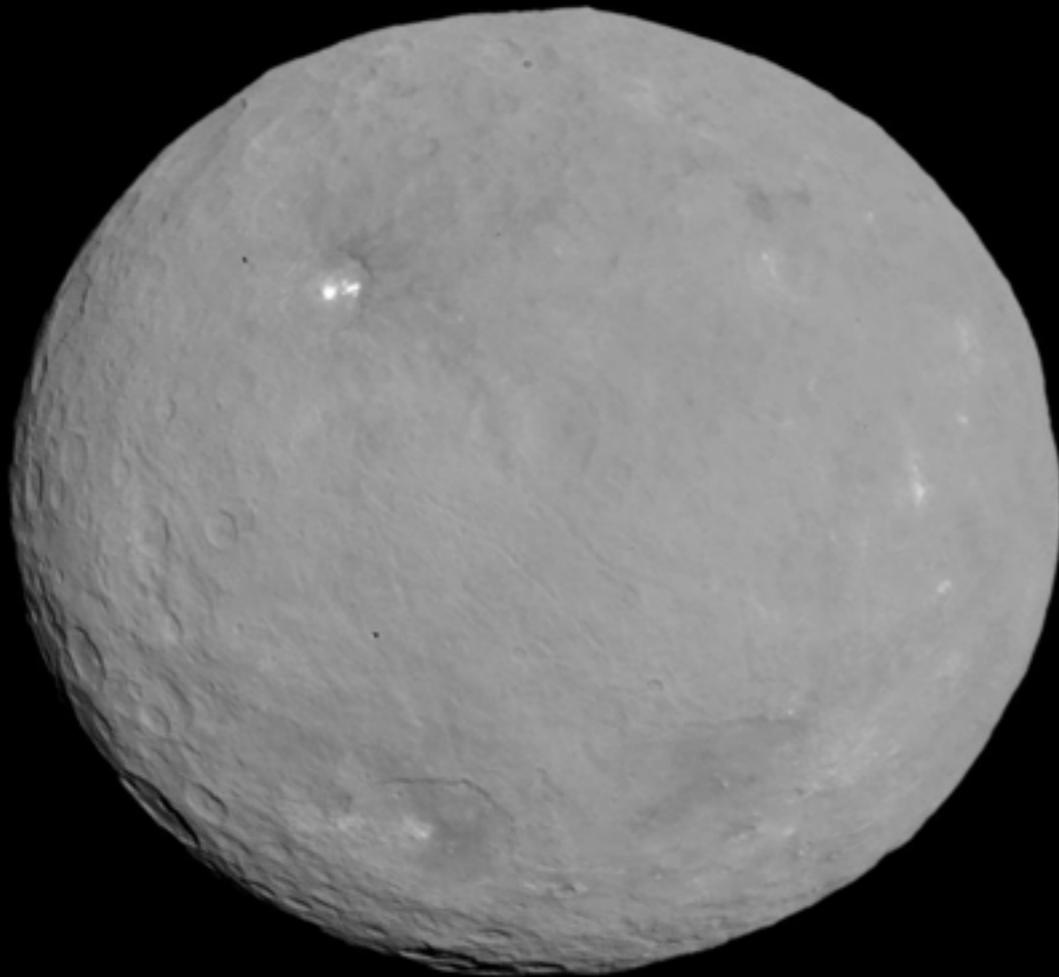
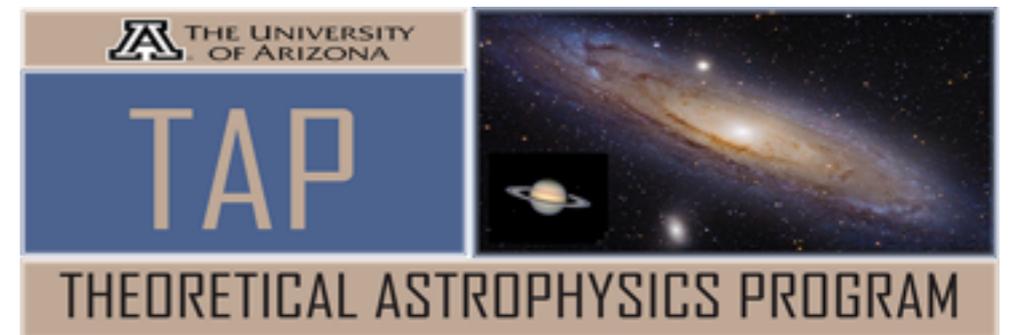


# The Formation of Planetesimals and Large Cores

Andrew Youdin

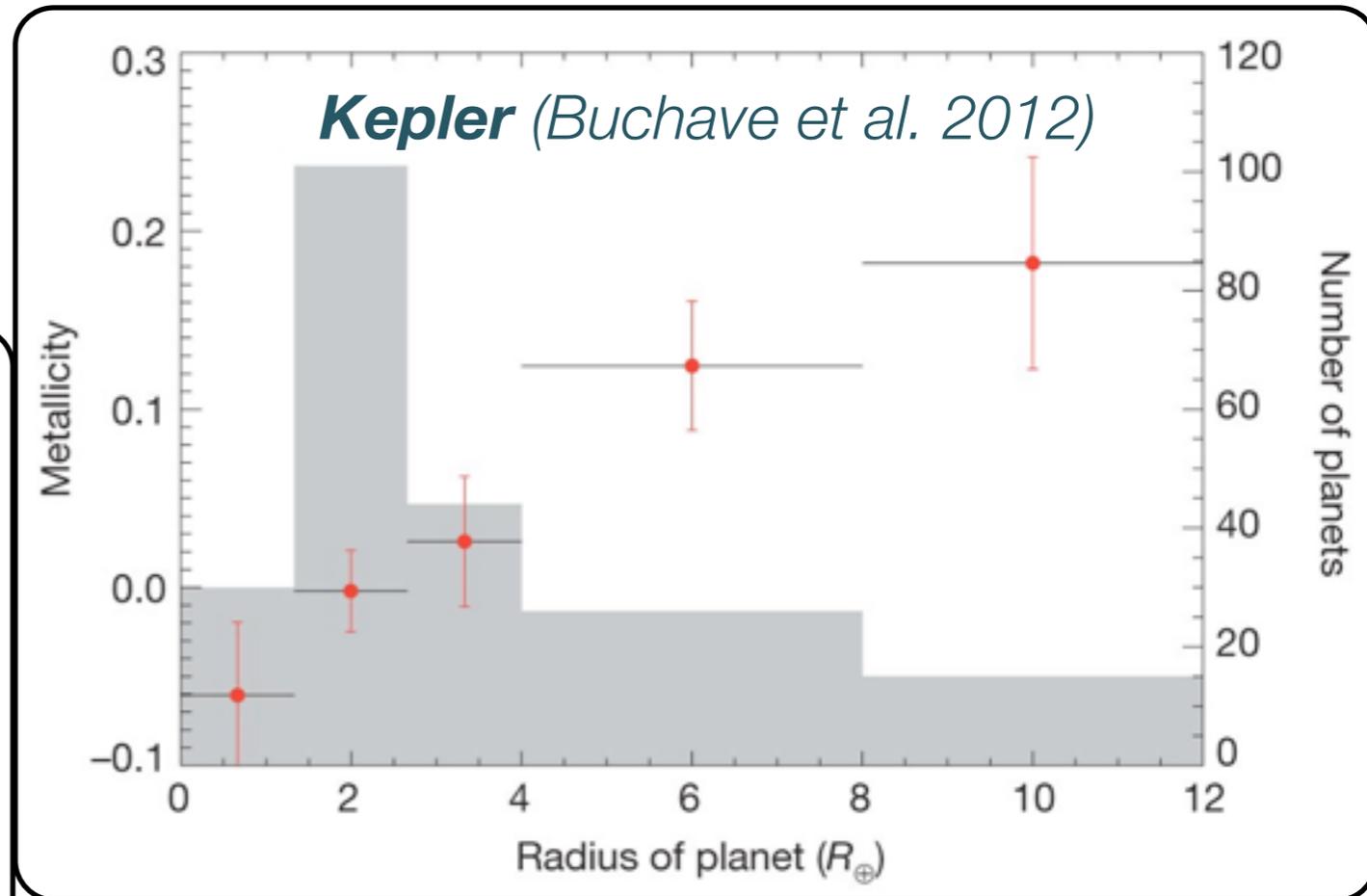
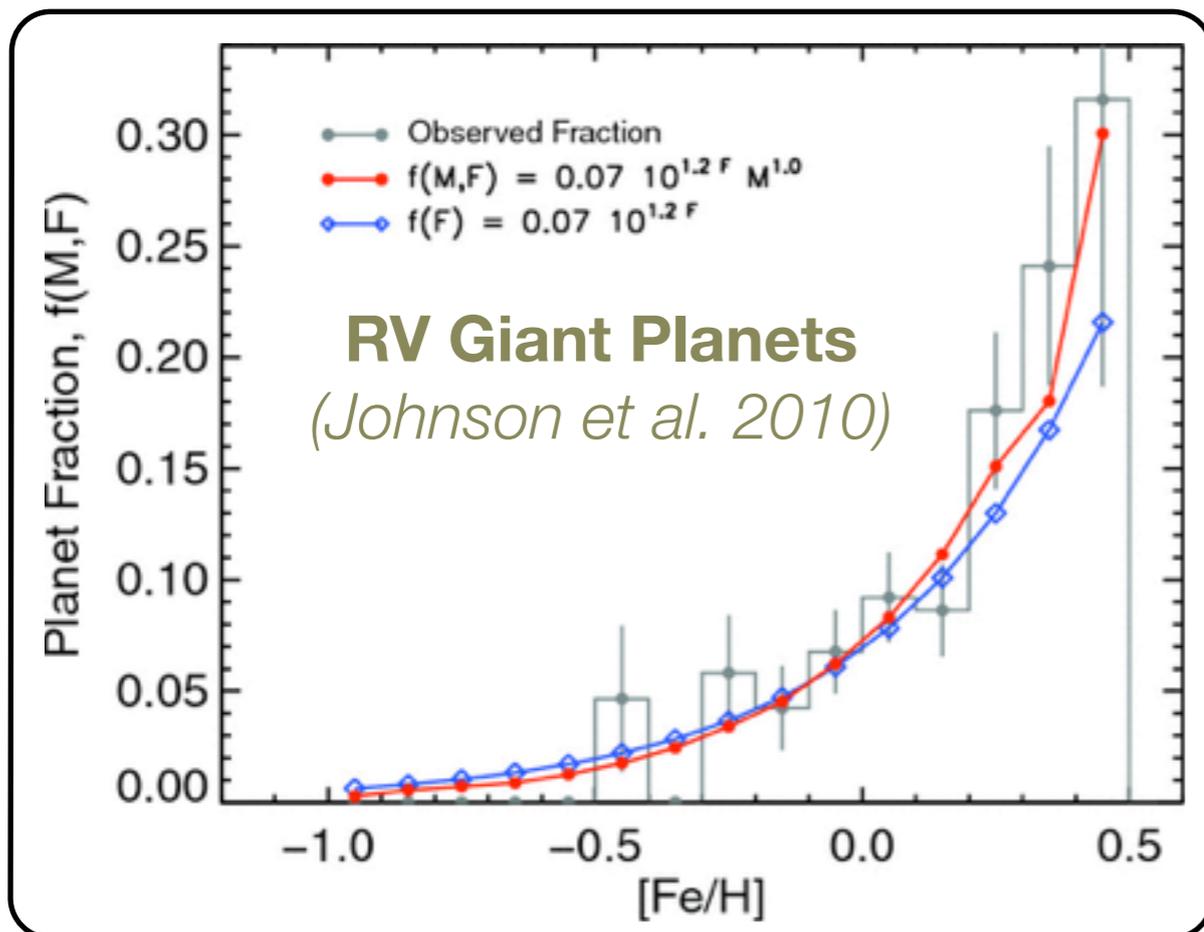


STEWARD  
OBSERVATORY



*(Youdin & Kenyon,  
1206:0738)*

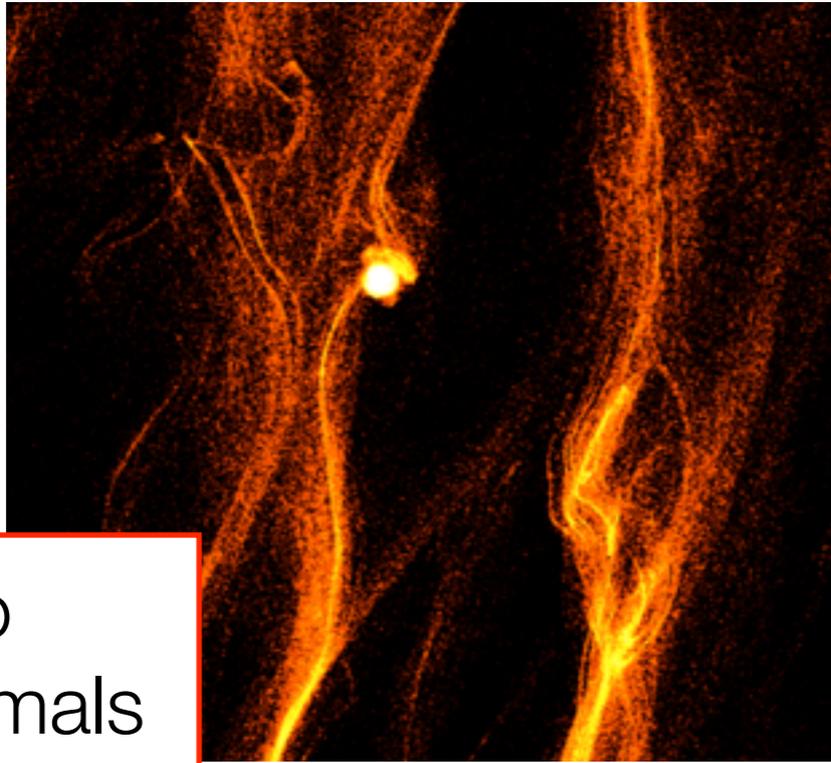
# Giant Planets are More Common Around Metal Rich Stars



Formation of Solid Planetesimals Holds the Key!

