

Post-formation dynamical evolution

Smadar Naoz
UCLA

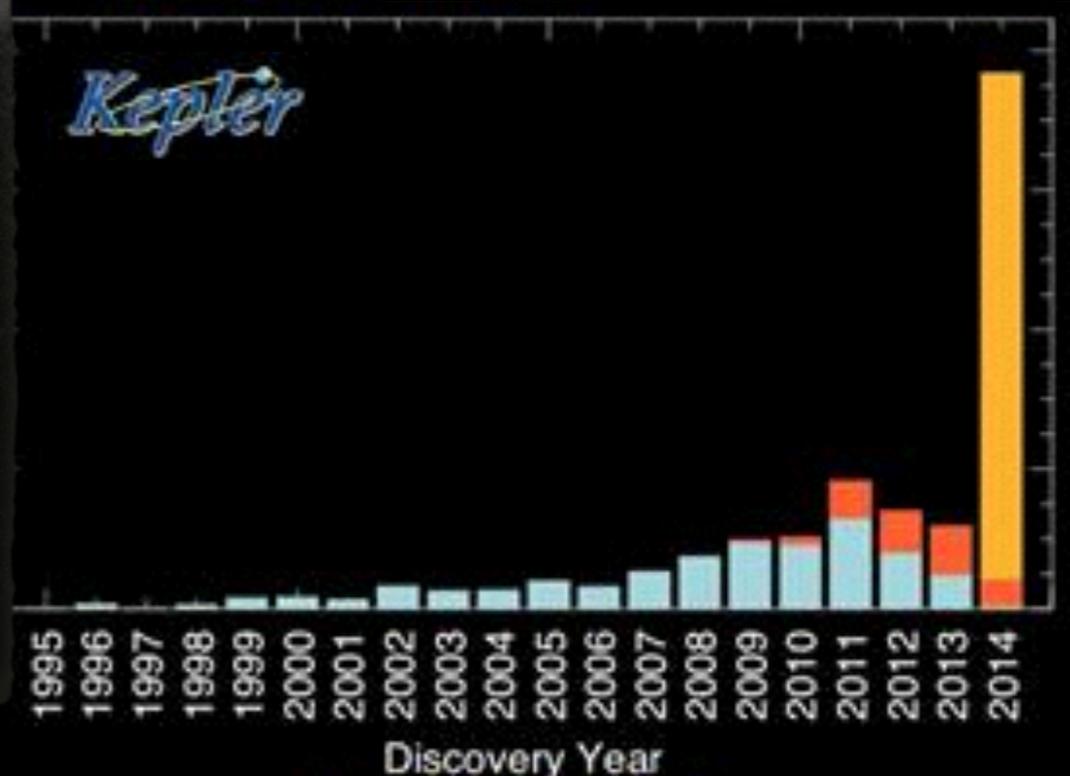
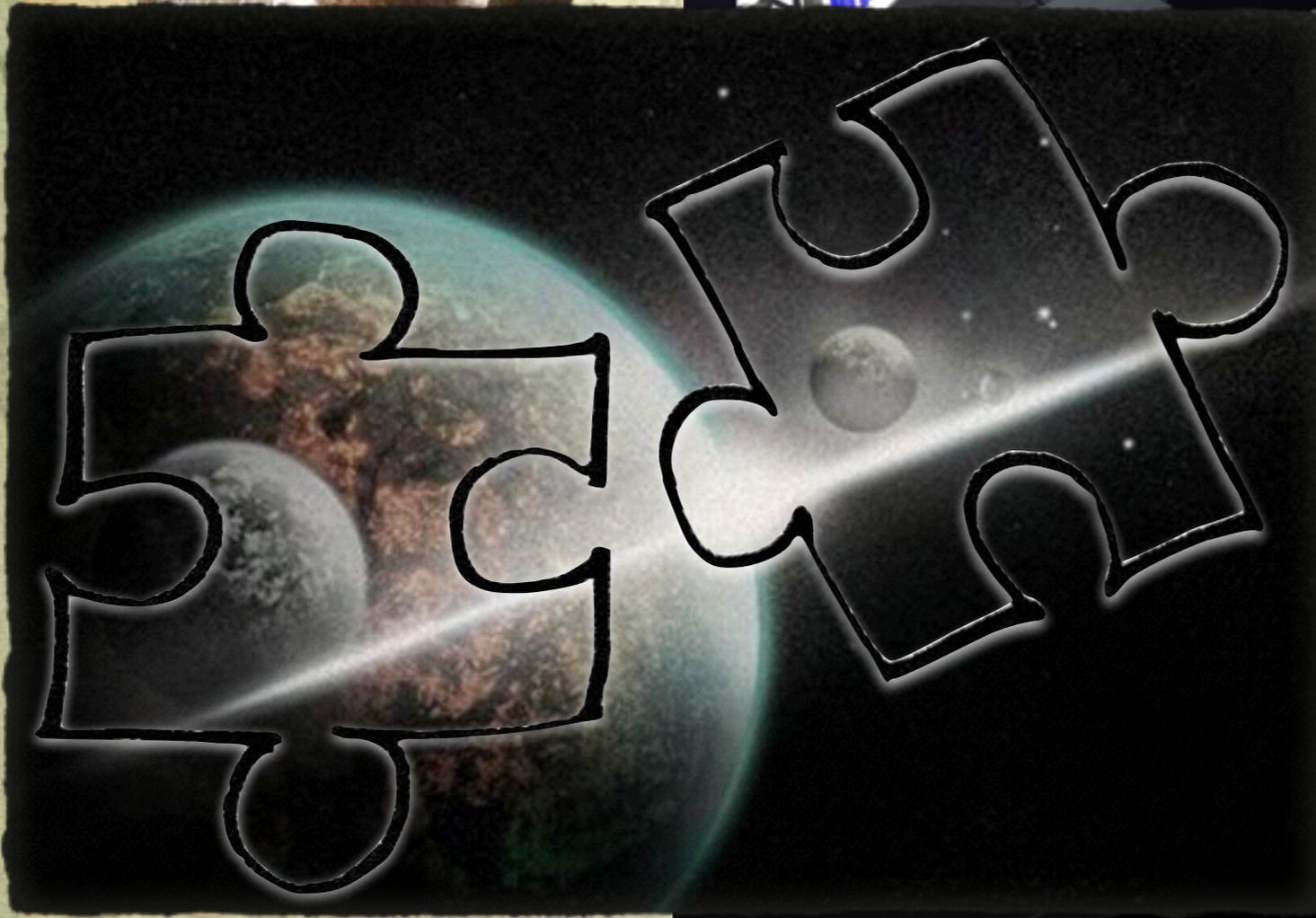
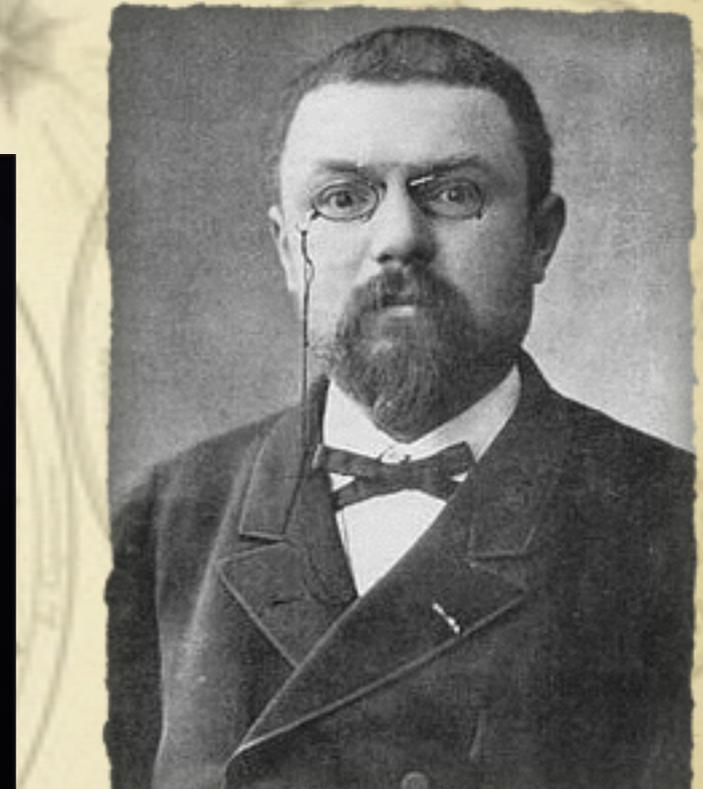
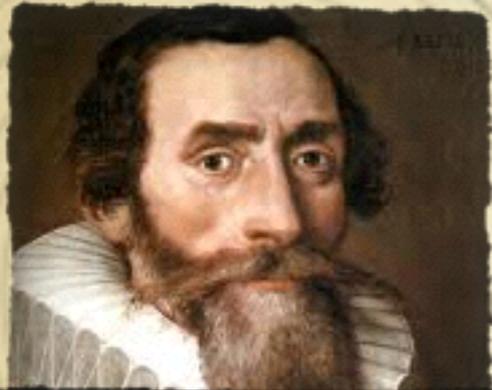


Sagan Workshop
July 2015

Copernicus 1661



AstroDynamics

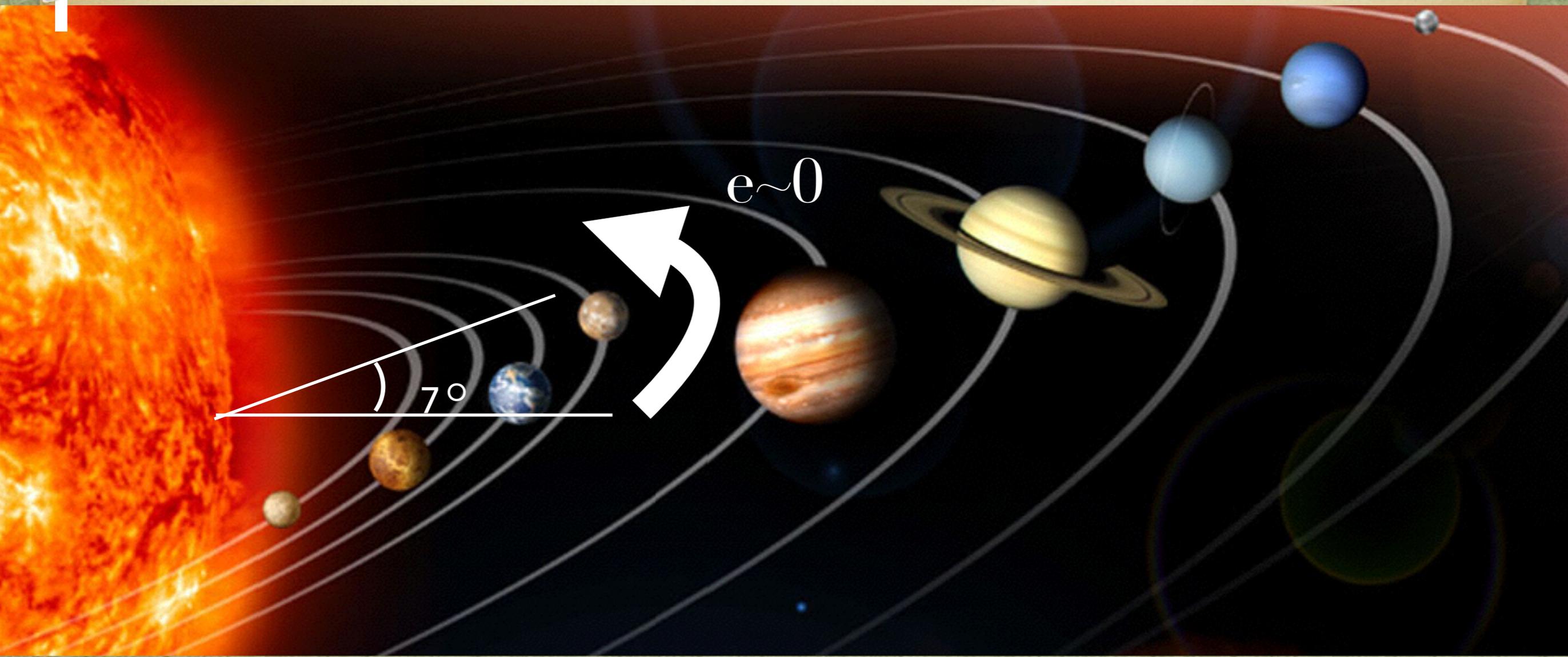


credit:Natalie Batalha

26 Feb 2014

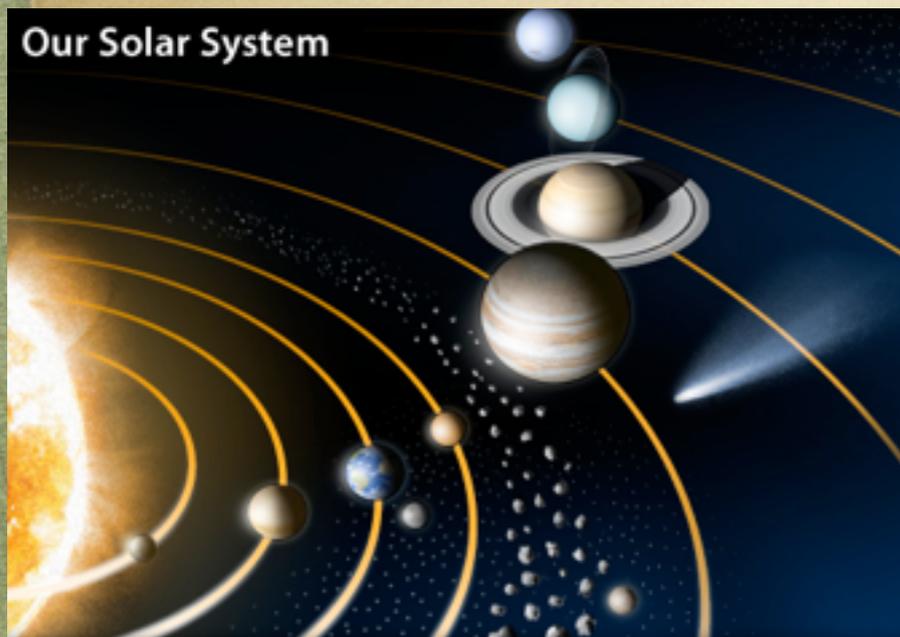
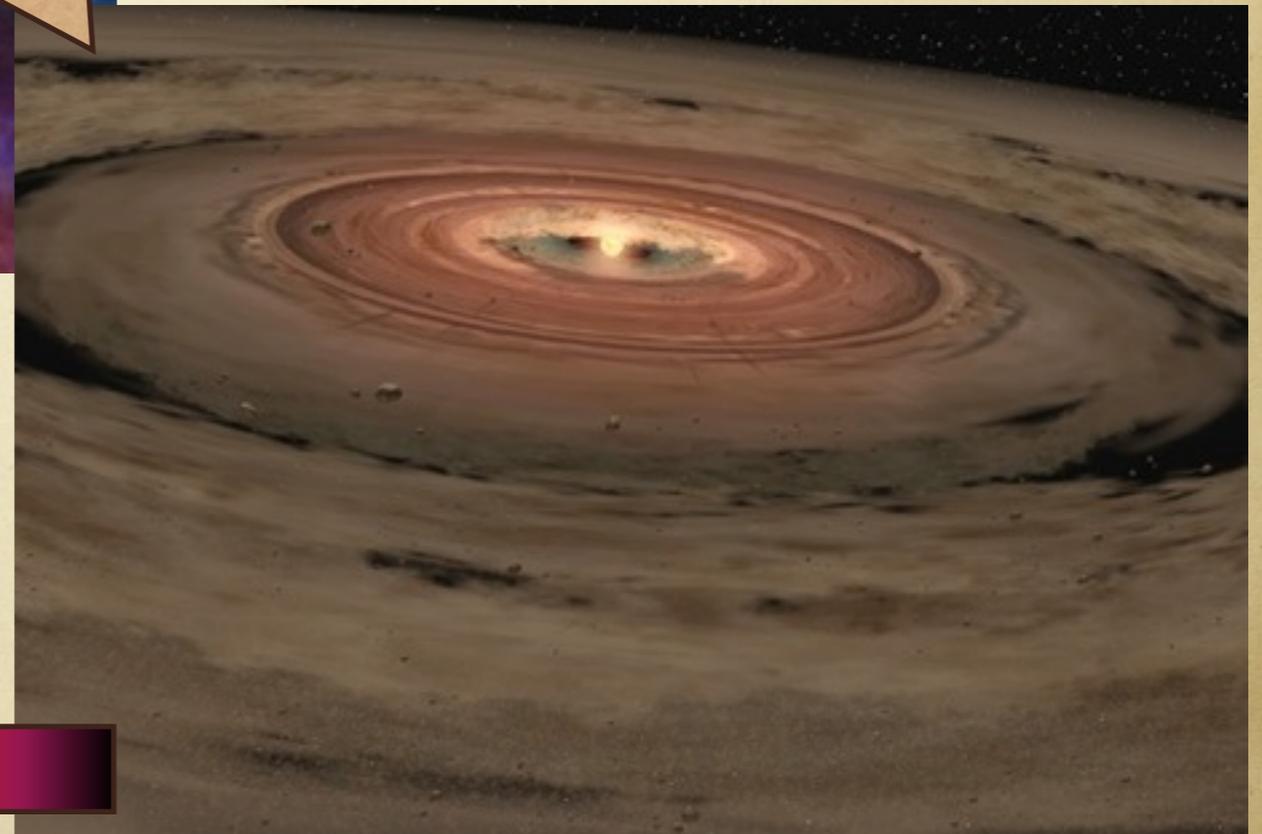
Our solar System

