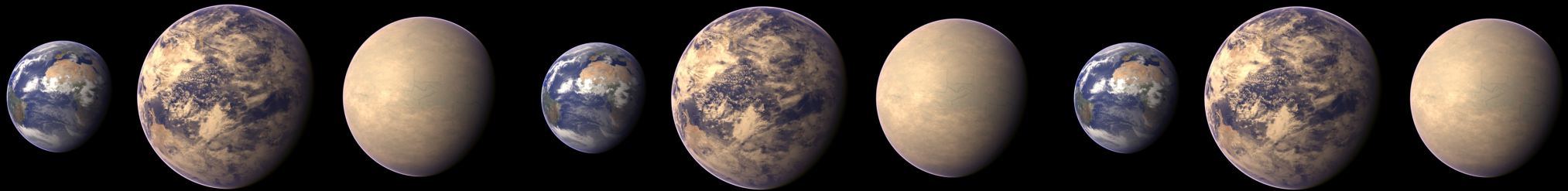


# The Microlensing-Transit Population Comparison:



## A Period-Dependent Mass-Radius Relation

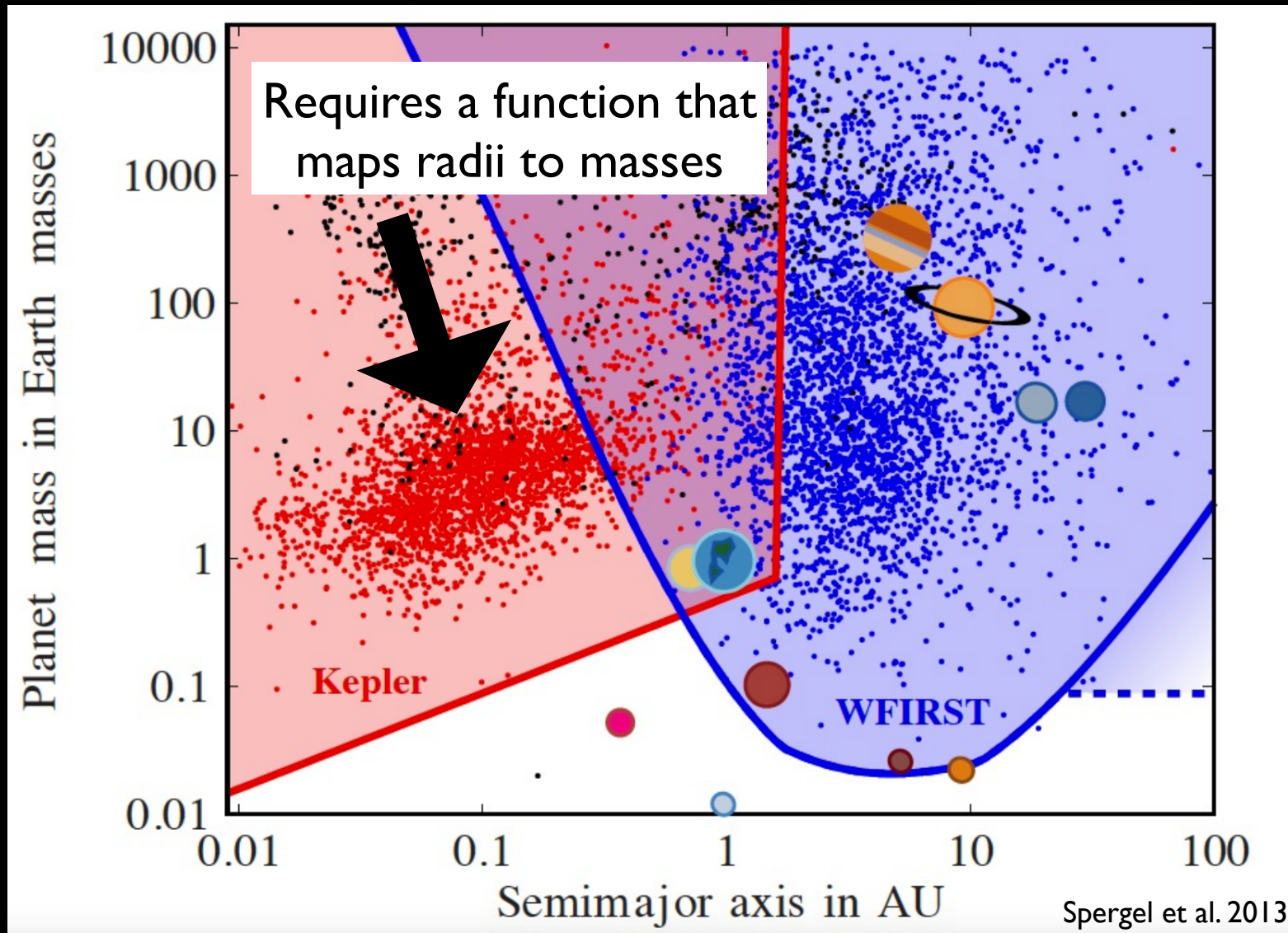
Angie Wolfgang

Penn State

NSF Postdoctoral Fellow

Eric Ford, Daniel Jontof-Hutter, Leslie Rogers, Eric Lopez

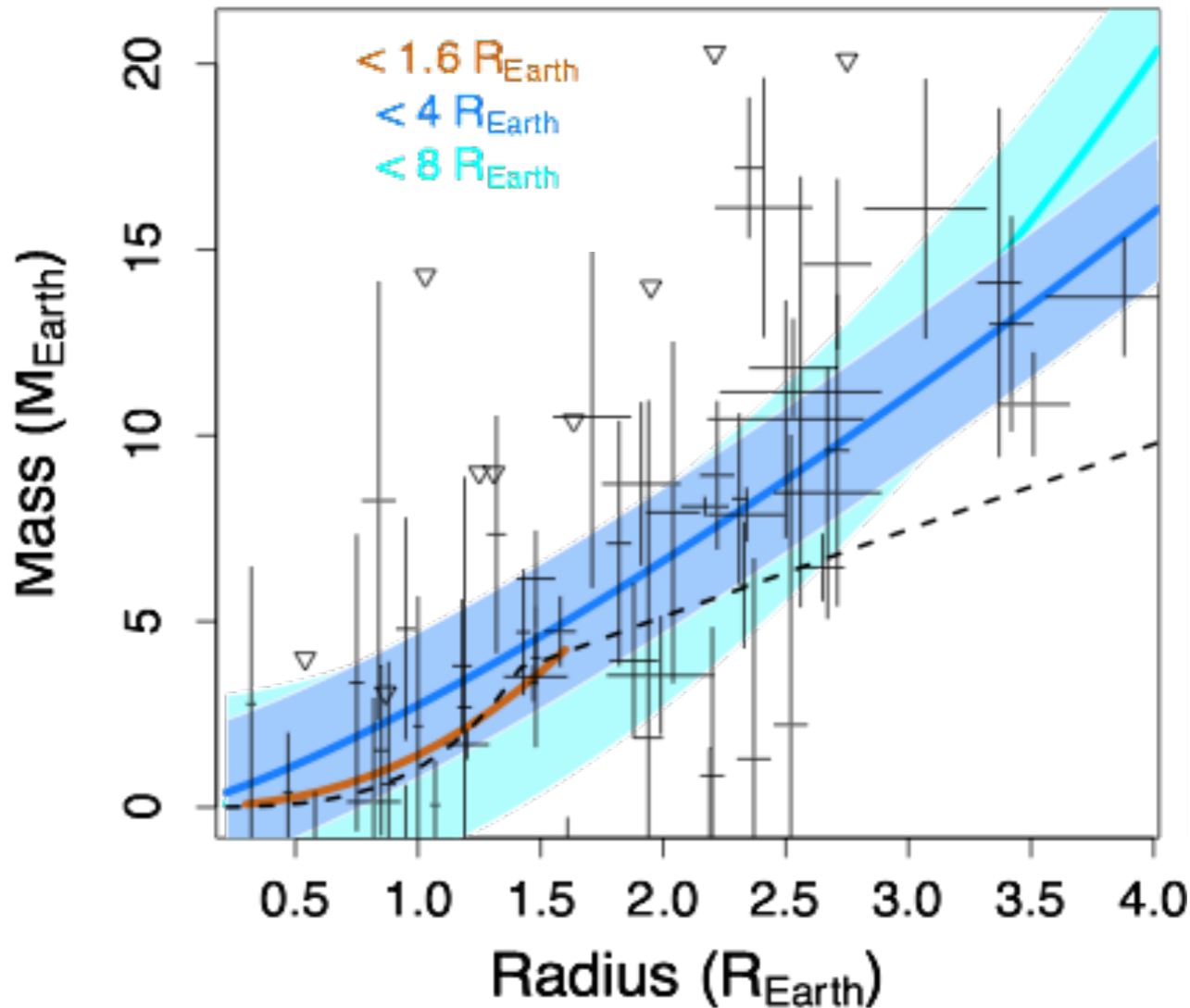