# Four Stages of Planet Formation: The Core Accretion Model

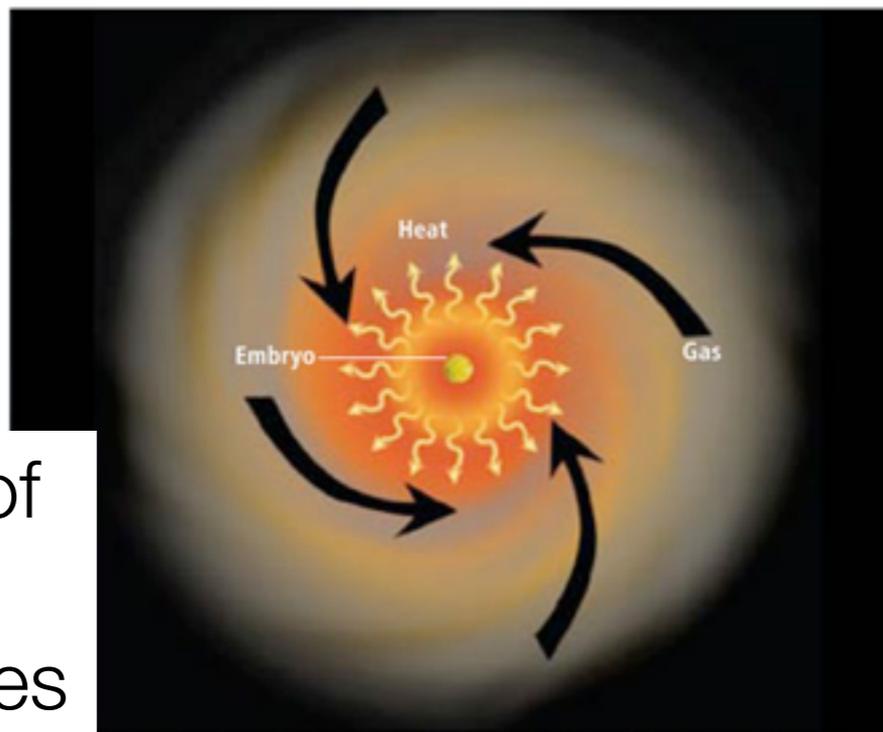
1. Dust to Planetesimals



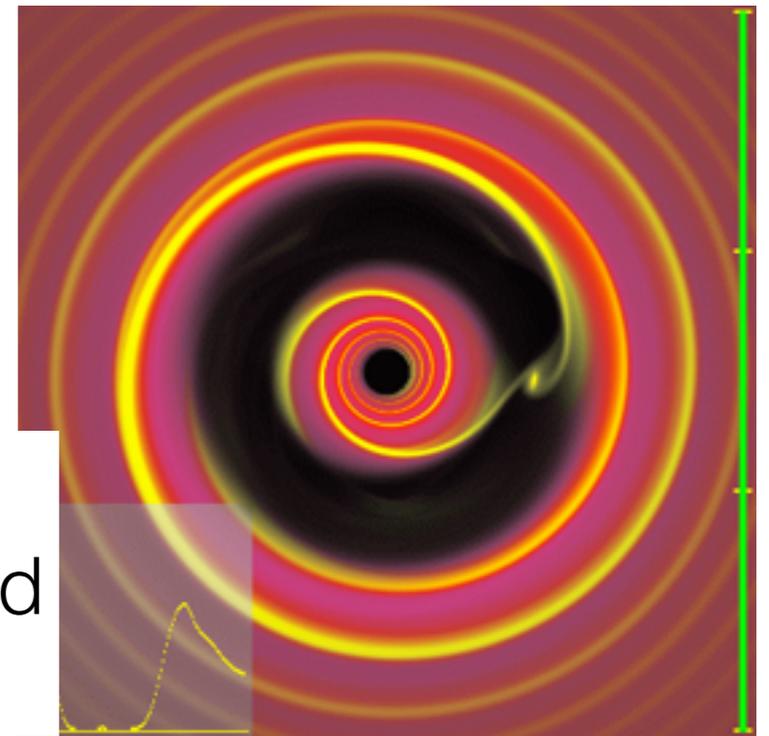
2. From Planetesimals to Planets & Cores



3. Growth of Gas Giant Atmospheres



4. Planet Migration and Scattering

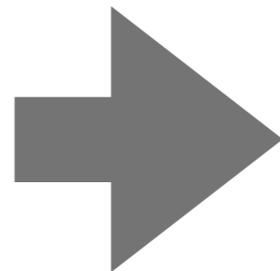
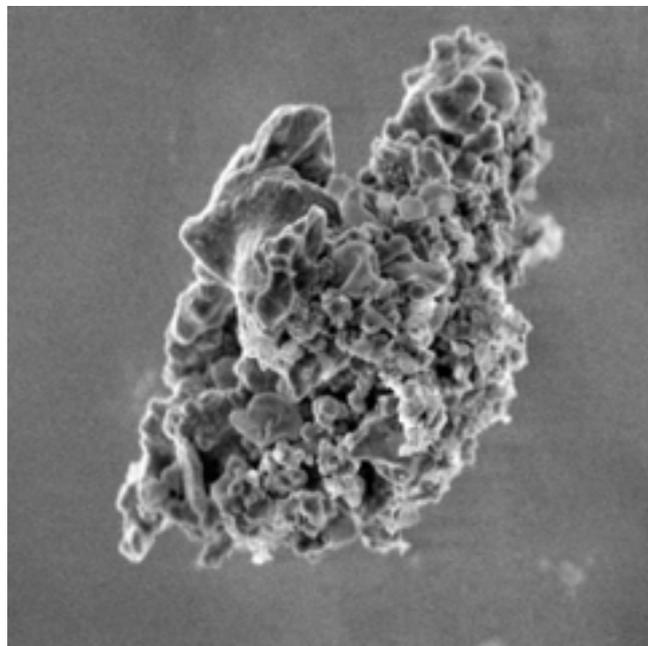


*Credits: A. Johansen, F. Sulehria, D. Lin, P. Armitage*

# Planetesimal Formation Spans Many Orders of Magnitude and Different Processes

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$\mu\text{m}$  dust

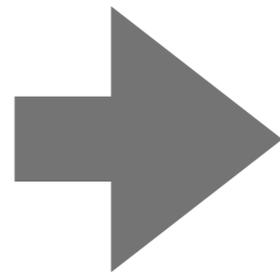
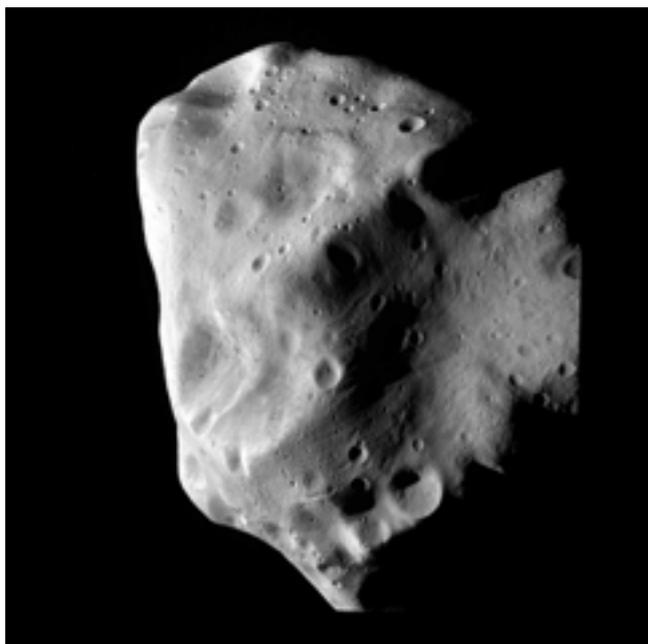


50 km planetesimal



mass growth  
 $\times 10^{33}$

50 km planetesimal



$M_{\text{Jup}}$  Giant Planet



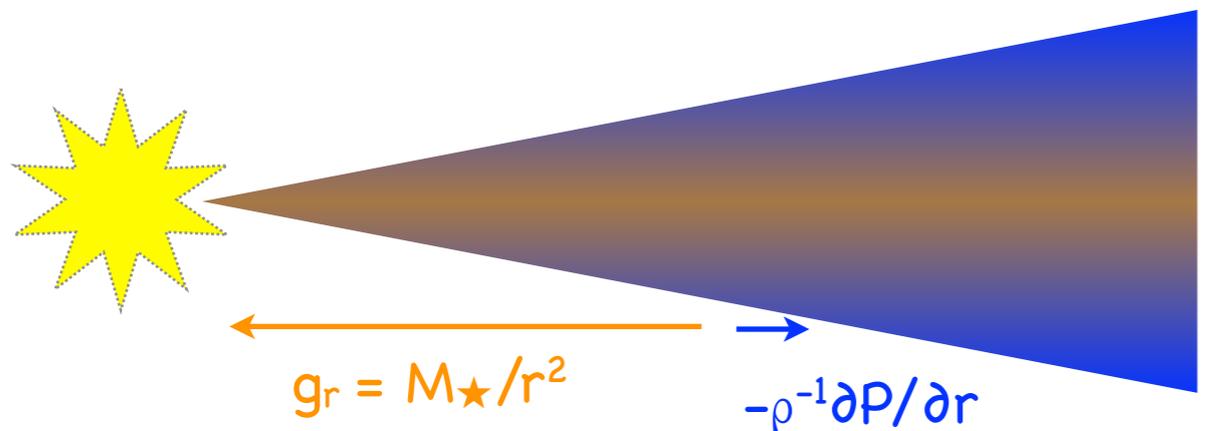
mass growth  
 $\times 10^9$

# Key Aspects of Planetesimal Formation: Starting Small in a Gas Disk

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- Surface gravity is weak
- Sticking is important for dust growth
- Aerodynamic gas drag is crucial
  - Radial drift introduces a “meter-size” barrier
- Resolution: particle concentration and gravitational collapse

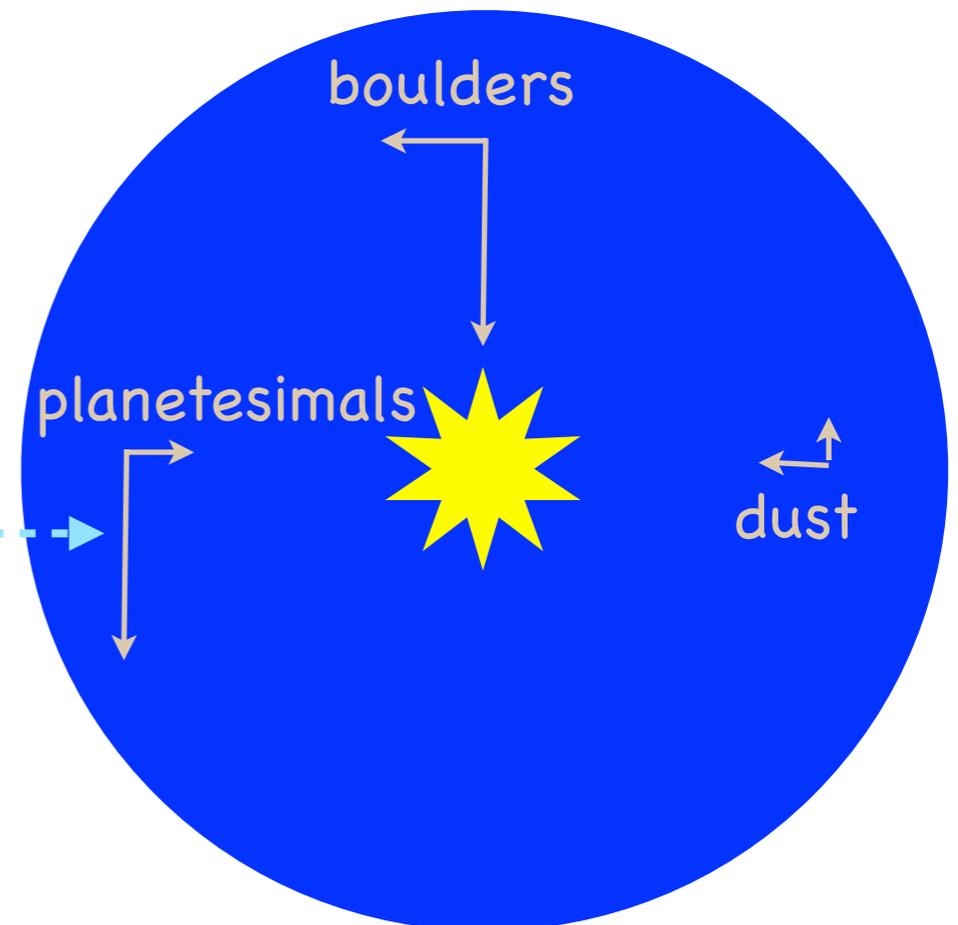
# Radial Drift Timescale Constraints (aka the “Meter-Size Barrier”)



sub-Keplerian gas rotation

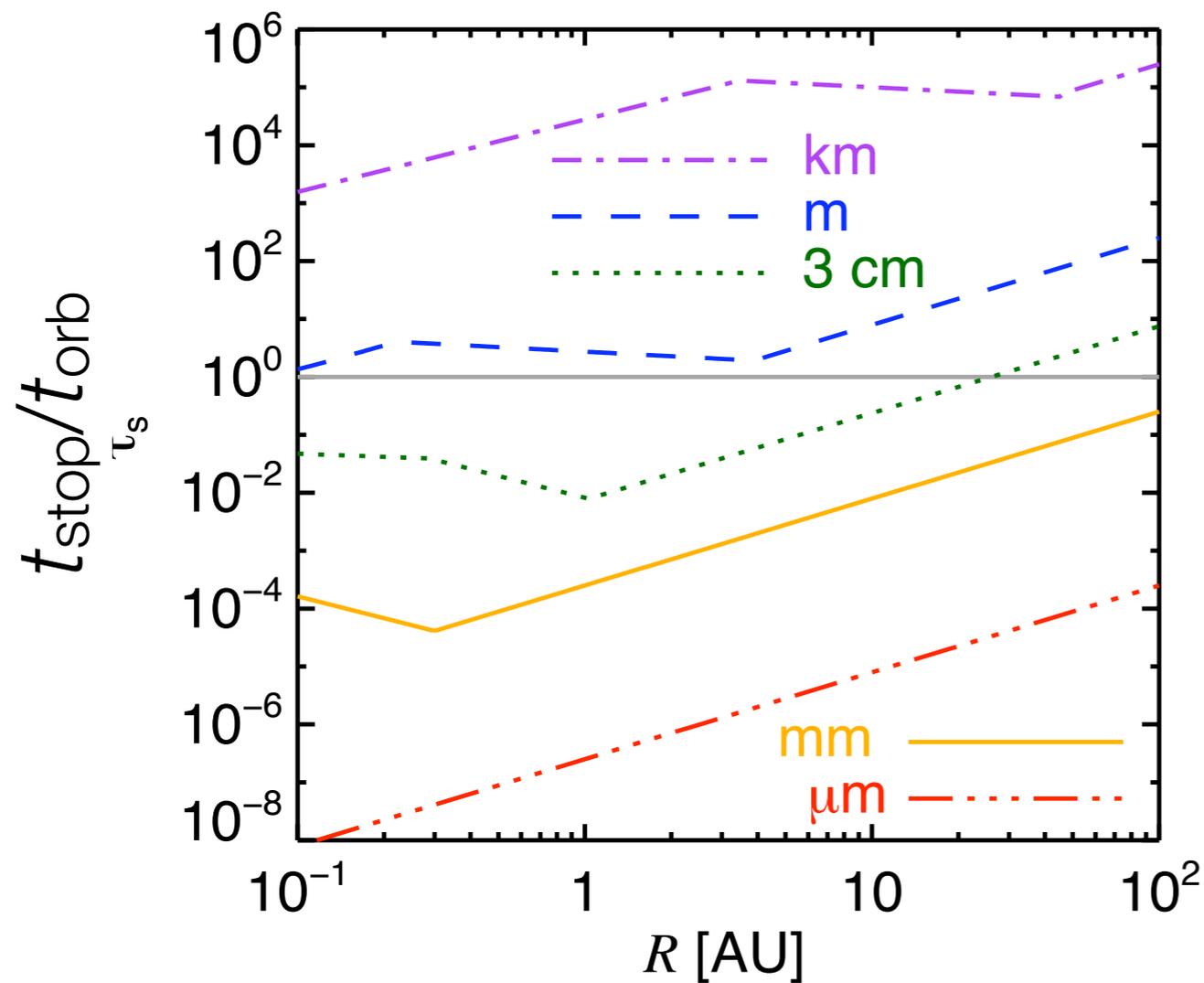
optimal coupling gives  
fastest drift:  
 $1 \text{ AU} / (50 \text{ m/s}) \sim 100 \text{ yr}$

