda = 30^\circ \pm 21^\circ$ (Narita et al 2007)



HD 149026: $\lambda = 12^\circ \pm 14^\circ$ (Wolf et al)

Spin-orbit alignment for exoplanets

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- Random alignments ruled out (>99.9% CL)

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$$\tau \sim \frac{4\pi r_g^2 Q_S}{3k} \frac{R_S^3}{GM_S P} \left(\frac{M_S}{M_P}\right)^2 \left(\frac{a}{R_S}\right)^6 \sim 5 \times 10^{12} \text{ yr}$$

Hut 1981; Queloz et al. 2000; Winn et al. 2005

Spin-orbit alignment for exoplanets

- Random alignments ruled out (>99.9% CL)
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Hut 1981; Queloz et al. 2000; Winn et al. 2005

- Migration generally preserves spin-orbit alignment?

Confirming Planets
Rossiter-McLaughlin
Effect

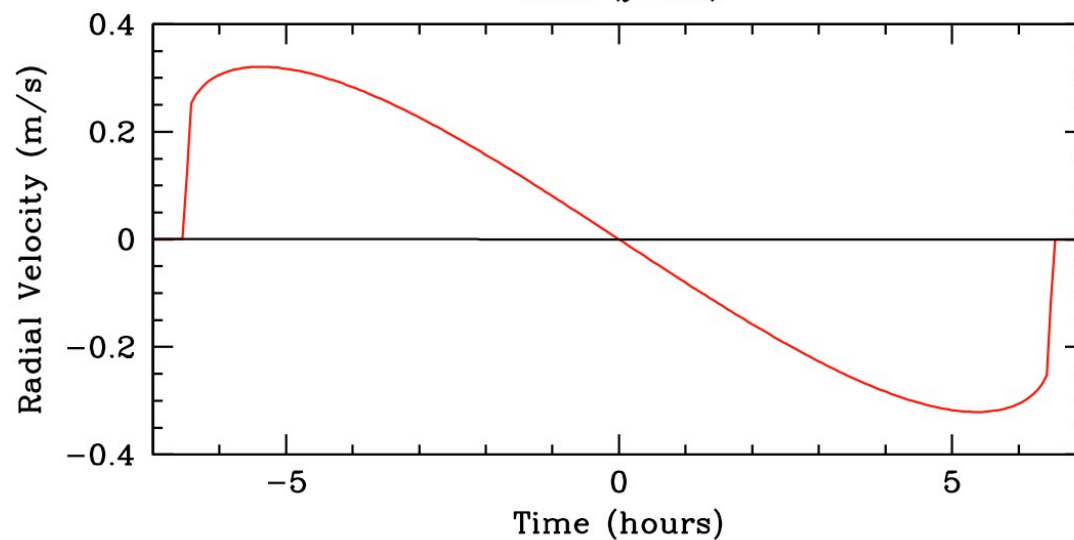
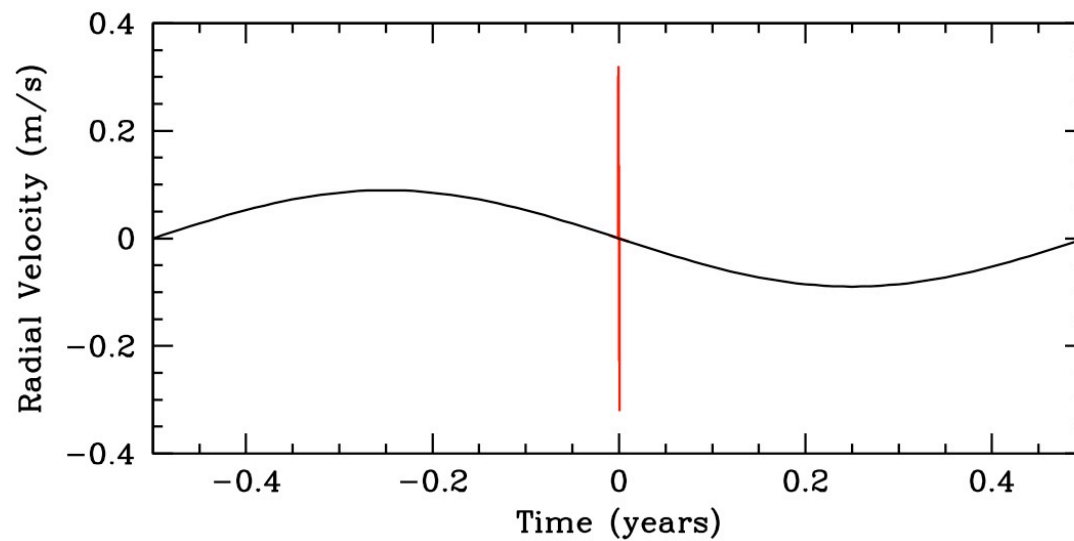
RM Effect Amplitude

$$\begin{aligned}\frac{K_R}{K_O} &\approx \left(\frac{P}{2\pi Gm} \right)^{1/3} V_* \sin I \\ &\approx 0.3 \left(\frac{m}{M_{Jup}} \right)^{-1/3} \left(\frac{P}{3 \text{ days}} \right)^{1/3} \left(\frac{V_* \sin I}{5 \text{ km/s}} \right)\end{aligned}$$