# To Complete the Planet Census:



To compare microlensing yields to transits,  
need period-dependent mass-radius relation!

# Observed M-R “Relation”

Wolfgang, Rogers, & Ford, 2016

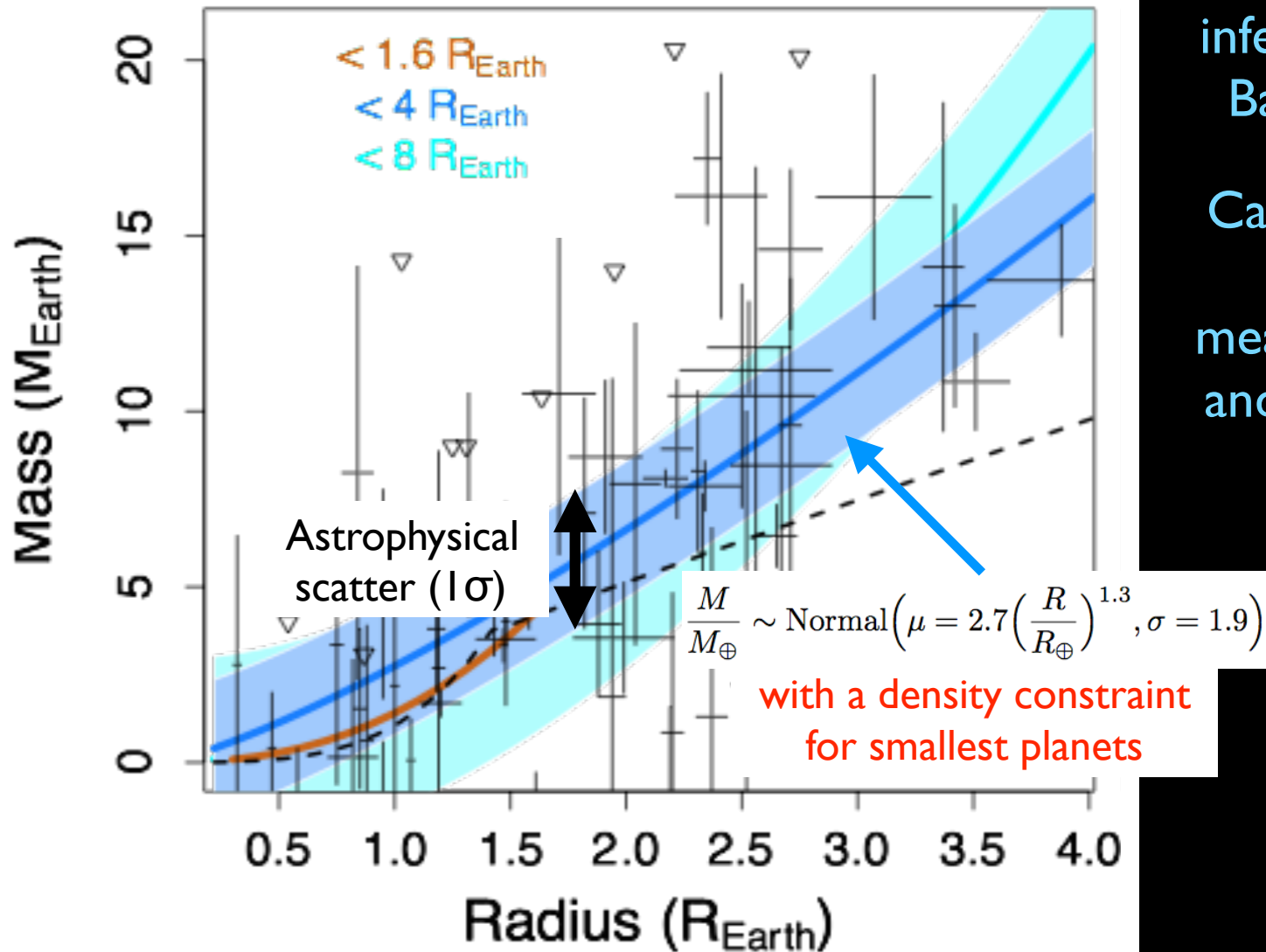


Population parameters  
(power law and  $\sigma$ )  
inferred via Hierarchical  
Bayesian Modeling ...

