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The **E**lectric **F**ield **C**onjugation

Controlling Amplitude and Phase

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Acknowledgments: Brian Kern, Laurent Pueyo, Stuart Shaklan



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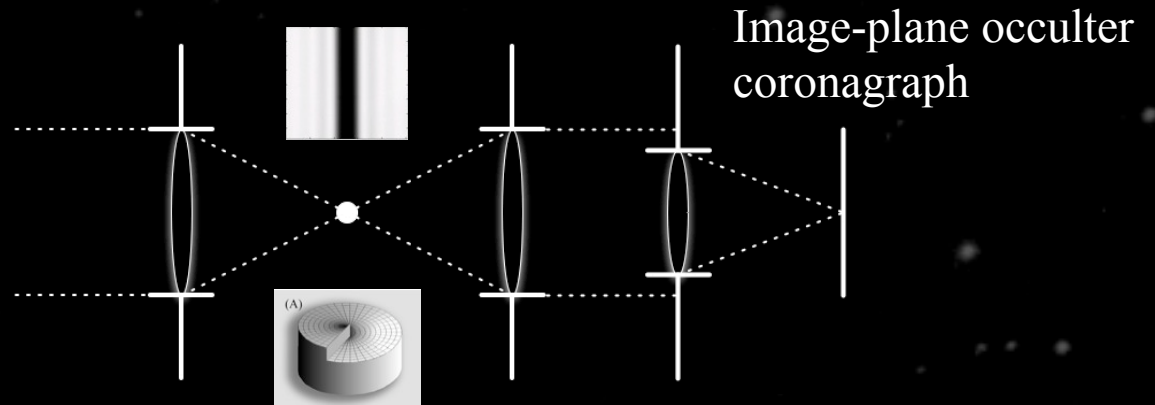
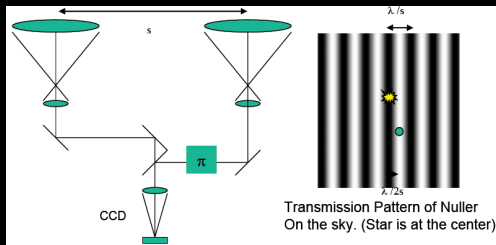
Are there other Earth-like planets?



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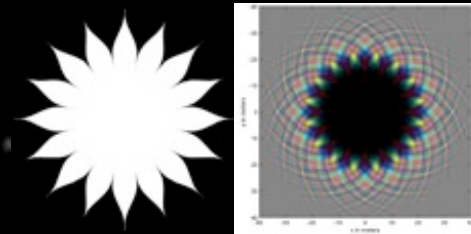
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Nulling interferometer

