

The Origin of Universality in the Inner Edges of Planetary Systems



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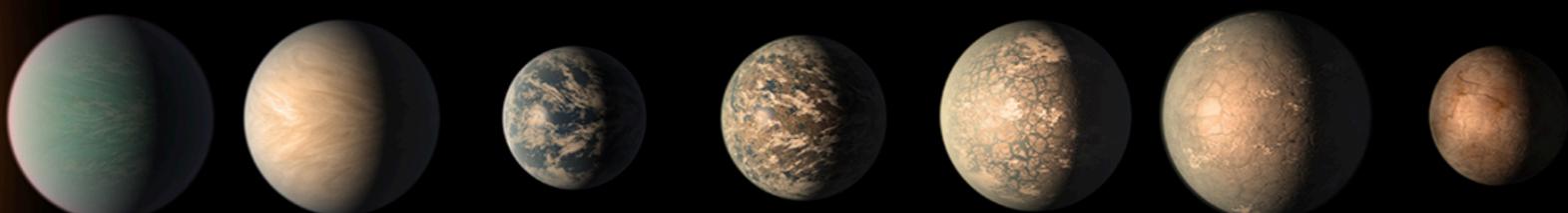
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Jupiter ($M \approx 0.001 M_{\text{sun}}$)



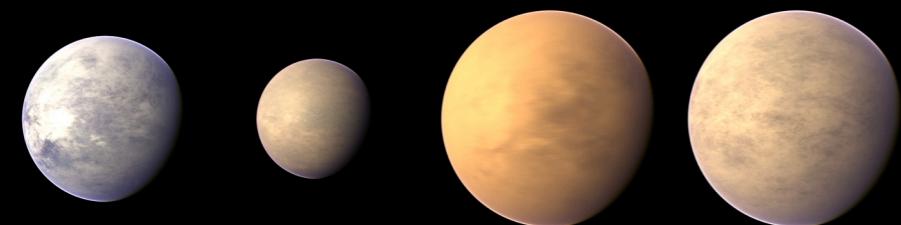
$P_{\text{Io}} \approx 1.8$ days

Trappist 1 ($M \approx 0.09 M_{\text{sun}}$)