Can distinguish between  
scatter due to  
measurement uncertainty  
and astrophysical scatter  
in the exoplanet  
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Is an empirical  
description of  
exoplanet  
composition  
distribution.

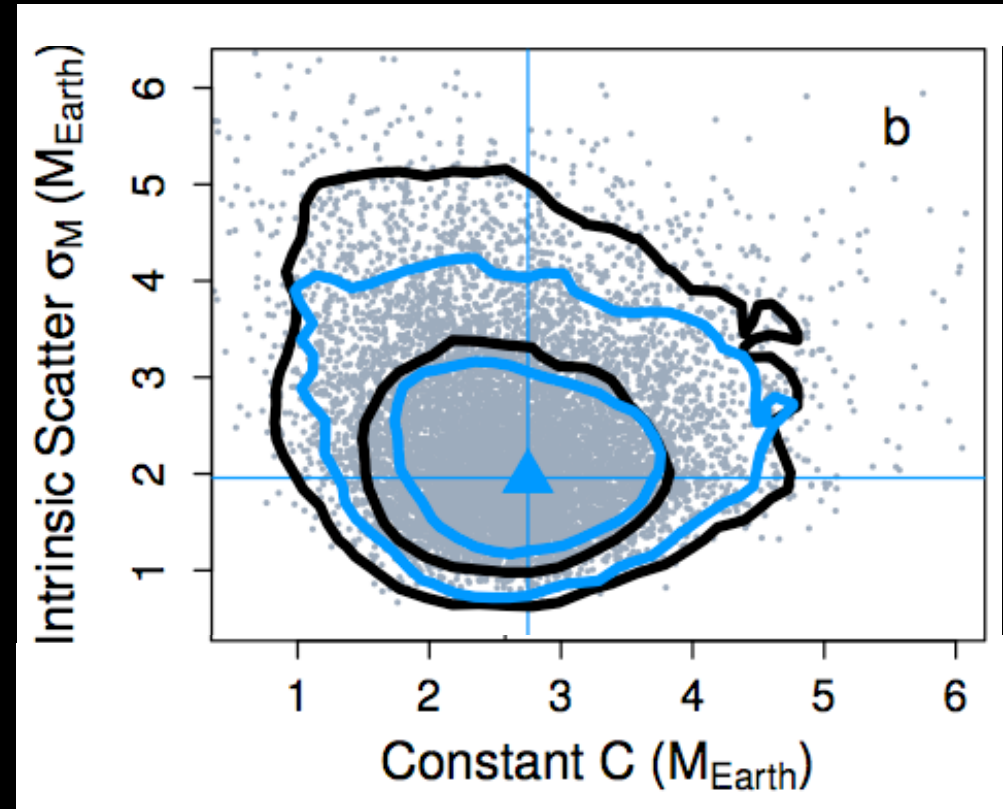
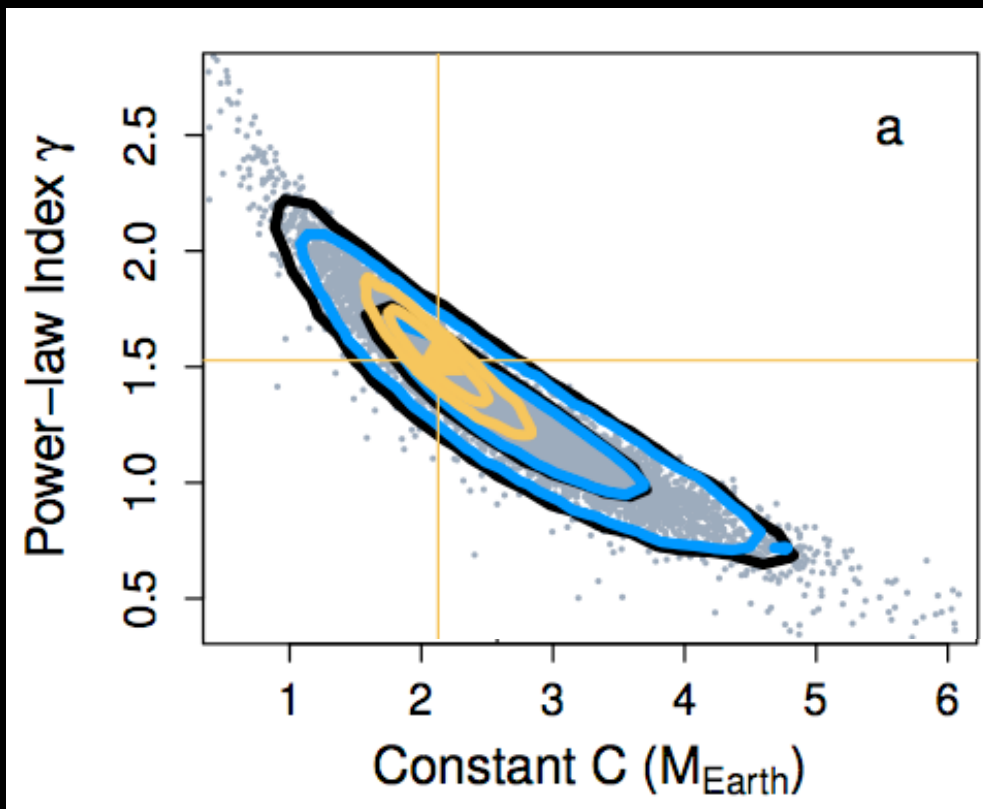
# In Parameter Space ...

deterministic M-R relation:

$$\frac{M}{M_{\oplus}} = C \left( \frac{R}{R_{\oplus}} \right)^{\gamma}$$

probabilistic M-R relation:

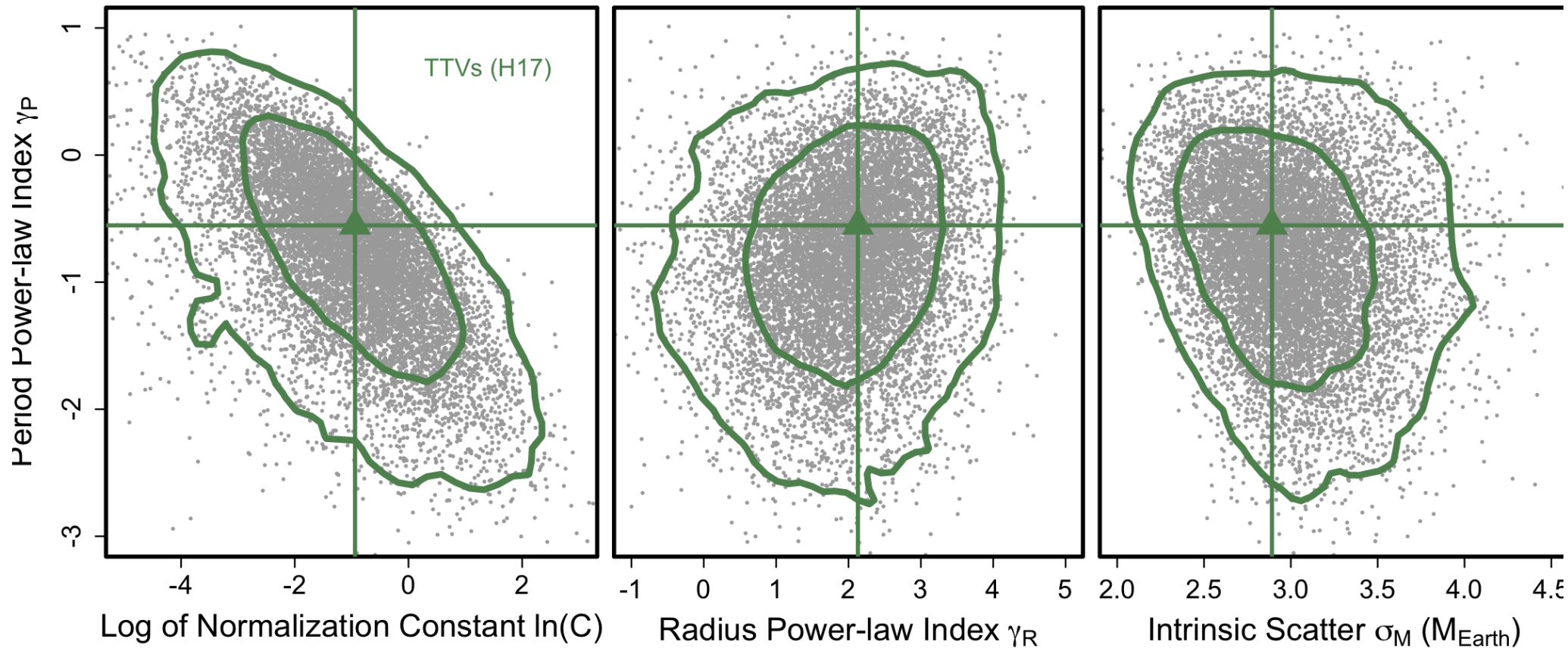
$$\frac{M}{M_{\oplus}} \sim \text{Normal} \left( \mu = C \left( \frac{R}{R_{\oplus}} \right)^{\gamma}, \sigma = \sigma_M \right)$$



There is intrinsic scatter in the current set of R,M measurements ...  
Nature produces a range of compositions for planets with similar masses!

# Allow a Period Dependence:

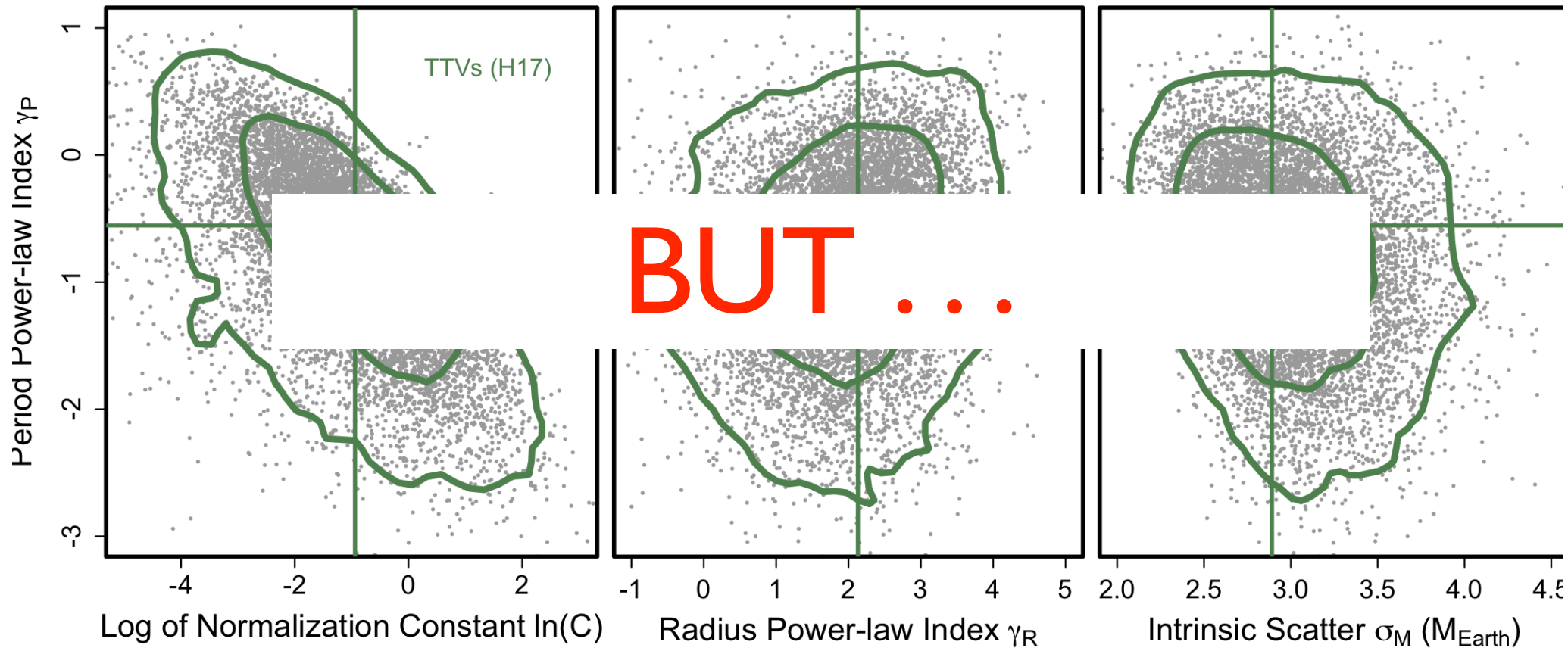
$$\frac{M}{M_{\oplus}} \sim \text{Normal}\left(\mu = C \left(\frac{R}{R_{\oplus}}\right)^{\gamma_R} \left(\frac{P}{P_{\oplus}}\right)^{\gamma_P}, \sigma = \sigma_M\right)$$