the rotation of
the sun

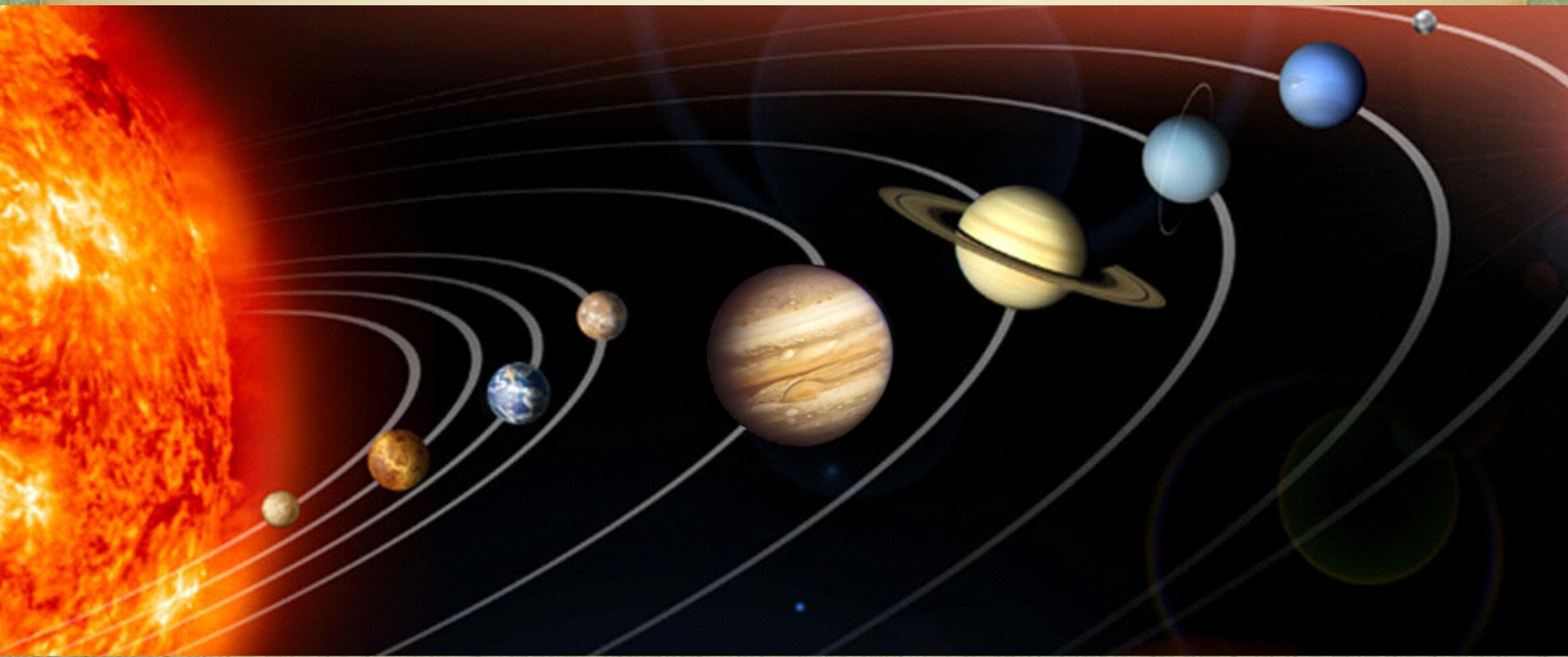


Our solar System

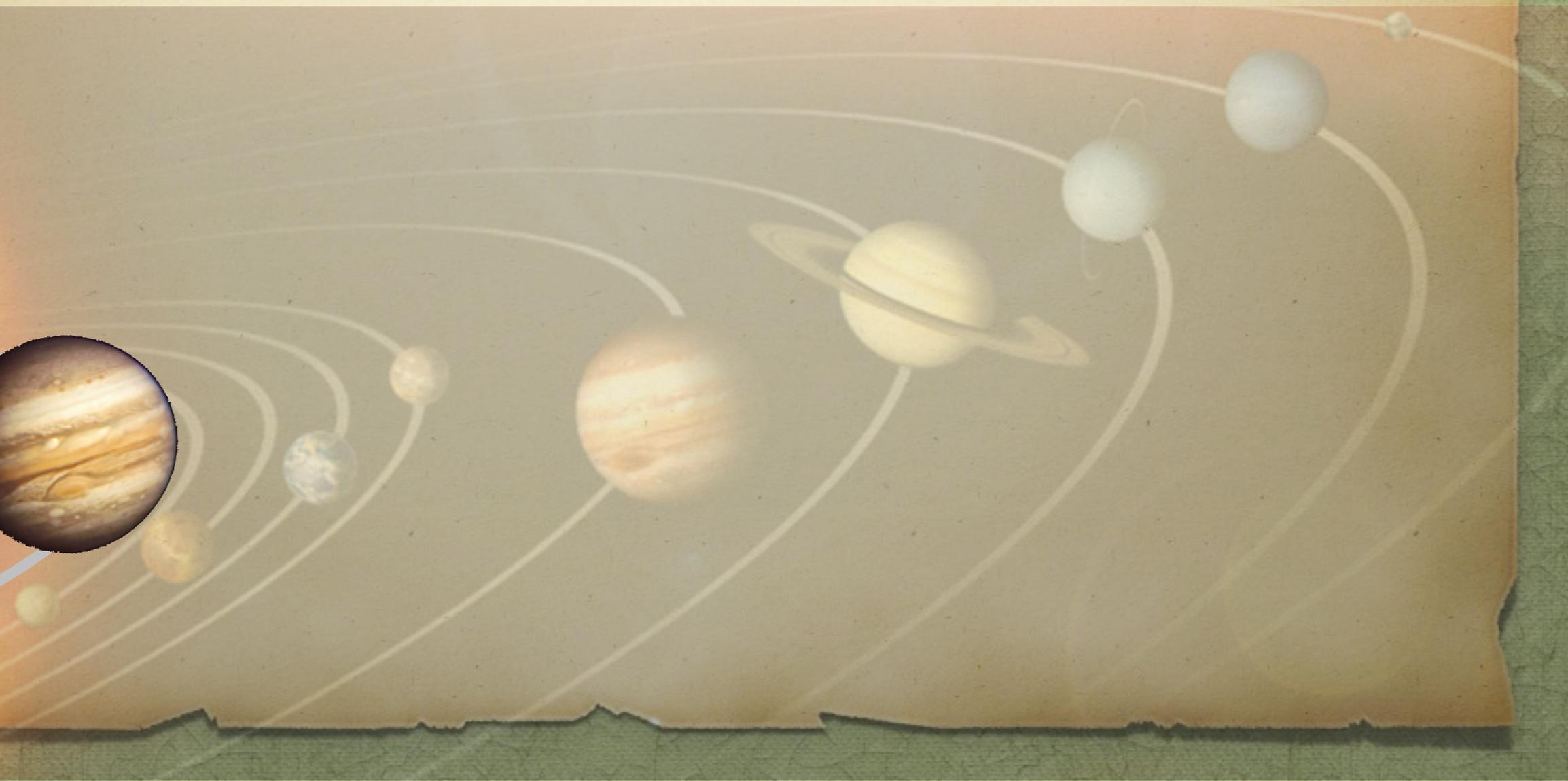
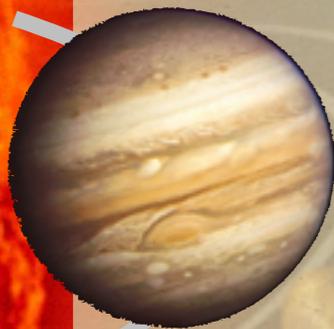
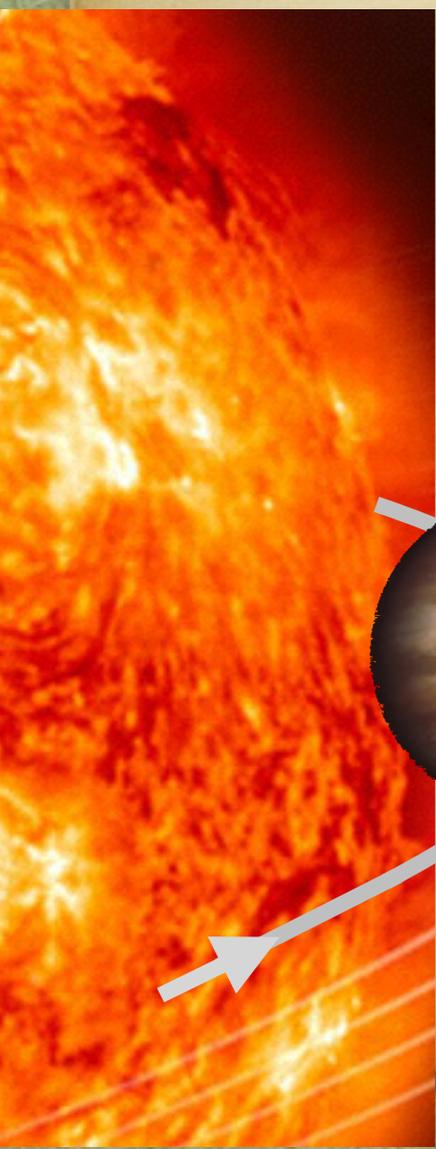
Formation story



Other solar systems

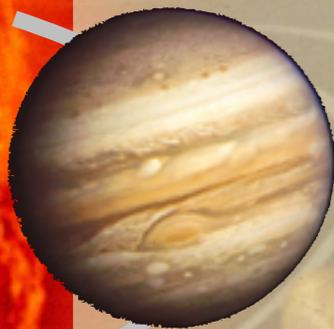
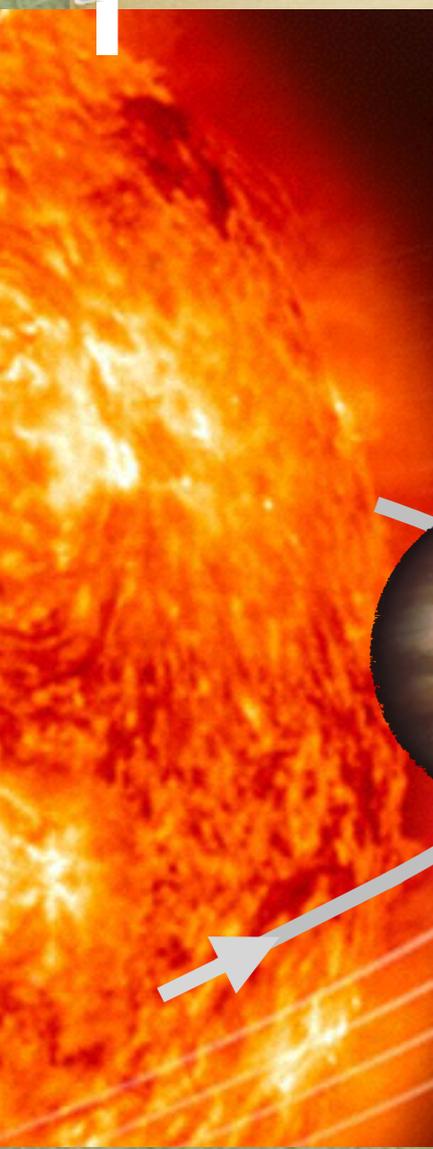


Other solar systems

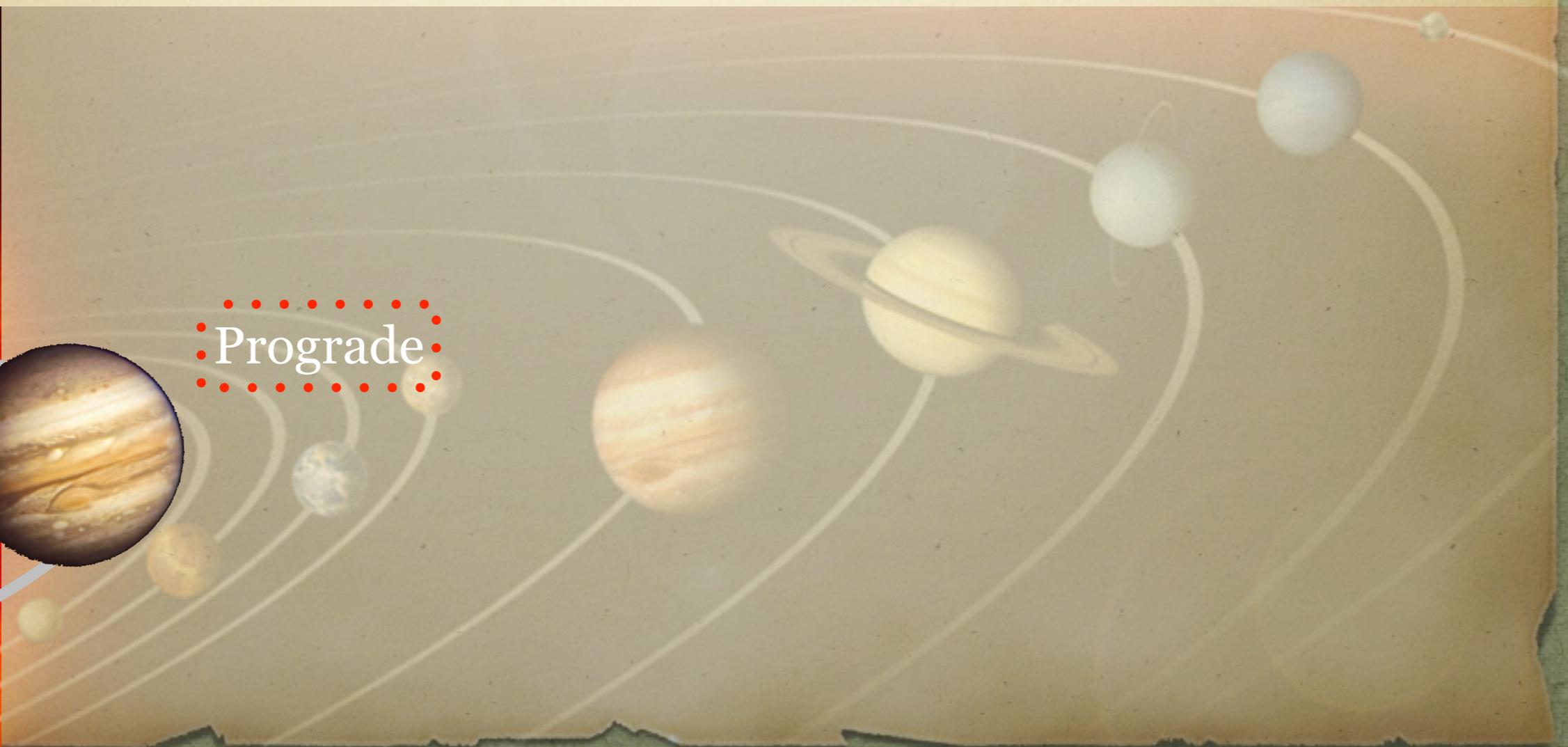


Other solar systems

the rotation of
the star

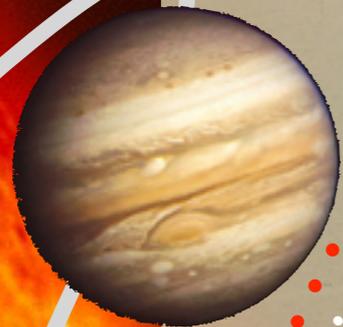
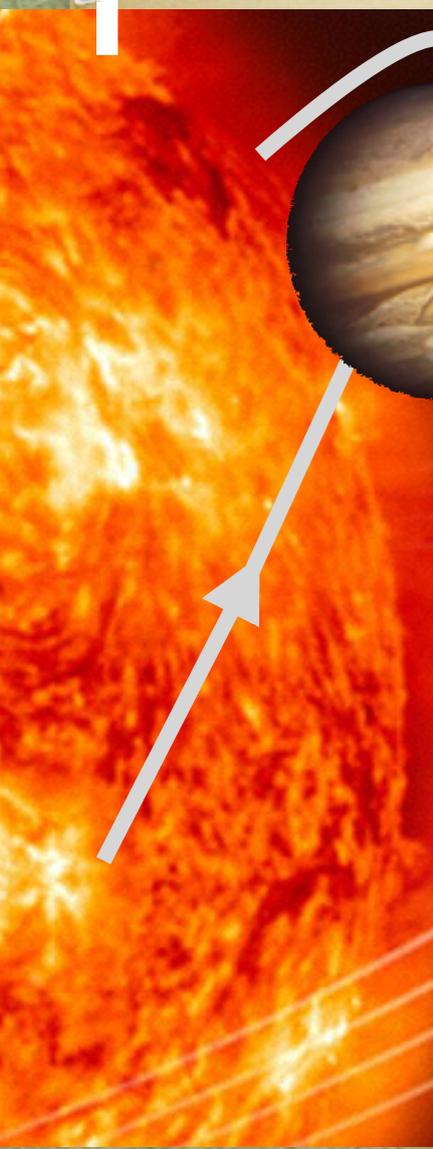


Prograde

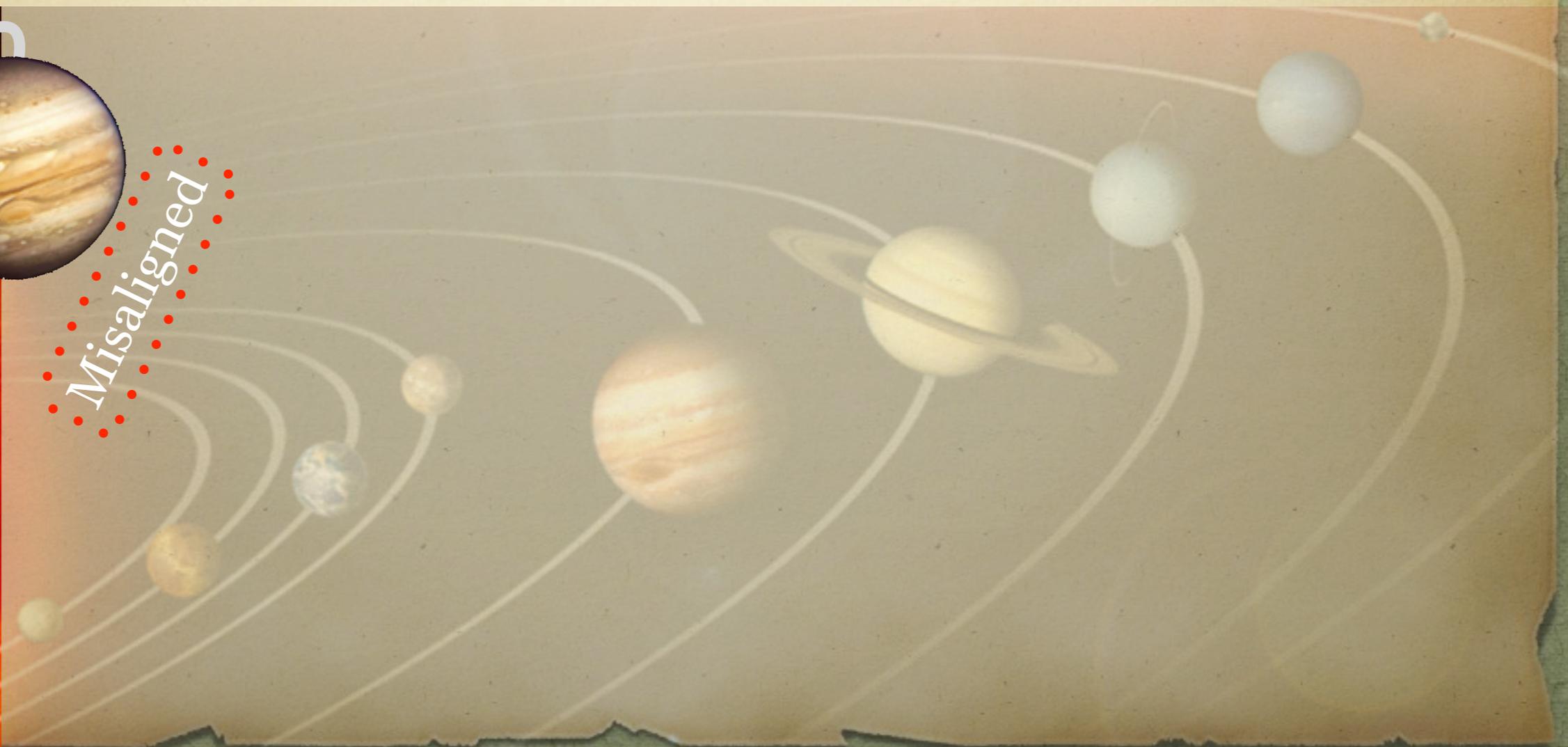


Other solar systems

the rotation of
the star

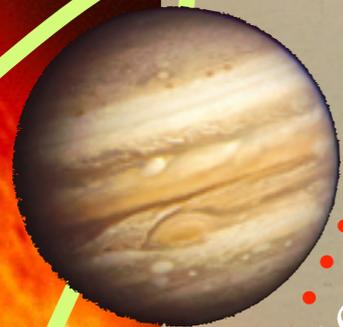
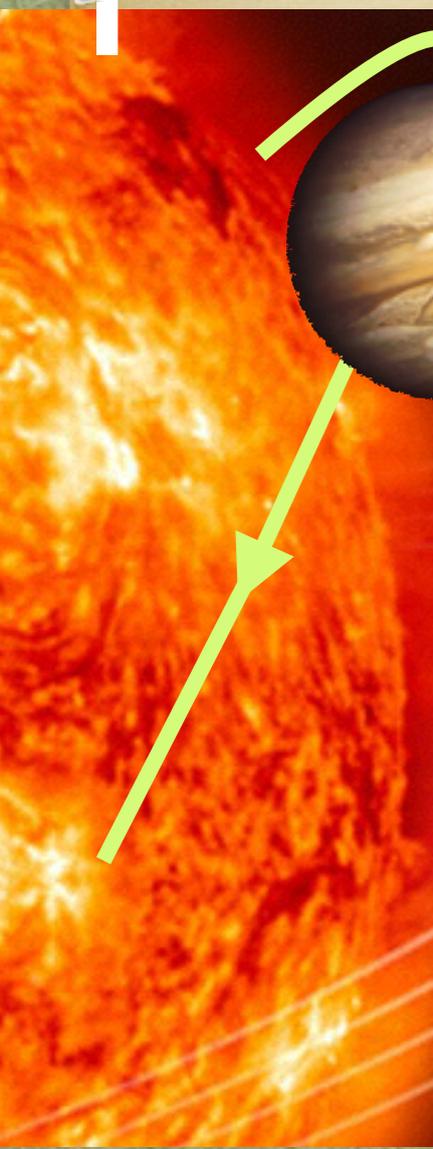