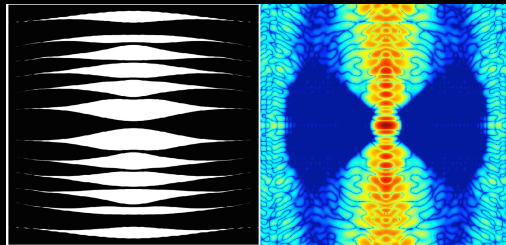


Solutions

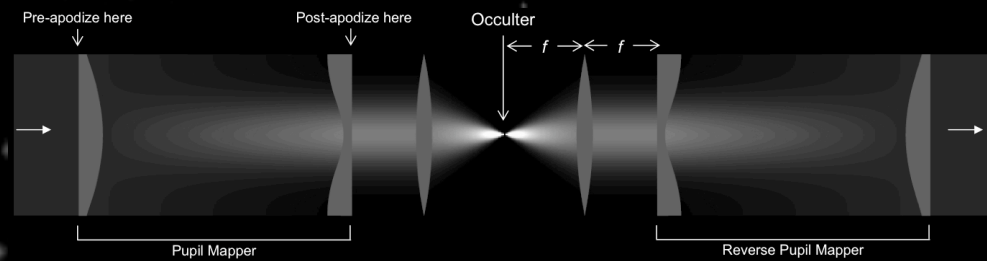
External occulter coronagraph



Shaped pupil coronagraph



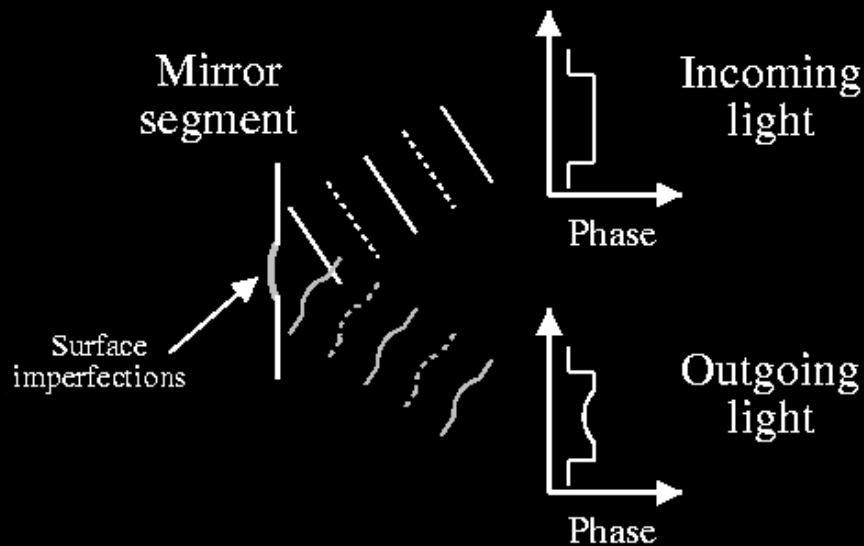
Pupil mapping coronagraph





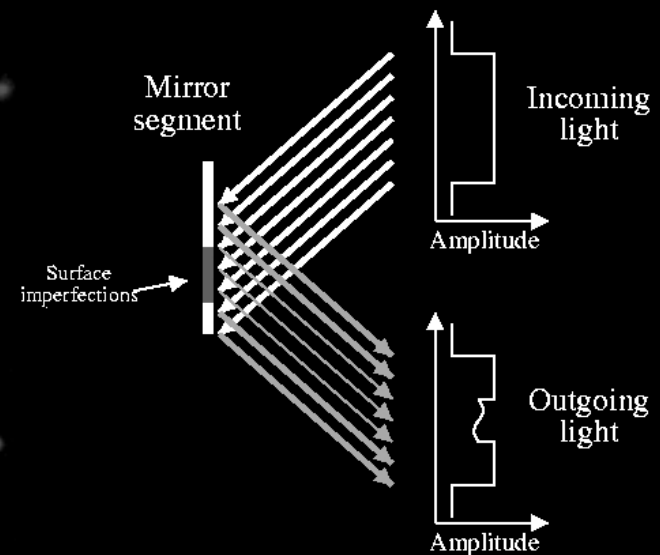
Problem: Wavefront aberrations!

Phase aberrations



Requirement: $\sim \lambda / 10,000$

Amplitude aberrations

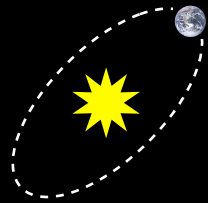


Requirement: $\sim 1 / 1,000$



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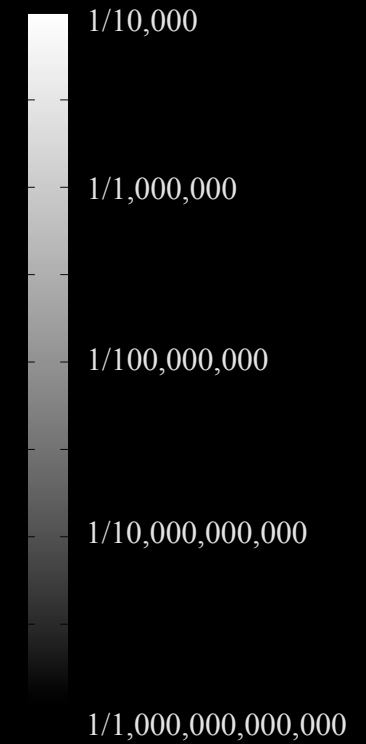
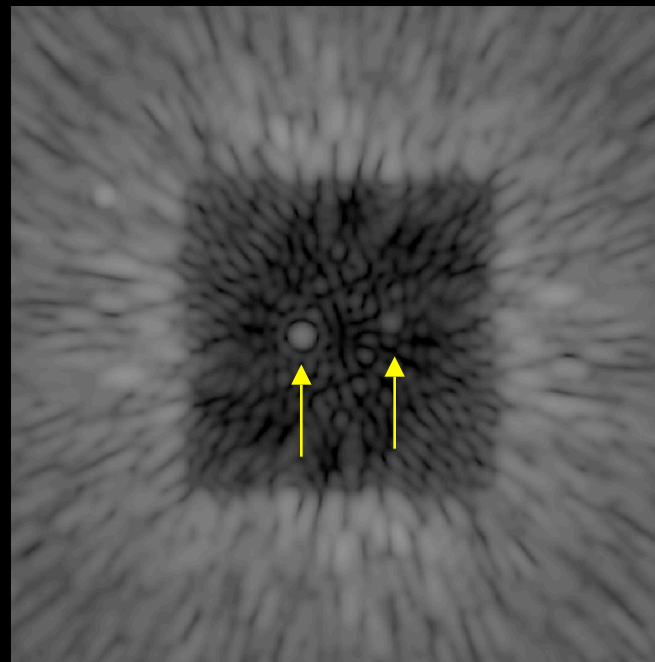
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30 light years