max 50 m/s headwind

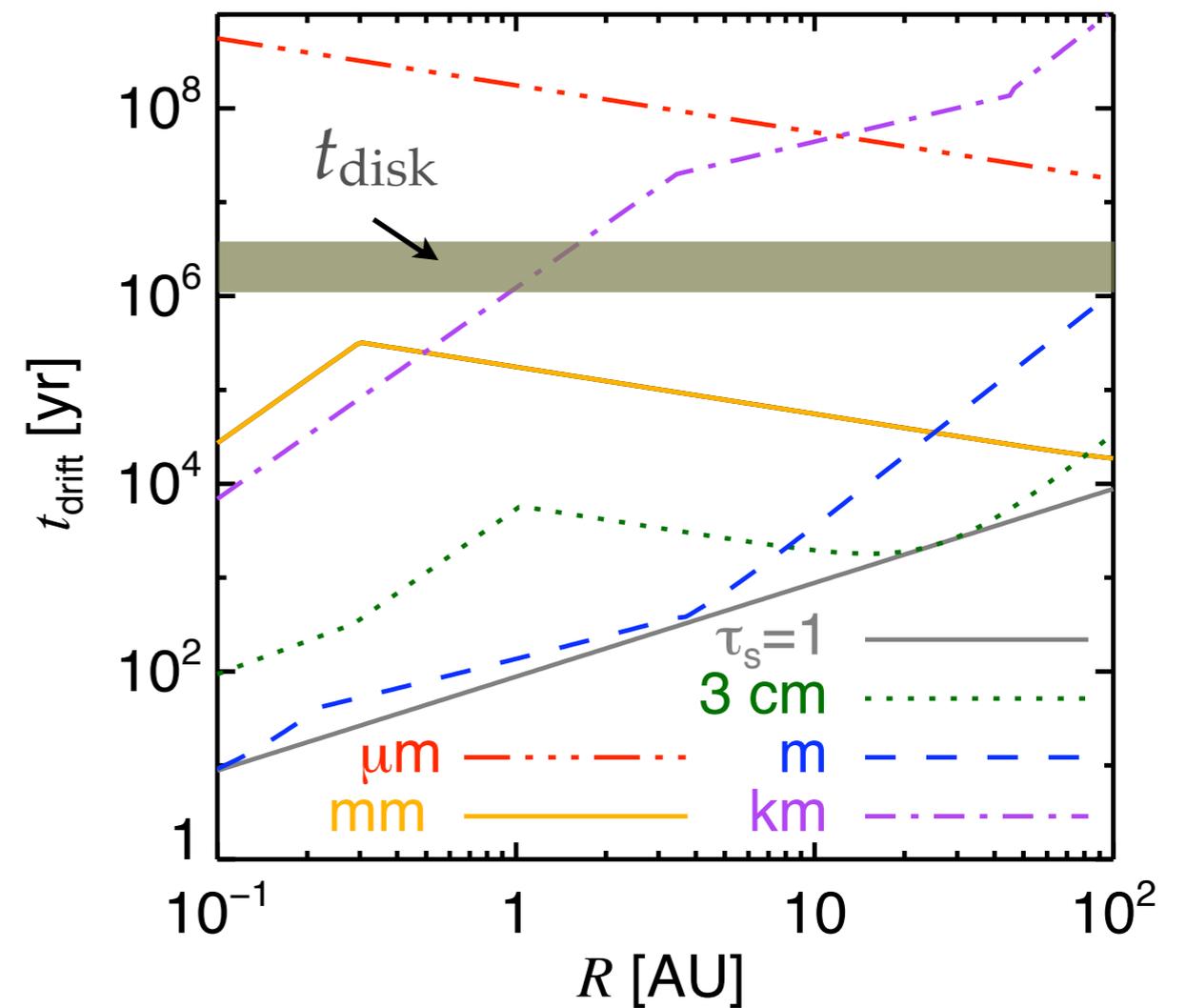


# Drag Forces in a “Minimum Mass” Disk Model

Dimensionless stopping time

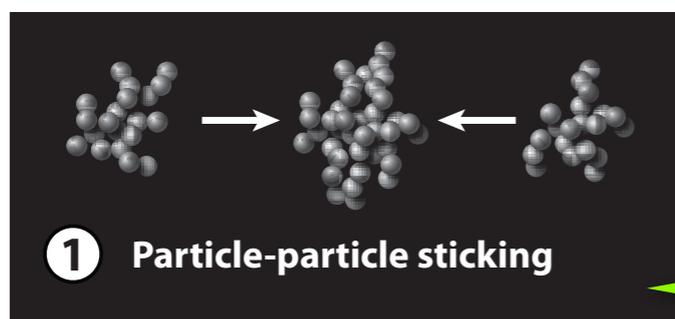
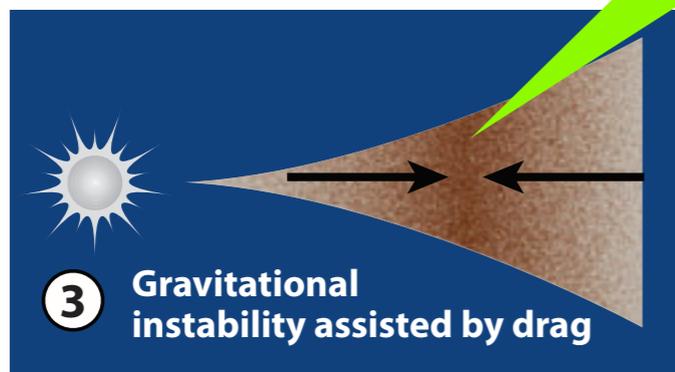
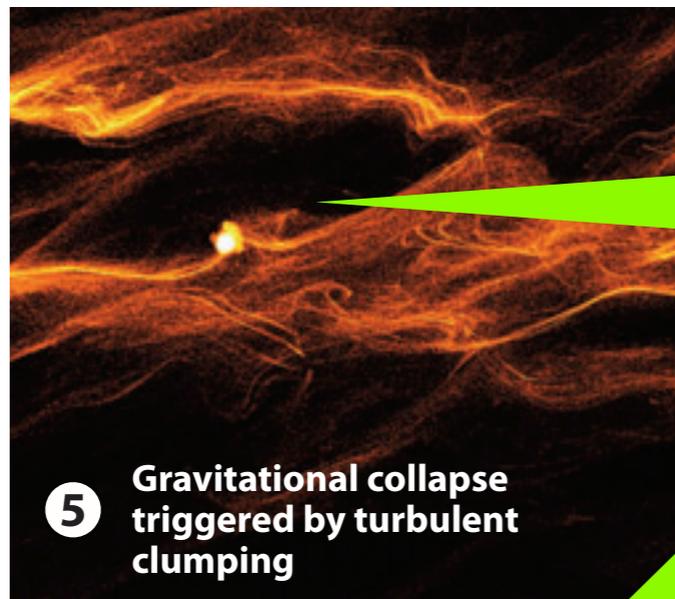


Radial drift time



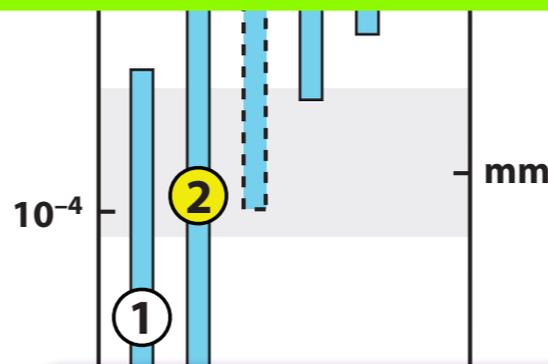
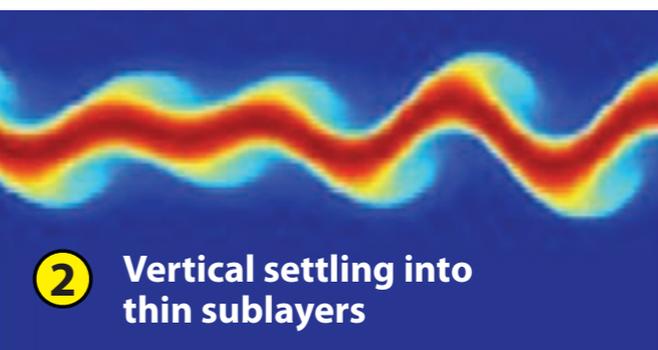
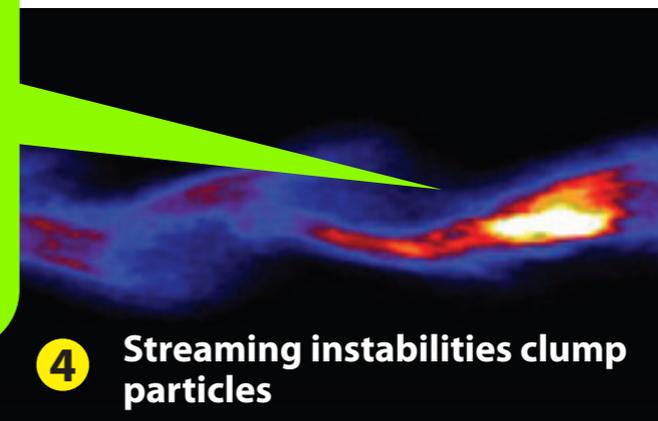
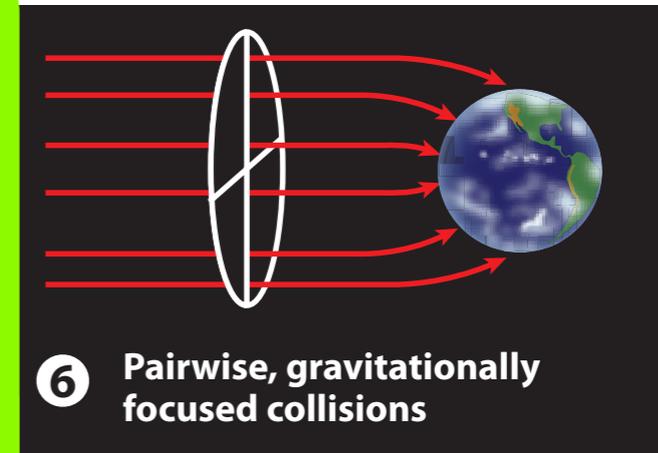
*Youdin (2010)*

# Climbing the size ladder



○ Growth    ● Concentration

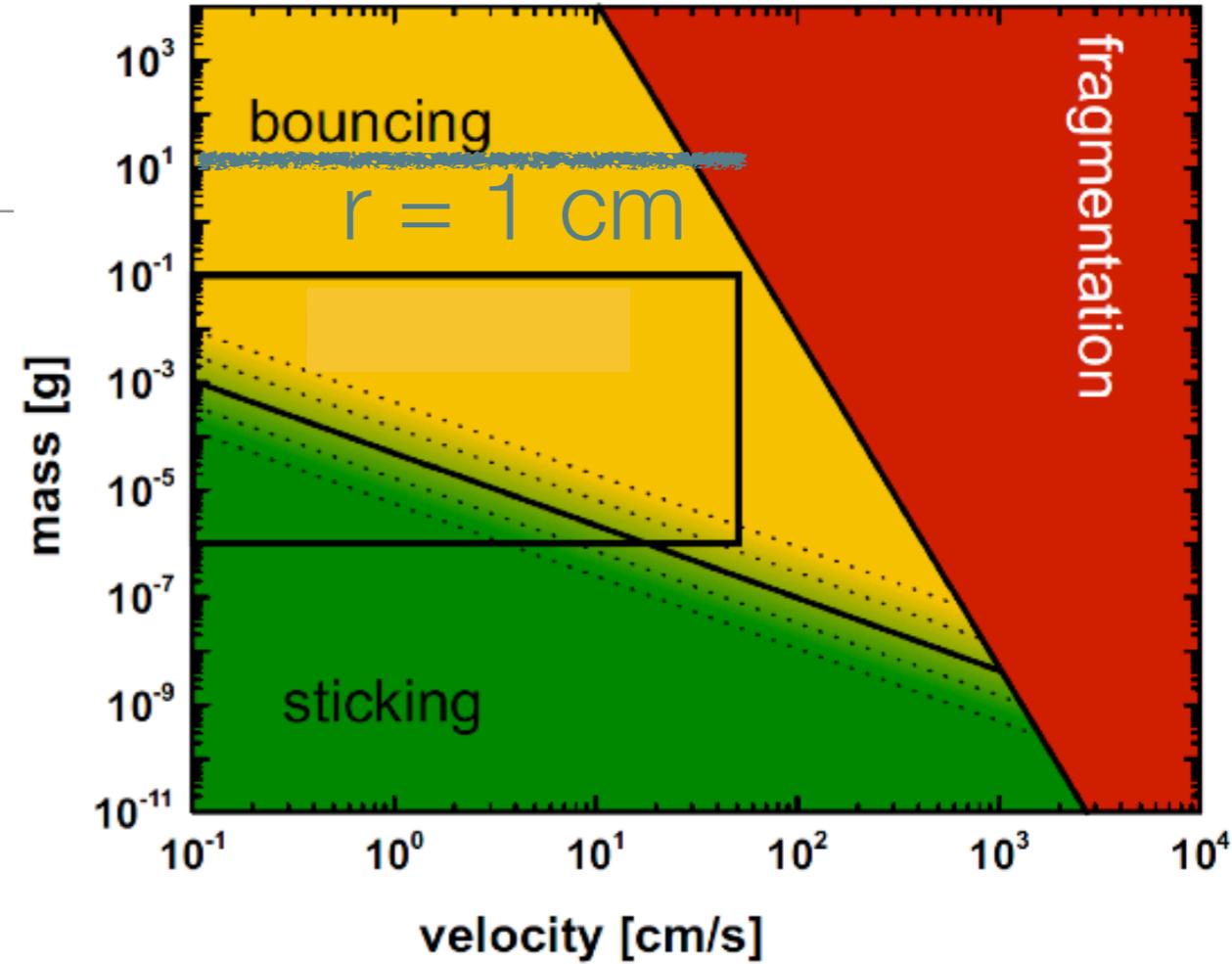
Top Down Formation  
(collecting particles with drag and self-gravity)