Doppler and RM amplitude of the same order for Hot Jupiters

Larger for less massive planets, or longer period planets

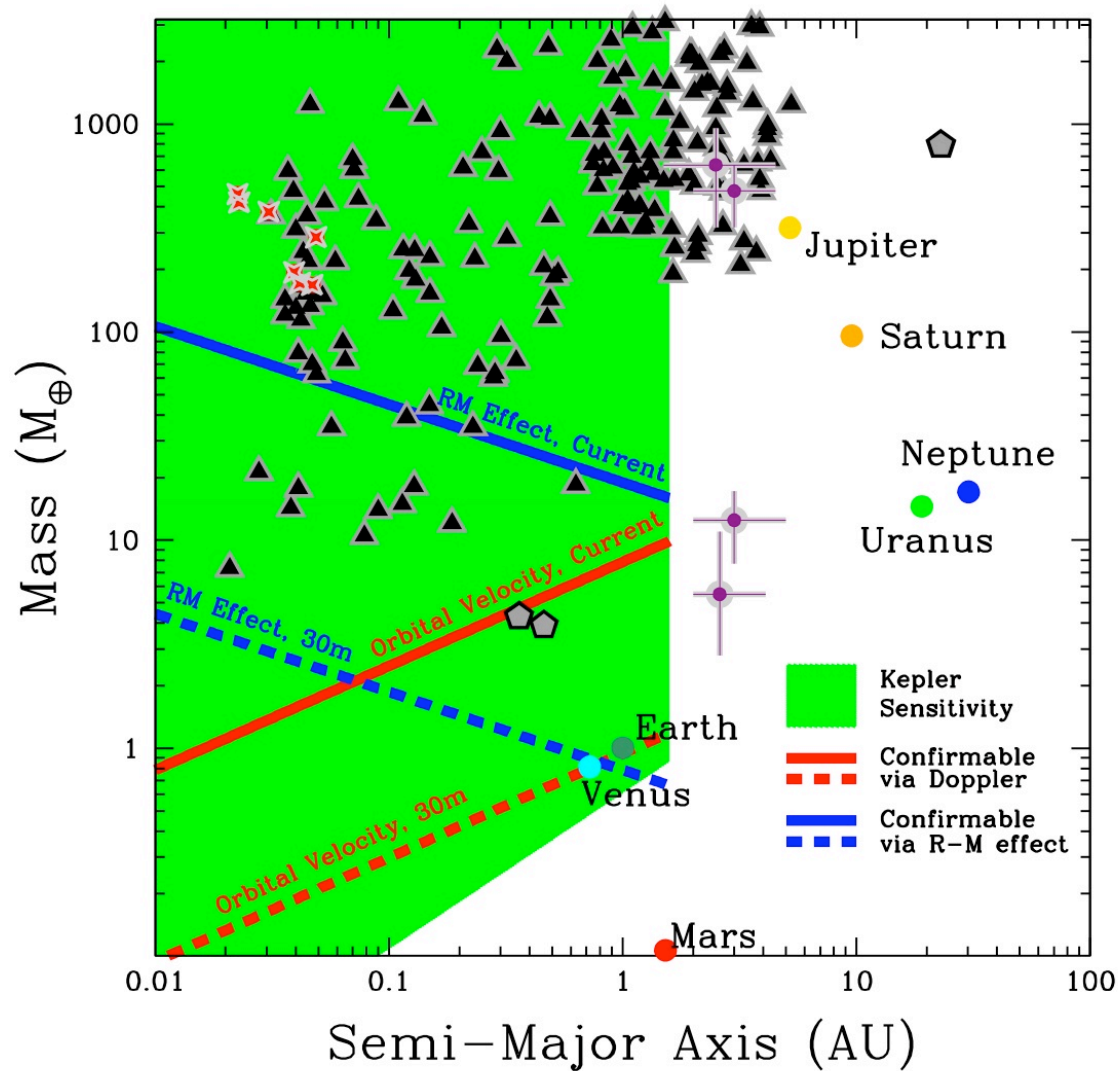
Earthlike Planet



Gaudi & Winn
(2007)

Welsh et al
(2004)

Confirming *Kepler* Detections



Gaudi &
Winn (2007)