Deformable mirror





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What is EFC?



vs.



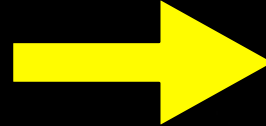
**EFC is a formalism of the correction problem
allowing us to use various tools to find the solution**



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All correction algorithms do the same thing...



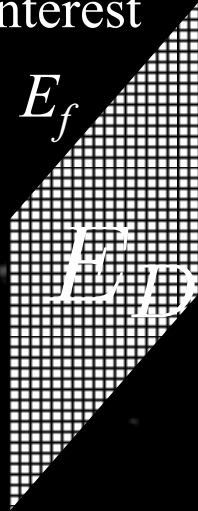


Electric Field Conjugation

DM plane



Plane of
interest



Find the shape of the DM such that its effect in the plane of interest **negates** the electric field present in this plane due to the coronagraph and the aberrations

$E_{abr+ideal}$

$$E_f = \quad + \quad = 0$$



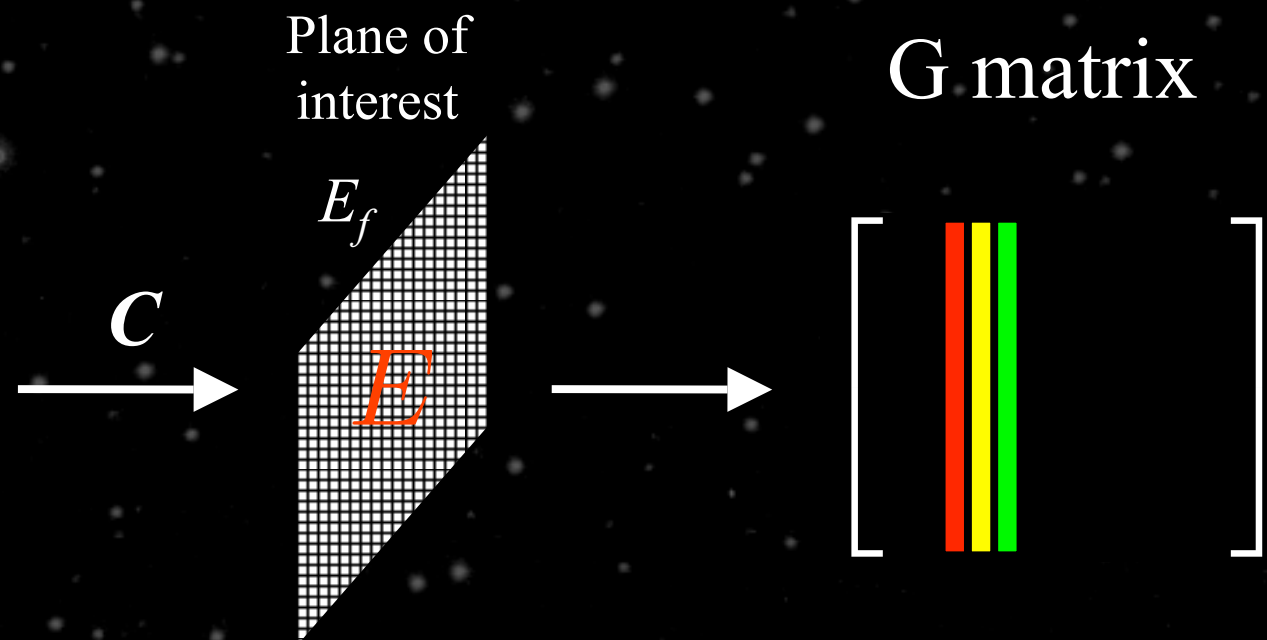
Linearize w.r.t
actuators heights



Electric Field Conjugation

How do we linearize the effect of the DM in the image plane?