Bottom Up Growth

# Growth by Sticking

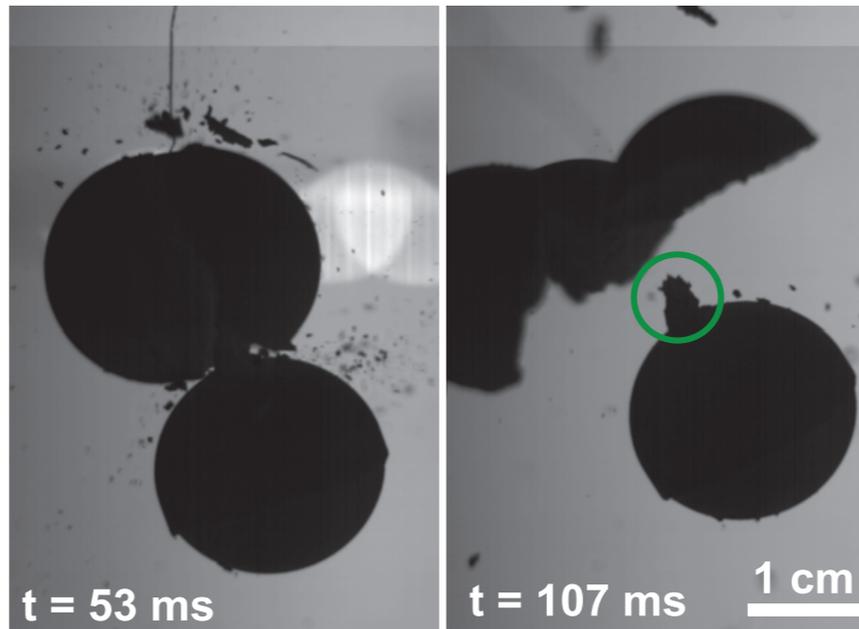
MANY OUTCOMES  
(GUTTLER ET AL. 2010)



inefficient growth  
from mm—km  
compounds  
meter-size barrier



**FRAGMENTATION**  
(BLUM & MEUNCH 1993)



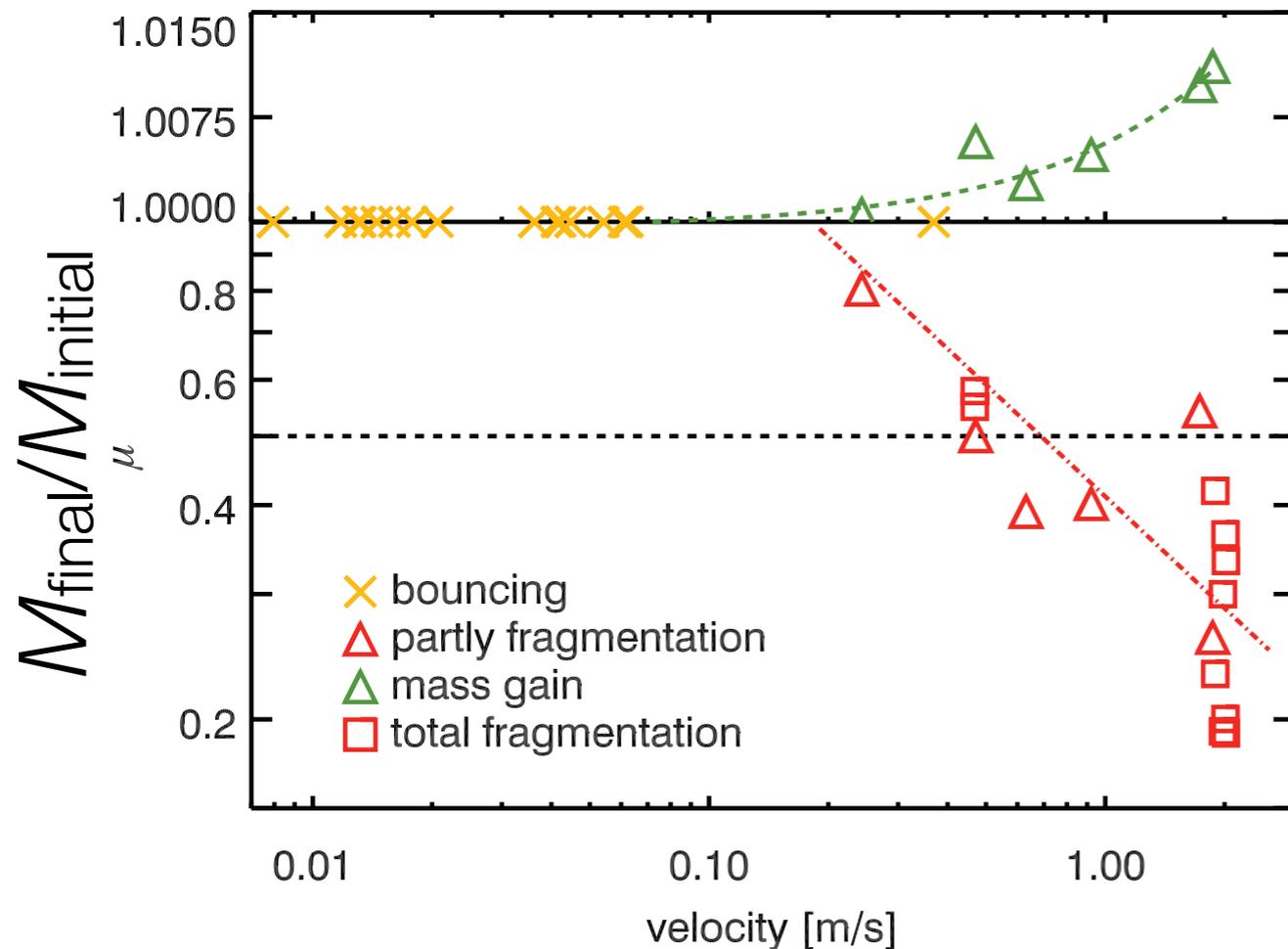
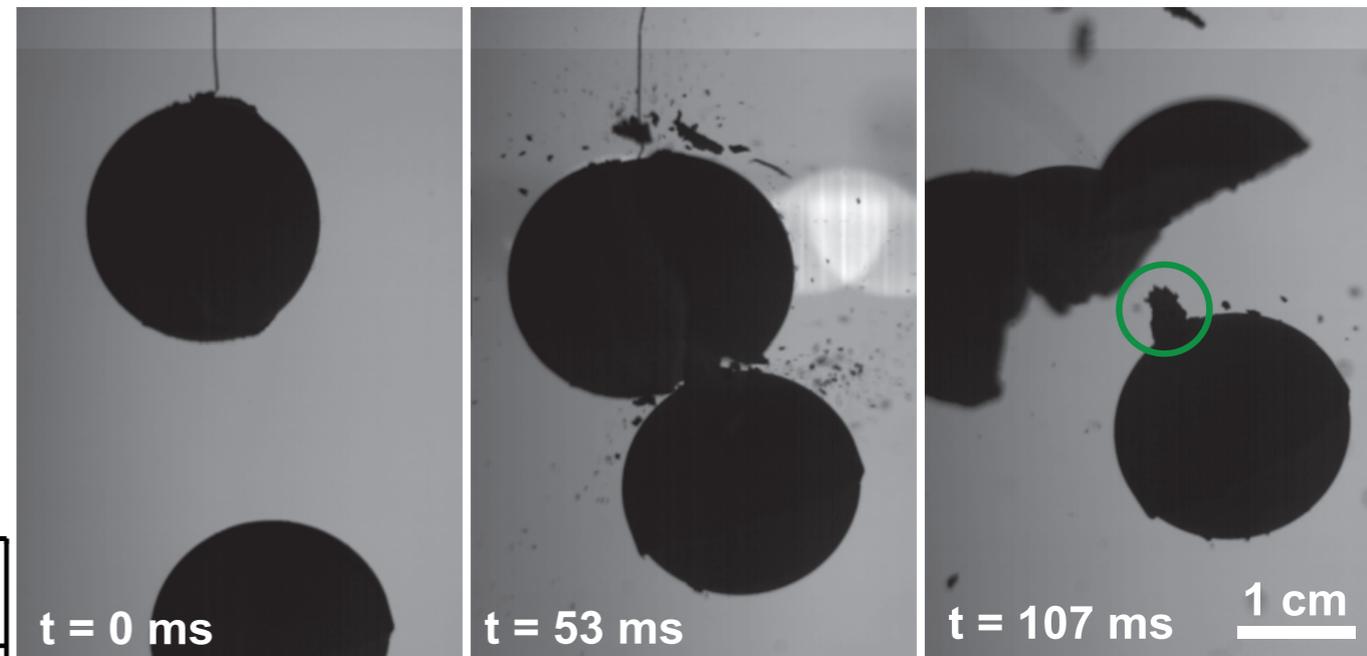
**MASS TRANSFER**  
(BEITZ ET AL. 2011)