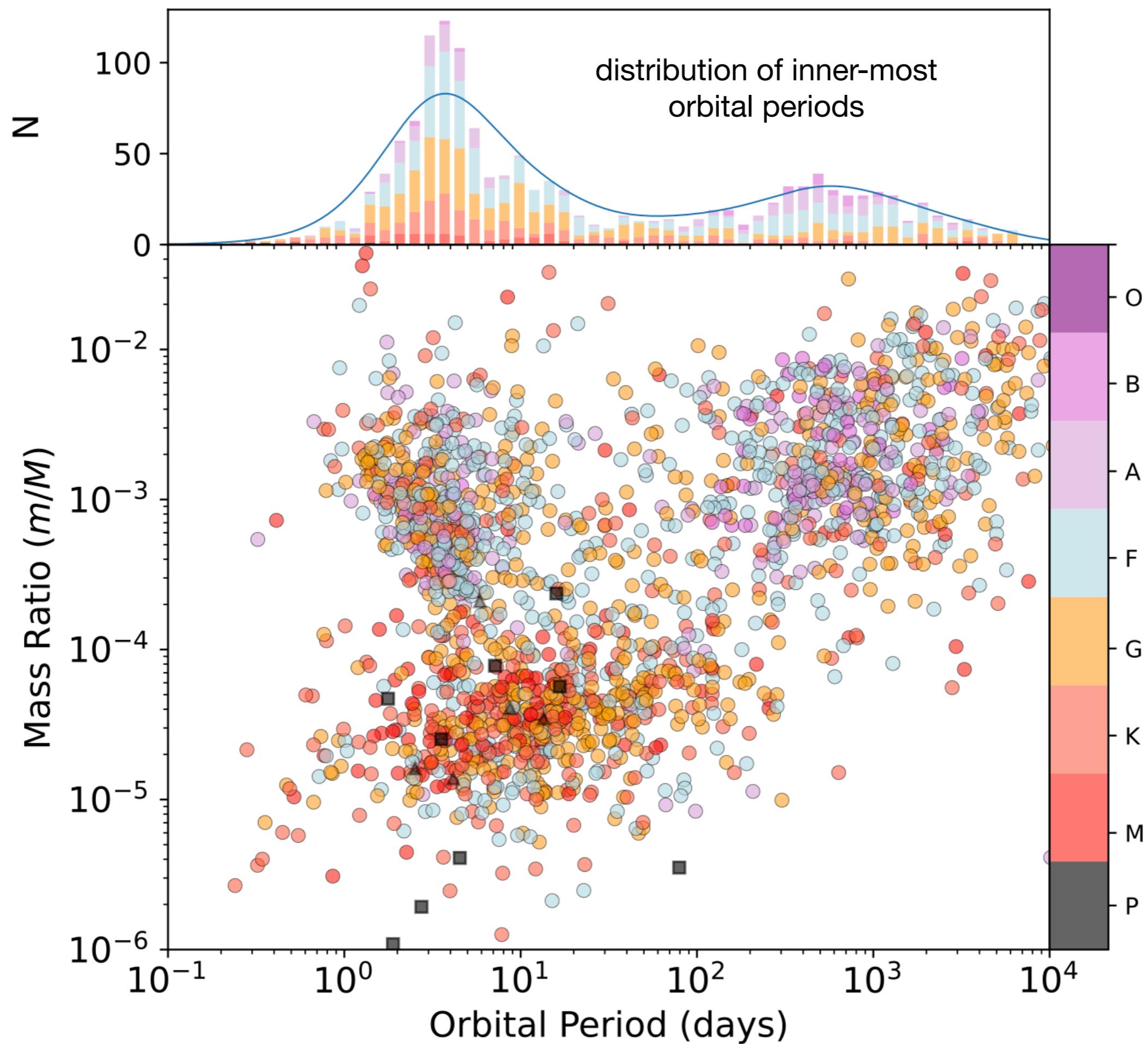


$P_b \approx 1.5$ days

Kepler 256 ($M \approx 1 M_{\text{sun}}$)



$P_b \approx 1.6$ days



Formation of rocky super-Earths from a narrow ring of planetesimals