Marginally negative  $\gamma_P \rightarrow$  decreasing average mass at longer periods;  
note that the astrophysical scatter is larger now ...

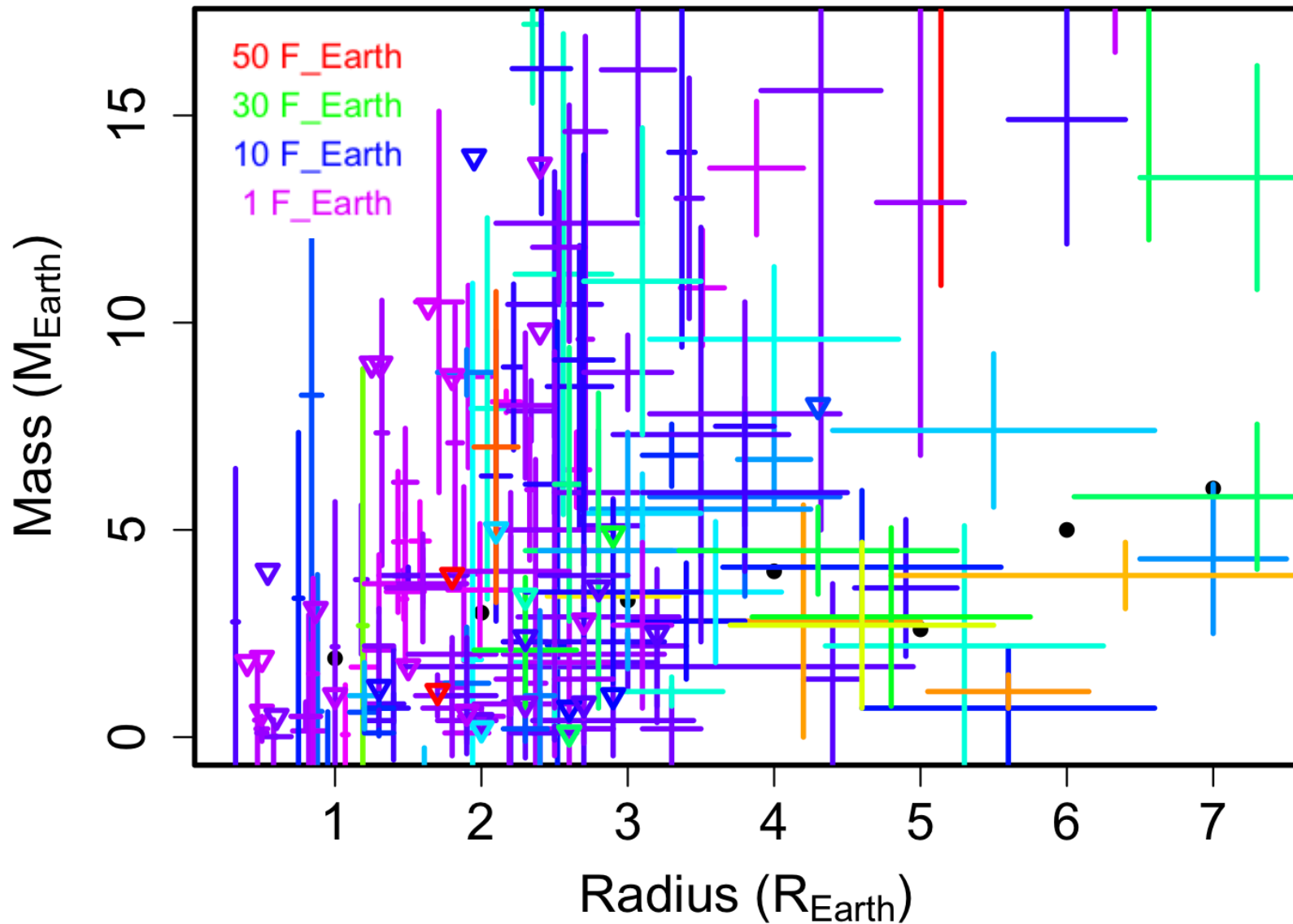
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# The Data?