Assume that the overall effect of the DM in the image plane is the sum of the effects of each of the actuators



The effect of the DM in the image plane will now be Ga , where a are the DM actuator heights.



Electric Field Conjugation

$$G\bar{a} = iE_{ab}$$



$$\bar{a} = \begin{bmatrix} \Re \{G\} \\ \dots \\ \Im \{G\} \end{bmatrix}^{-1} \begin{bmatrix} \Re \{iE_{ab}\} \\ \dots \\ \Im \{iE_{ab}\} \end{bmatrix}$$

This guarantees a real valued solution for the DM actuators heights



$$\bar{a}^* = \arg \min_{\bar{a} \in X} \|E_{ab} + iG\bar{a}\|^2$$



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The EFC correction method requires the
complex wavefront at the image plane...



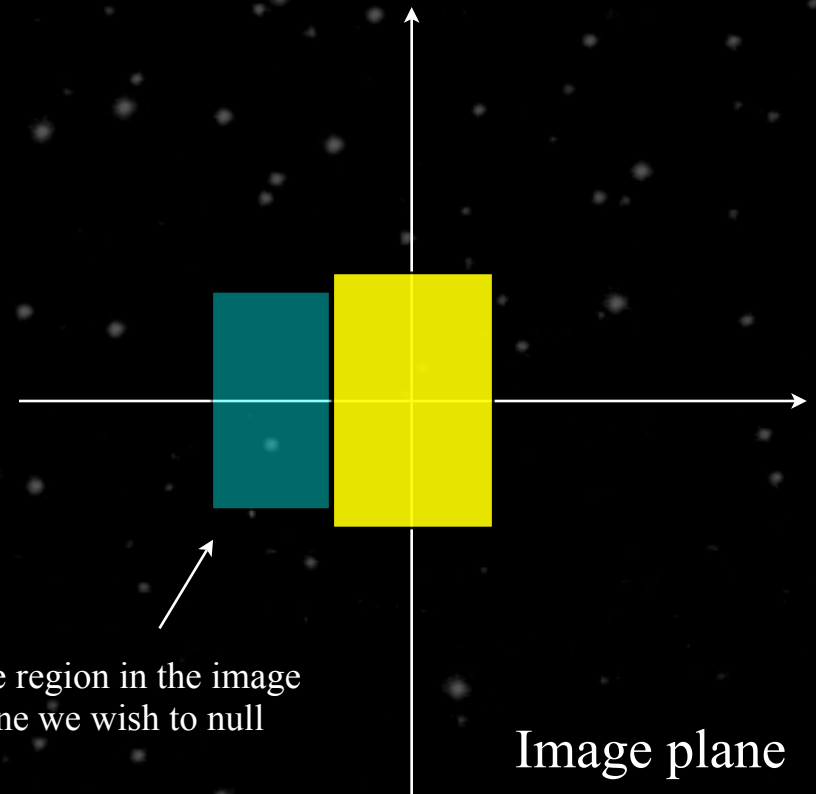
The cosine spatial frequency
determines the center location
of the diversity region