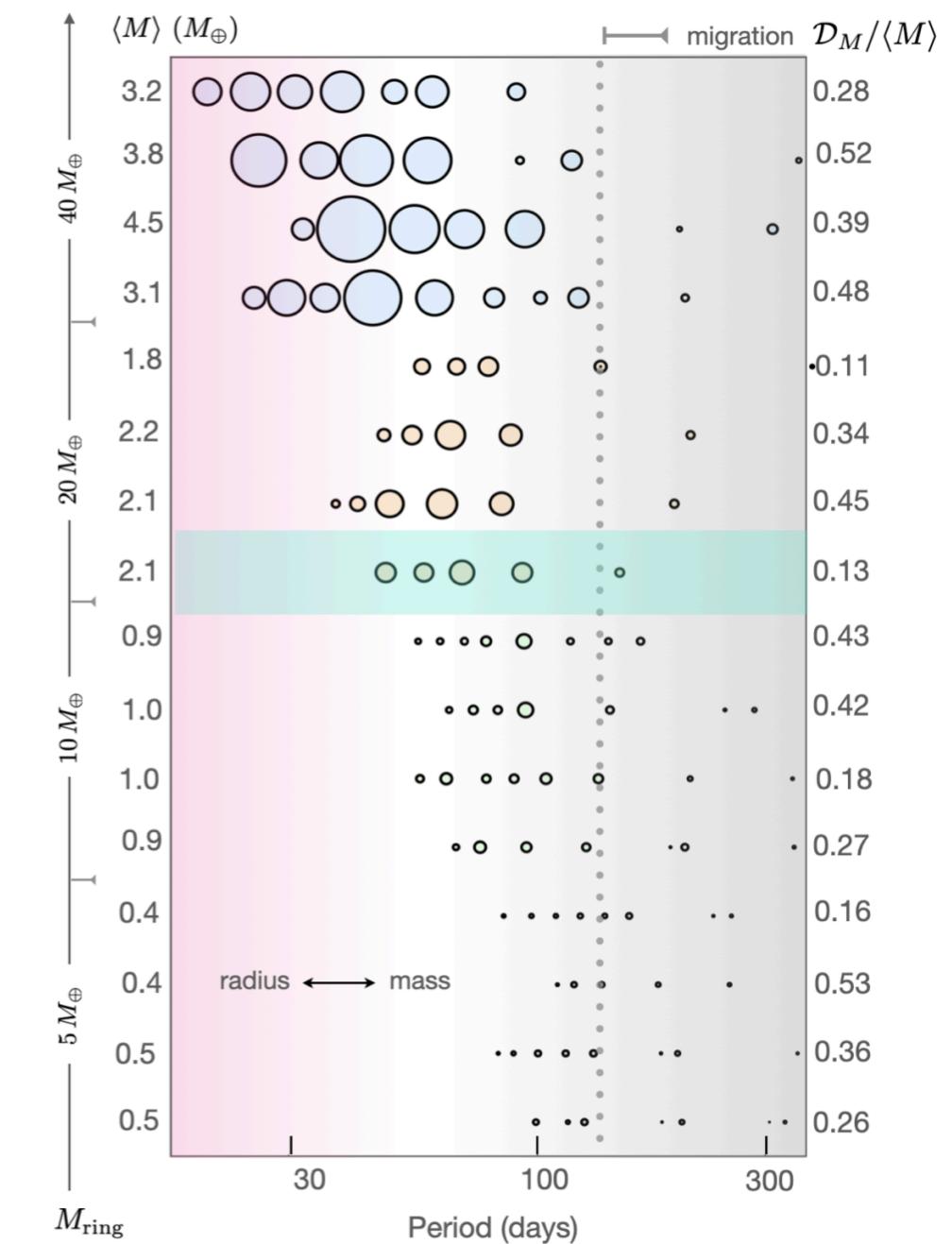
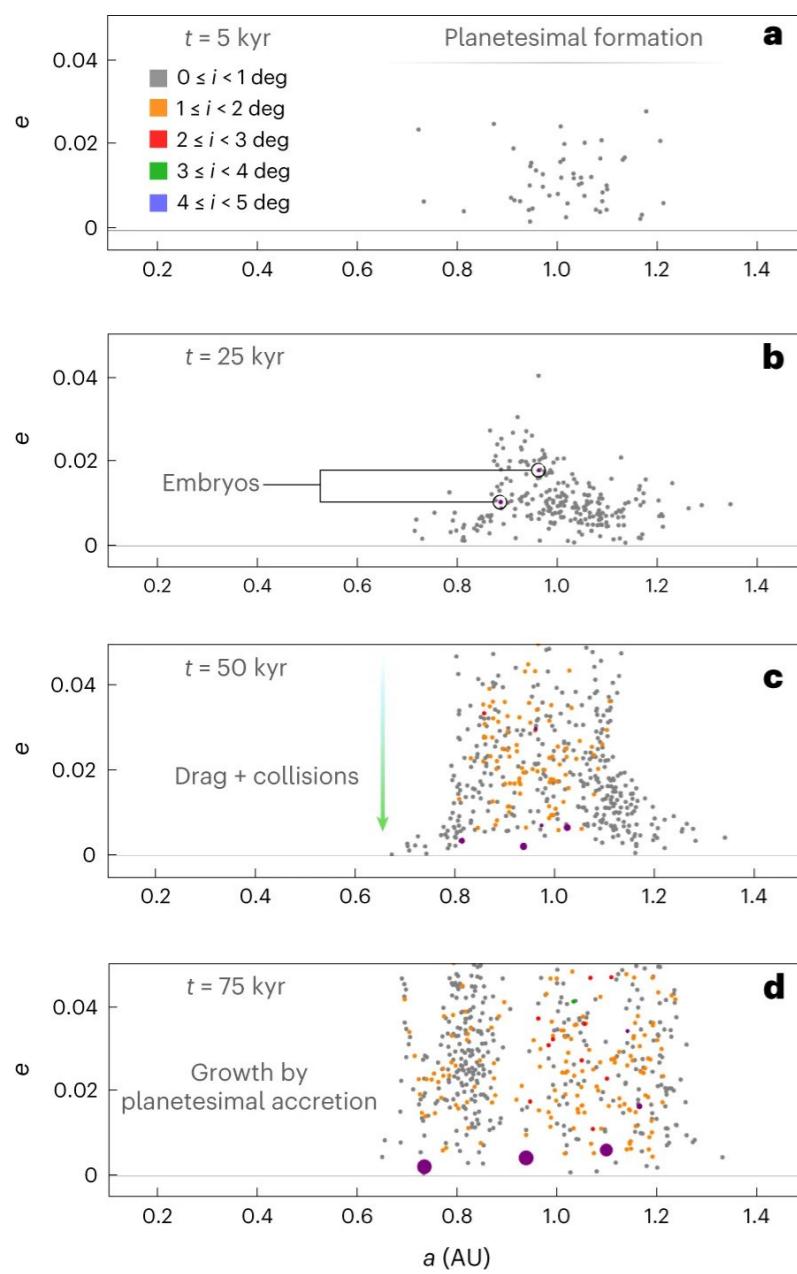
Konstantin Batygin & Alessandro Morbidelli *Nature Astronomy* 7, 330–338 (2023) | [Cite this article](#)