Misaligned

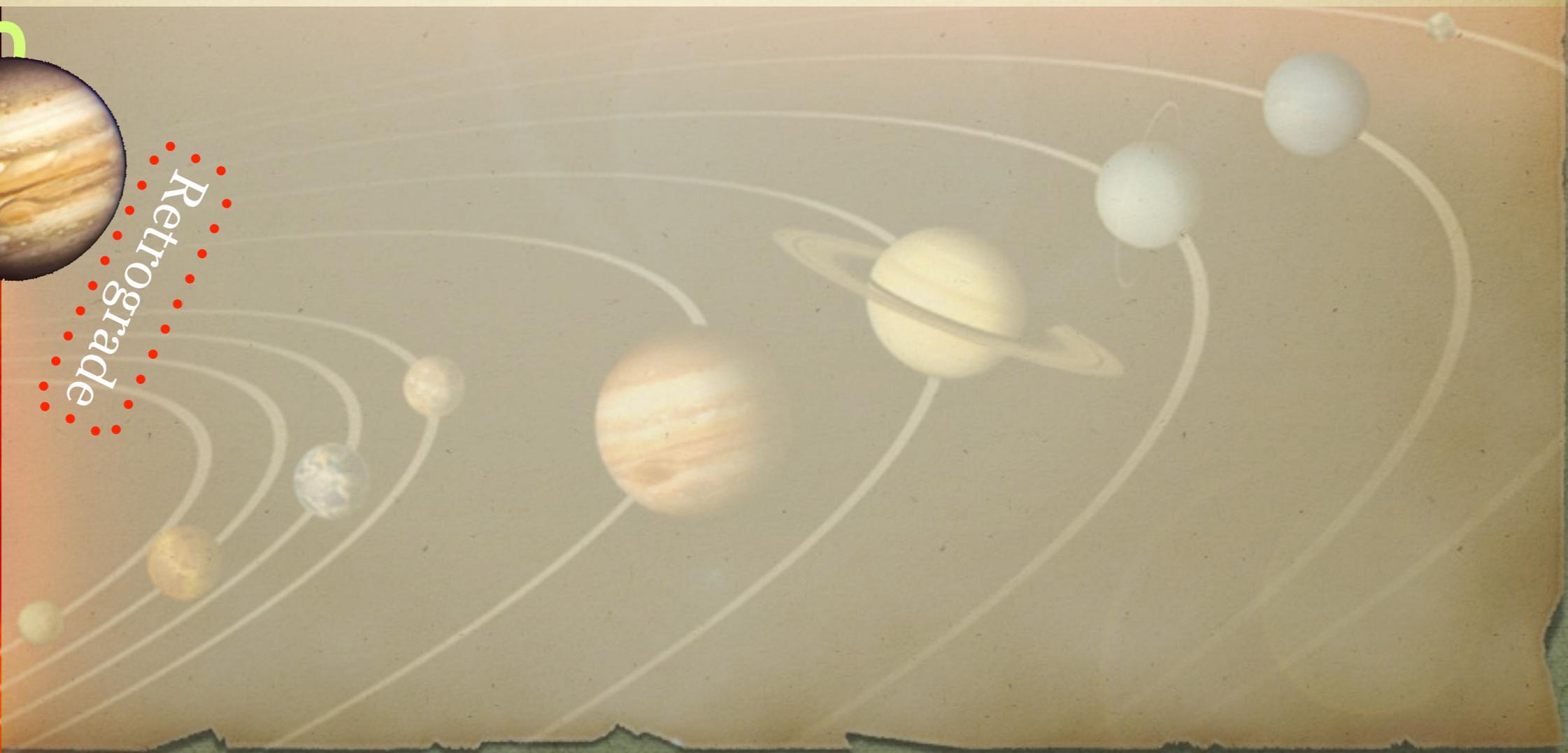


Other solar systems

the rotation of
the star



Retrograde

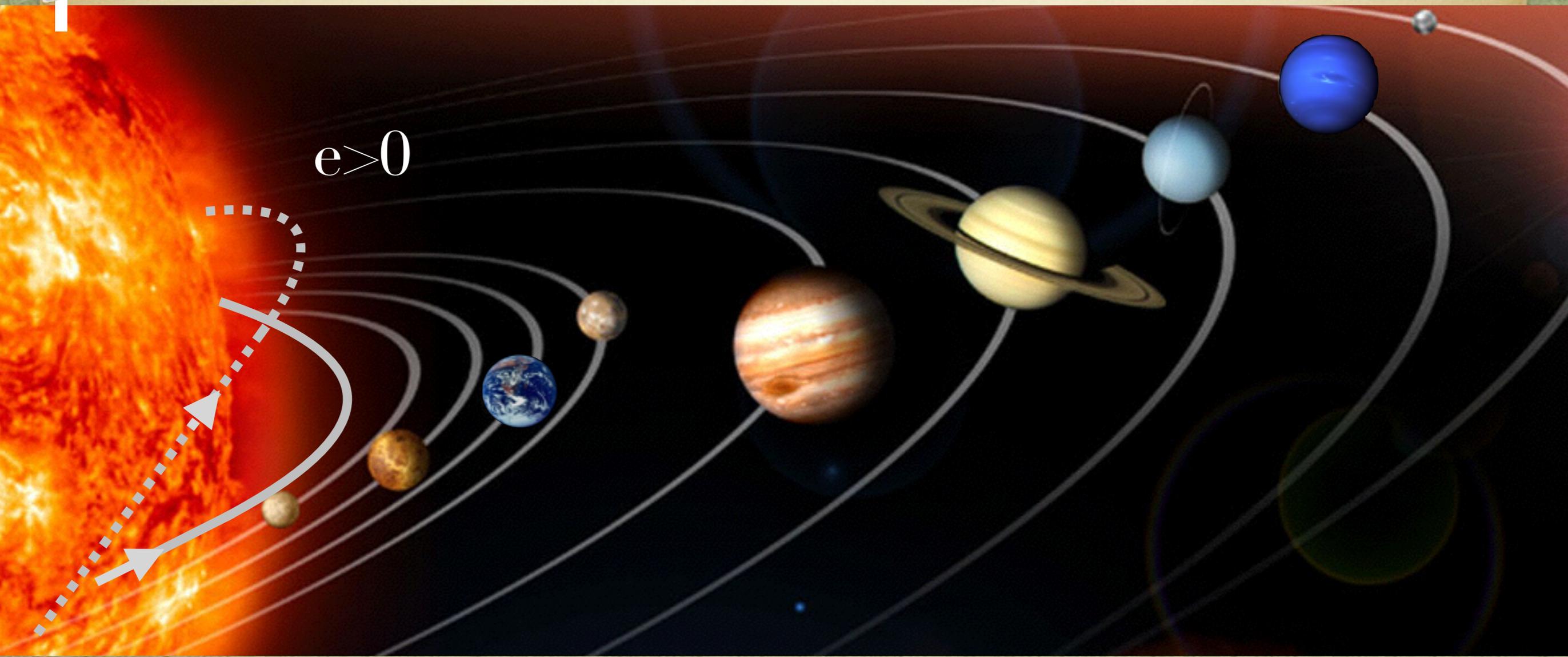


Other solar systems

the rotation of
the star



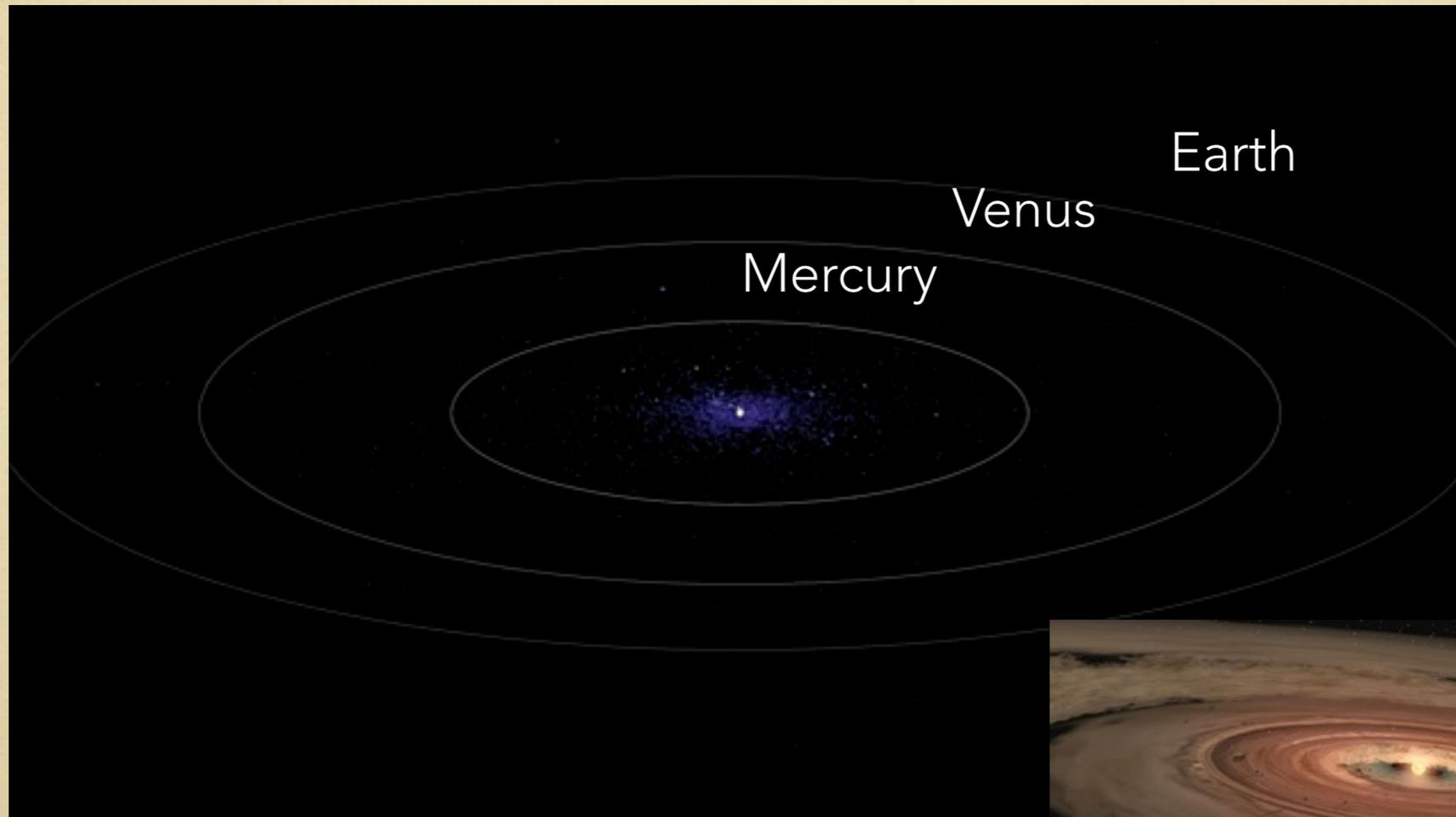
$e > 0$



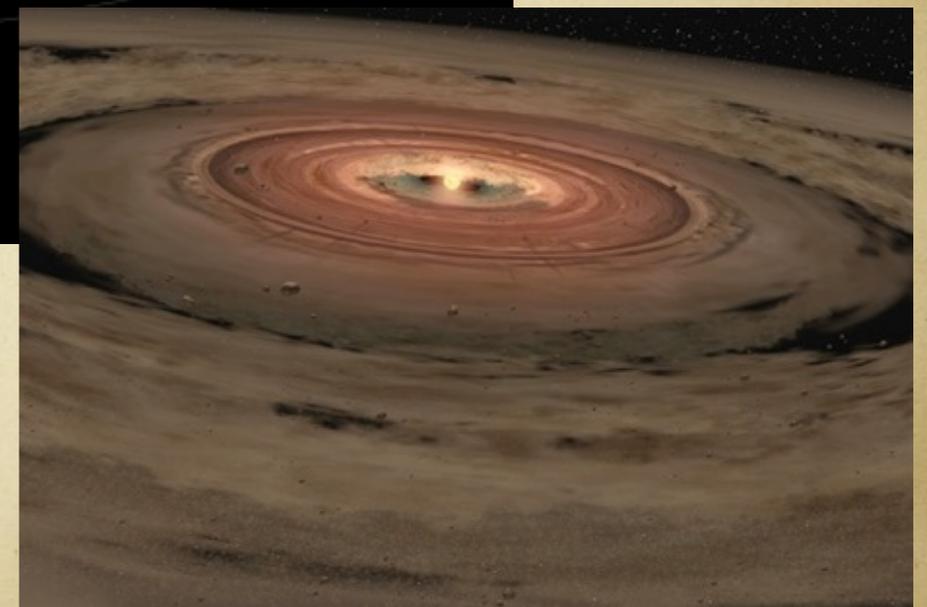
Kepler planet candidates are in a very close orbit

90% of all planets and planet candidates are in a very close orbit

Illustration of the planets and planet candidates as if they orbit a single star



movie by Alex Parker



Astrodynamics is alive!



Selected dynamical processes

- Planet-Planet scattering
- Mean motions resonances
- “Classical” secular evolution
- The eccentric Kozai-Lidov (EKL) mechanism

Selected dynamical processes

- **Planet-Planet scattering**
- Mean motions resonances
- “Classical” secular evolution
- The eccentric Kozai-Lidov (EKL) mechanism

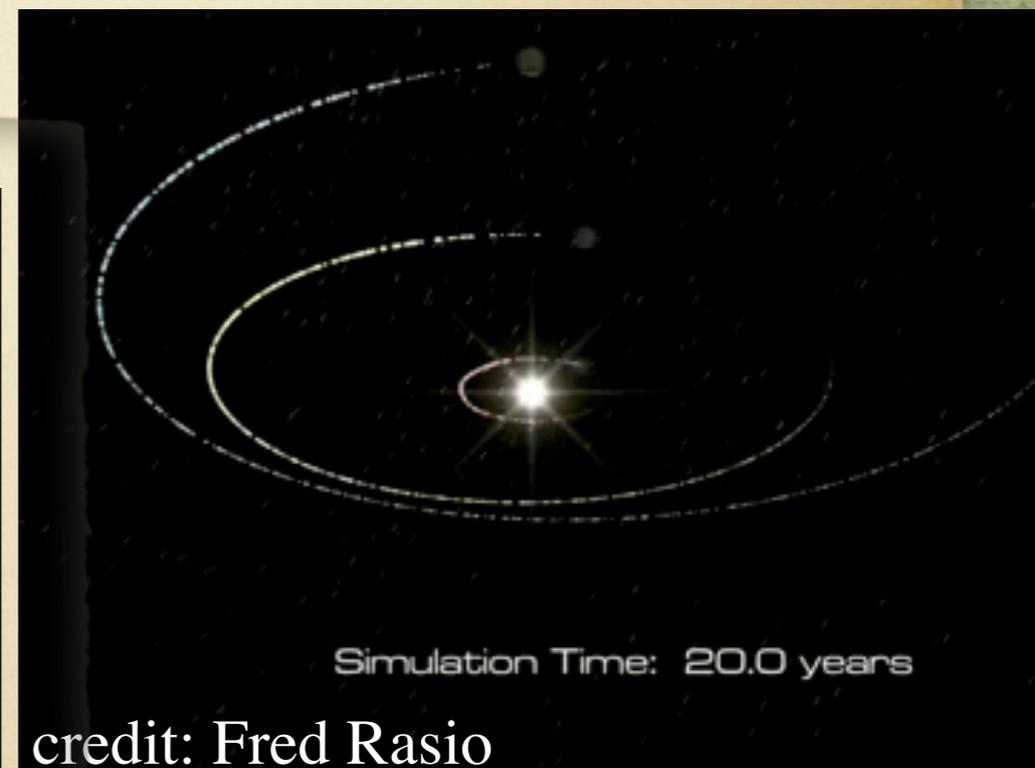
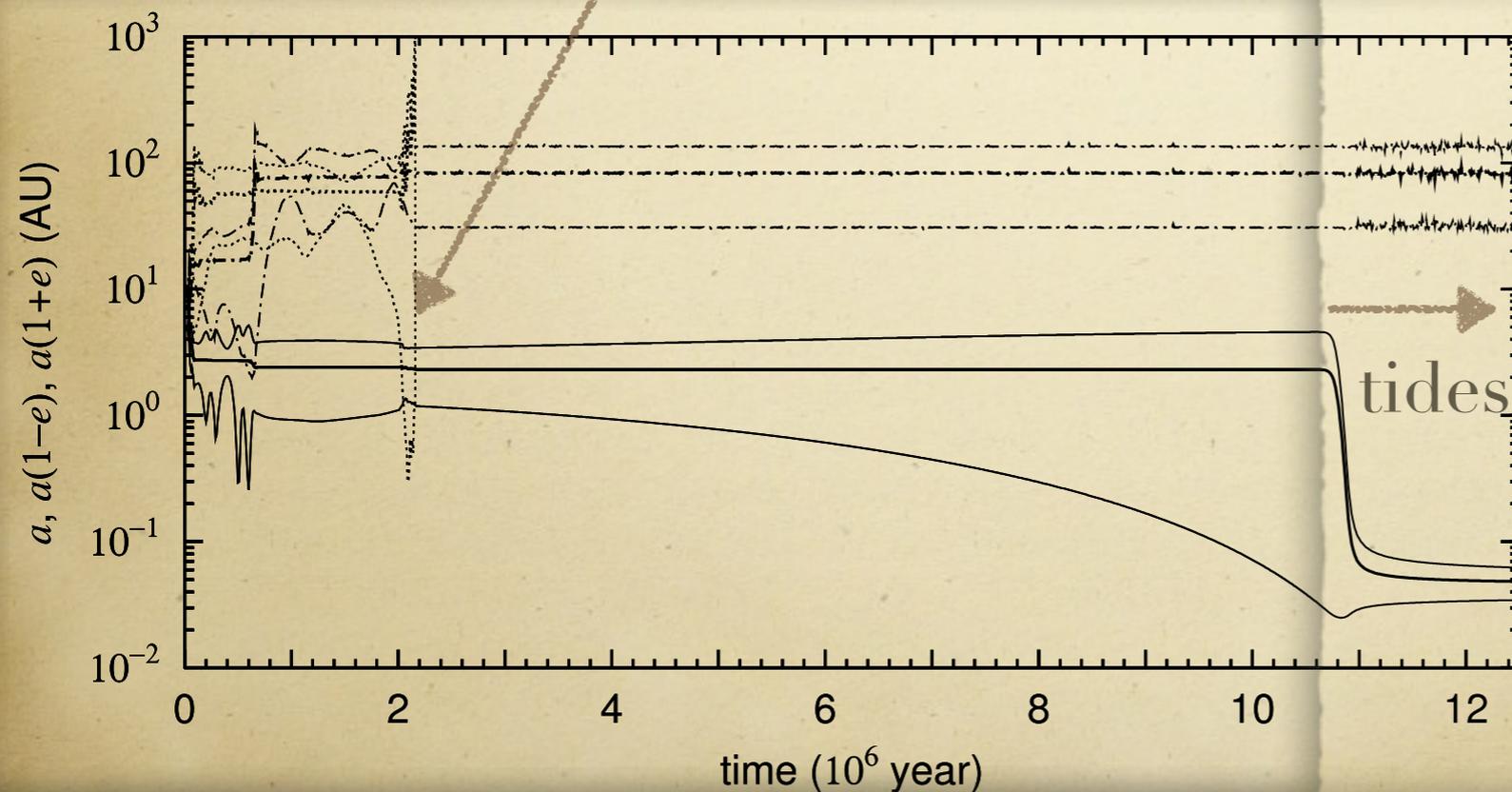
Post evolution dynamics in planetary systems

1. Scattering events Rasio & Ford 1996

Short Time Scale
larger than orbital

Packed systems, outcome: inclined, eccentric, ejection

ejection



Selected dynamical processes

- Planet-Planet scattering
- **Mean motions resonances**
- “Classical” secular evolution
- The eccentric Kozai-Lidov (EKL) mechanism

Post evolution dynamics in planetary systems

Resonances

2. Mean Motion Resonances

$$\frac{P_1}{P_2} \sim \frac{n}{m}$$

Orbital Time Scale

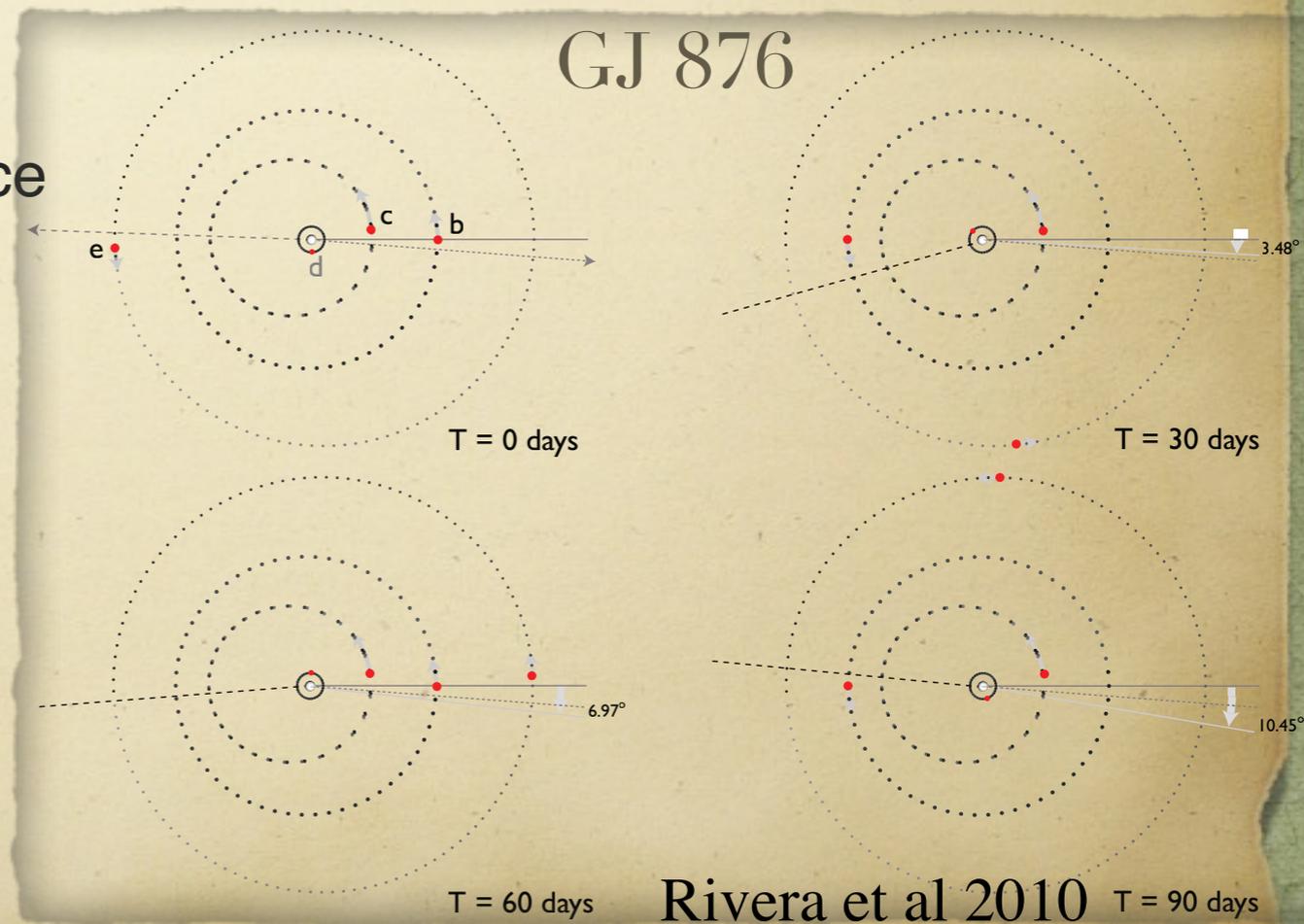
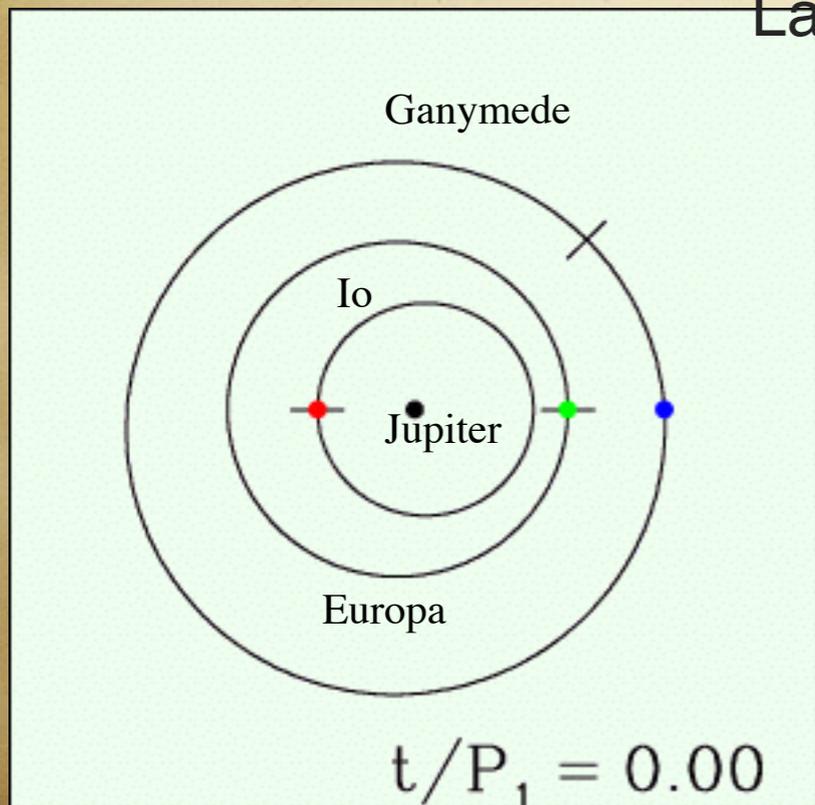
outcome: in most cases lead to unstable config.

sometimes we stable config.