The spatial phase of the
cosine determines the overall
phase of the diversity

$$DM(x, y) = ?$$

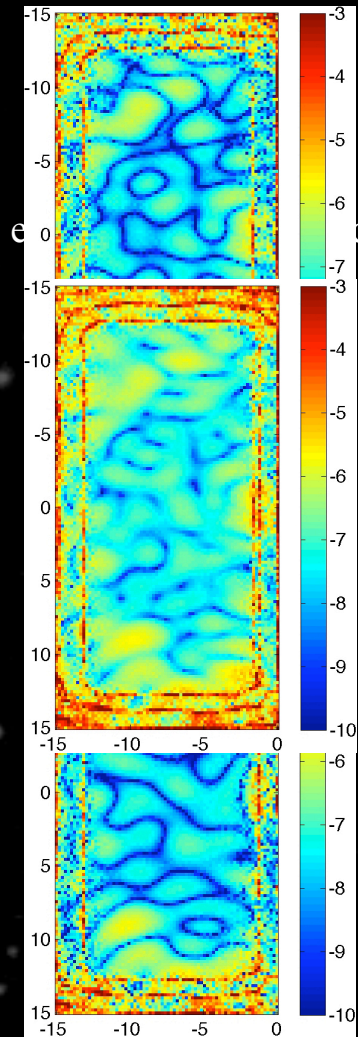
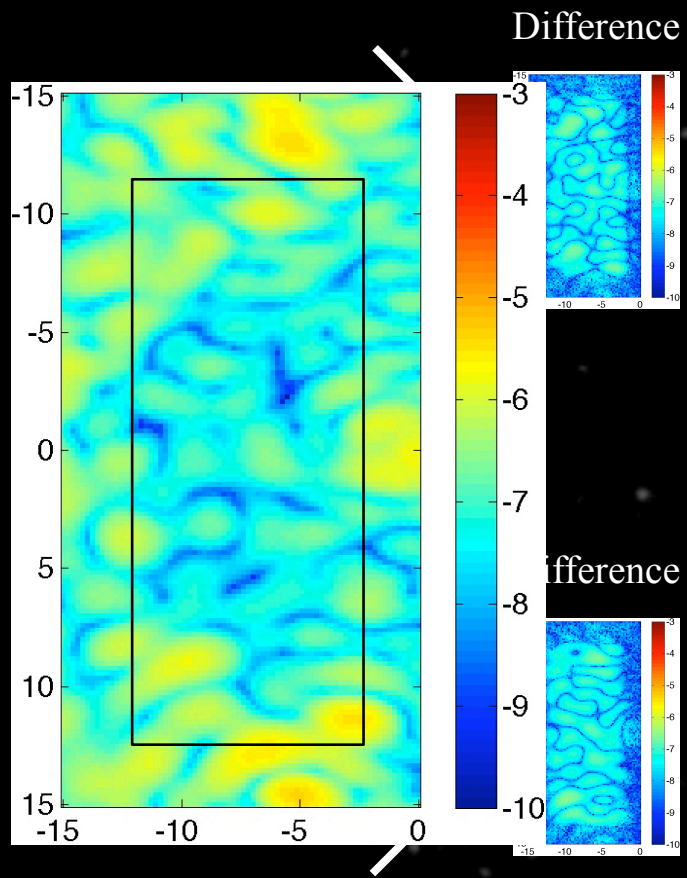
The sincs determine
the general amplitude
shape of the diversity

- The wavefront is reconstructed by applying 4 different shapes on the DM (“probes”).
- The additional probes to the current DM shape is chosen such that the diversity is uniform over the region of interest with the ability to change the spatial phase.

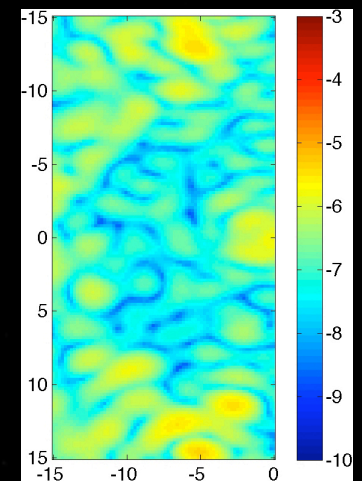




Real and imaginary parts of the estimated Electric field



Measured intensity





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How EFC is related to other correction algorithms