silicate-rich composition

intra-system uniformity

typical mass ~ few x Earth

link to Jup, Sol



Orbital migration delivers planets to the disk's inner edge, where they stabilize. Thus, at face-value, the data appears to suggest that disks are truncated at an orbital period of ~3 days, independent of the central mass...

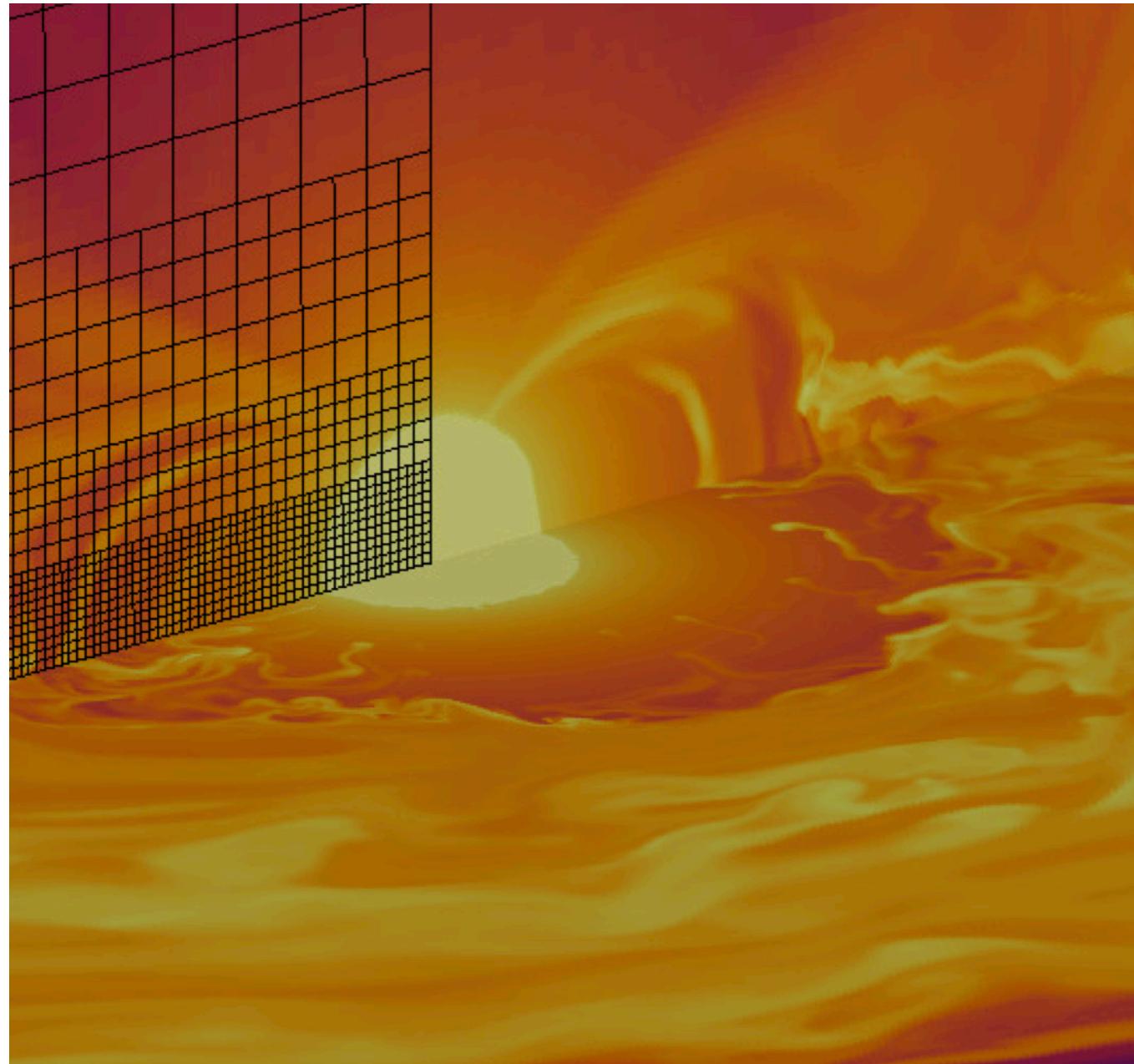


Fig. from Zhu et al (2023)