**EROSION**  
(COLWELL 2003)

# The cm-size barrier of bouncing and fragmentation

Mass transfer  
overwhelmed by  
fragmentation



compare to:  
drift speeds  $\sim 50$  m/s  
turbulent speeds  $\sim$

$$10 \sqrt{\frac{\alpha}{10^{-4}}} \text{ m/s}$$

# Three modes of particle concentration

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1. Static

2. Passively Dynamic

3. Spontaneous

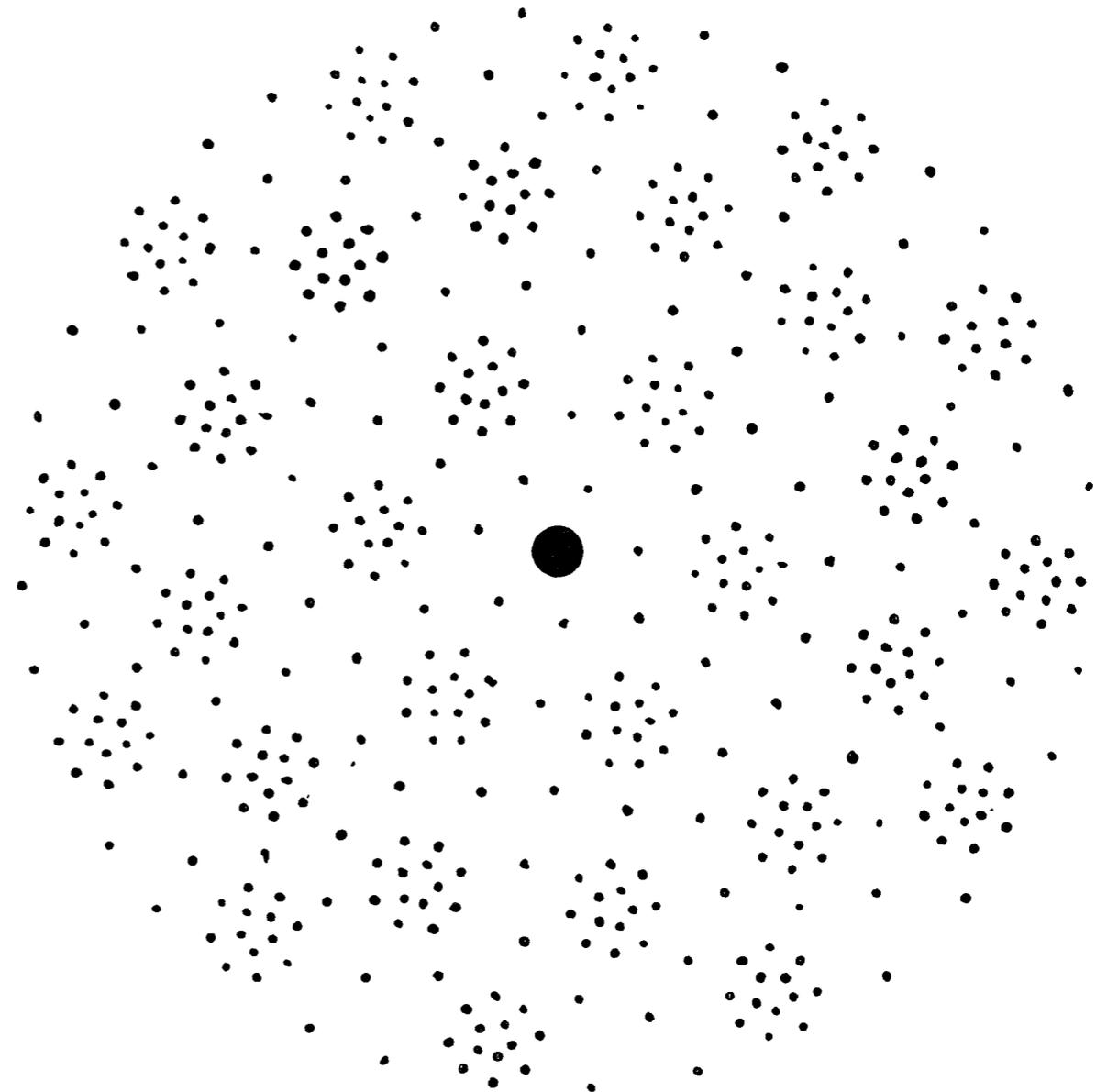


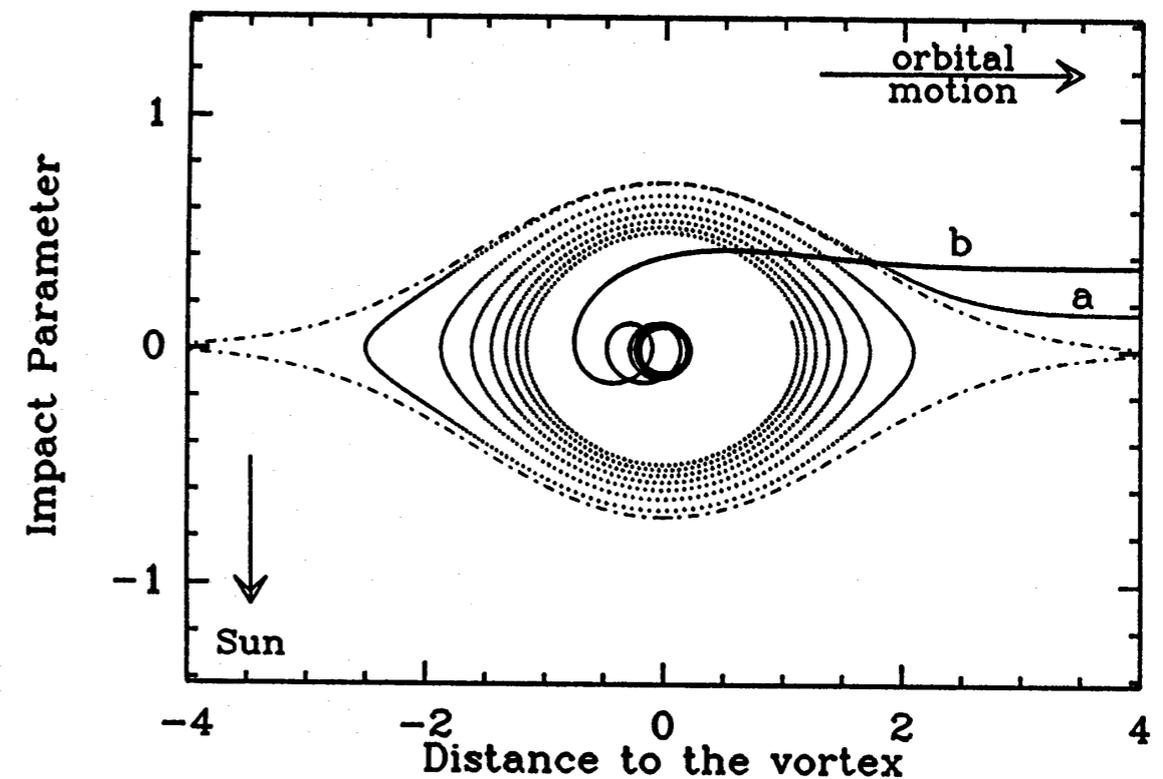
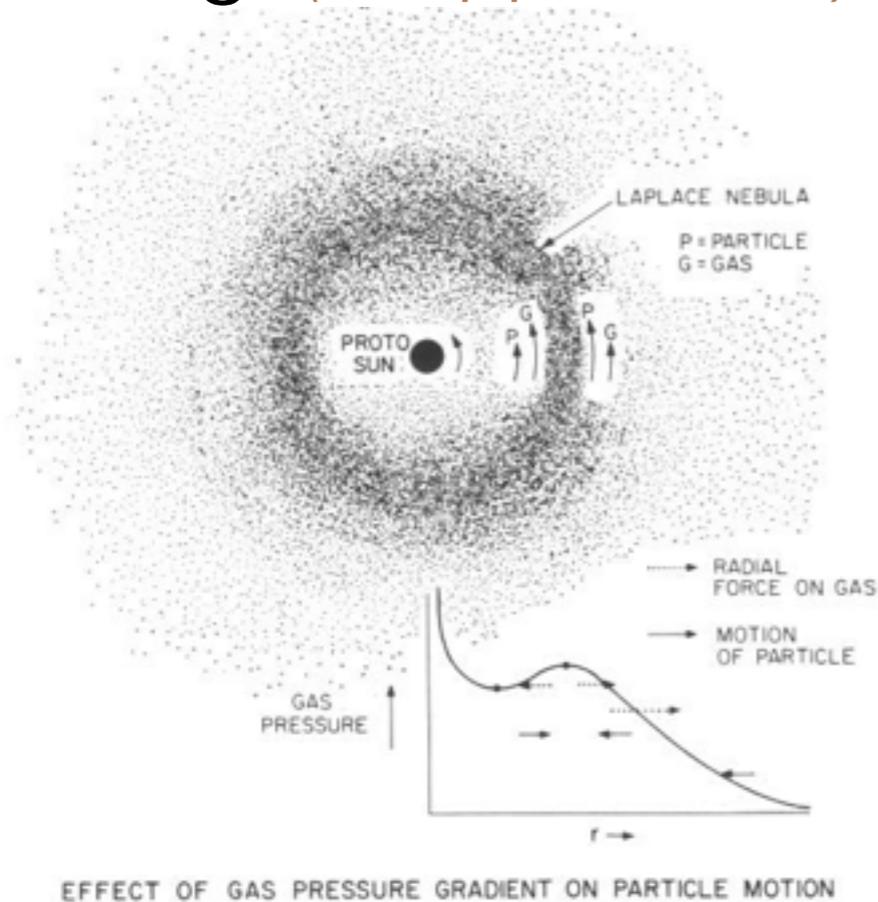
FIG. 3.

“local condensations”  
*(Edgeworth 1943)*

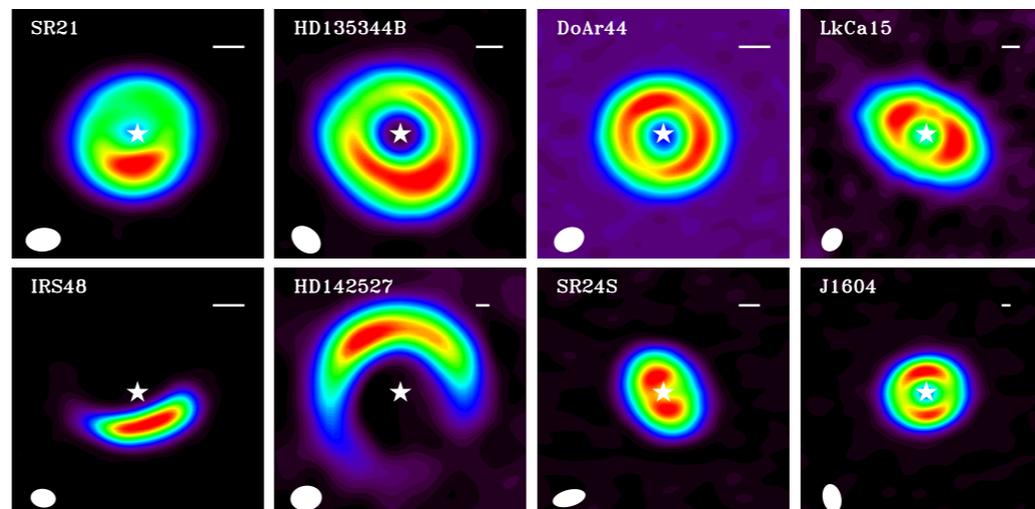
# 1. Static Concentration: Particles collect in long-lived pressure maxima.

Ring (*Whipple 1972*)

Vortex (*Barge & Sommeria 1995*)



sources: dead zone boundaries, snow lines, zonal flows, spiral arms and more



Seen by ALMA?!  
(*van Dishoeck et al. 2015*)

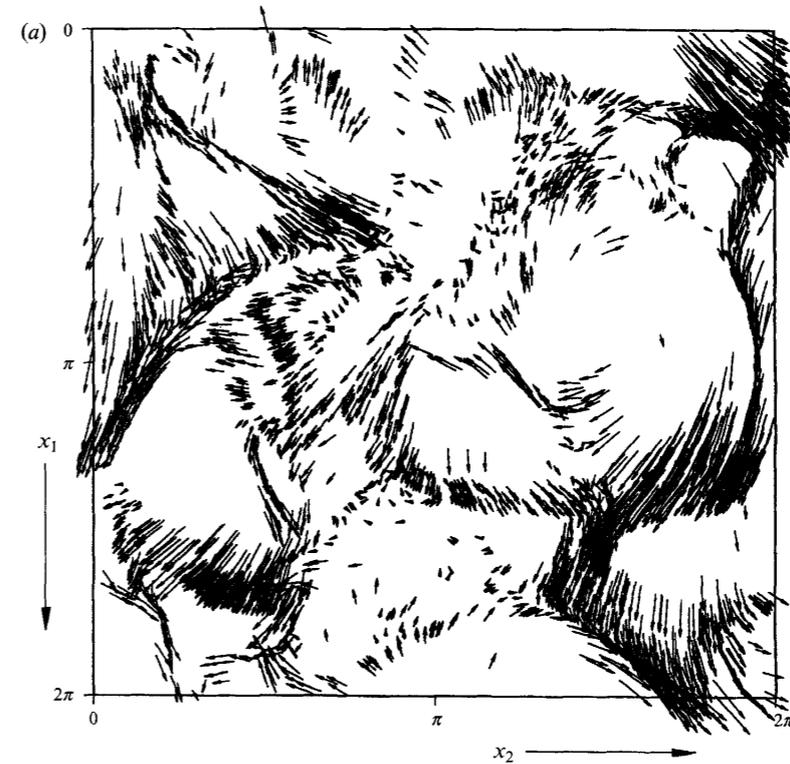
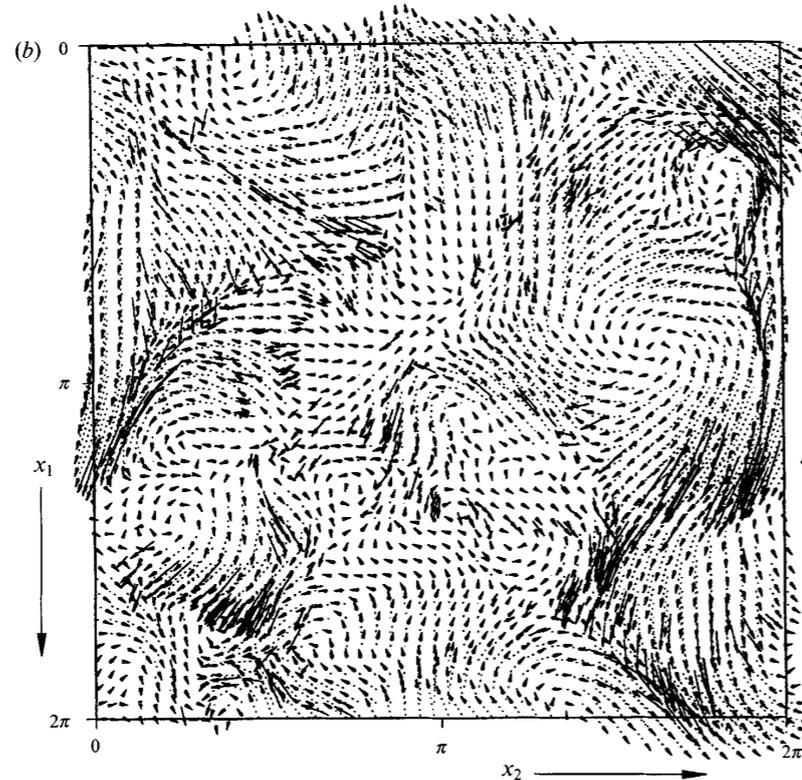
## 2. Passively Dynamic, i.e. Turbulent Concentration: Particles concentrate briefly by interacting with eddies.

---



“dust devils” are dynamic, but a different effect  
*(credit: Joseph Brauer)*

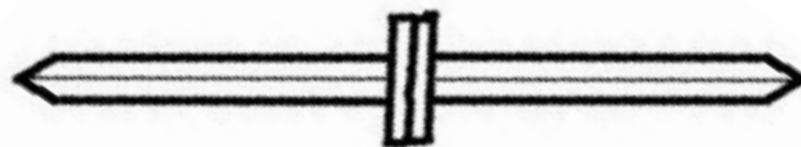
## 2. Passively Dynamic, i.e. Turbulent Concentration: Particles concentrate briefly when **expelled** from eddies.



*(Wang &  
Maxey  
1993)*

Are concentrations long-lived and massive enough to  
form planetesimals?

*(Cuzzi et al. 2008; Pan et al. 2011; Hopkins 2014)*



### 3. Spontaneous: Particles trigger their own concentration via the streaming instability



*(credit: Martine Maes)*

# The streaming instability: Complex behavior from simple ingredients

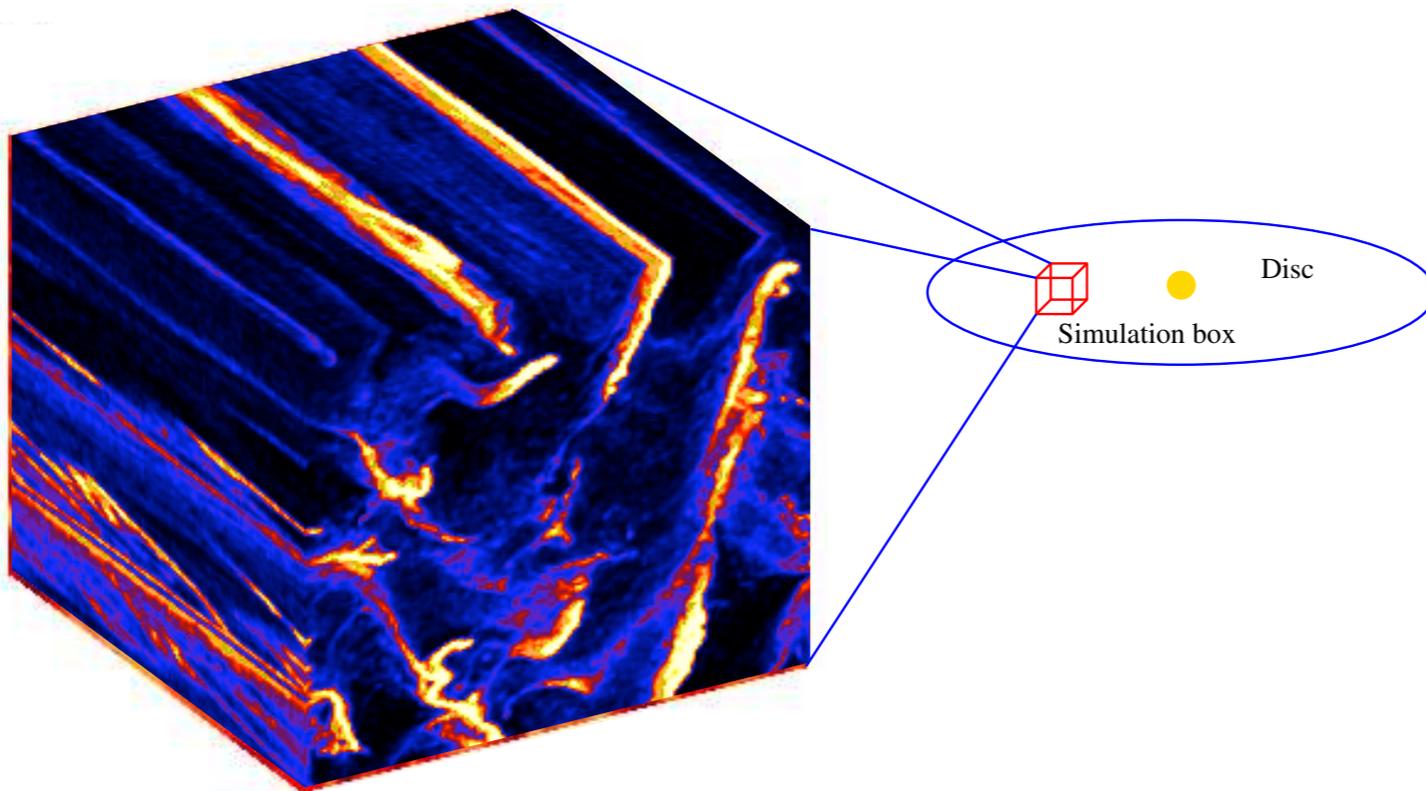
Two-way drag forces &  
Radial pressure gradient  
*(Youdin & Goodman 2005)*