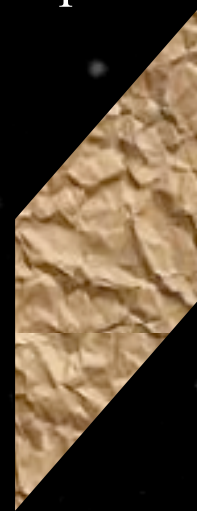


Phase conjugation

DM plane



DM plane



Poyneer et. al 2004



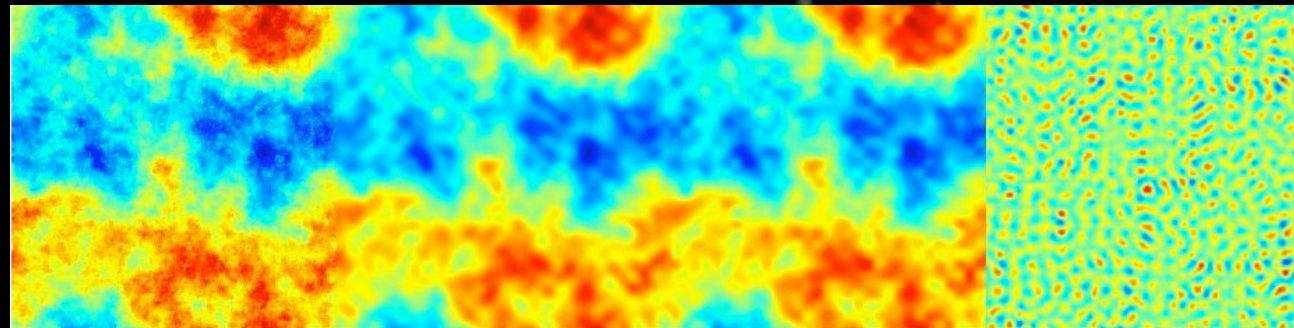
Sinusoids basis set
(Fourier series)
or
Influence functions

Original

LPF

Reconstructed

Difference (10x)





Speckle nulling

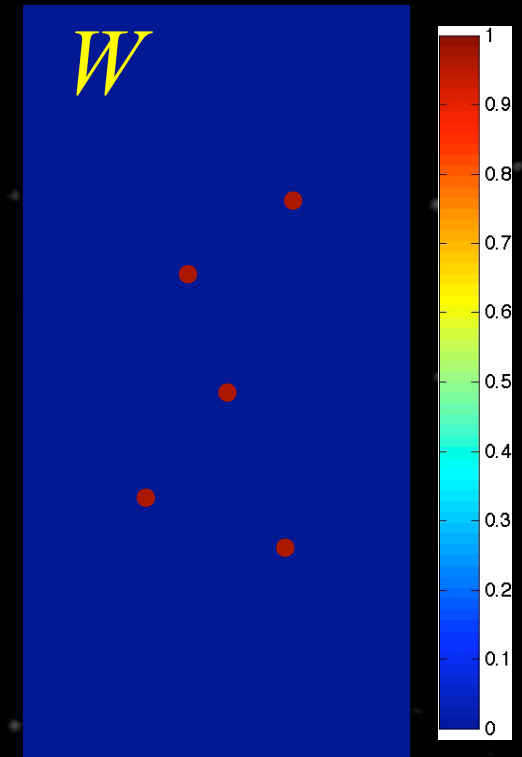
Trauger et. al 2004

$$W G \bar{a} = i W E_{ab}$$

If the system model is reduced to a single Fourier transform of an infinite aperture and the weighting function W reduces to isolated pixels that change their location according to the brightest peaks in the region of interest,



EFC = speckle nulling





Energy minimization

Borde et. al 2005

$$\mathcal{E} = \|E_{ab} + iC \{\phi\}\|^2$$



$$\frac{\partial}{\partial \bar{a}} \mathcal{E} = 0$$

EFC

$$G\bar{a} + E_{ab} = 0$$

Least squares solution



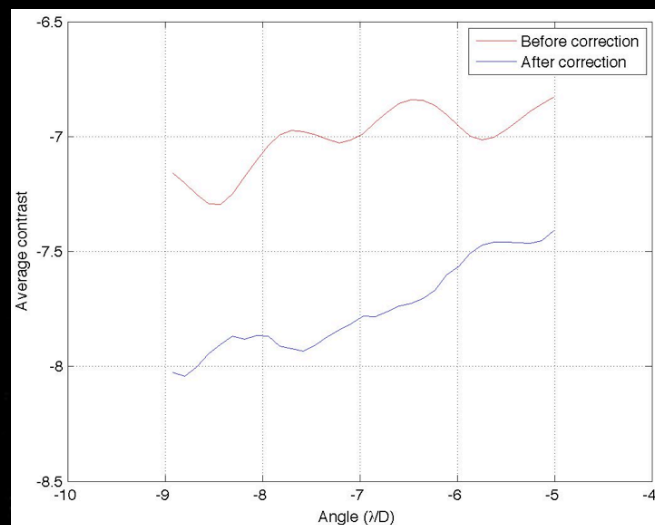
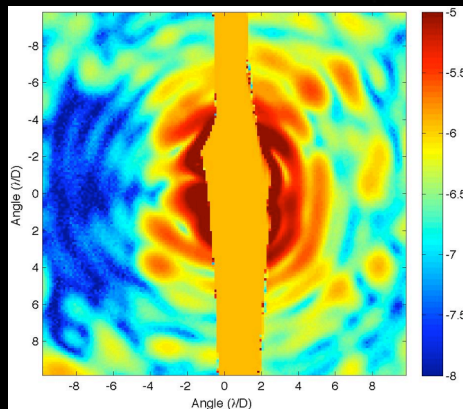
$$\bar{a}^* = \arg \min_{\bar{a} \in X} \|E_{ab} + iC \{\phi\}\|^2.$$