Galilean Satellites

Io, Europa, and Ganymede 1:2:4

Laplace resonance



Post evolution dynamics

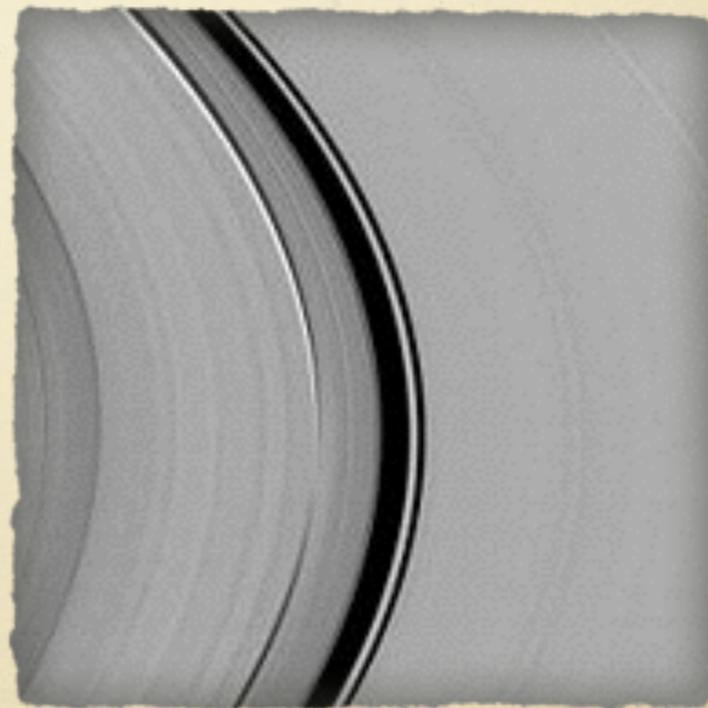
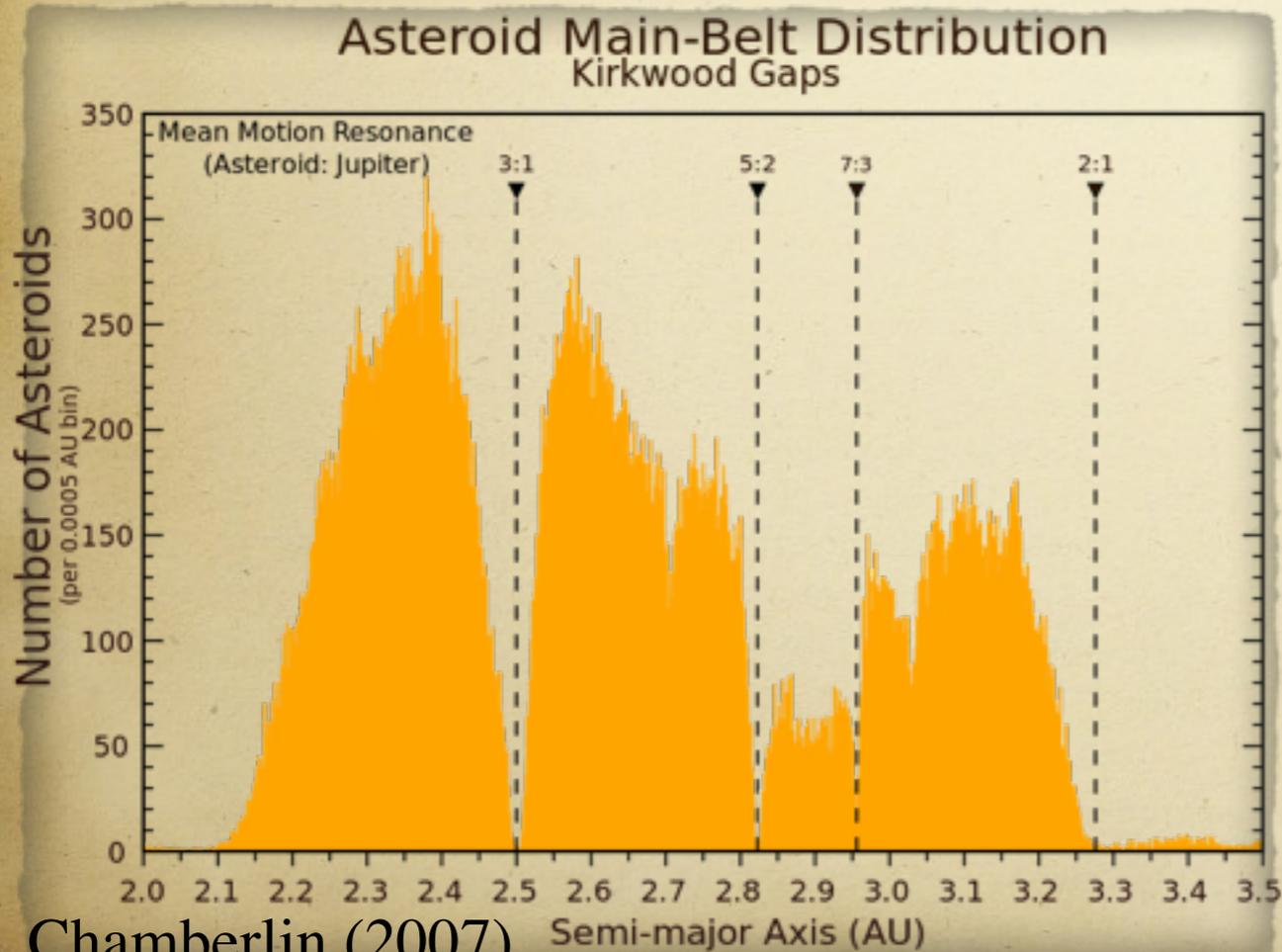
in planetary systems

Resonances

2. Mean Motion Resonances

$$\frac{P_1}{P_2} \sim \frac{n}{m}$$

unstable config:



Post evolution dynamics

in planetary systems

Resonances

2. Mean Motion Resonances

$$\frac{P_1}{P_2} \sim \frac{n}{m}$$

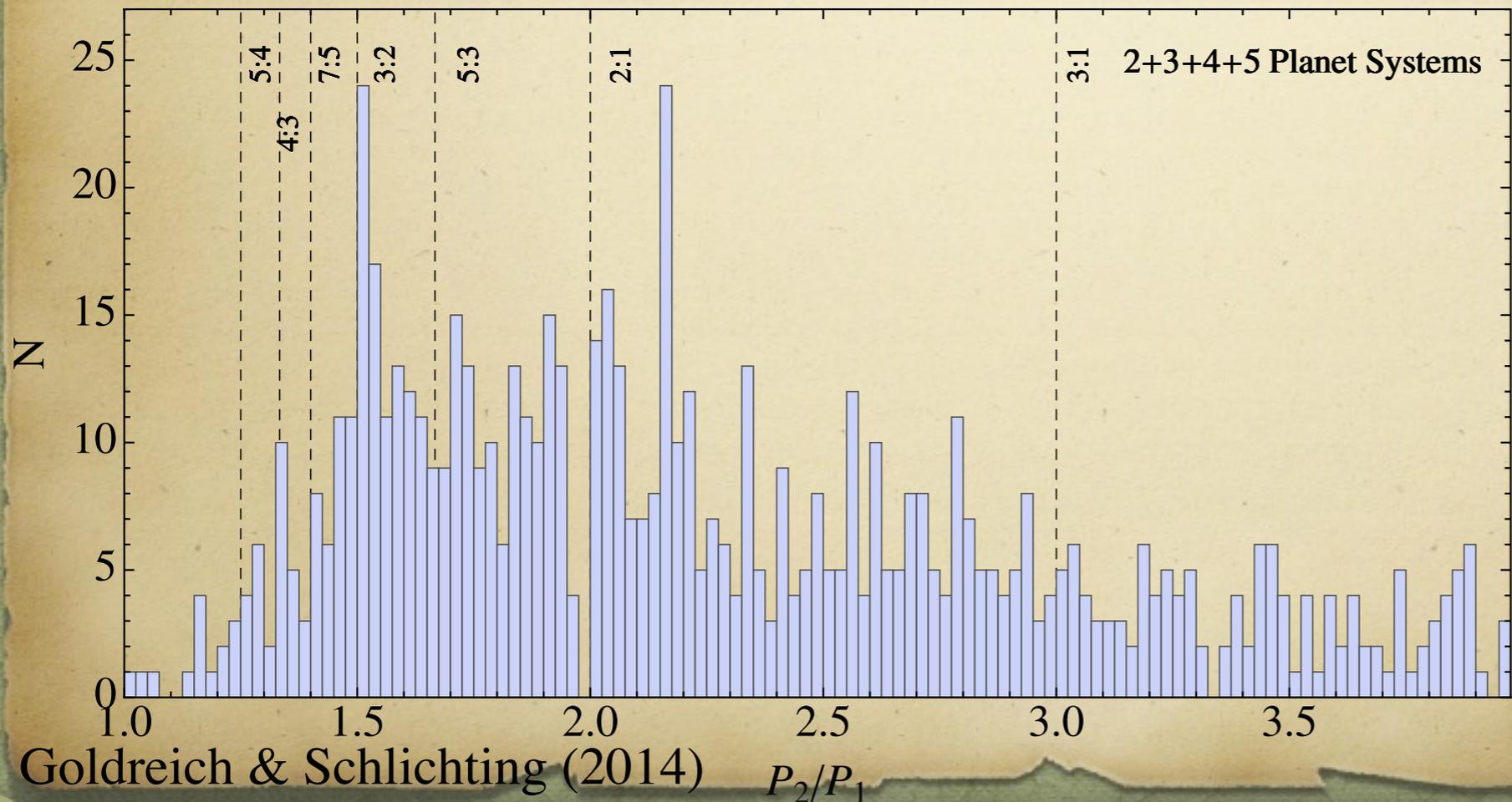
Extrasolar...

Problem: predicted migration rates: most planets in resonances.

But reality ...

Few possible explanations:

- Accretion of mass e.g., Petrovich et al (2013)
- Dissipation (maybe tides?) Lithwick & Wu (2012), Batygin & Morbidelli (2013)
- Resonance capture is temporary Goldreich & Schlichting (2014)
- and more



Selected dynamical processes

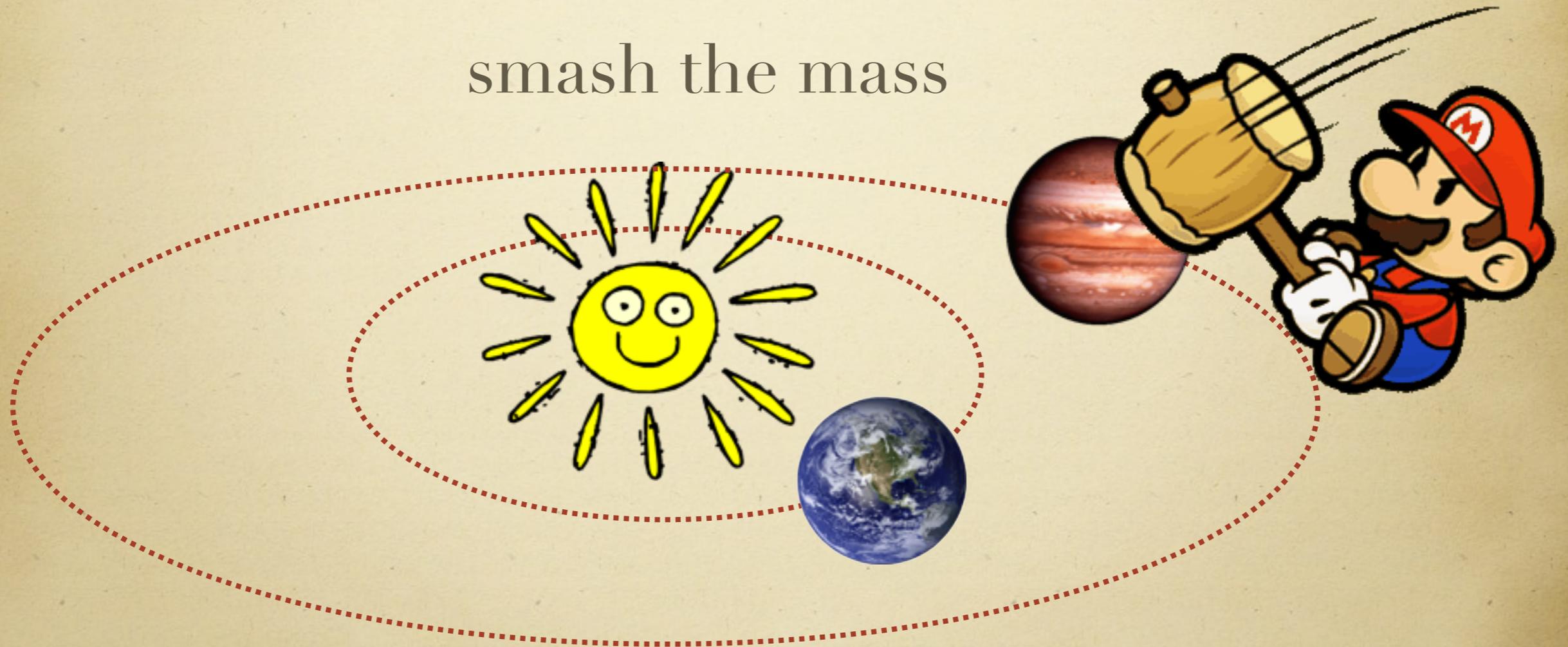
- Planet-Planet scattering
- Mean motions resonances
- **“Classical” secular evolution**
- The eccentric Kozai-Lidov (EKL) mechanism

Post evolution dynamics in planetary systems

3. The secular interactions

Long Time Scale

smash the mass



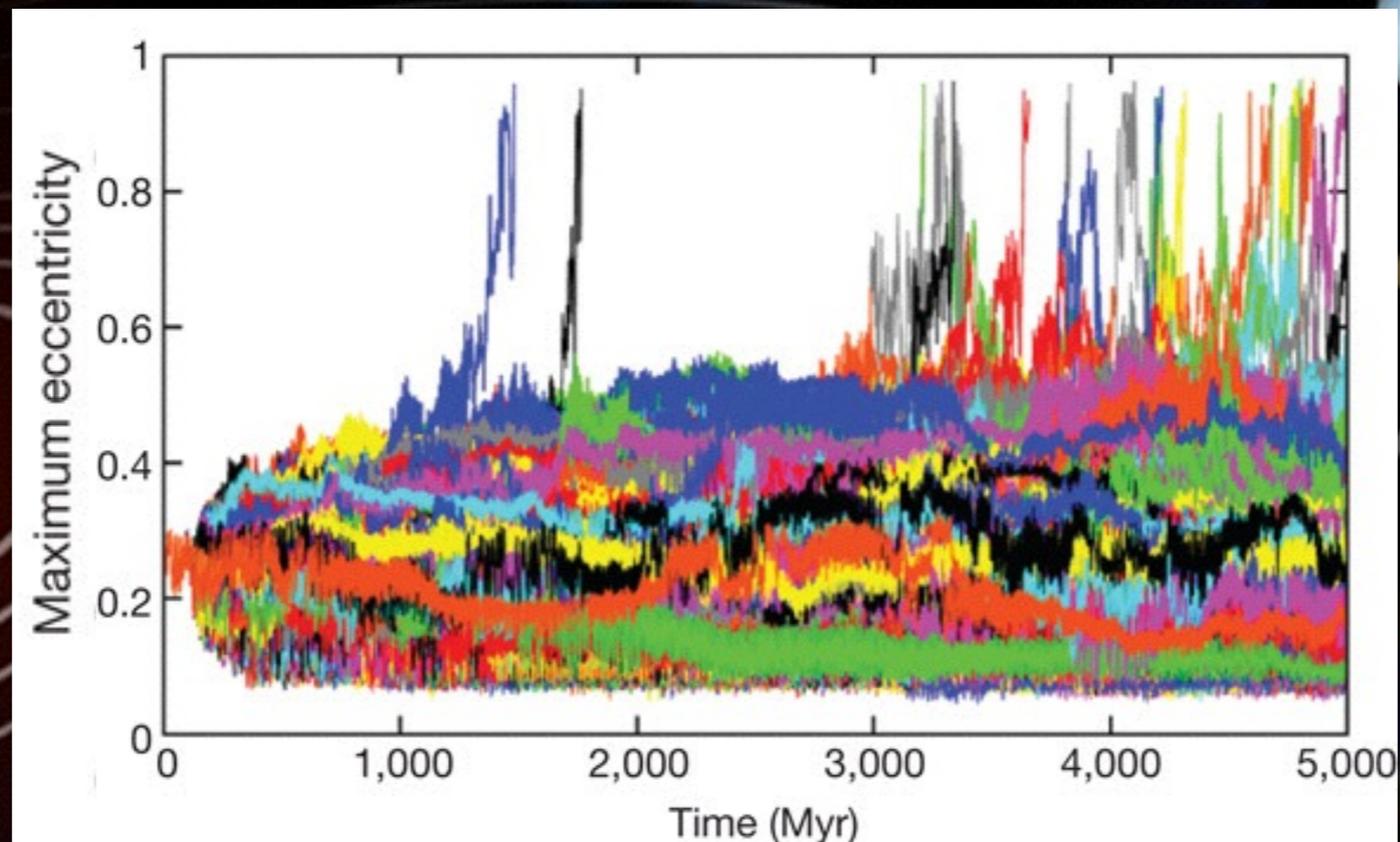
Post evolution dynamics in planetary systems

3. The secular interactions

~circular orbits, concentric, coplanar

Long Time Scale

Laskar & Gastineau (2009)



Selected dynamical processes

- Planet-Planet scattering
- Mean motions resonances
- “Classical” secular evolution
- **The eccentric Kozai-Lidov (EKL) mechanism**

Post evolution dynamics in planetary systems

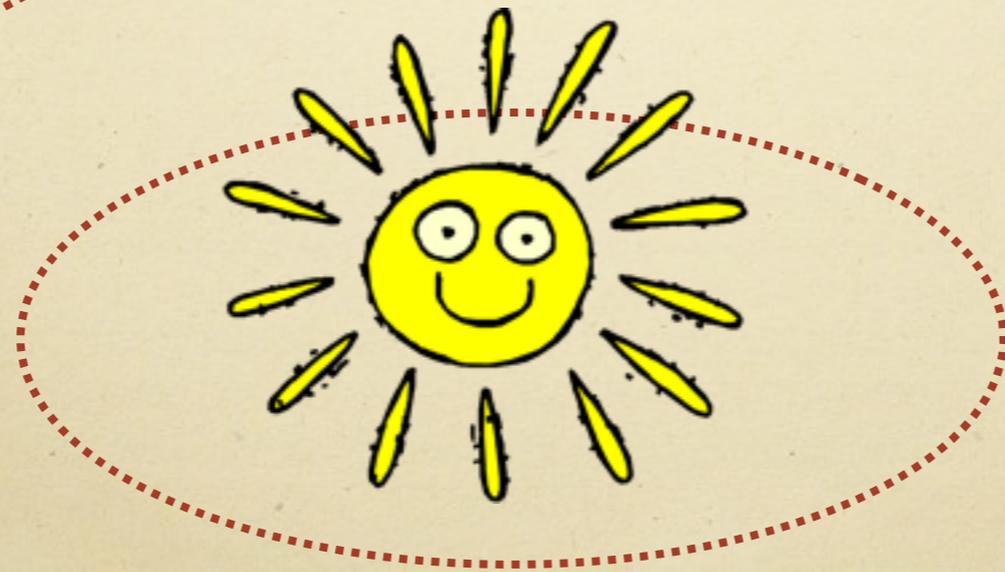
4. The secular interactions

~can be eccentric, hierarchical, inclined

Long Time Scale

Analytical treatment 3
body config.

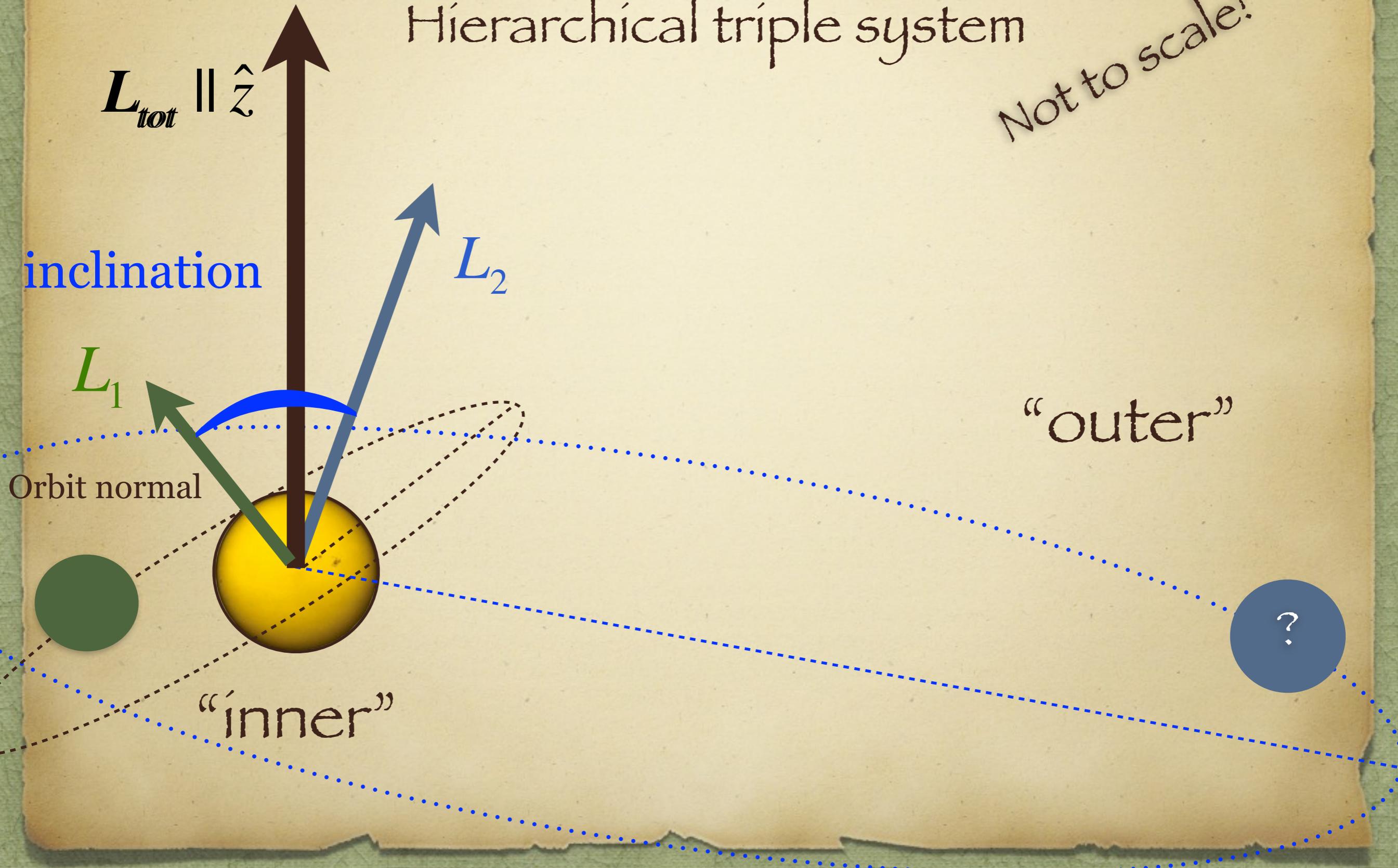
Perturbations from a far
away perturber



The Kozai-Lidov Formalism

Hierarchical triple system

Not to scale!