$$\frac{\partial \rho_p}{\partial t} + \nabla \cdot (\rho_p \mathbf{V}_p) = 0,$$

$$\nabla \cdot \mathbf{V}_g = 0,$$

$$\frac{\partial \mathbf{V}_p}{\partial t} + \mathbf{V}_p \cdot \nabla \mathbf{V}_p = -\Omega_K^2 \mathbf{r} - \frac{\mathbf{V}_p - \mathbf{V}_g}{t_{\text{stop}}},$$

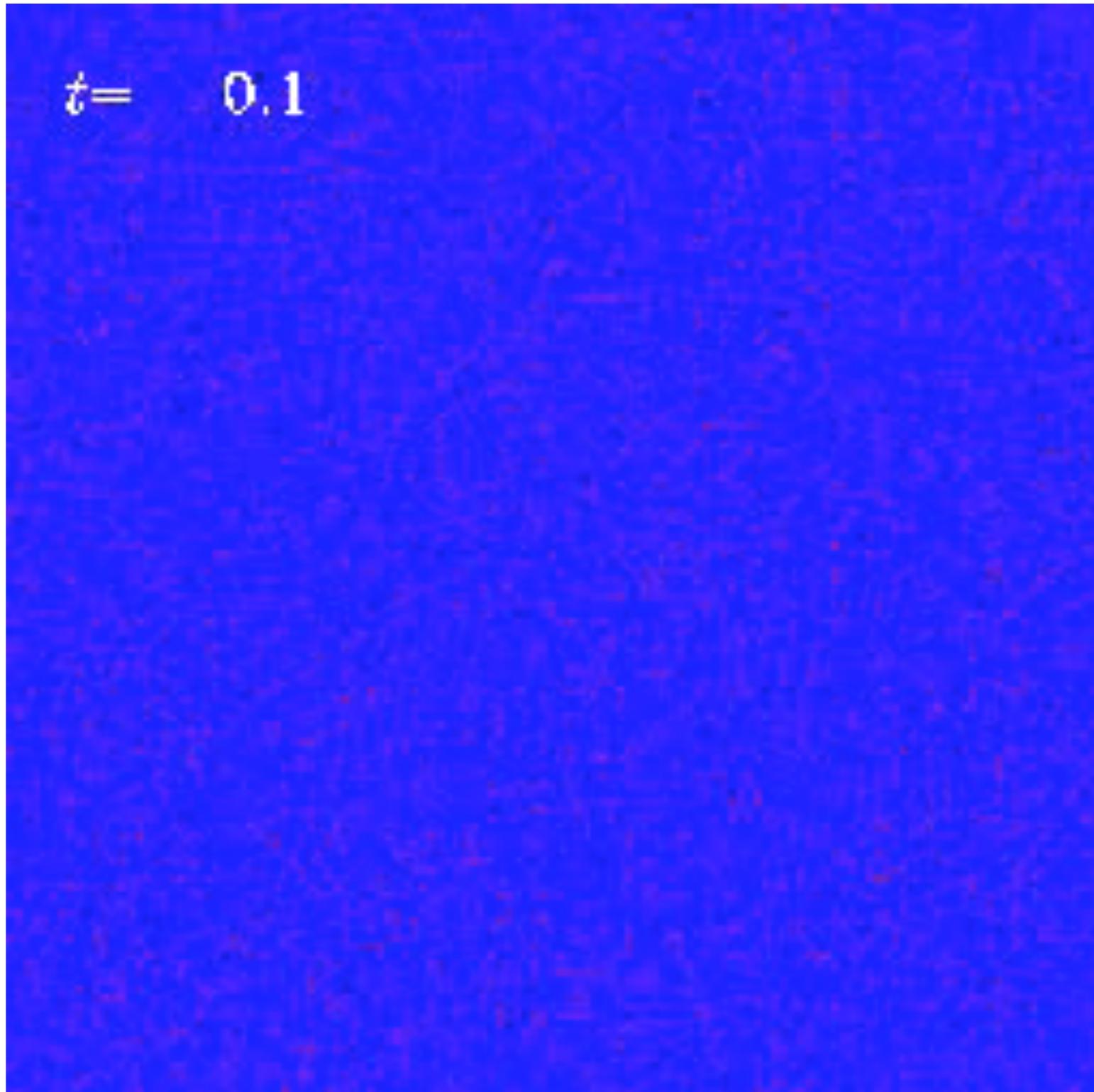
$$\frac{\partial \mathbf{V}_g}{\partial t} + \mathbf{V}_g \cdot \nabla \mathbf{V}_g = -\Omega_K^2 \mathbf{r} + \frac{\rho_p}{\rho_g} \frac{\mathbf{V}_p - \mathbf{V}_g}{t_{\text{stop}}} - \frac{\nabla P}{\rho_g},$$



Local box simulations of  
gas & “super”-particles  
*(Youdin & Johansen 2005,  
Johansen et al. 2007, etc;  
Bai & Stone 2010)*

# Particles trigger their own concentration via the streaming instability

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feeds off of  
radial drift  
*(Johansen &  
Youdin 2007)*

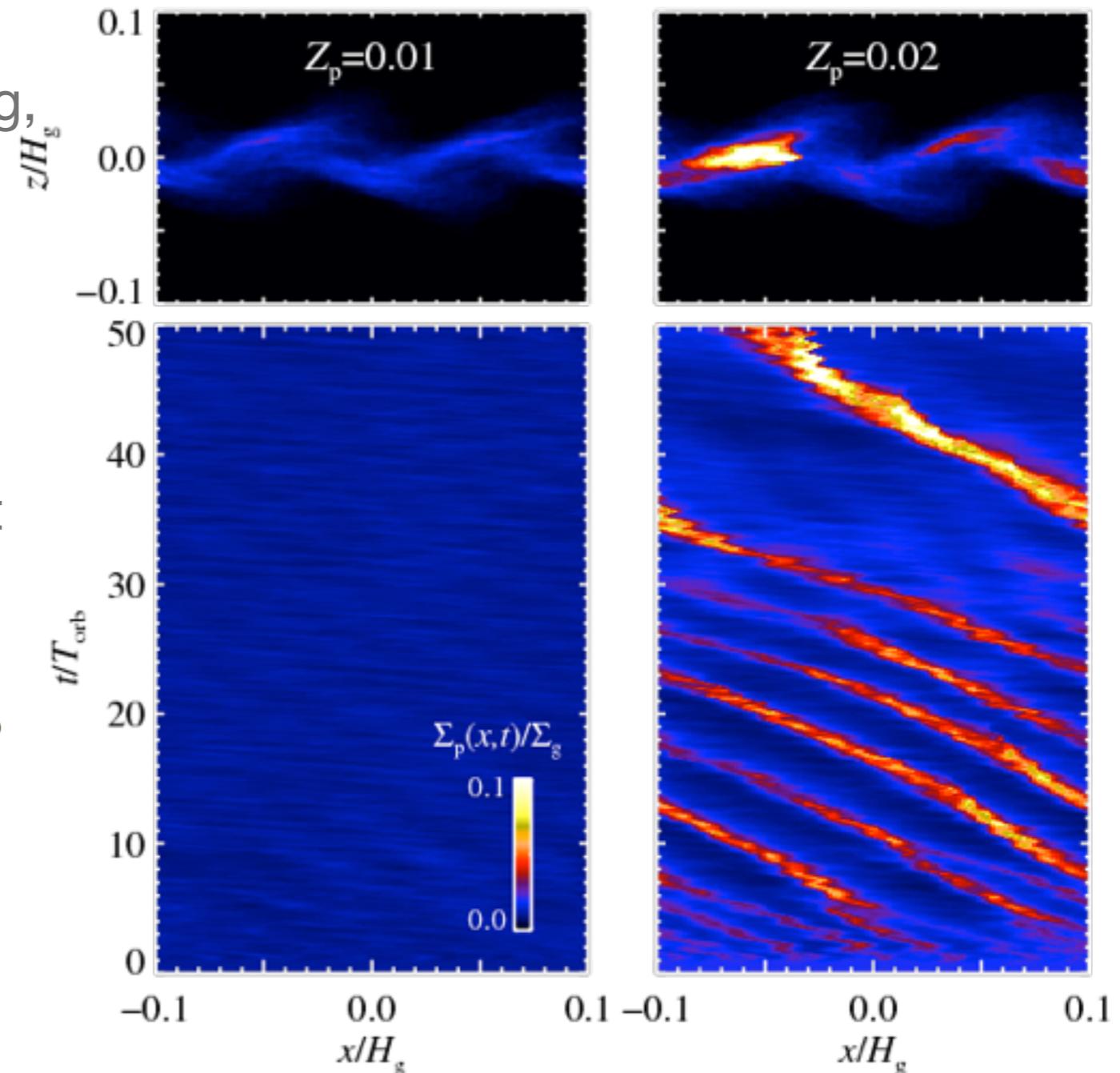
# Conditions for strong particle concentration

(Johansen, Youdin & Mac Low 2009)

“Sub-Solar:”  
weak clumping

“Super-Solar:”  
strong clumping

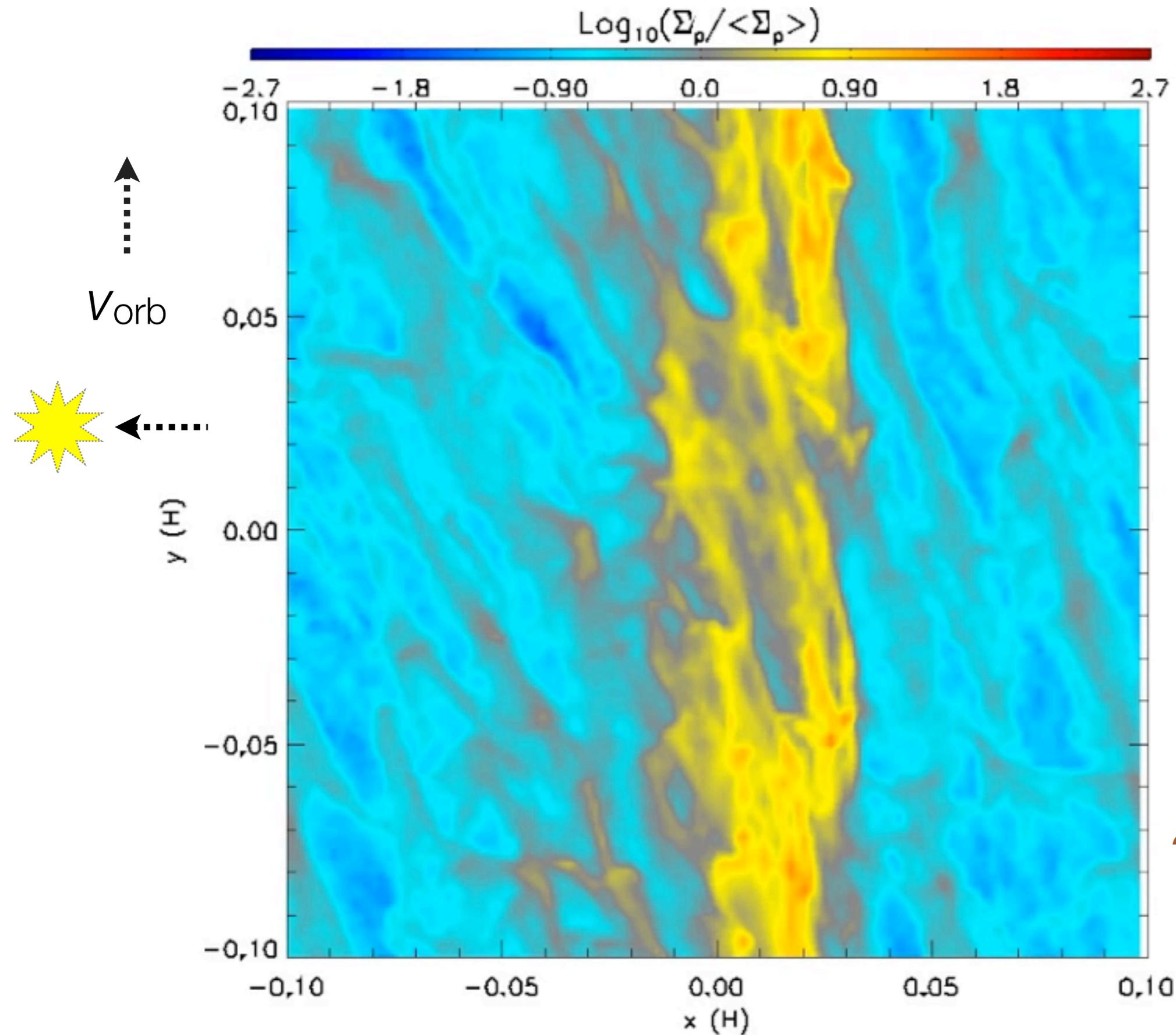
1. Particle sizes near optimal coupling,  
 $\tau_s \approx 0.1-1.0$
2. Particle-gas ratio,  $Z \gtrsim 1\%$ 
  - varies w/ radial pressure gradient  
(Bai & Stone, 2010b)
  - exoplanet-metallicity correlation?
- Role of box size and boundary conditions? *See poster by Rixin Li*



Particle density:  
radius vs. height (*top*)  
radius vs. time (*bottom*)

$\tau_s = 0.1-0.4$ ,  
3-12 cm @ 5 AU

# Streaming Inst. triggering planetesimal formation



Gravitational collapse from ~few cm-sizes into ~100 km, planetesimals

*(Simon et al., in prep; also Johansen, Youdin & MacLow 2009; Johansen et al 2007, 2012)*

# The bouncing and fragmentation barriers remain

- What if particles don't grow large enough, to  $\tau_s \approx 0.1-1.0$ ?