Some results

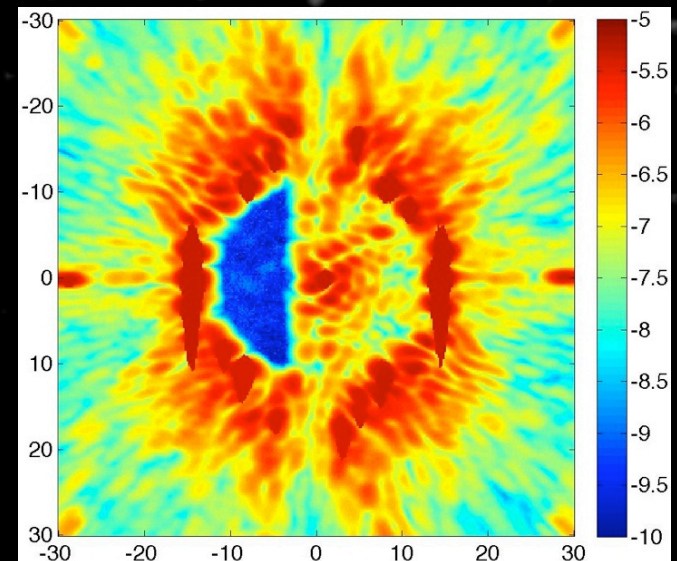
UC Santa Cruz testbed

using an Apodized Pupil
Coronagraph



JPL's High Contrast
Imaging Testbed (HCIT)

using a Lyot Coronagraph



$6.5 * 10^{-10}$ in 10% light

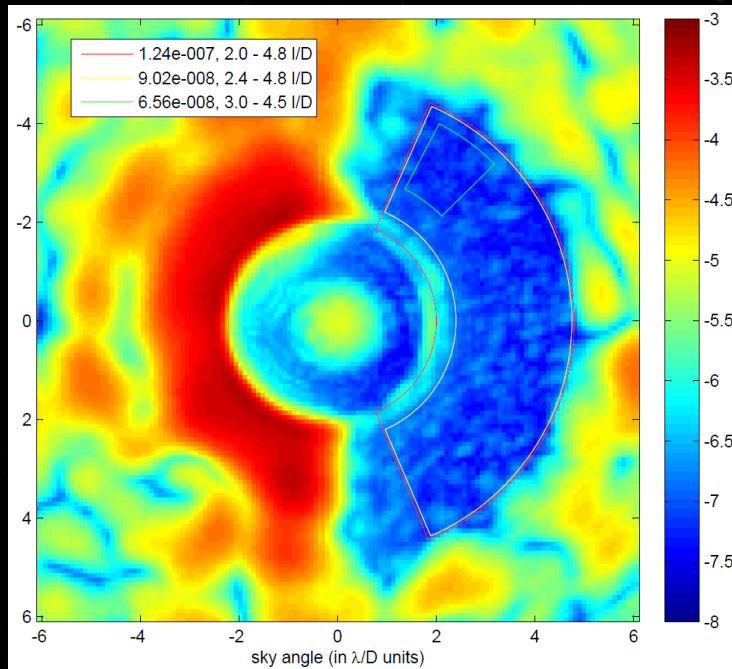


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NASA Ames Coronagraph Laboratory