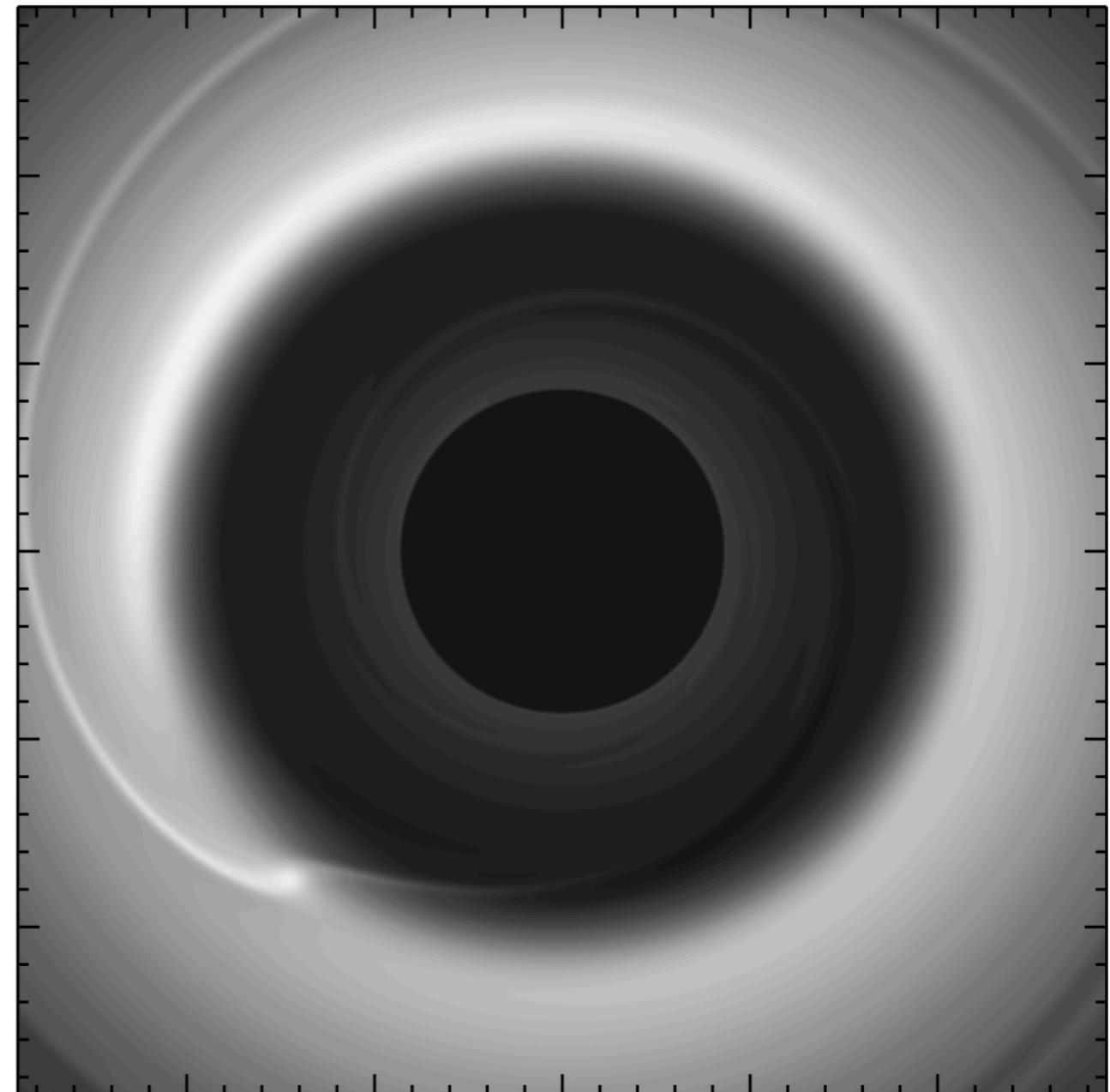
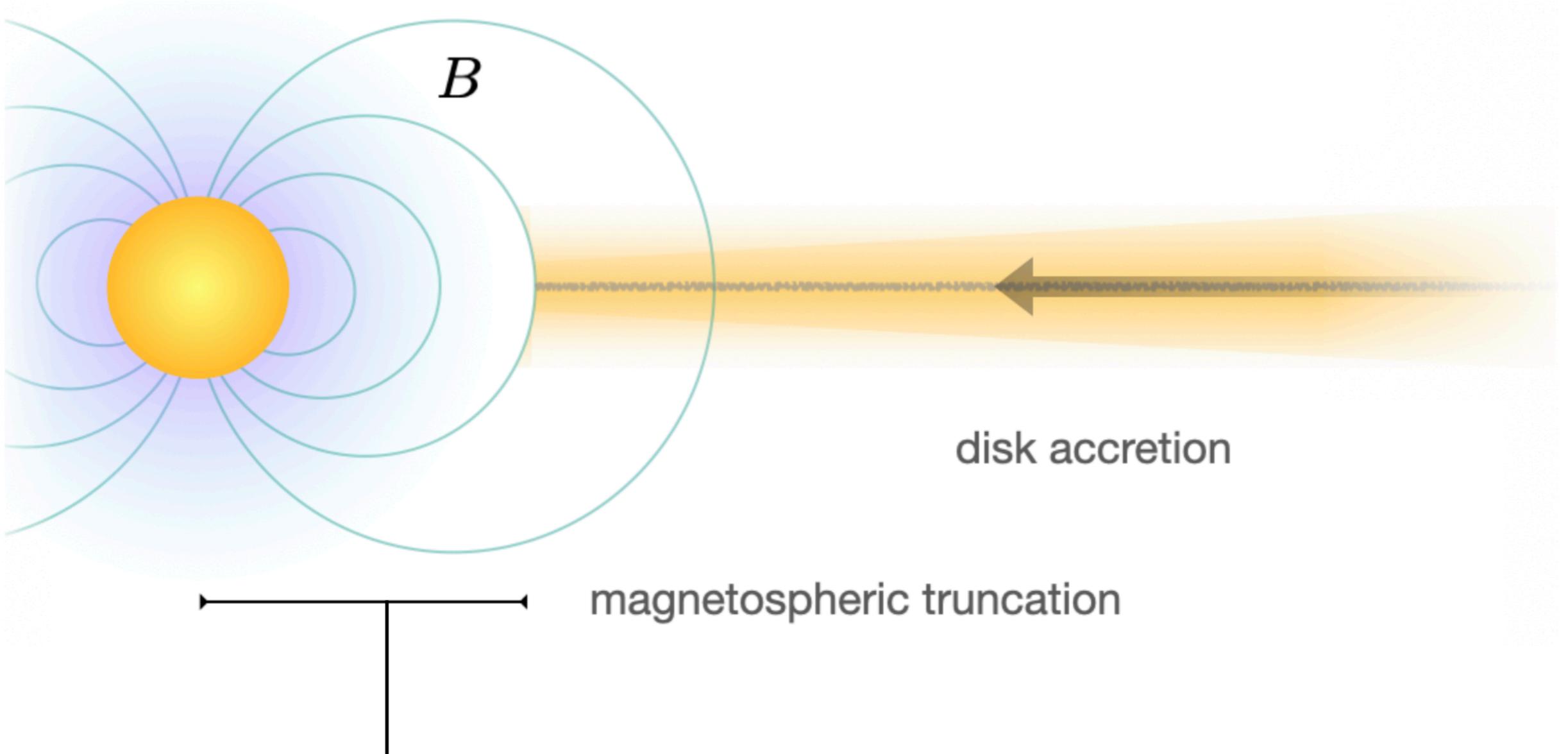