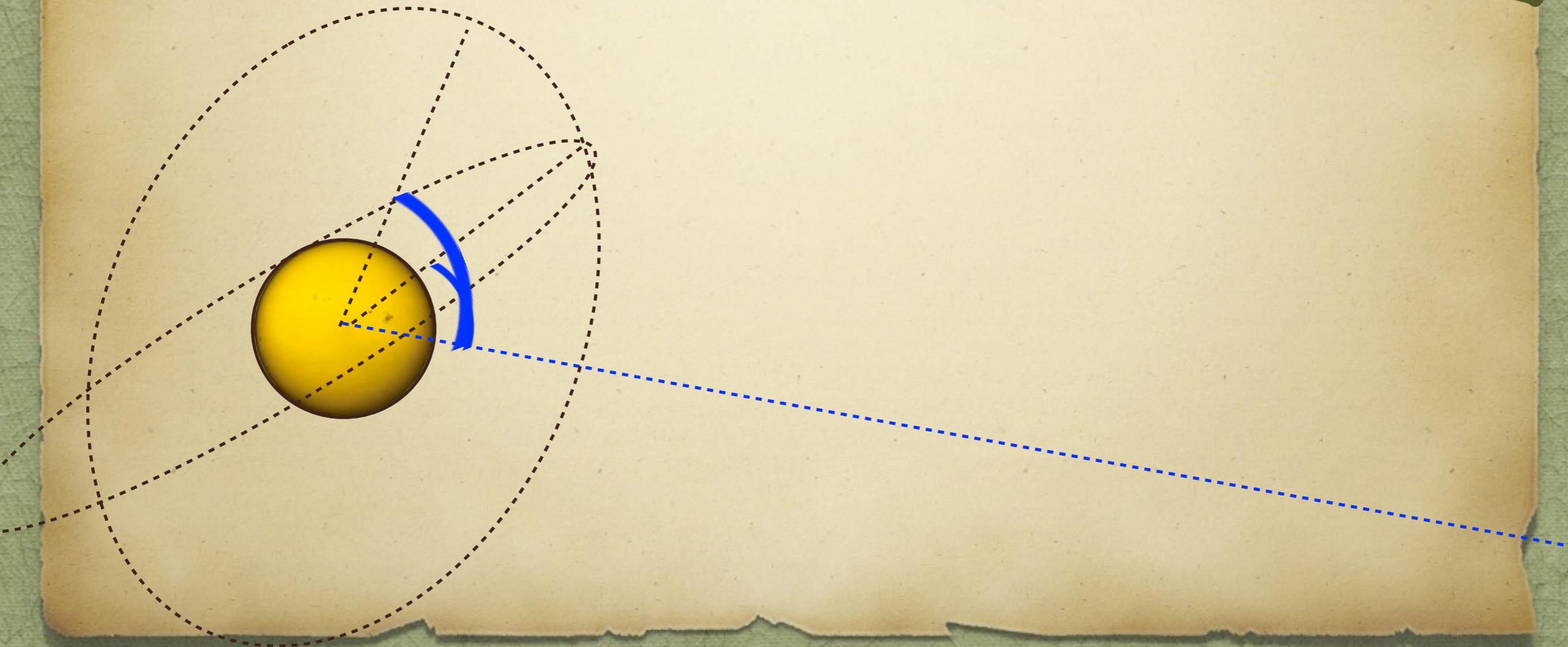


The Kozai-Lidov Formalism

The eccentricity and inclination oscillate

Kozai 1962, Lidov 1962

For initially inclined system $\gtrsim 40^\circ$



The Kozai-Lidov Formalism

The eccentricity and inclination oscillate

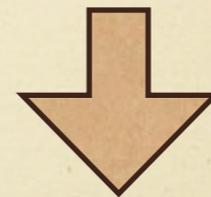
Kozai 1962, Lidov 1962

Conservation of the z component of angular momentum for both the inner outer orbits

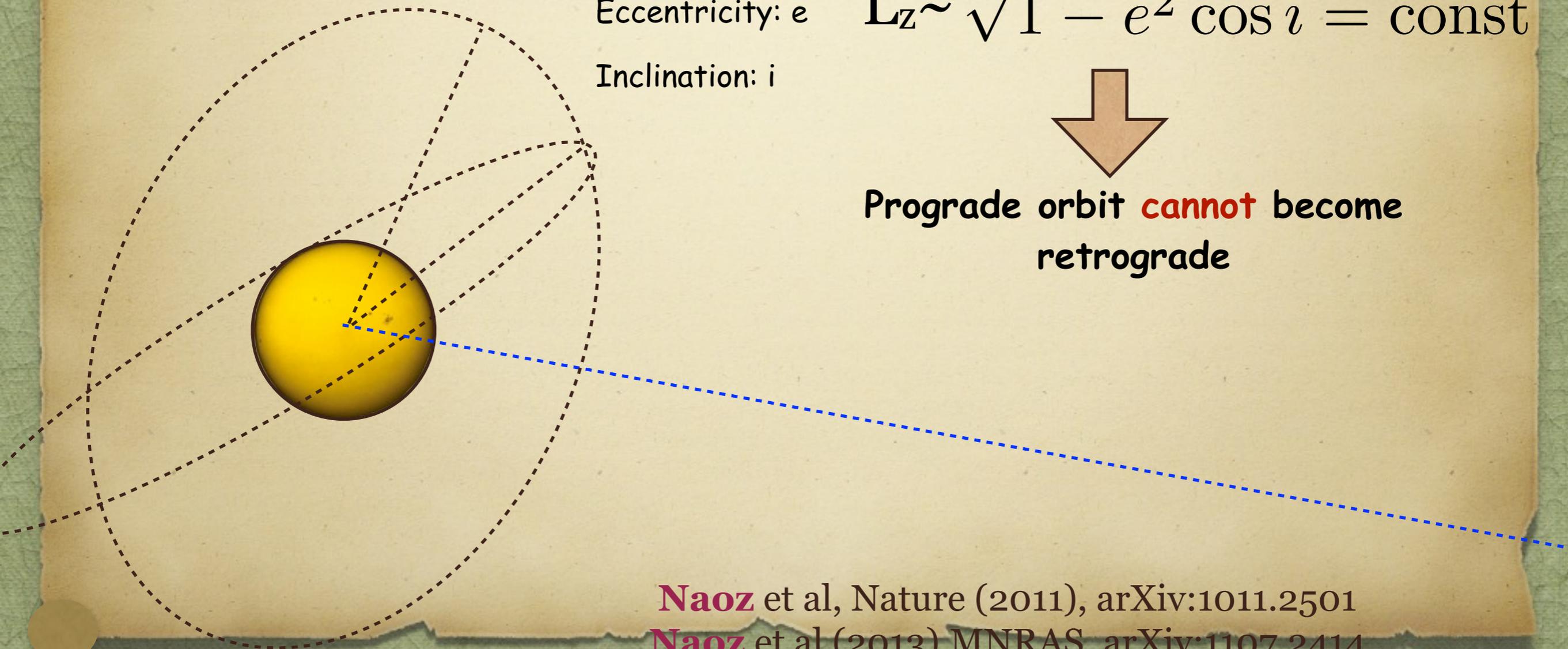
The orbital elements:

Eccentricity: e $L_z \sim \sqrt{1 - e^2} \cos i = \text{const}$

Inclination: i



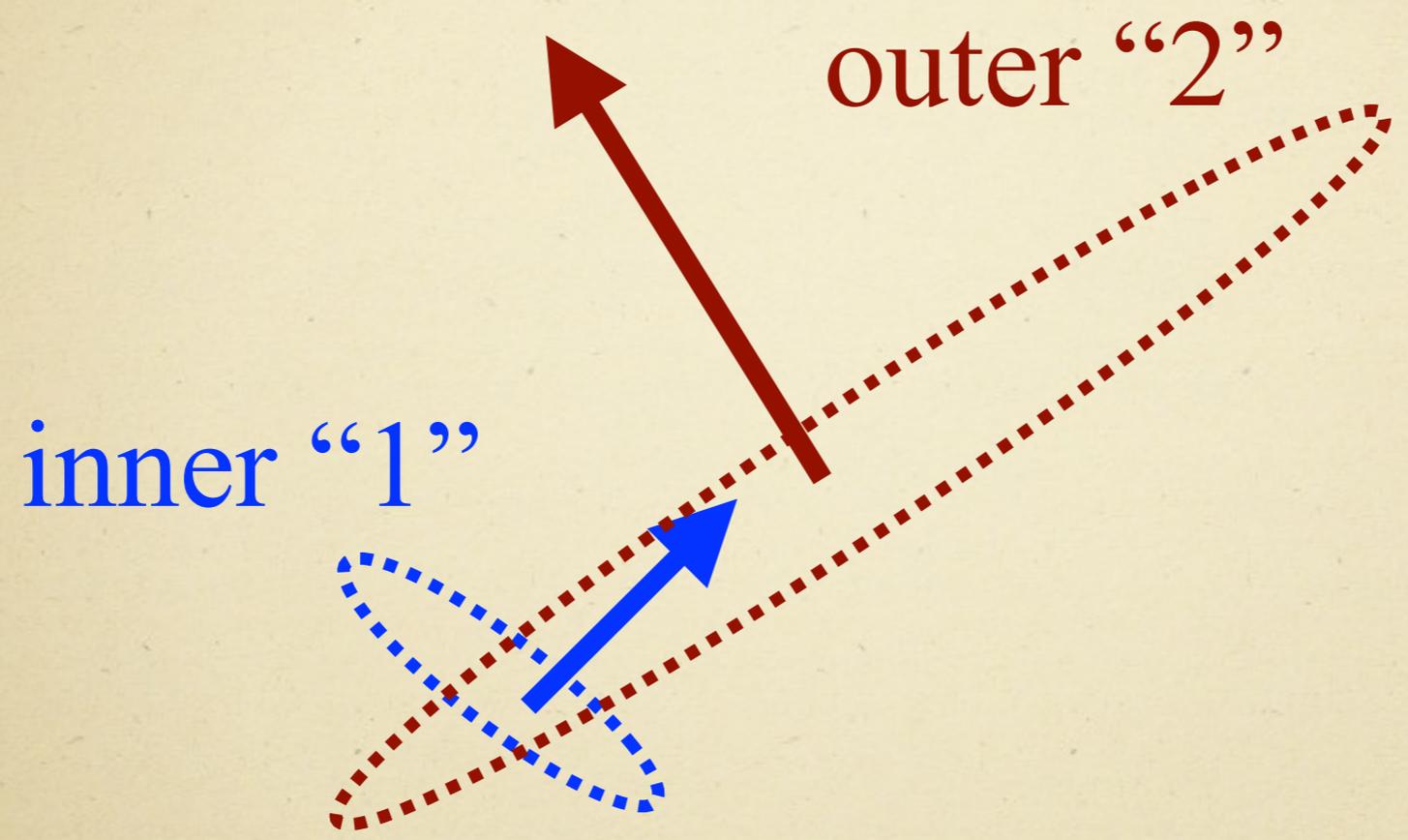
Prograde orbit **cannot** become retrograde



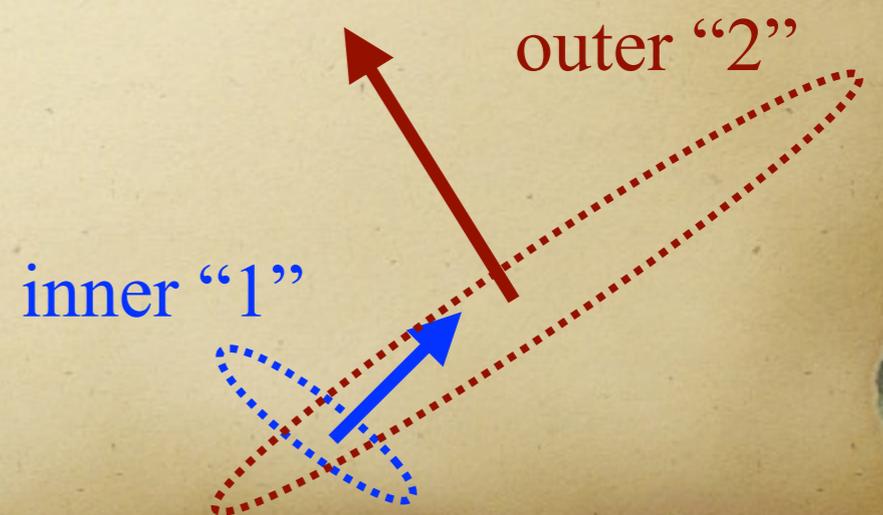
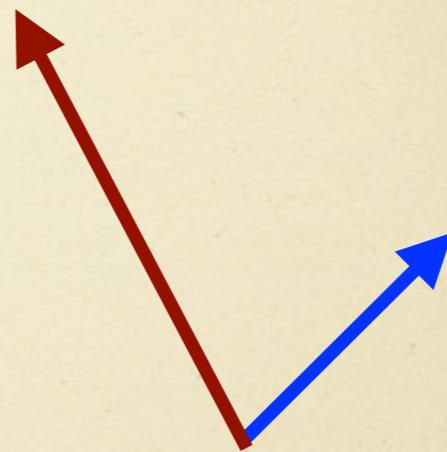
Naoz et al, Nature (2011), arXiv:1011.2501

Naoz et al (2013), MNRAS, arXiv:1107.2414

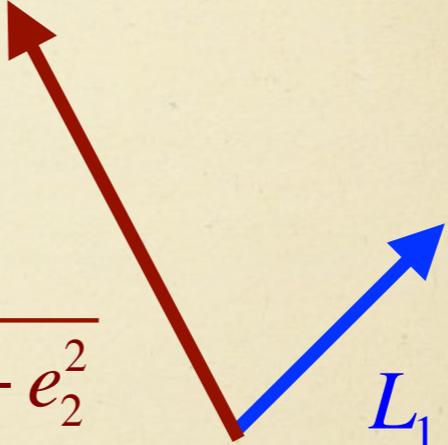
Is it constant?

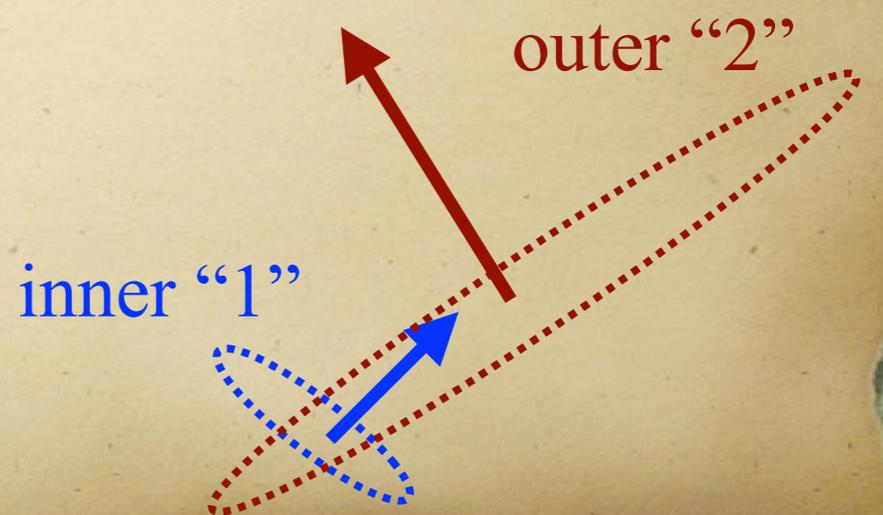


Is it constant?



Is it constant?

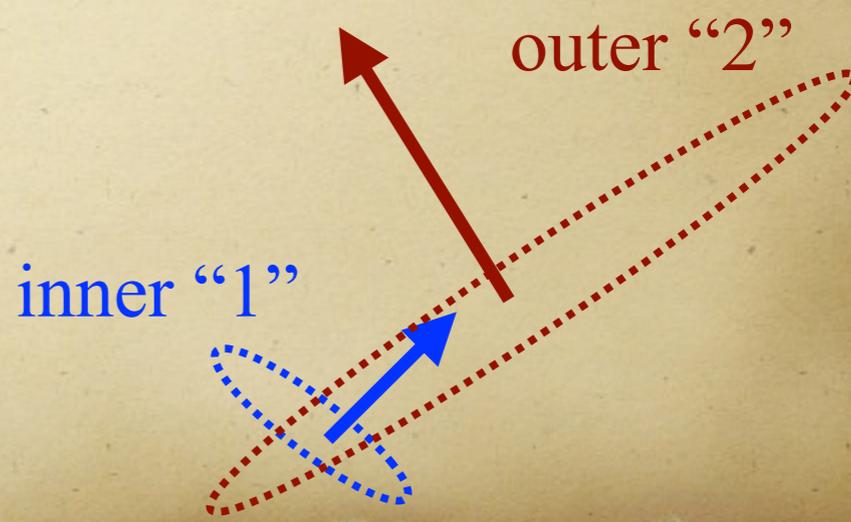
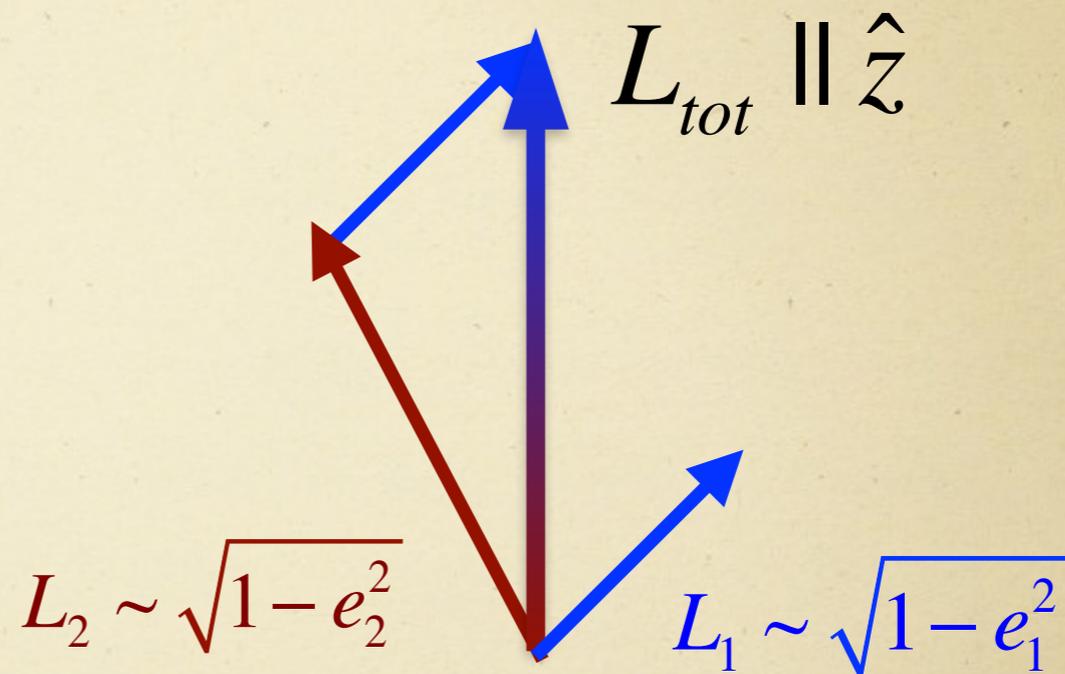

$$L_2 \sim \sqrt{1 - e_2^2}$$
$$L_1 \sim \sqrt{1 - e_1^2}$$



Is it constant?

Adding vector ...

$$\vec{L}_{tot} = \vec{L}_1 + \vec{L}_2$$

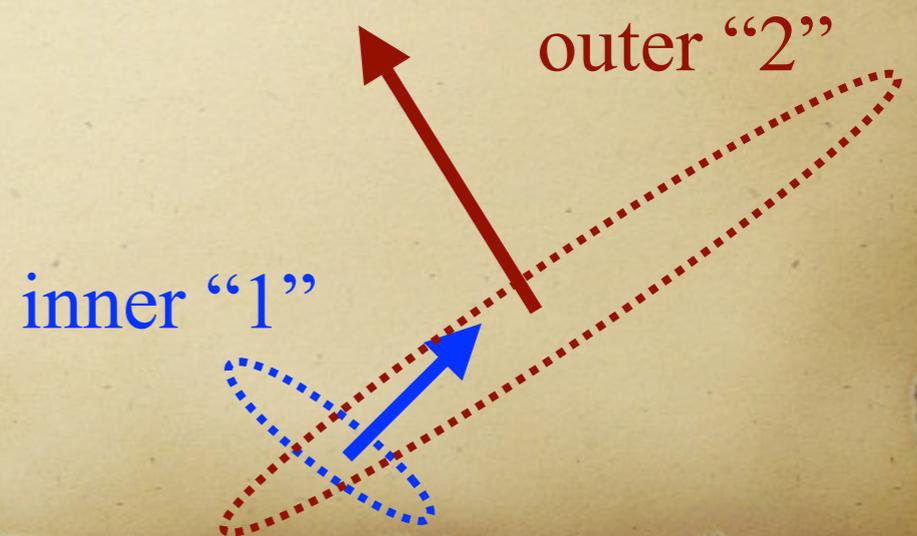
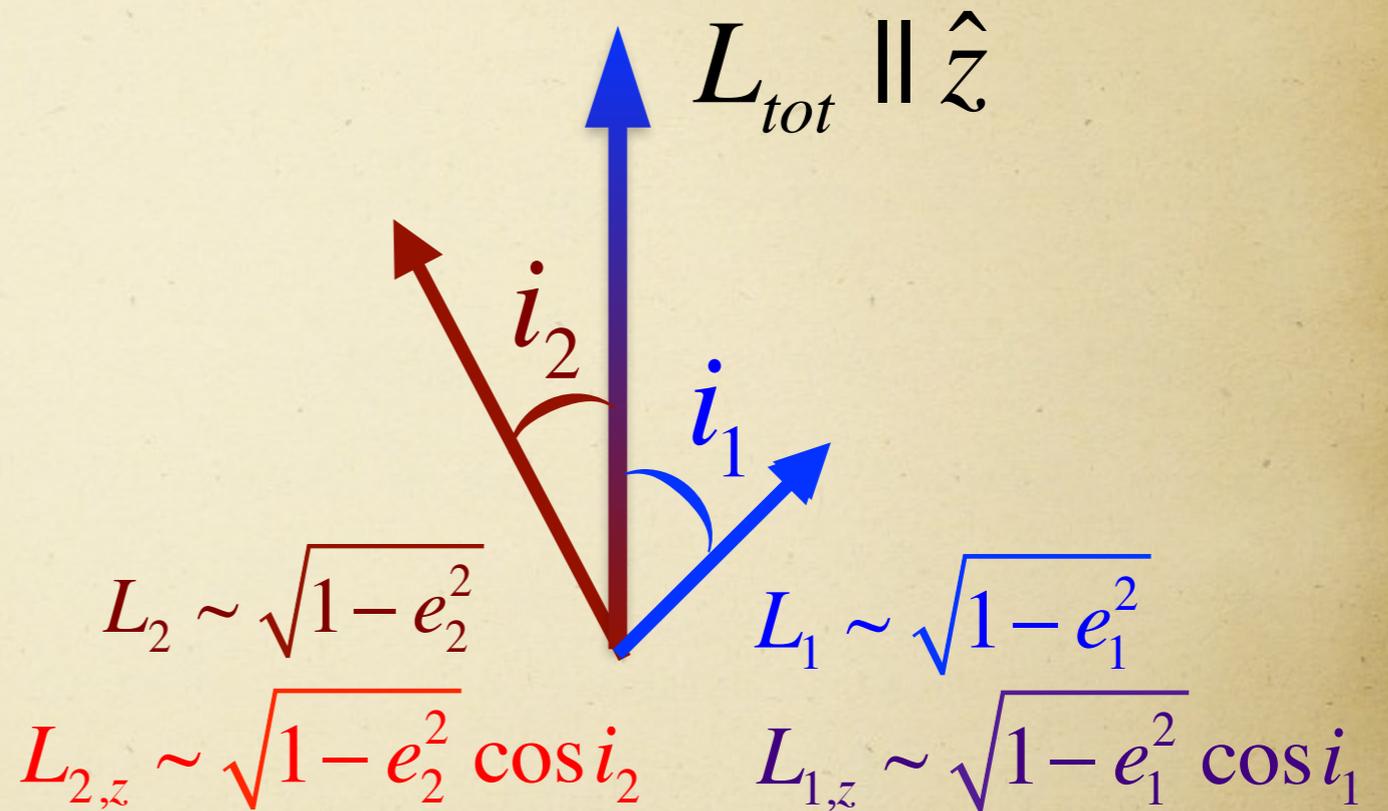


Is it constant?