A. Less gas

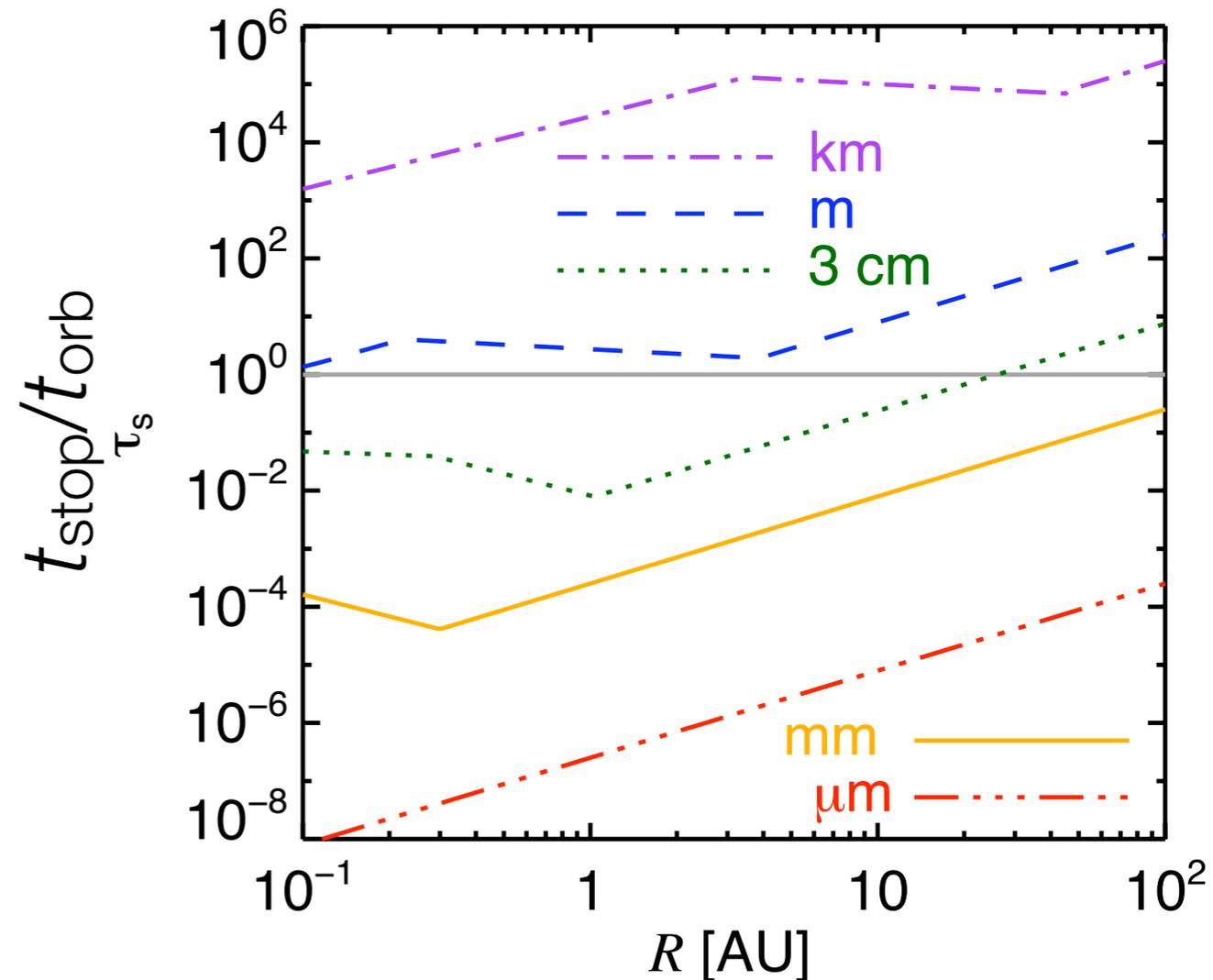
B. Look at interplay with other mechanisms

- pressure bumps

- direct gravitational instability (*Safronov '69, Goldreich & Ward '73*)

Goal:

$\sim 10$  cm @ 1 AU,  
 $\sim$ mm @ 30 AU



# Slow “secular” gravitational instabilities collect small particles into wide rings



- Current studies analytic  
*(Ward 1976; Youdin 2005, 2011; Shariff & Cuzzi 2011, Takahashi & Inutsuka 2014)*
- Long time and length scales
- Opportunity to explain observed disk structures

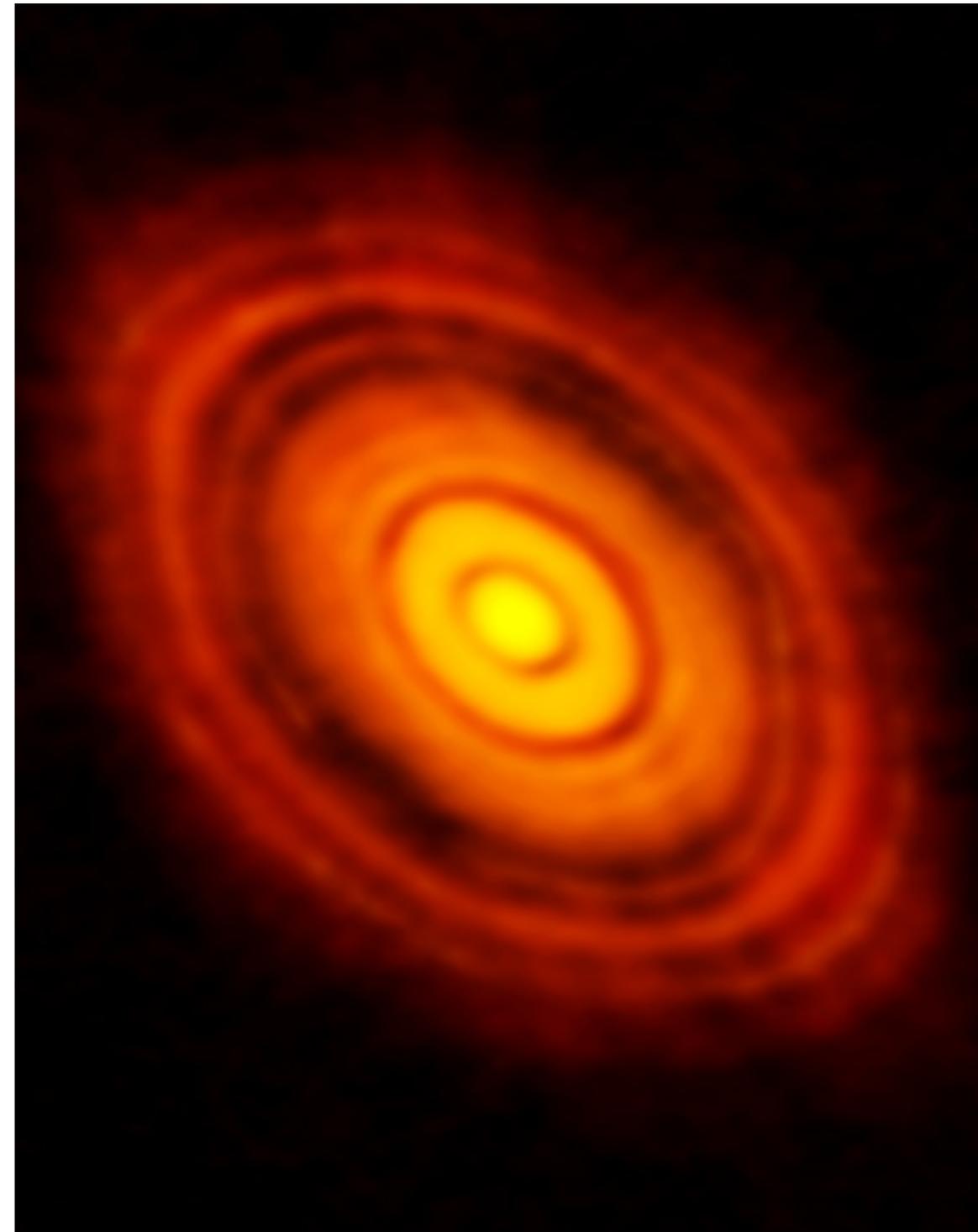


image: ALMA

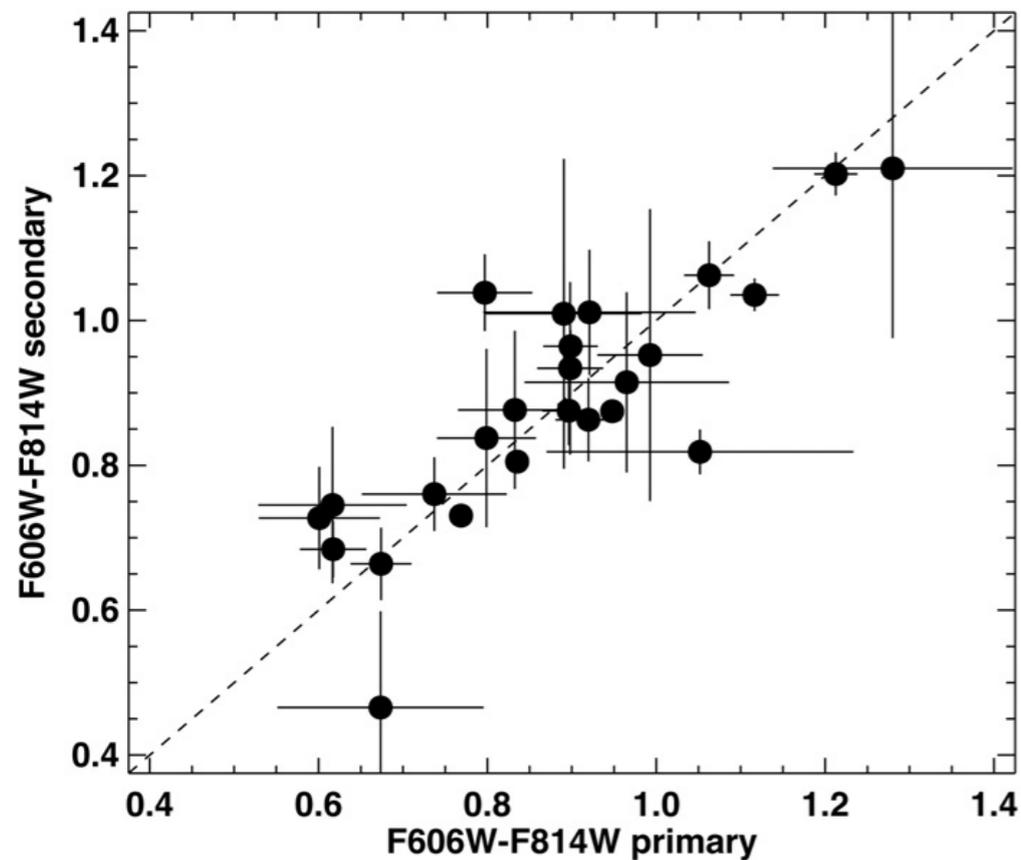
# SS evidence for Gravitational Collapse

image: John Laborde



## KBO binary colors match!

*(Benecchi et al. 2009,  
Nesvorny, Youdin & Richardson 2010)*



## Comets have tails!

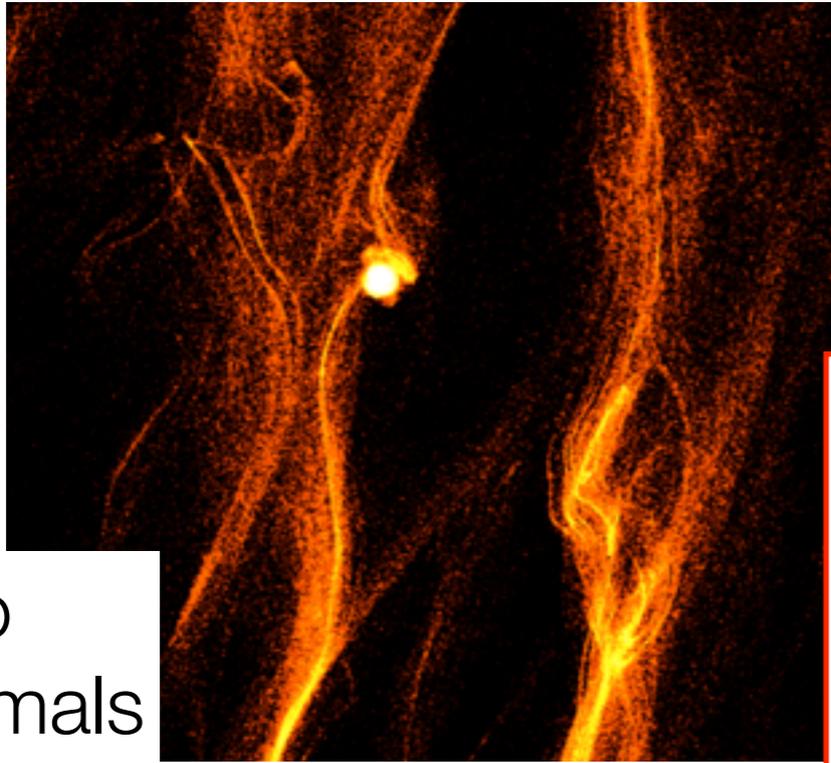
*(Blum et al. 2014)*

Comets formed in solar-nebula instabilities! – An experimental and modeling attempt to relate the activity of comets to their formation process