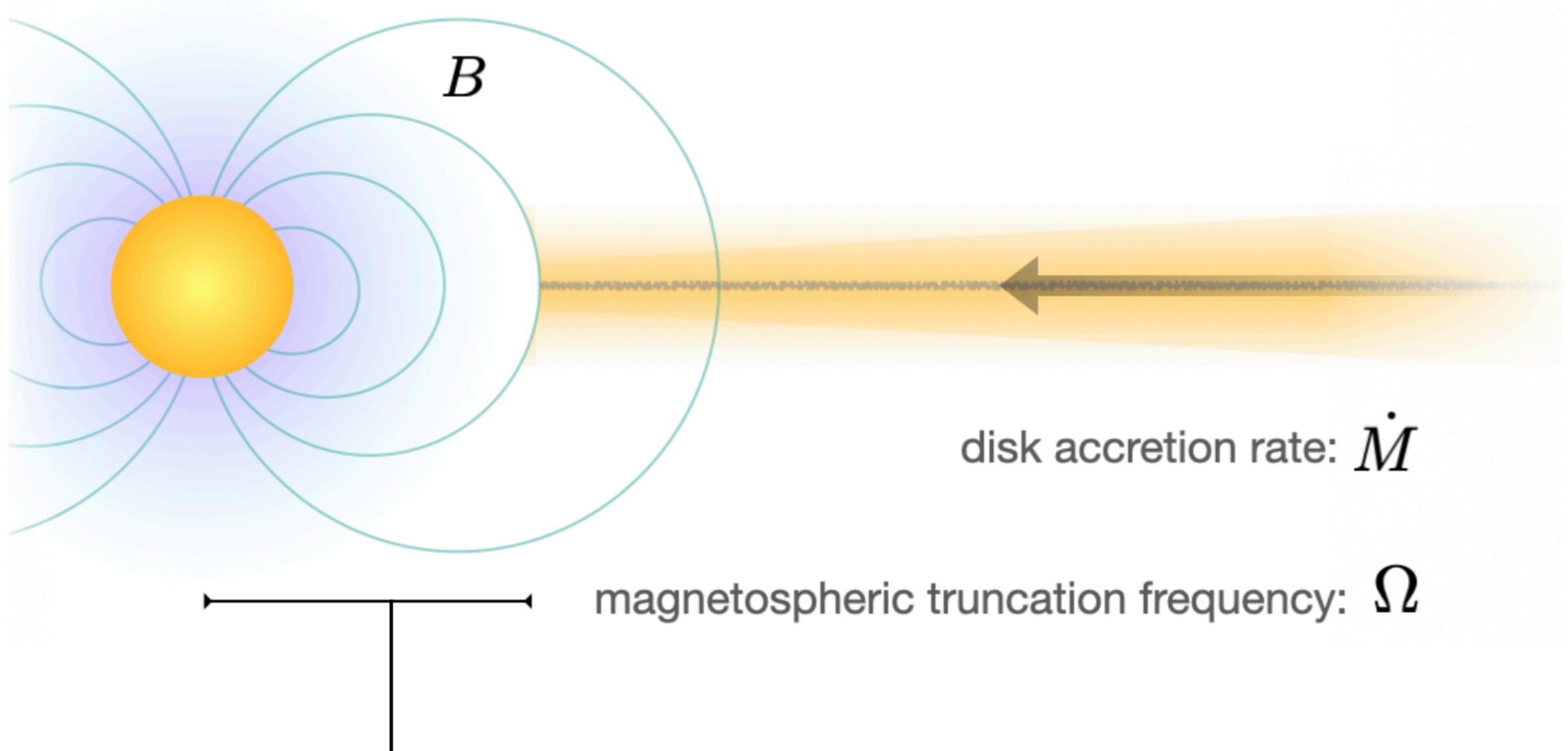