Adding vector ...

$$\vec{L}_{tot} = \vec{L}_1 + \vec{L}_2$$

$$\vec{L}_2 = \vec{L}_{tot} - \vec{L}_1$$



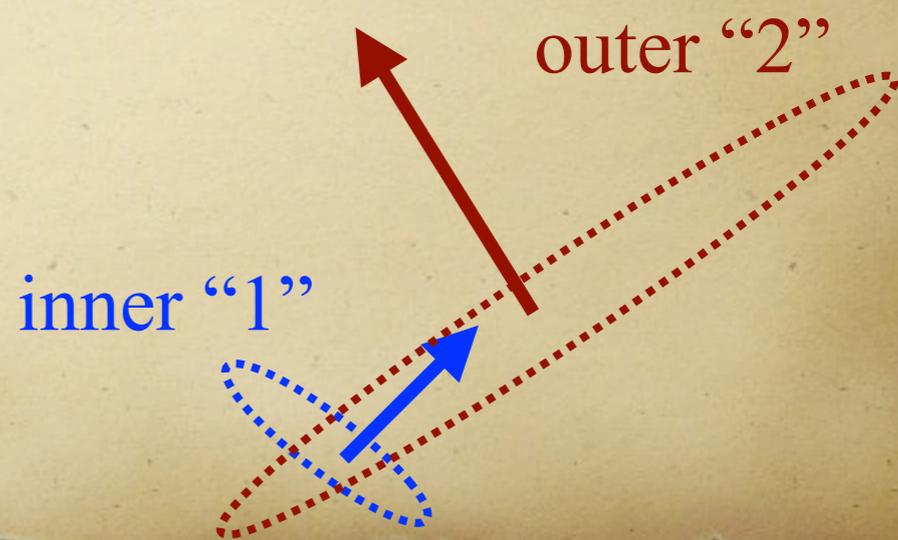
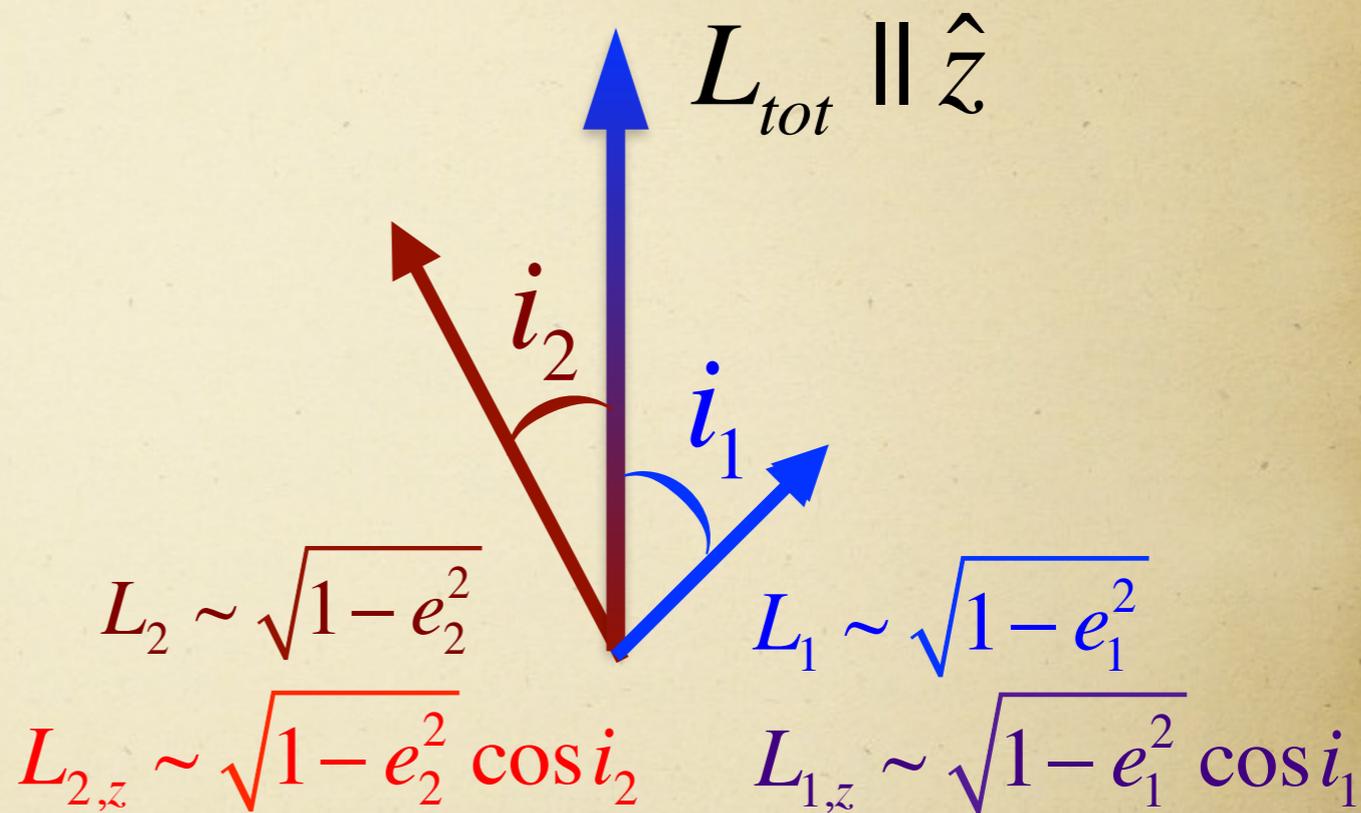
Is it constant?

Adding vector ...

$$\vec{L}_{tot} = \vec{L}_1 + \vec{L}_2$$

$$\vec{L}_2 = \vec{L}_{tot} - \vec{L}_1$$

$$L_2^2 = L_{tot}^2 + L_1^2 - 2L_{tot}L_1 \underbrace{\cos i_1}_{L_{1,z}}$$



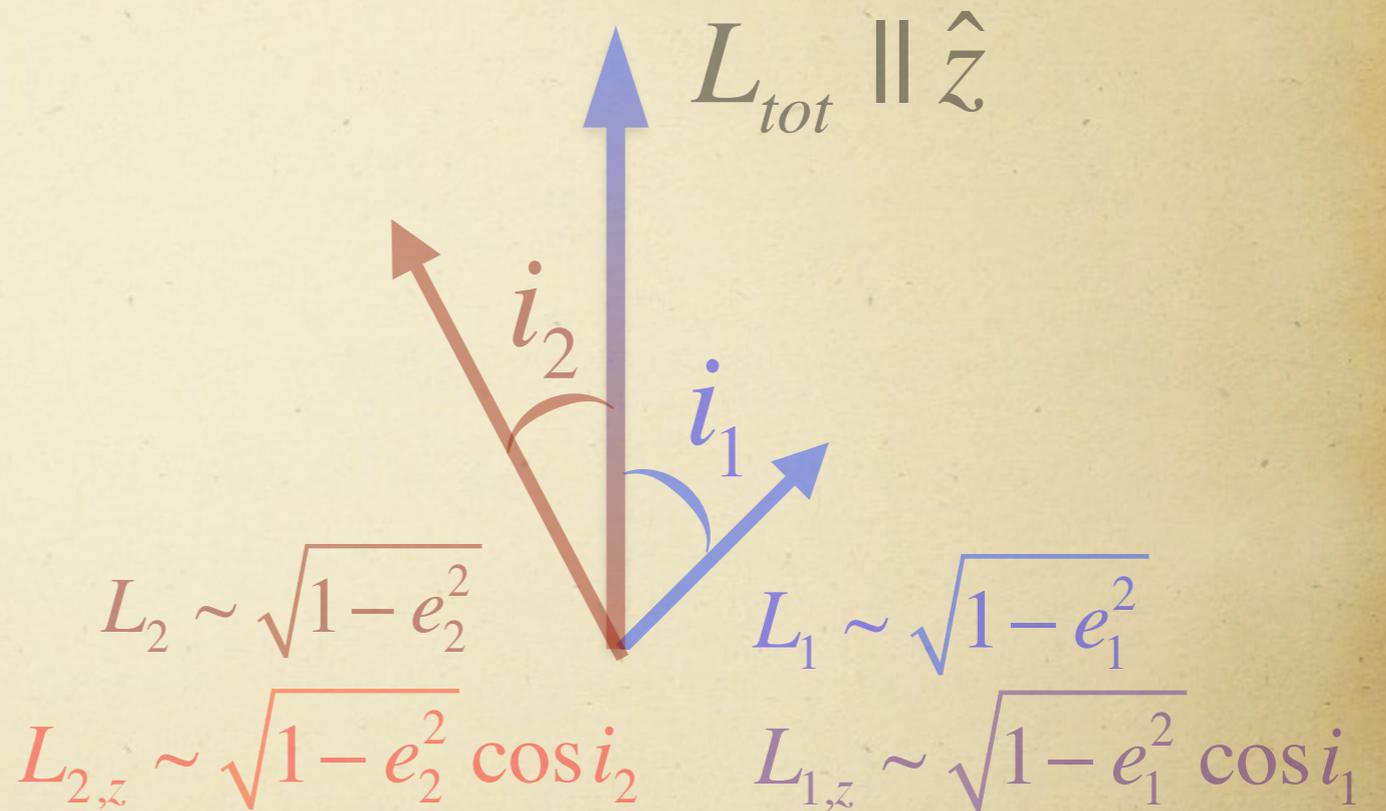
Is it constant?

Adding vector ...

$$\vec{L}_{tot} = \vec{L}_1 + \vec{L}_2$$

$$\vec{L}_2 = \vec{L}_{tot} - \vec{L}_1$$

$$L_2^2 = L_{tot}^2 + L_1^2 - 2L_{tot}L_1 \underbrace{\cos i_1}_{L_{1,z}}$$



Yoshihide Kozai

THE ASTRONOMICAL JOURNAL

VOLUME 67, NUMBER 9

NOVEMBER 1962

Secular Perturbations of Asteroids with High Inclination and Eccentricity

YOSHIHIDE KOZAI*

Smithsonian Astrophysical Observatory, Cambridge, Massachusetts

(Received August 29, 1962)

Secular perturbations of asteroids with high inclination and eccentricity moving under the attraction of the sun and Jupiter are studied on the assumption that Jupiter's orbit is circular. After about periodic time

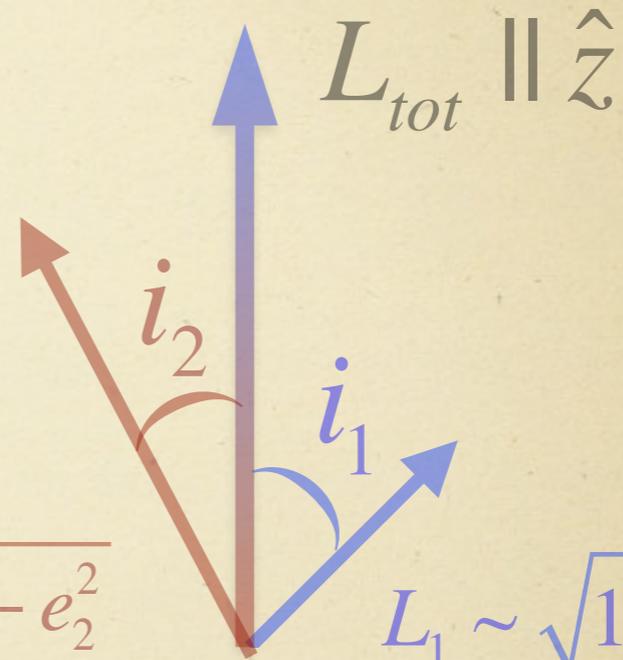
Is it constant?

Adding vector ...

$$\vec{L}_{tot} = \vec{L}_1 + \vec{L}_2$$

$$\vec{L}_2 = \vec{L}_{tot} - \vec{L}_1$$

$$L_2^2 = L_{tot}^2 + L_1^2 - 2L_{tot}L_1 \underbrace{\cos i_1}_{L_{1,z}}$$



$$L_2 \sim \sqrt{1 - e_2^2}$$

$$L_1 \sim \sqrt{1 - e_1^2}$$

$$L_{2,z} \sim \sqrt{1 - e_2^2} \cos i_2$$

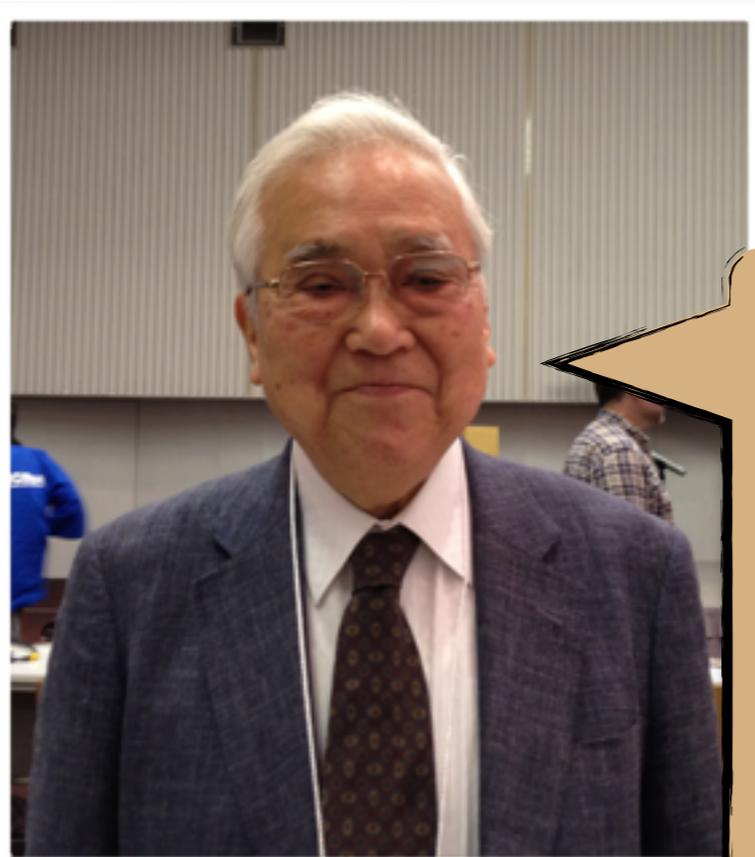
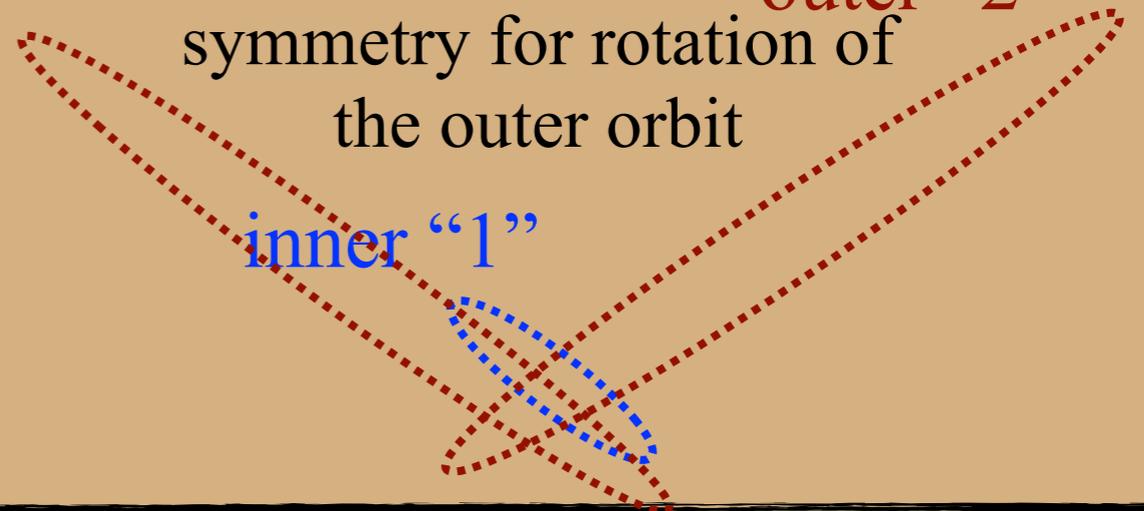
$$L_{1,z} \sim \sqrt{1 - e_1^2} \cos i_1$$

for the quadrupole approx. $\sim (a_1/a_2)^2$:

$$L_2 = Const.$$

outer "2"
symmetry for rotation of
the outer orbit

inner "1"



Yoshihde Kozai

Is it constant?

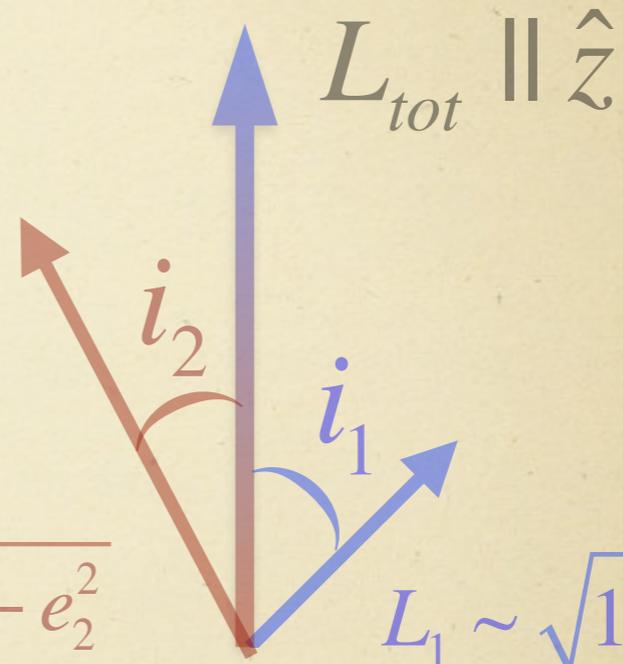
Adding vector ...

$$\vec{L}_{tot} = \vec{L}_1 + \vec{L}_2$$

$$\vec{L}_2 = \vec{L}_{tot} - \vec{L}_1$$

$$L_2^2 = L_{tot}^2 + L_1^2 - 2 L_{tot} L_1 \cos i_1$$

$$\underbrace{L_1 \cos i_1}_{L_{1,z}}$$



$$L_2 \sim \sqrt{1 - e_2^2}$$

$$L_1 \sim \sqrt{1 - e_1^2}$$

$$L_{2,z} \sim \sqrt{1 - e_2^2} \cos i_2$$

$$L_{1,z} \sim \sqrt{1 - e_1^2} \cos i_1$$

for the quadrupole approx. $\sim (a_1/a_2)^2$:

$$L_2 = \text{Const.}$$

$$L_{1,z} = \text{Const.}$$

$$L_{2,z} = \text{Const.}$$

$$L_1 \neq \text{Const.}$$

$$\mathcal{H}_{quad}(\omega_1)$$



Yoshihde Kozai

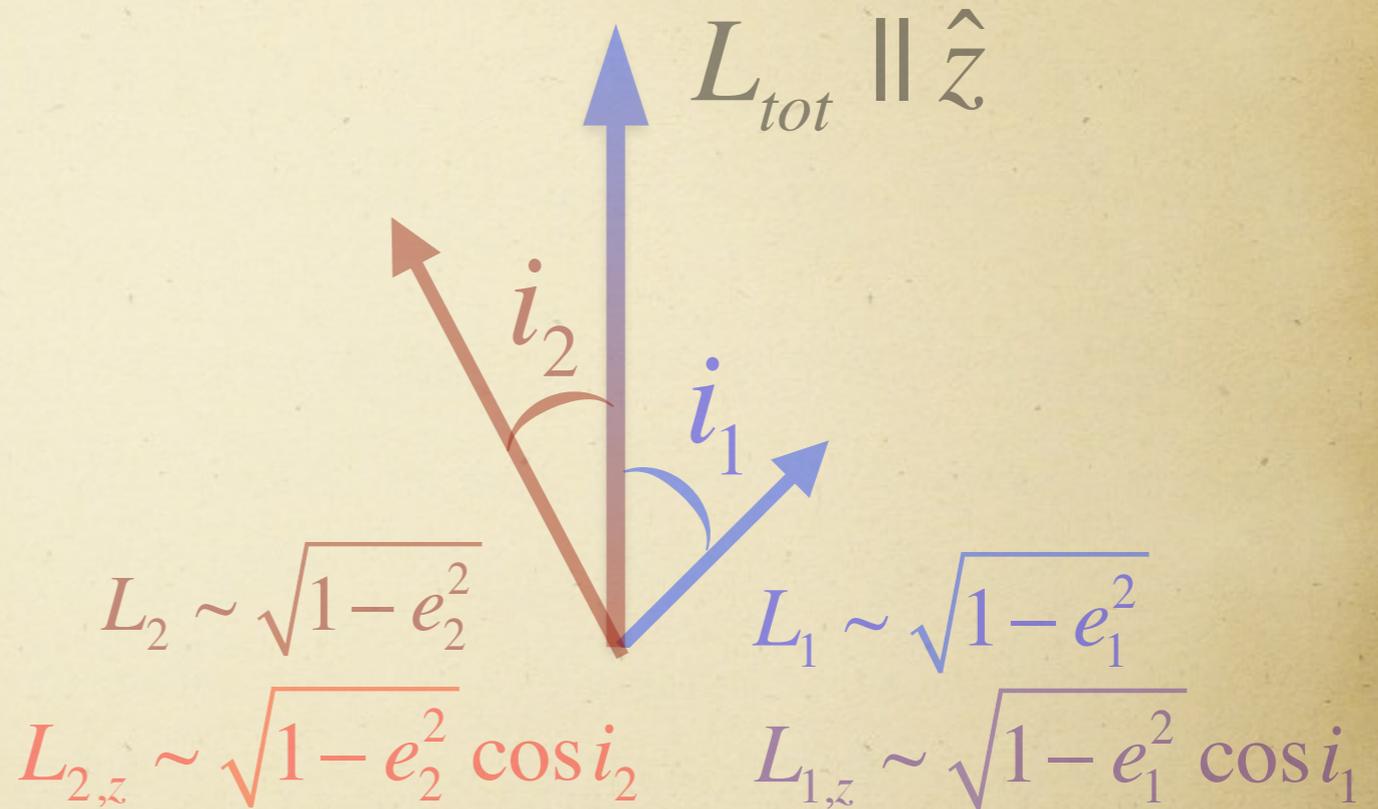
Is it constant?