J. Blum <sup>a</sup>, B. Gundlach <sup>a,\*</sup>, S. Mühle <sup>a</sup>, J.M. Trigo-Rodriguez <sup>b</sup>

# Four Stages of Planet Formation: The Core Accretion Model

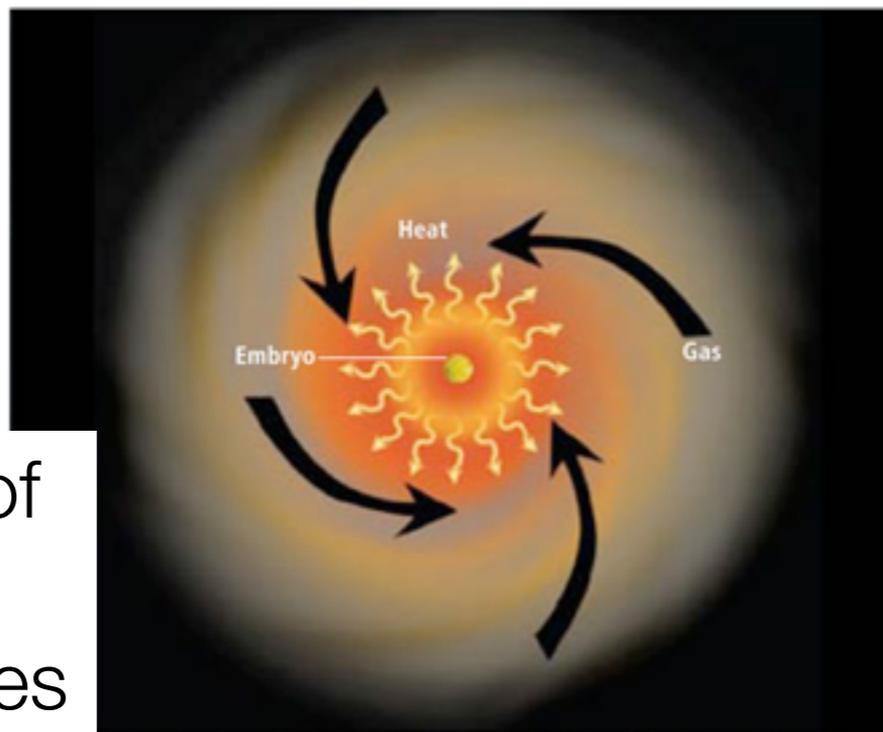
1. Dust to  
Planetesimals



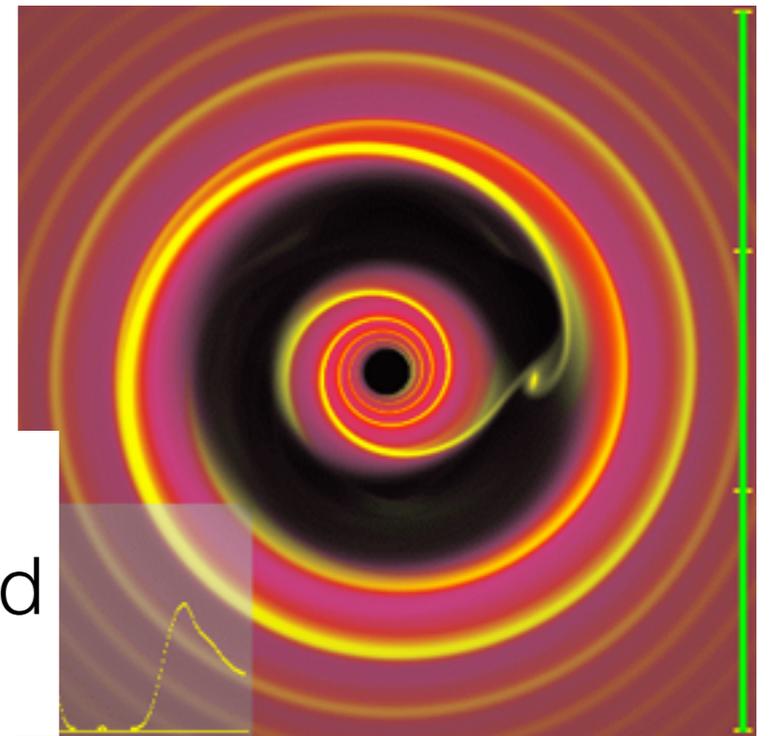
2. From  
Planetesimals  
to Planets &  
Cores



3. Growth of  
Gas Giant  
Atmospheres



4. Planet  
Migration and  
Scattering



*Credits: A. Johansen, F. Sulehria, D. Lin, P. Armitage*

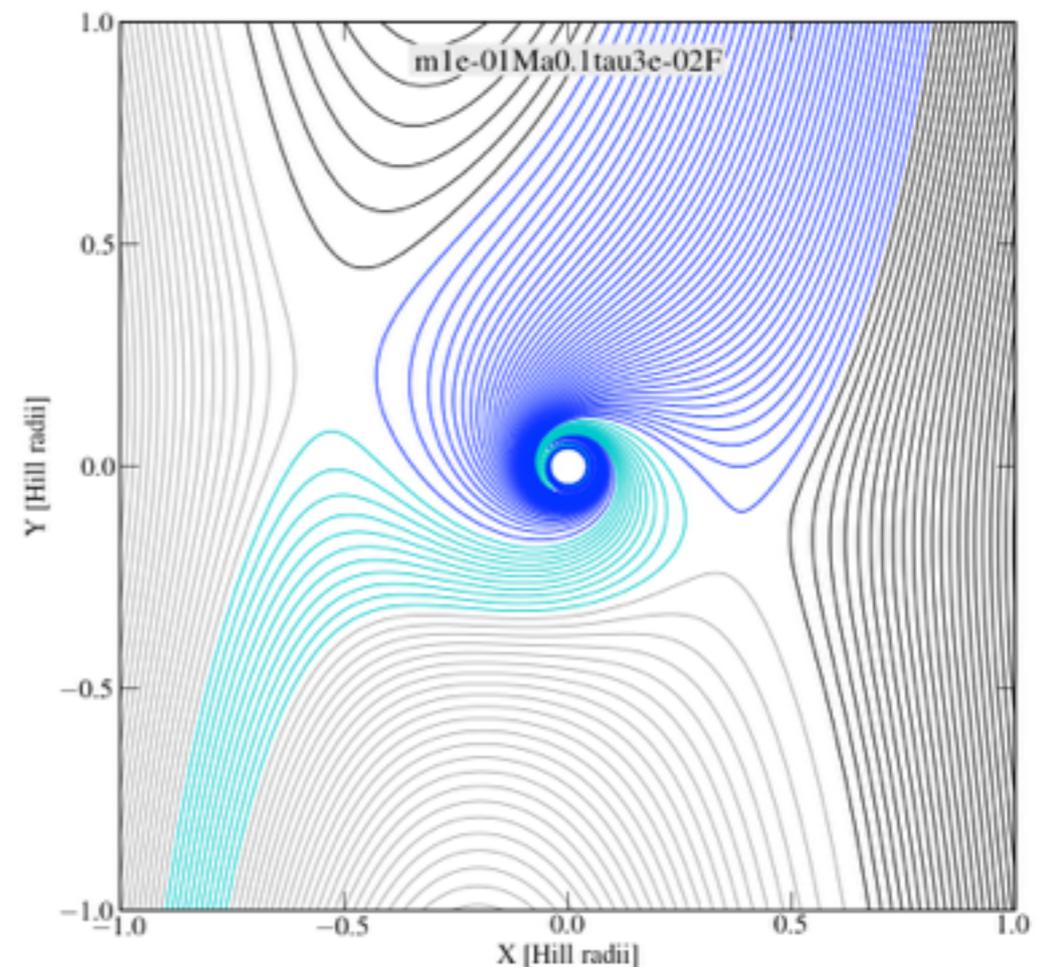
# Options for growing terrestrial planets and cores

---

## 1. Giant impacts



## 2. Aerodynamically assisted “pebble accretion”



*Ormel & Youdin (unpublished)*

# Key Issues in Terrestrial Planet & Core Growth

## 1. Timescale

- Potentially faster for aerodynamic pebbles

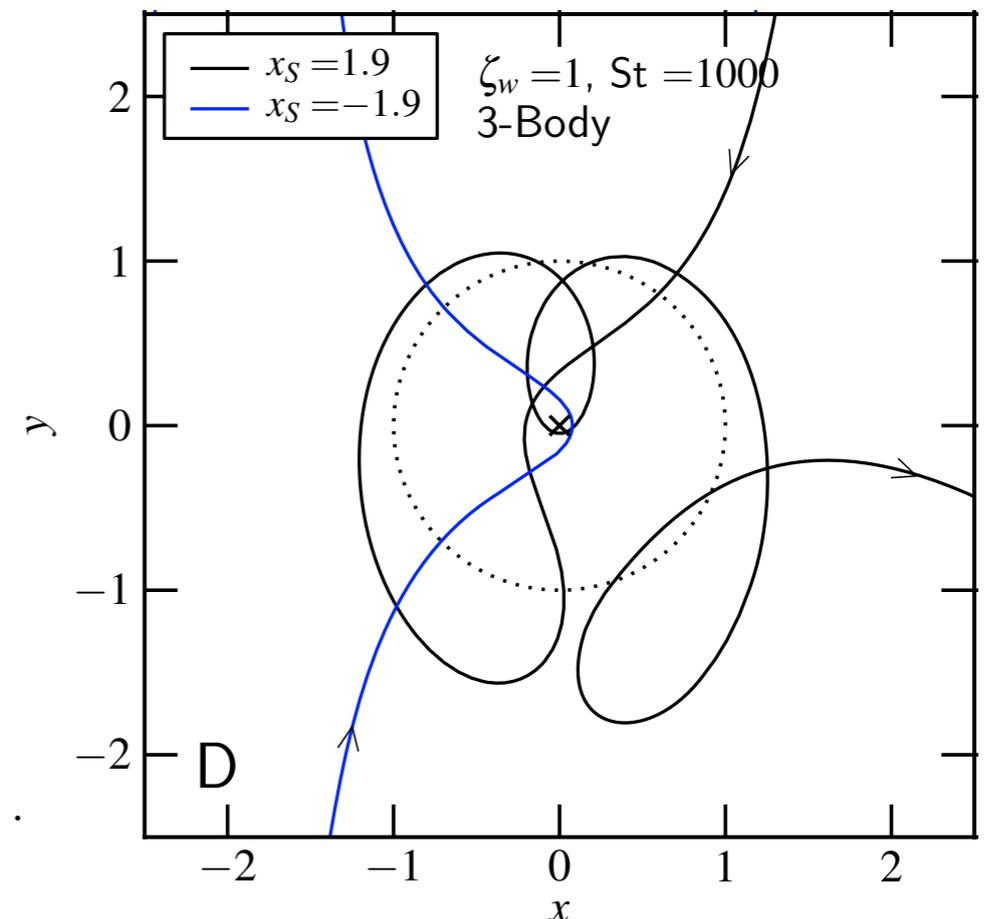
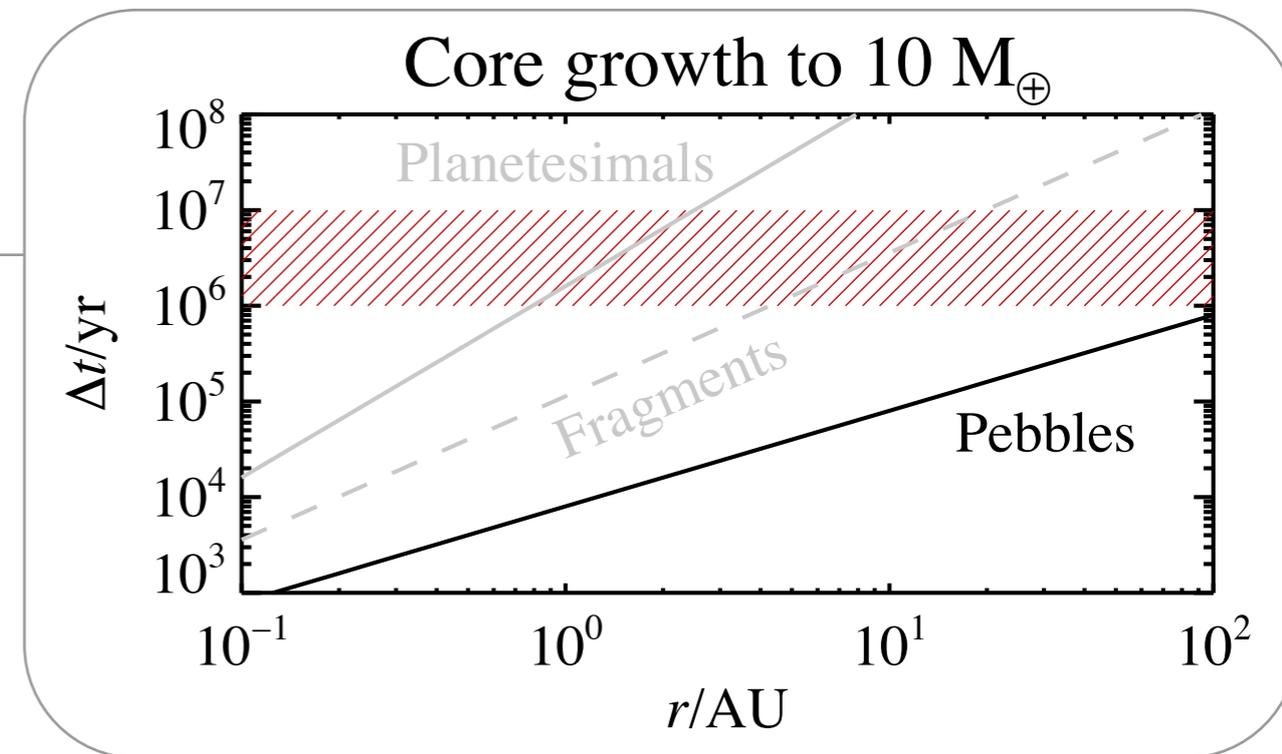
## 2. Availability of Mass

- Planetesimal accretion stalls at “isolation mass”
- Radial drift overcomes isolation

$$m_{iso} = \frac{(2\pi B\Sigma)^{3/2}}{(3M_\star)^{1/2}} a^3 \approx 0.08 \left(\frac{B}{7}\right)^{3/2} \left(\frac{FZ_{rel}}{0.33}\right)^{3/2} \left(\frac{M_\star}{M_\odot}\right)^{-1/2} \left(\frac{a}{AU}\right)^{3/4} M_\oplus$$

*Youdin & Kenyon (2012)*

*Lambrechts & Johansen (2012)*



The problem w/ weak drag

*Ormel & Klahr (2012)*

# Summary

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color me bad  
image?

- Planetesimal formation
  - Starts with dust coagulation
  - Ends with gravitational collapse
  - Streaming instability and other particle concentration mechanisms bridge the “meter-size barrier”
- Terrestrial planet and core formation
  - New: an early phase of aerodynamic pebble accretion