Fig. from Masset et al (2006)

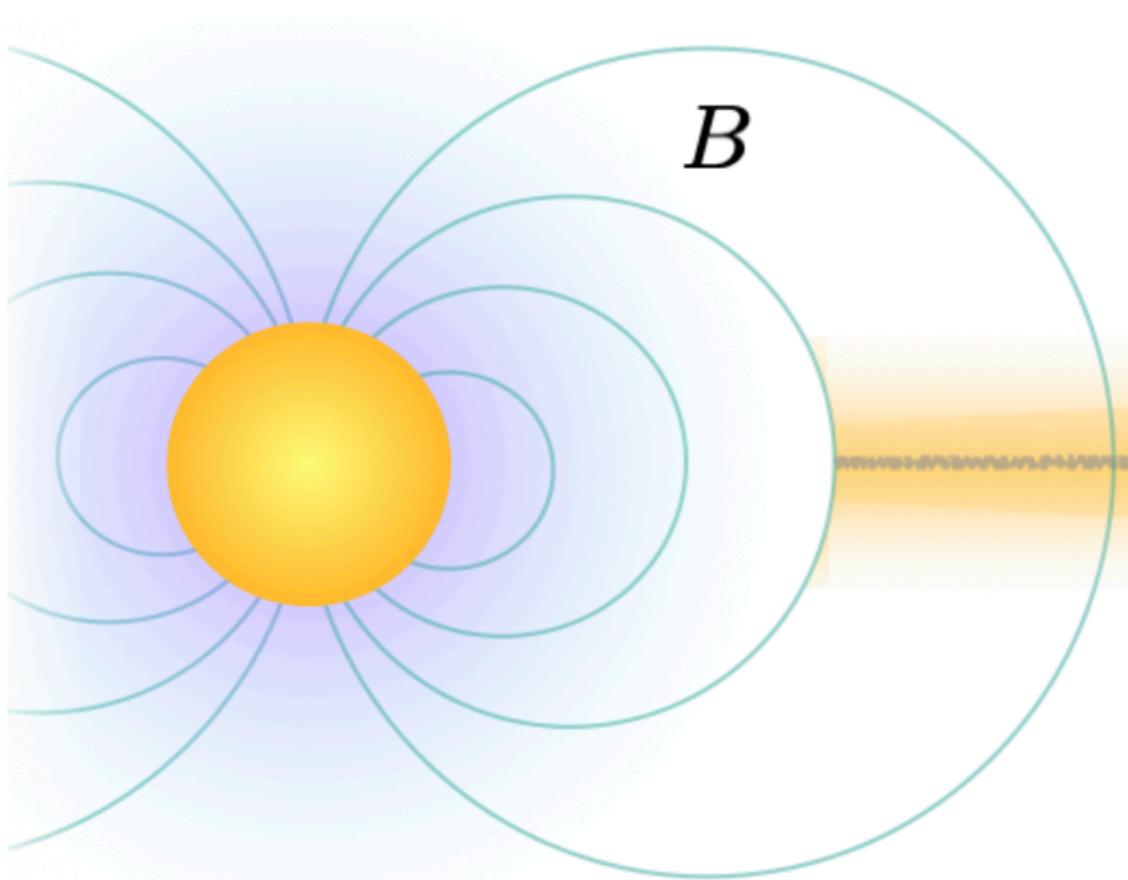


$$P_{\text{mag}} \sim P_{\text{ram}}$$

We need a theory that will connect stellar field (B),
radius (R), accretion rate (M -dot) etc.



$$\frac{B^2}{2\mu_0} \sim \frac{B_\star^2}{2\mu_0} \left(\frac{R_\star}{r} \right)^6 \sim \frac{\dot{M}}{4\pi r^2} \sqrt{\frac{2G M_\star}{r}}$$