Adding vector ...

$$\vec{L}_{tot} = \vec{L}_1 + \vec{L}_2$$

$$\vec{L}_2 = \vec{L}_{tot} - \vec{L}_1$$

$$L_2^2 = L_{tot}^2 + L_1^2 - 2 \underbrace{L_{tot} L_1 \cos i_1}_{L_{1,z}}$$



for the quadrupole approx. $\sim (a_1/a_2)^2$:

$$L_2 = \text{Const.}$$

$$L_{1,z} \neq \text{Const.}$$

$$L_{2,z} \neq \text{Const.}$$

$$L_1 \neq \text{Const.}$$

$$\mathcal{H}_{quad}(\omega_1, \underbrace{\Omega_1 - \Omega_2}_{\pi})$$

$$\frac{df}{dx}_{x=2} \neq \frac{df(x=2)}{dx}$$

Naoz et al, Nature (2011), arXiv:1011.2501

The Kozai-Lidov Formalism EKL

The eccentricity and inclination oscillate

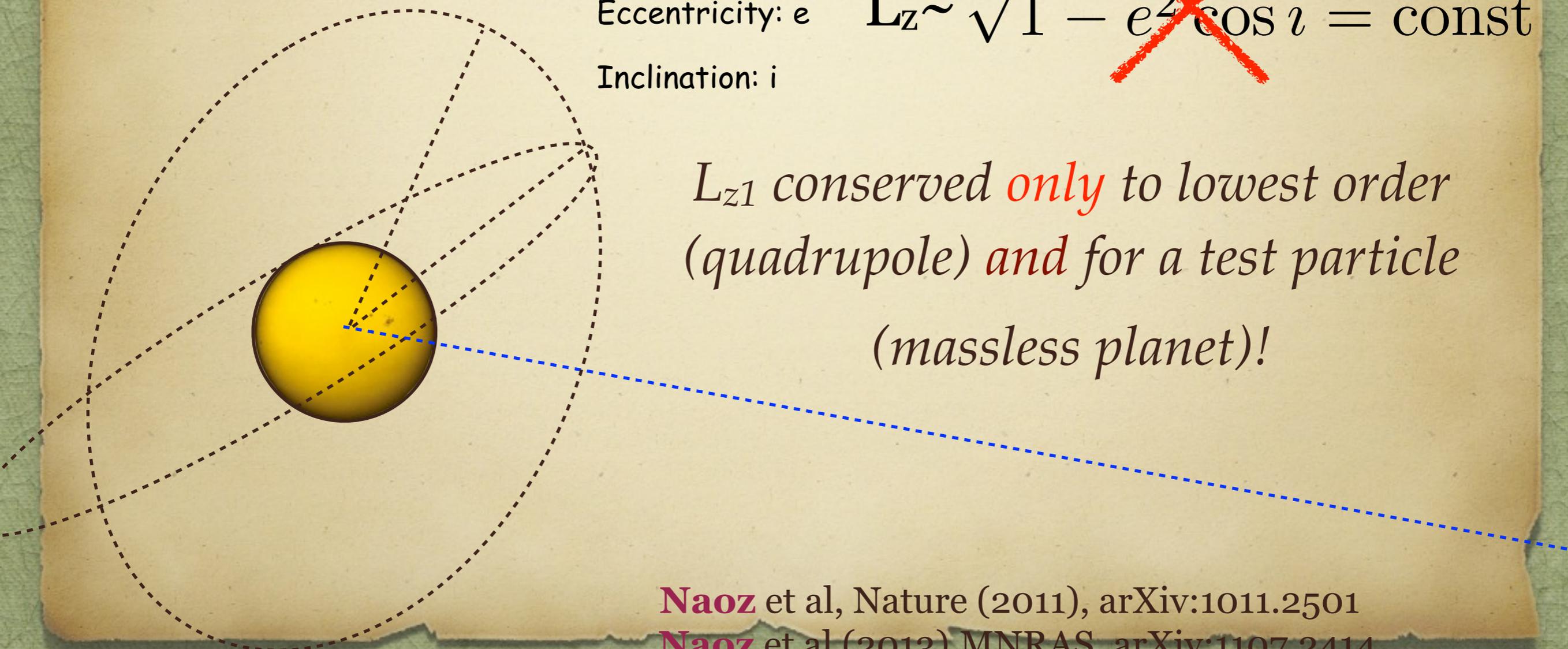
Conservation of ~~the~~ z component of angular momentum for both the inner ~~outer~~ orbits

The orbital elements:

Eccentricity: e $L_z \sim \sqrt{1 - e^2} \cos i = \text{const}$

Inclination: i

L_{z1} conserved *only* to lowest order (quadrupole) *and* for a test particle (massless planet)!



Naoz et al, Nature (2011), arXiv:1011.2501

Naoz et al (2013), MNRAS, arXiv:1107.2414

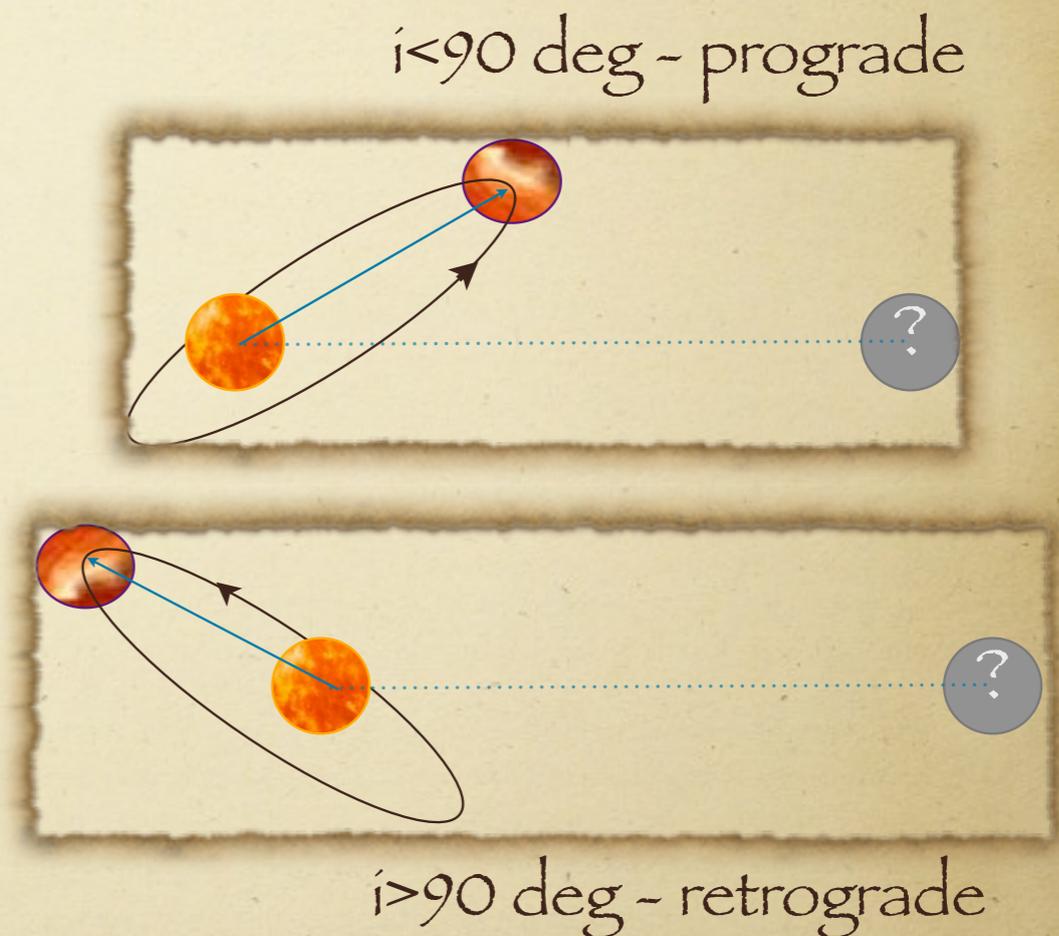
Our treatment

The eccentric Kozai-Lidov mechanism - KEL

- Allow for the **z-component** of the angular momenta of the **inner** and **outer** orbit to change - already at the **quadrupole level**
- Expanding the approximation to the **octupole level** (e.g., Ford et al 2000, Blaes et al 2002 - already done before us!!!)
- Both the magnitude and orientation of the angular momentum can change

larger parts of the parameter space

Naoz et al, Nature (2011), arXiv:1011.2501
Naoz et al (2013), MNRAS, arXiv:1107.2414



for test particle approx. see:
Lithwick & **Naoz** (2011), ApJ, arXiv:1106.3329
Katz, Dong Malhotra (2011), arXiv:1106.3340

Lets...flip the planet



point mass limit

Lets...flip the planet

Example system: $a_1=6\text{AU}$, $a_2=100\text{AU}$, $m_1=1.M_{\text{sun}}$ $M_2=1M_j$, $M_3=40M_j$ $i=65$ deg secular dynamics + GR

GR effects: e.g., Ford et al 2000,
Naoz, Kocsis, Loeb, Yunes 2013

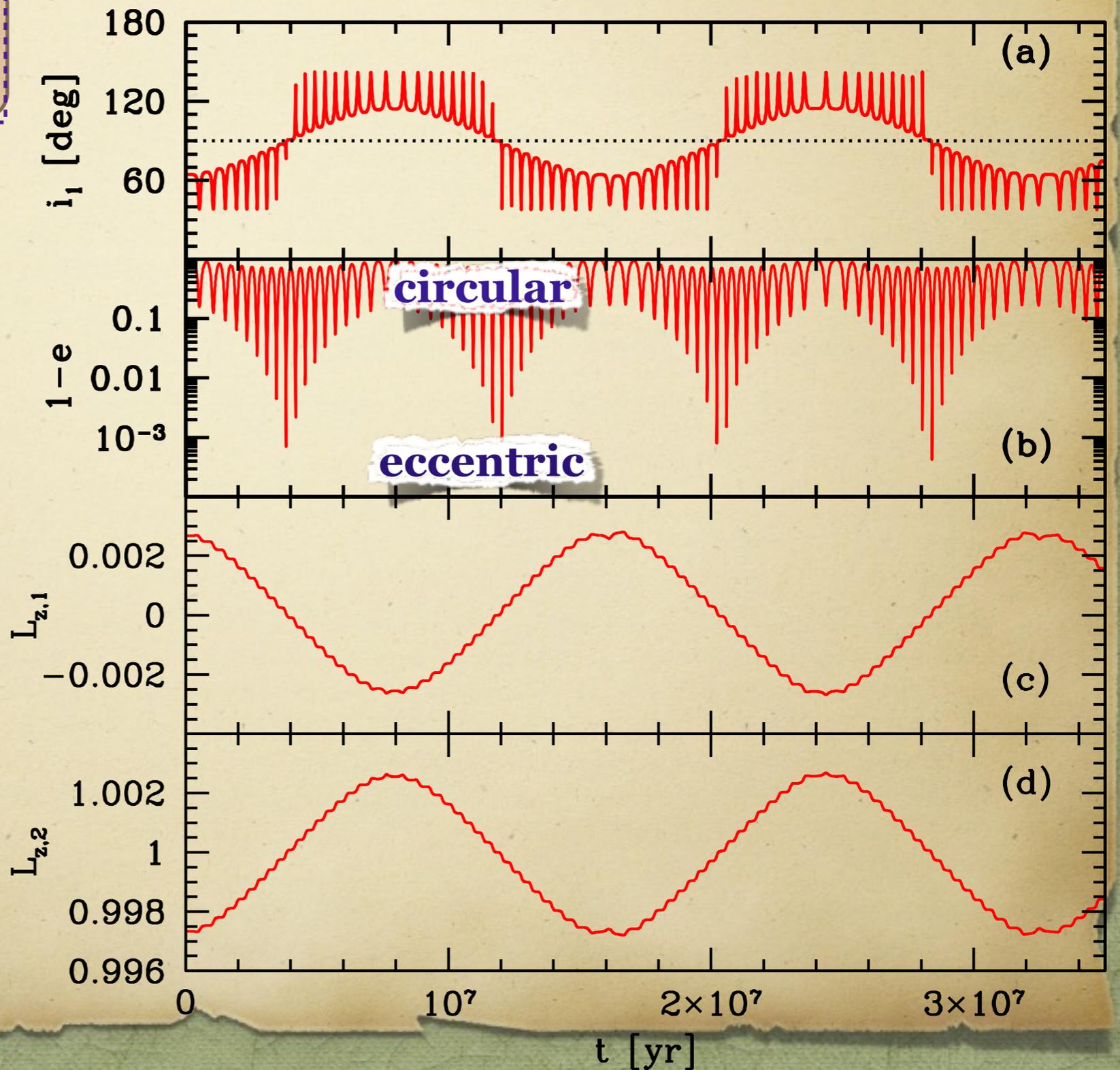
(a) inner orbit inclination

(b) inner orbit eccentricity

(c) inner orbit z-com.
angular momentum

(d) inner orbit z-com.
angular momentum

Naoz et al, Nature (2011)



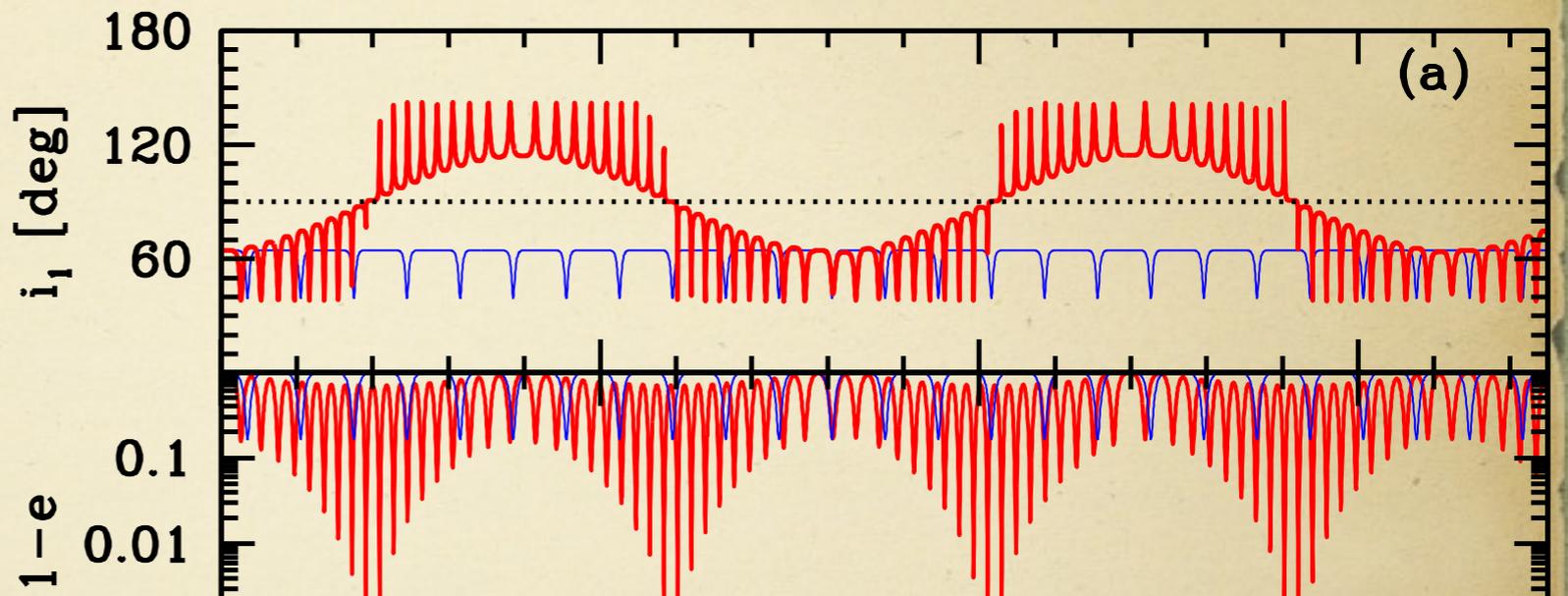
point mass limit

Lets...flip the planet

Example system: $a_1=6\text{AU}$, $a_2=100\text{AU}$, $m_1=1.M_{\text{sun}}$ $M_2=1M_j$, $M_3=40M_j$ $i=65$ deg secular dynamics + GR

GR effects: e.g., Ford et al 2000,
Naoz, Kocsis, Loeb, Yunes 2013

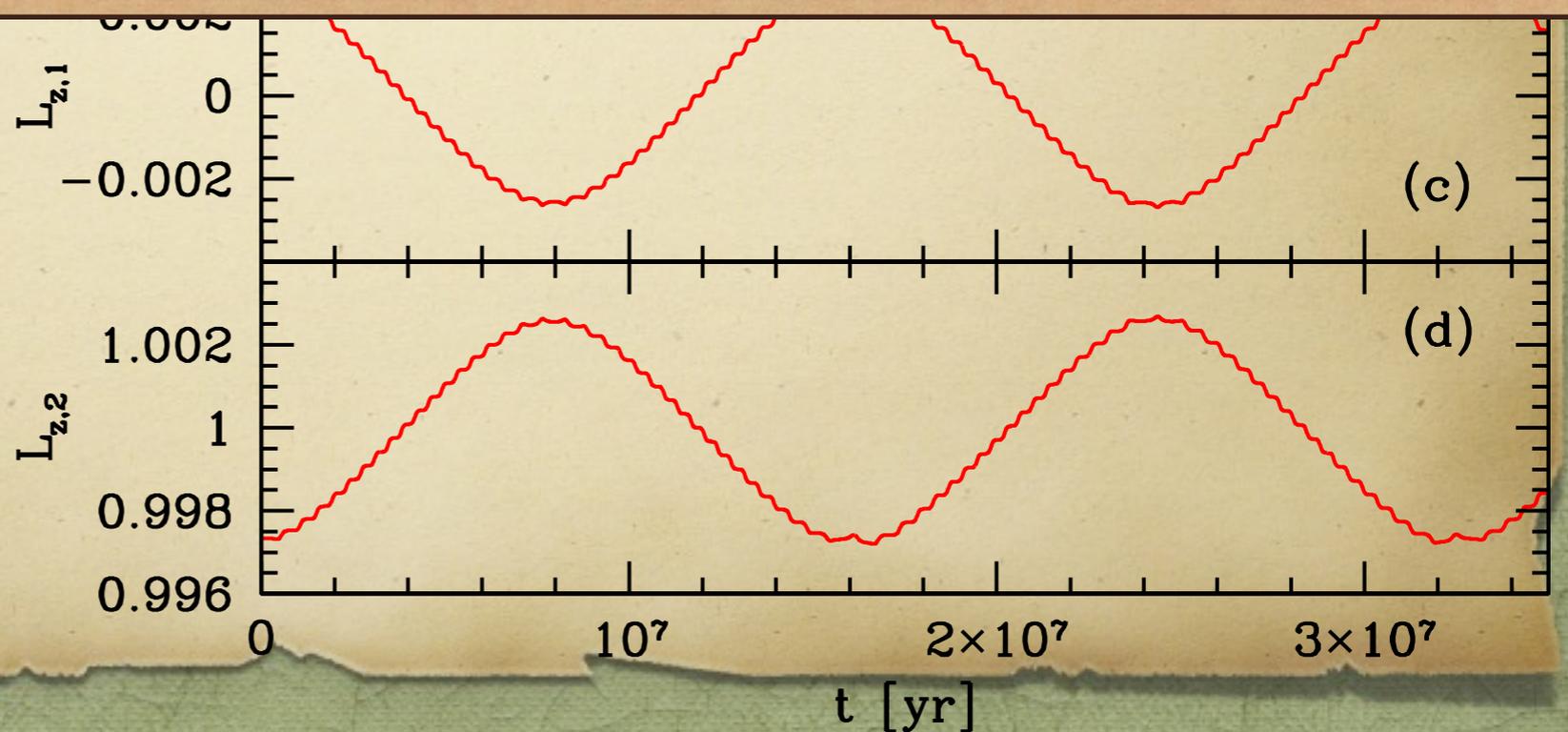
(a) inner orbit inclination



(b) inner orbit eccentricity

(c) inner orbit z-com.
angular momentum

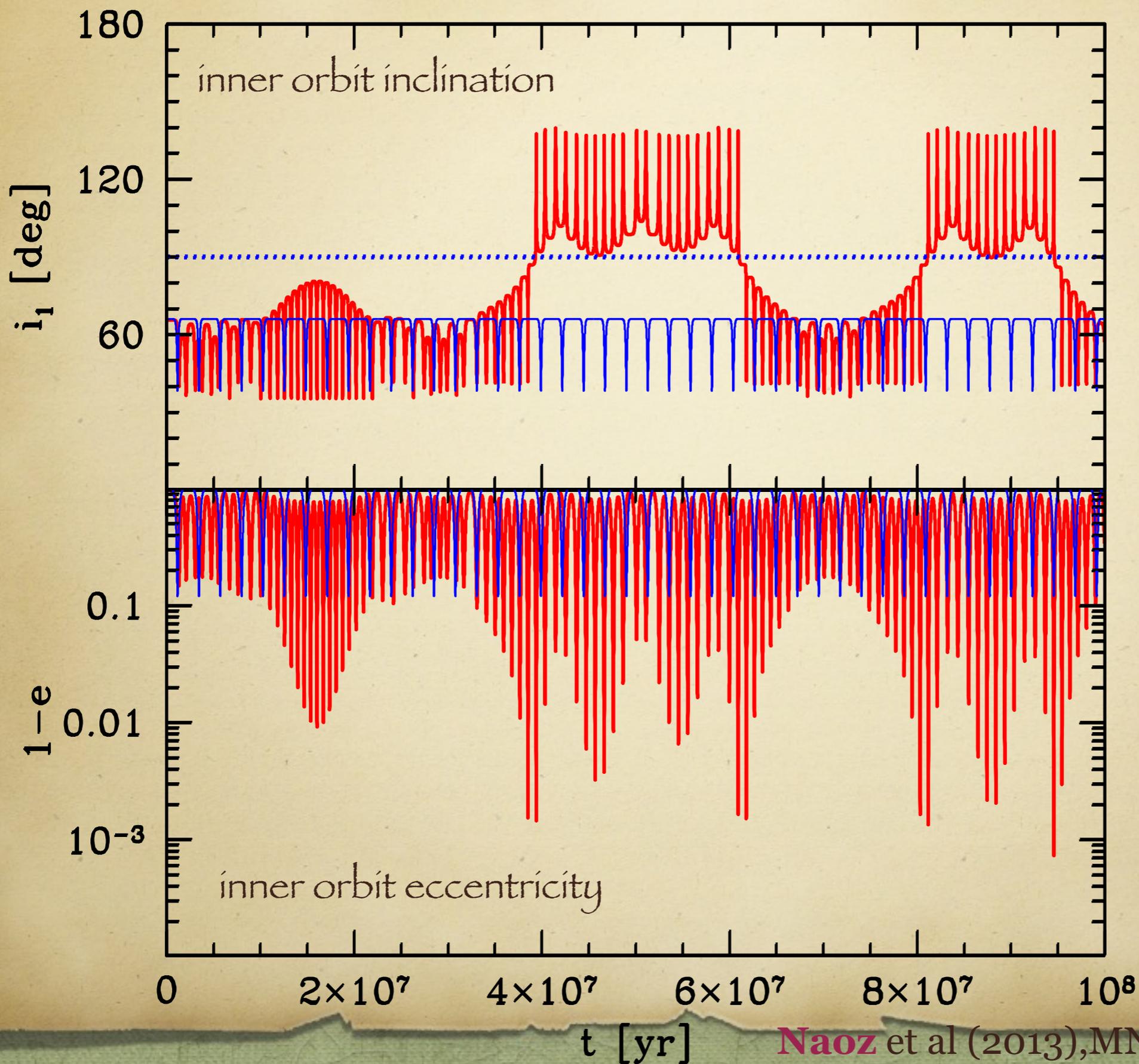
Compare to: "Standard" (quadrupole) Kozai



(d) inner orbit z-com.
angular momentum

Naoz et al, Nature (2011)

EKL



$$M_1 = 1 M_\odot$$

$$M_2 = 1 M_J$$

$$M_3 = 4 M_J$$

$$a_1 = 5 \text{ AU}$$

$$a_2 = 51 \text{ AU}$$

$$i = 71^\circ$$

Question

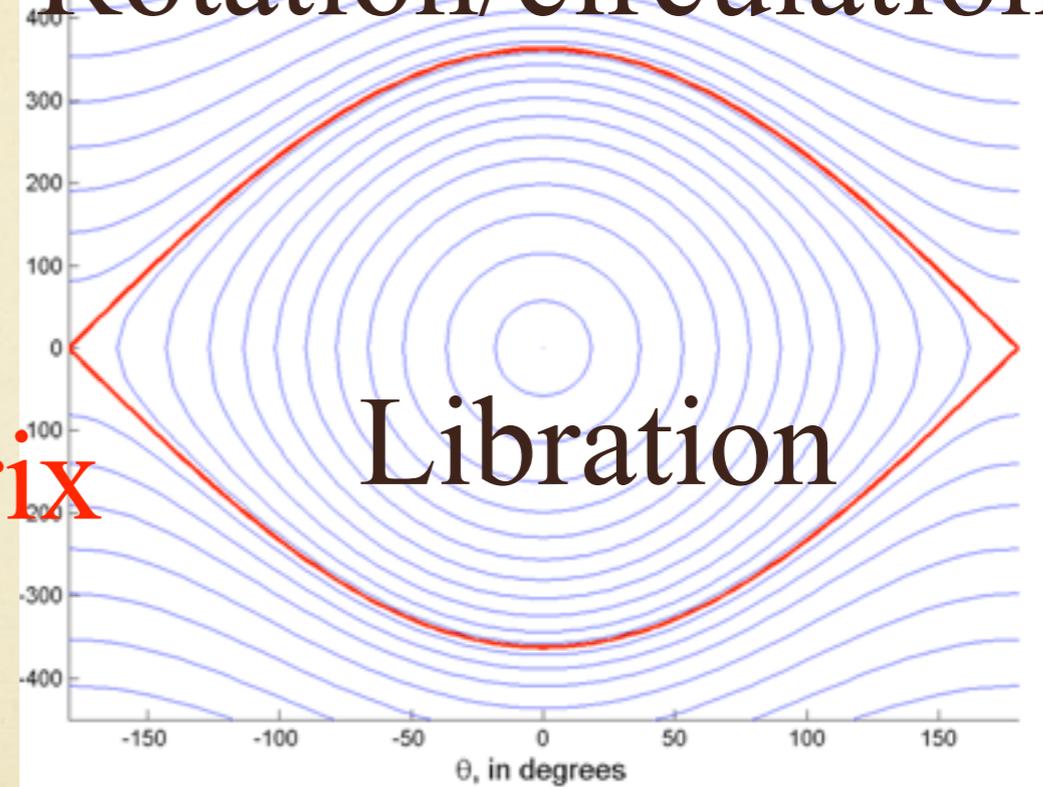
- Why high inclination $>40^\circ$?
- Is high inclination required also in the EKL mechanism?
- What about chaos?