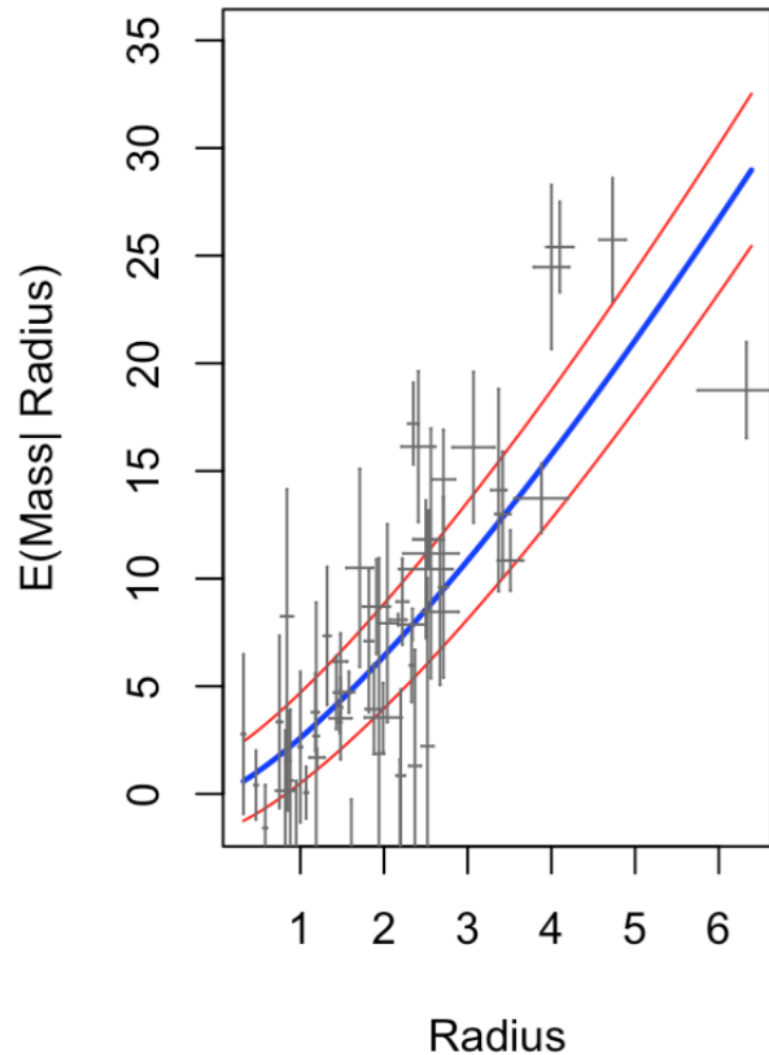
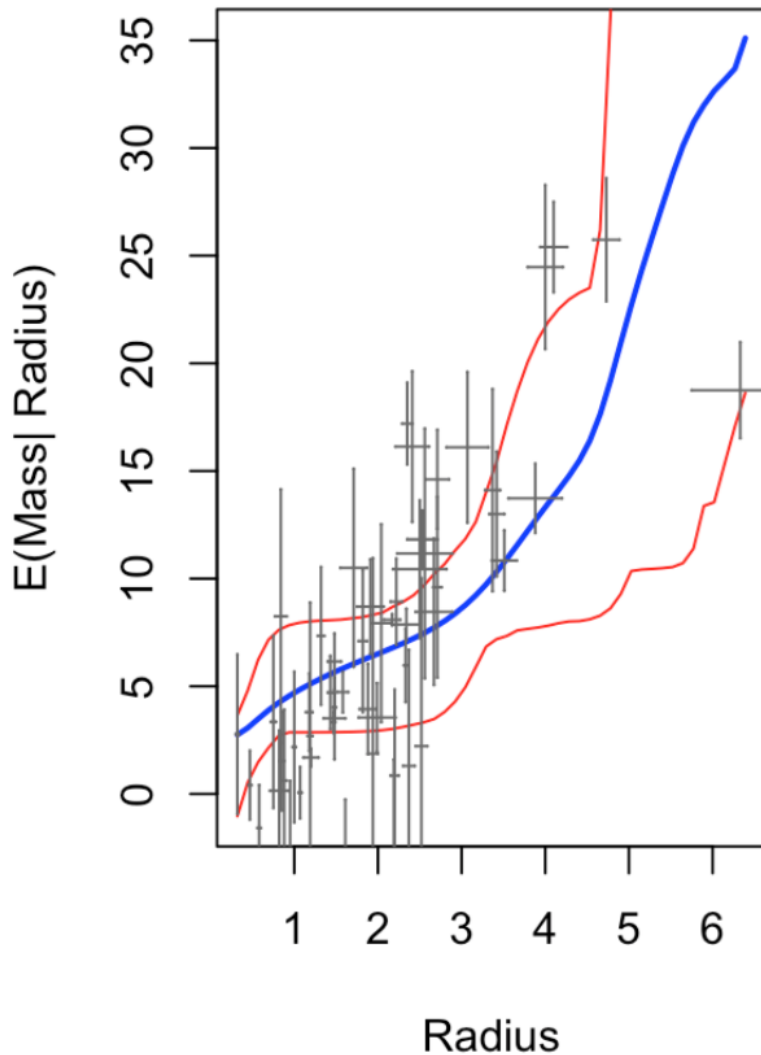
Not clear a power law is warranted any longer ...



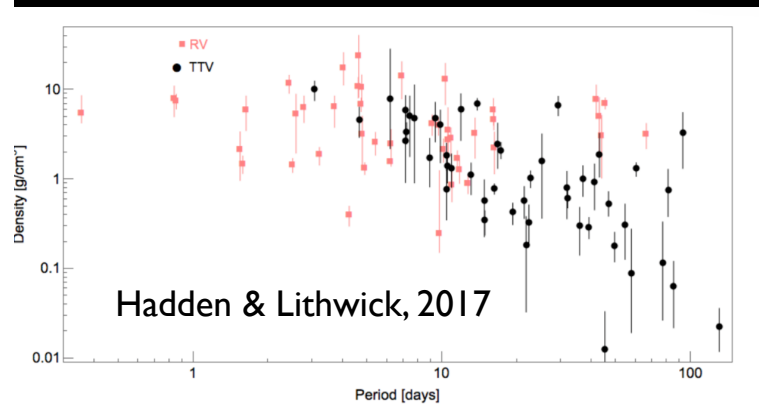
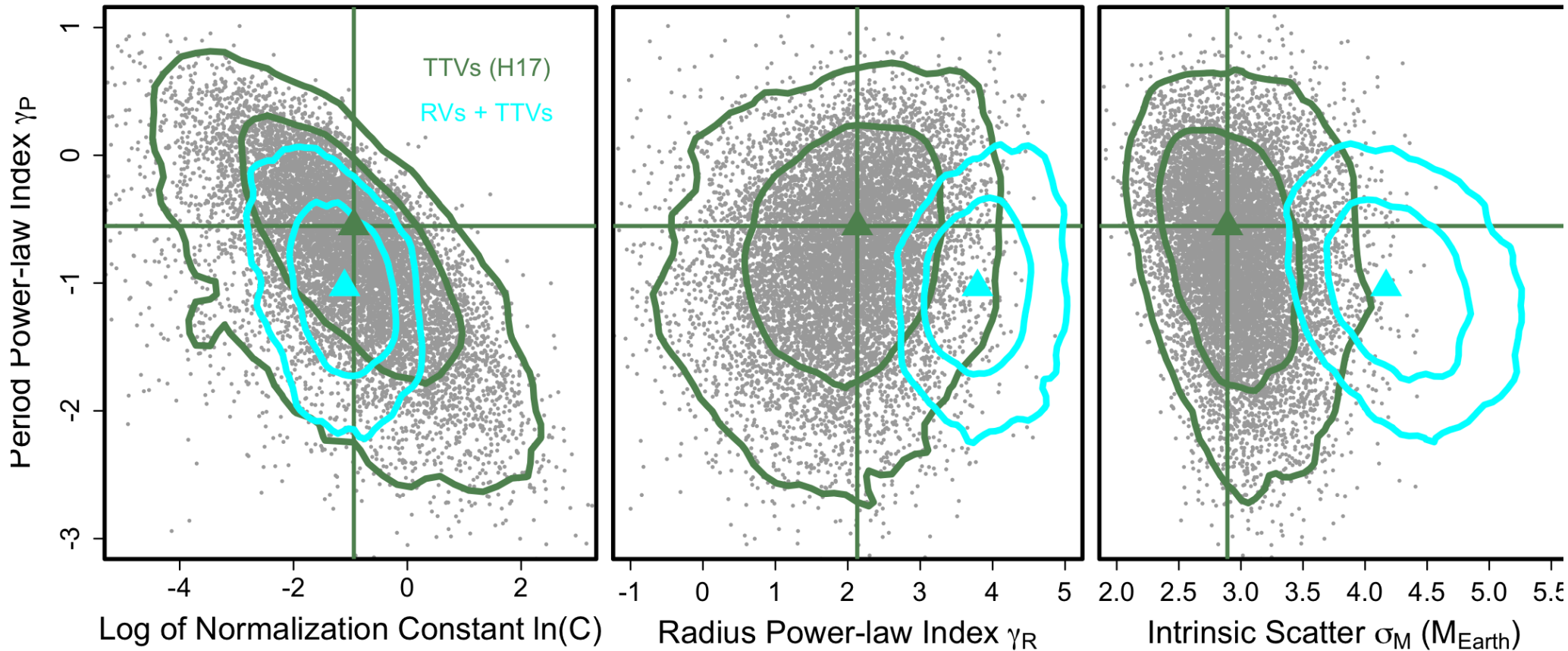
# Beyond the Power Law:

$$E[M|R = r] = \frac{\int m f(m, r) dm}{\int f(m, r) dm}$$

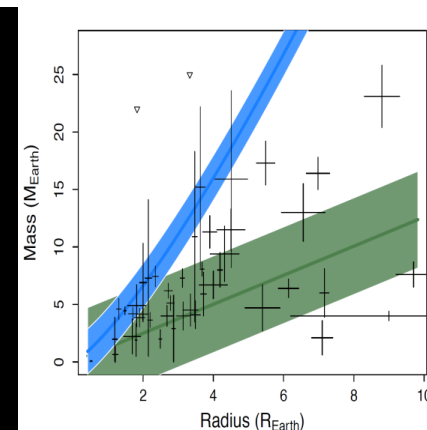
Ning, Wolfgang, &  
Ghosh, in prep.



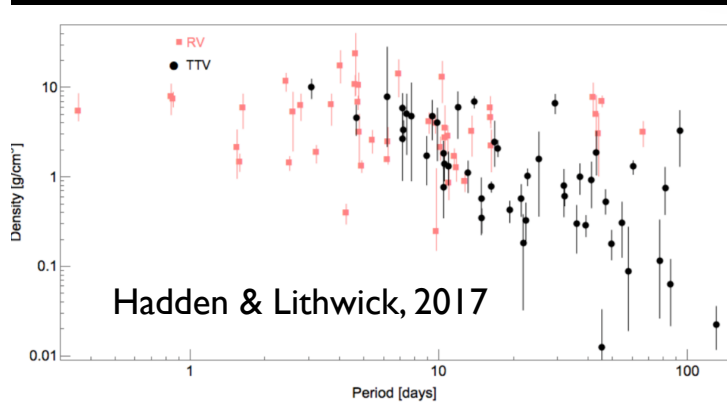
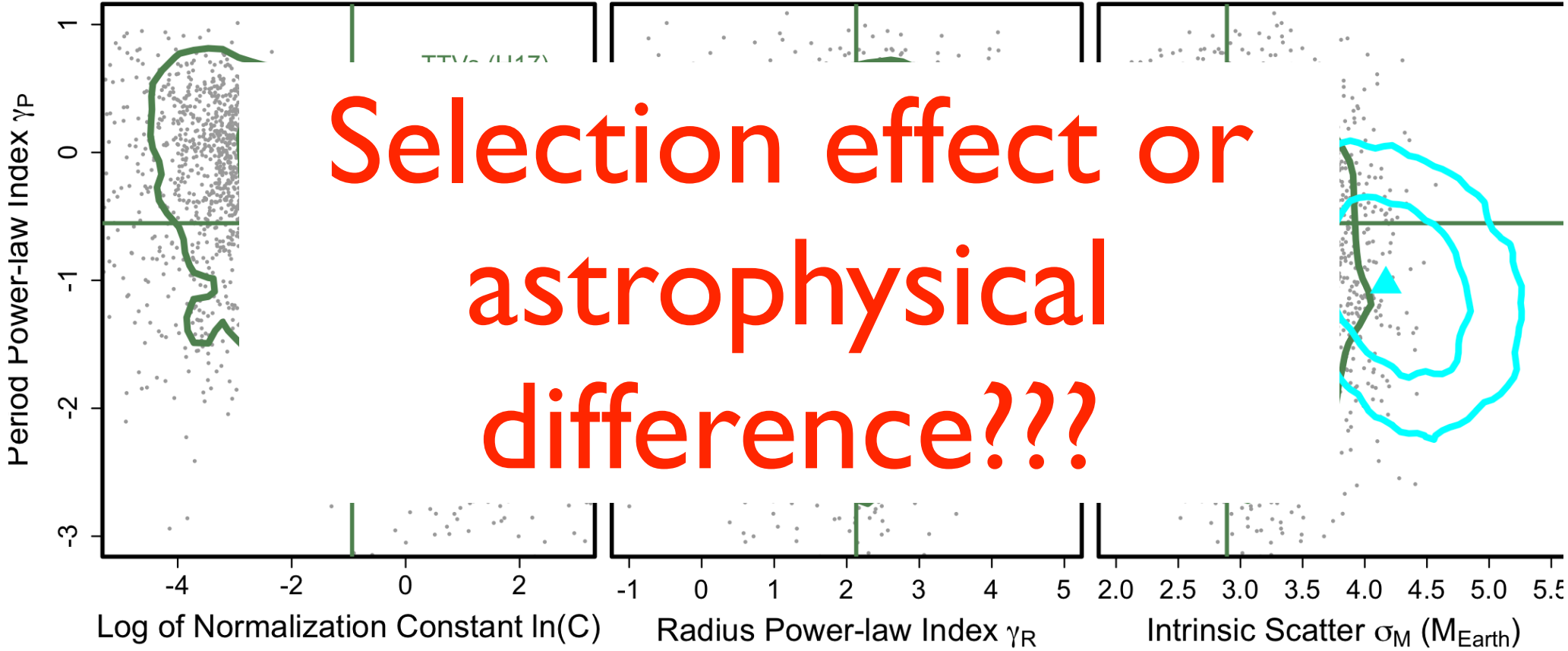
# Depends on Mass Method