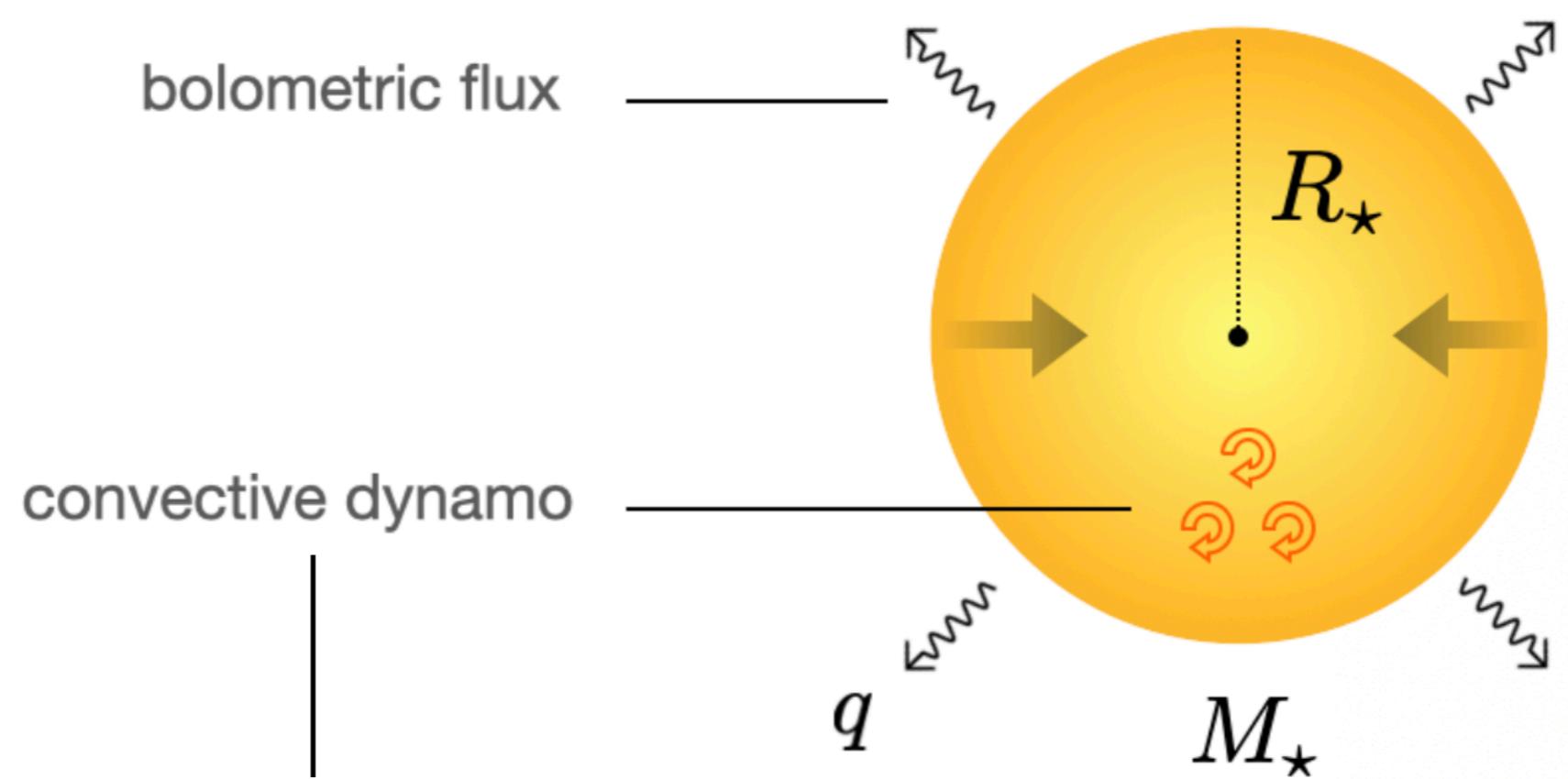


$$\dot{M} \sim \beta \frac{M_\star}{\tau}$$

disk accretion rate: \dot{M}

magnetospheric truncation frequency: Ω

$$\frac{B_\star^2}{2\mu_0} \left(\frac{R_\star}{r} \right)^6 \sim \frac{\dot{M}}{4\pi r^2} \sqrt{\frac{2\mathcal{G} M_\star}{r}}$$



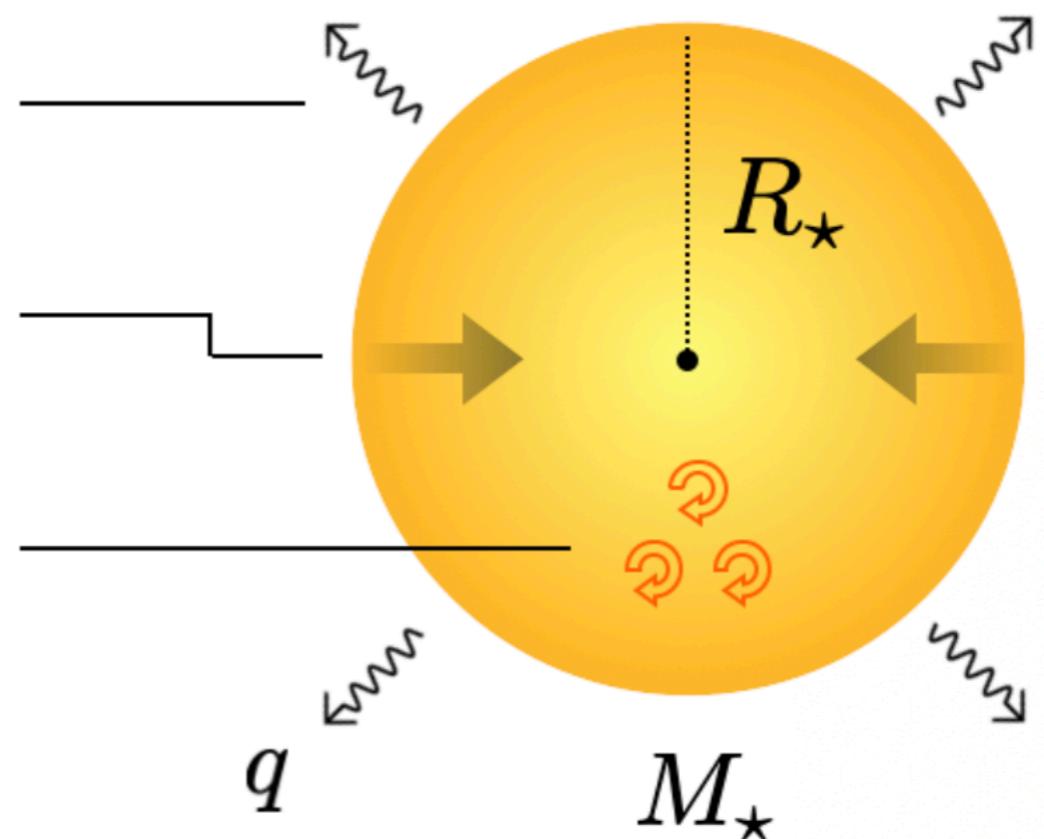
$$\frac{\langle B \rangle^2}{2\mu_0} \sim \rho v_{\text{conv}}^2 = c f_{\text{ohm}} \langle \rho \rangle^{1/3} (\mathcal{F} q)^{2/3}$$

$$R_\star \approx \left(\frac{b G M_\star^2}{12 \pi q \tau} \right)^{1/3}$$

bolometric flux
central body undergoing gravitational
(Kelvin-Helmholtz) contraction

convective dynamo

$$\frac{\langle B \rangle^2}{2 \mu_0} = c f_{\text{ohm}} \langle \rho \rangle^{1/3} (\mathcal{F} q)^{2/3}$$



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Received 2023 March 22; revised 2023 June 1; accepted 2023 June 2; published 2023 July 3

$$\Omega = 2 \xi \left[\frac{\sqrt{2}}{(3 b \mathcal{F})^2} \left(\frac{\pi \beta \gamma^2}{c f_{\text{ohm}}} \right)^3 \frac{(\mathcal{G} \langle \rho \rangle)^3}{\tau} \right]^{1/7}$$

$$\approx 2.4 \times 10^{-5} \text{ s}^{-1} \approx \frac{2 \pi}{3 \text{ day}}$$