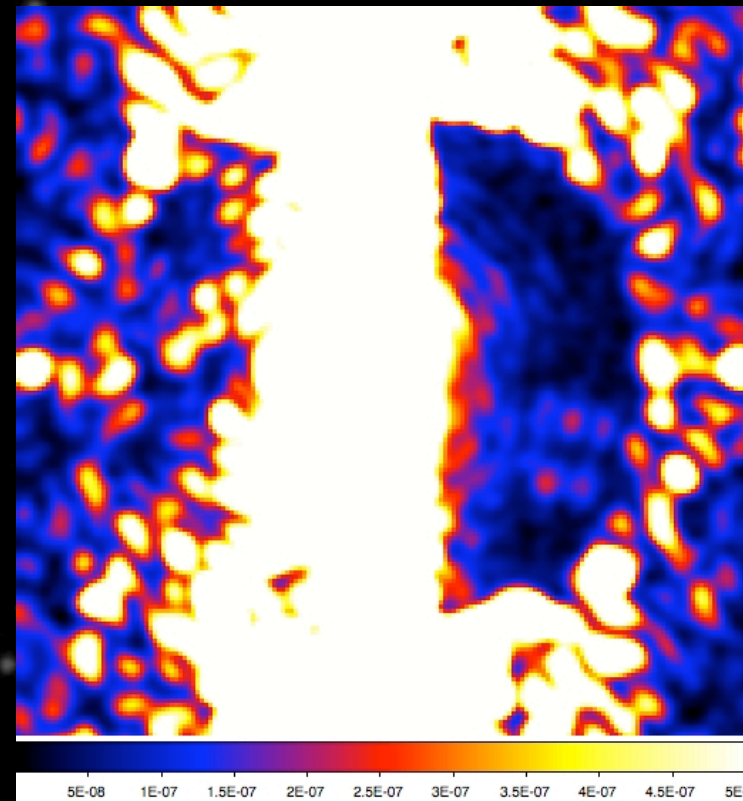
using a Phase Induced
Amplitude Apodization
Coronagraph



Ruslan Belikov, NASA Ames Coronagraph Laboratory

JPL's High Contrast Imaging Testbed (HCIT)

using a Vector Vortex
Coronagraph



Dimitri Mawet, JPL

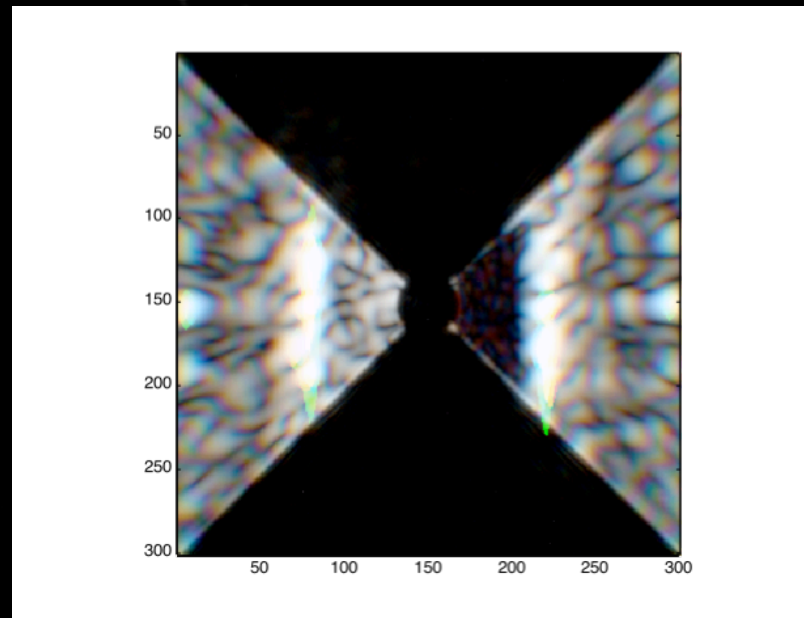


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JPL's High Contrast Imaging Testbed (HCIT)

using a Shaped Pupil
Coronagraph



Contrast: 2.4×10^{-9}
Bandwidth: 10% @ 800nm
IWA: $4 \lambda/D$



Summary

- EFC is a formalism of the correction problem that provides many tools to find a suitable solution.
- All the common correction algorithms, namely, phase conjugation, speckle nulling and energy minimization can be viewed as special cases of EFC.
- EFC has used very successfully on several testbeds using different coronagraphs