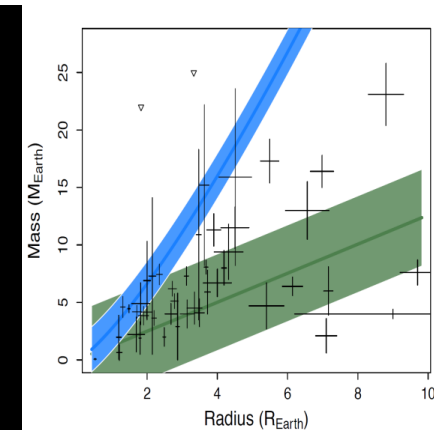
Most RVs at  $P < 20$  days, so use TTVs to probe period dependence ...  
But the two samples produce different M-R relations!



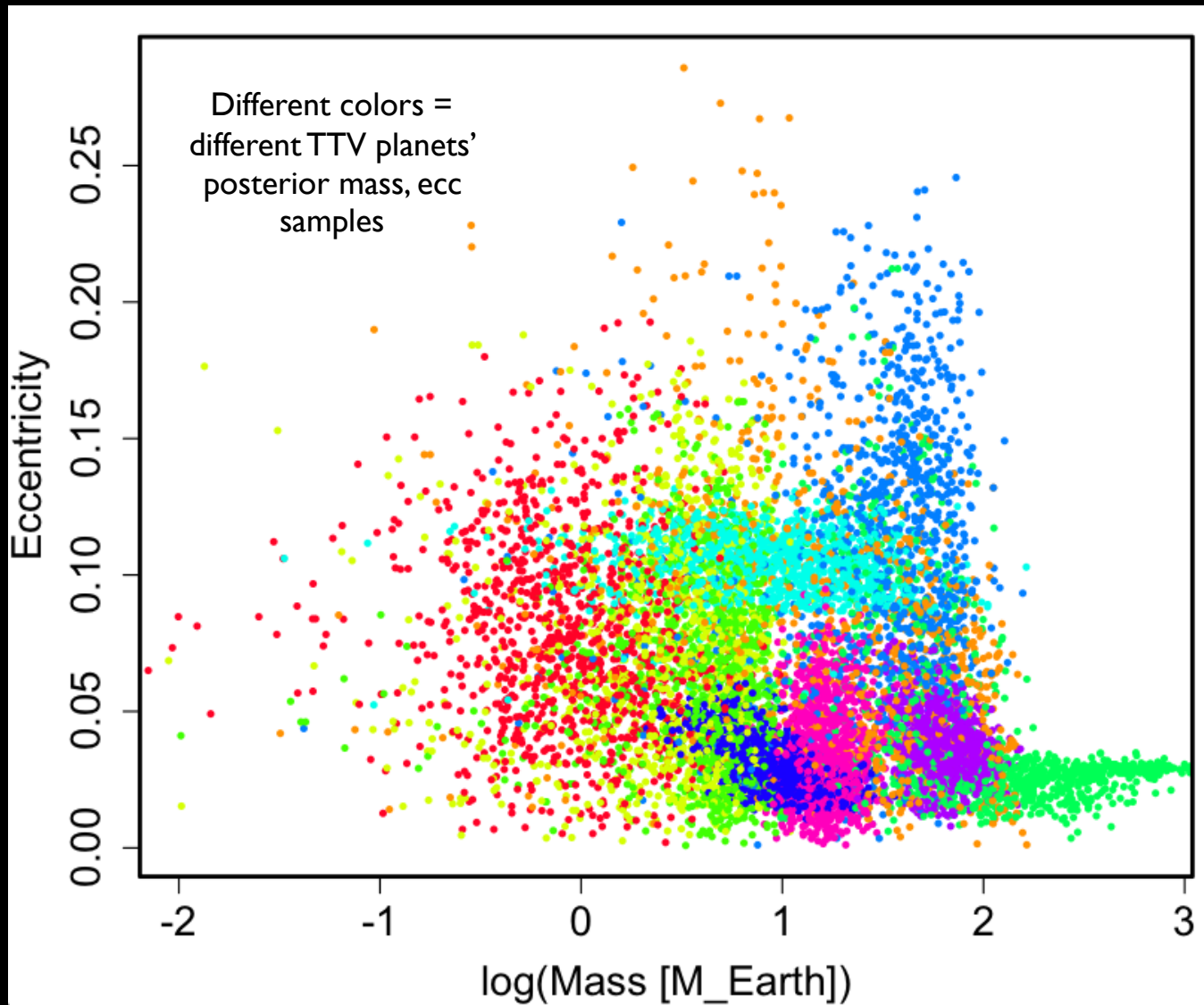
# Depends on Mass Method



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But the two samples produce different M-R relations!



# TTV Masses Degenerate w/ e



State-of-the-art:  
incorporate joint  $M, e$   
posteriors into the  
hierarchical modeling

Ongoing effort with  
collaborators Daniel  
Jontof-Hutter and Eric  
Ford to characterize  
TTV sample selection  
effects and  
systematics

But need similar work  
on RV side ...

# Summary

The observed **mass-radius relation** is an **empirical** description of the exoplanet **composition distribution**.

A **period-dependent** relation is crucial for **comparing microlensing and transit** surveys.

Suggestive weak period dependence:  
how much is **astrophysical vs. selection effect?**

**Lots of work needed** to understand biases in M-R relation and how we can **characterize its multi-dimensional nature**.