EKL and the Pendulum

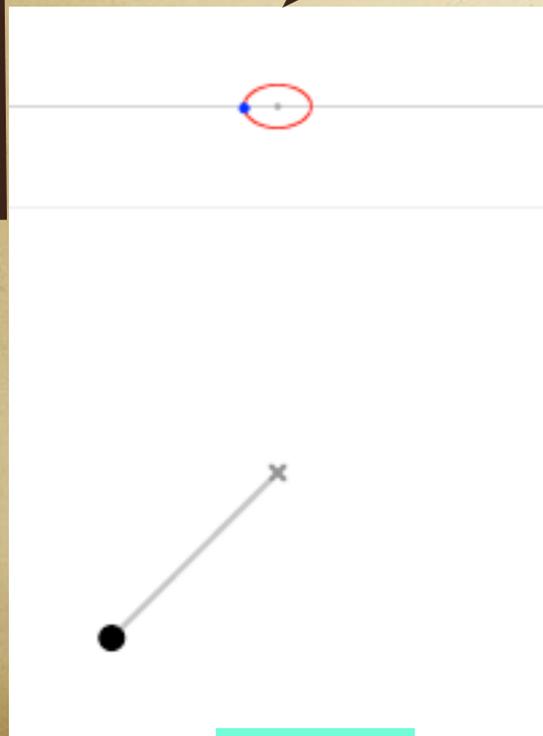
The Pendulum

$$H(\theta, p) = \frac{p^2}{2mL} - mgL \cos \theta$$

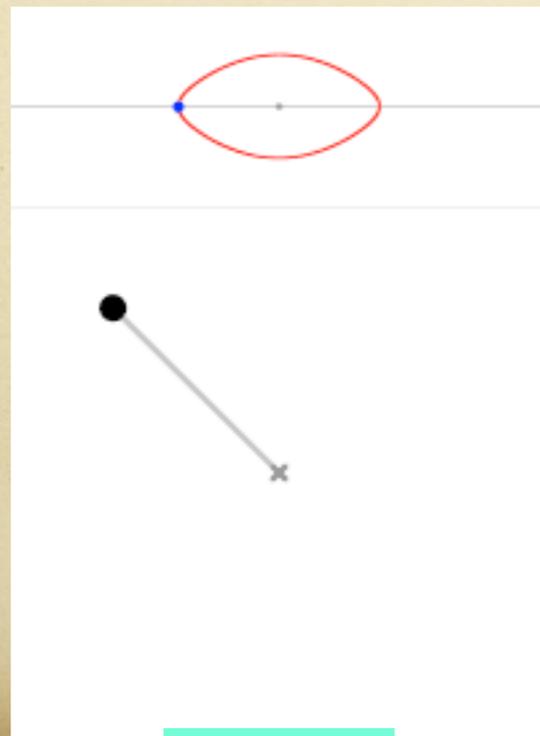
Rotation/circulation



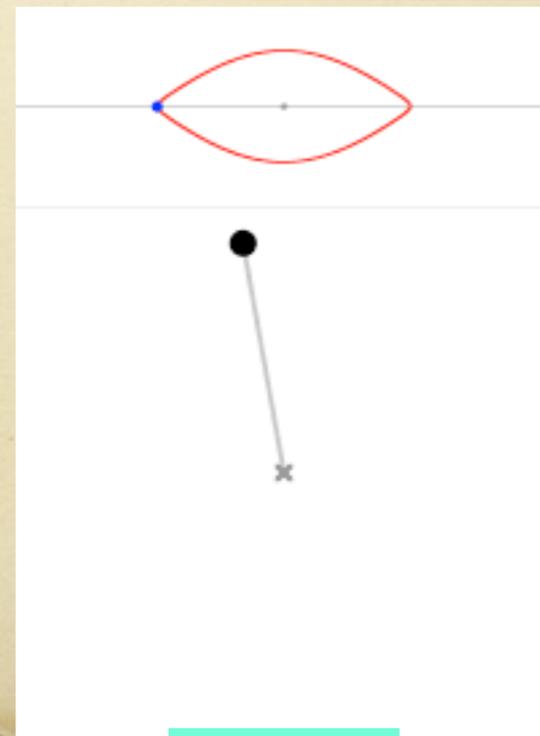
The separatrix



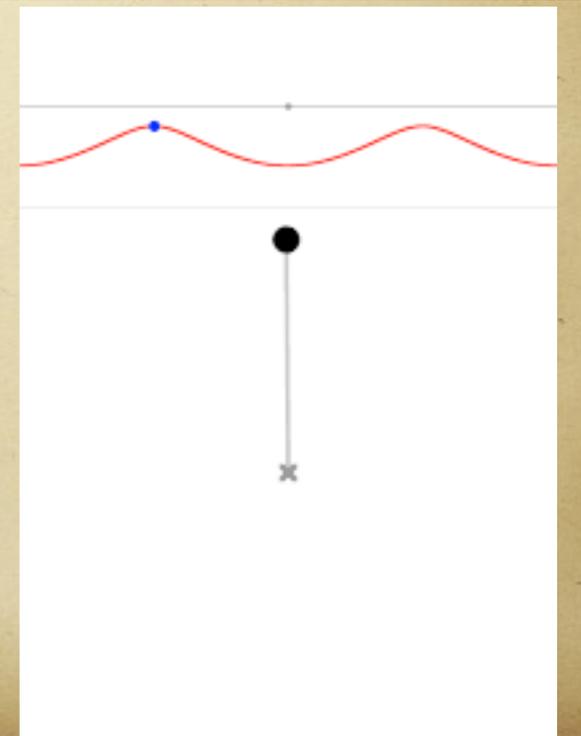
$\theta_0 = 45^\circ$



$\theta_0 = 135^\circ$



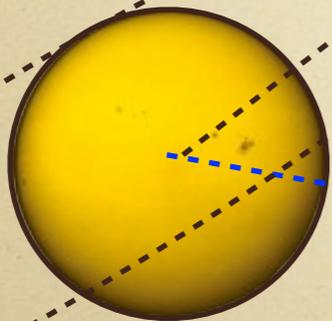
$\theta_0 = 170^\circ$



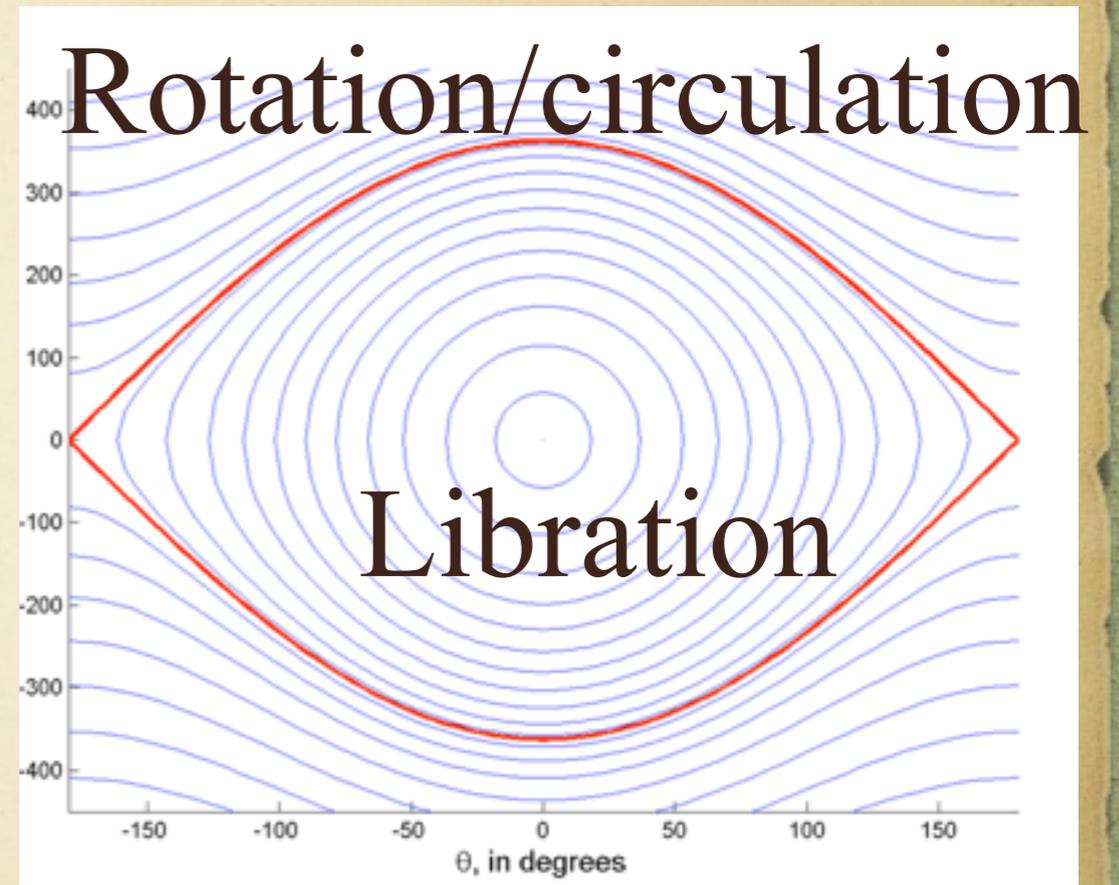
EKL and the Pendulum

Quadrupole test particle limit:

$$e_0 = 0$$

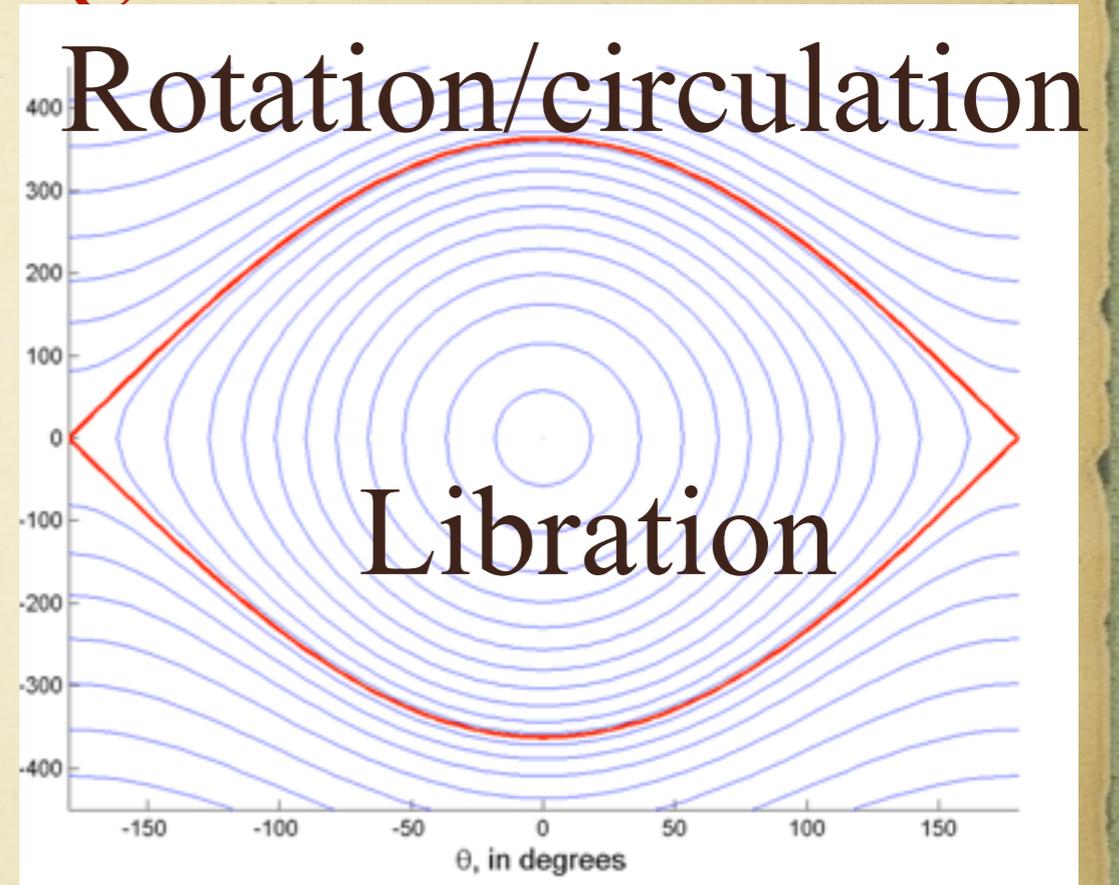
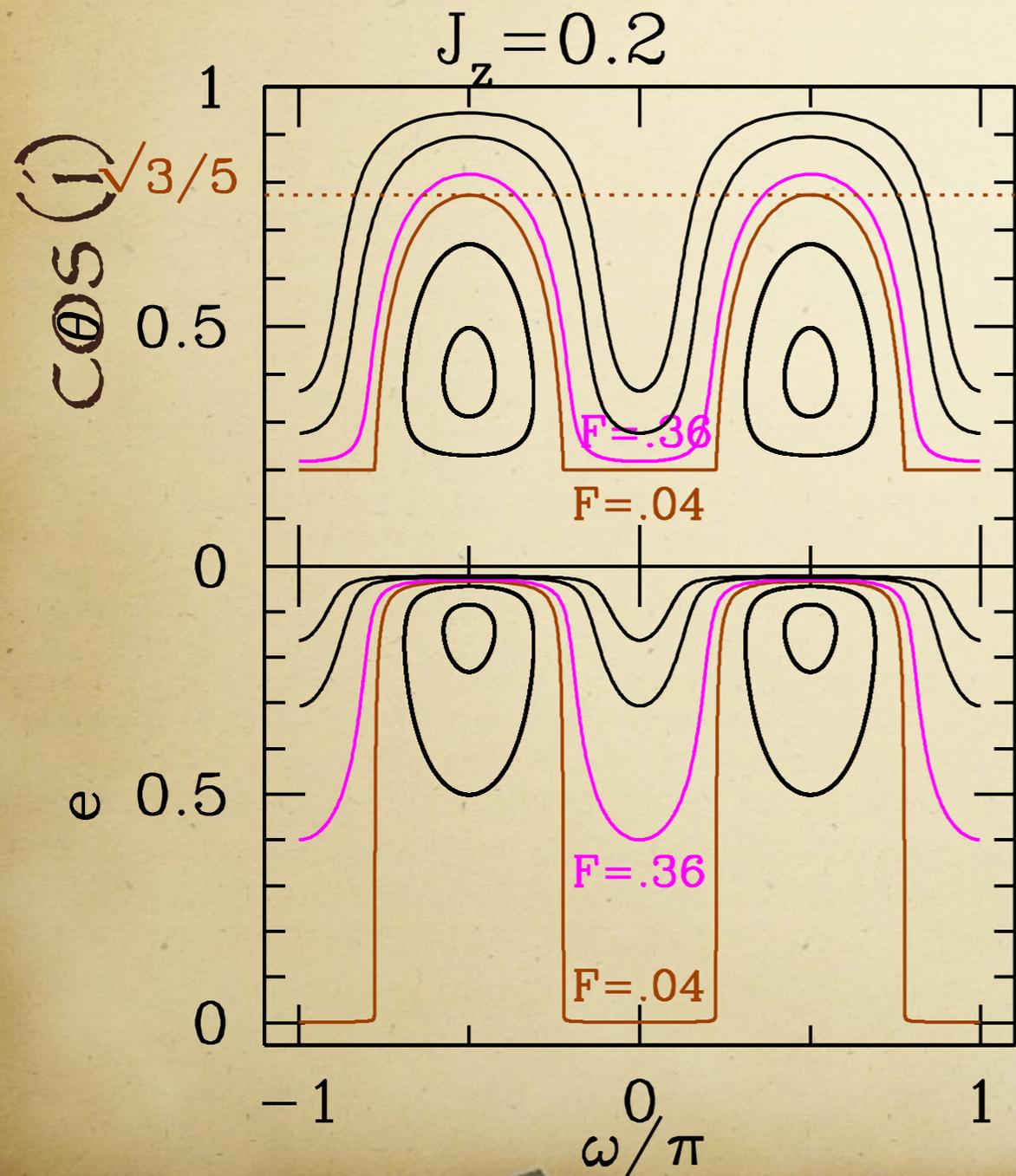


circular outer orbit



Q: Why 40 - 140 degrees limits?

Quadrupole test particle limit:

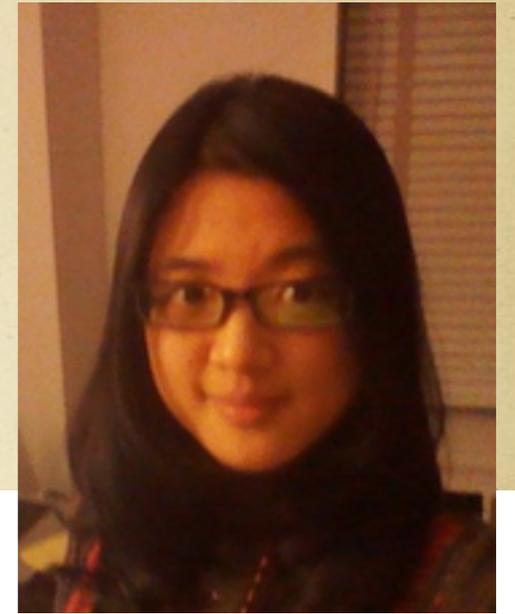


A: The separatrix has:

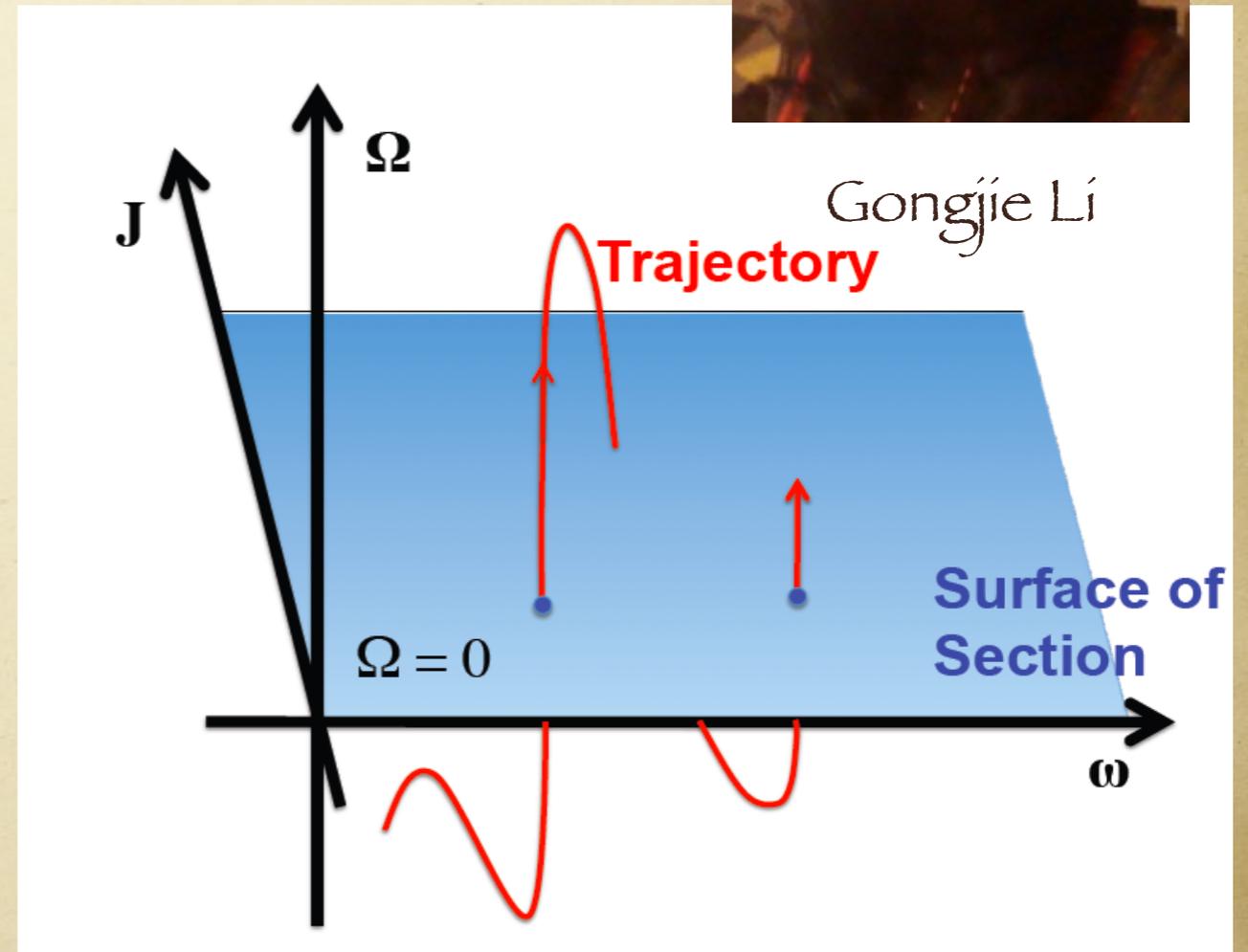
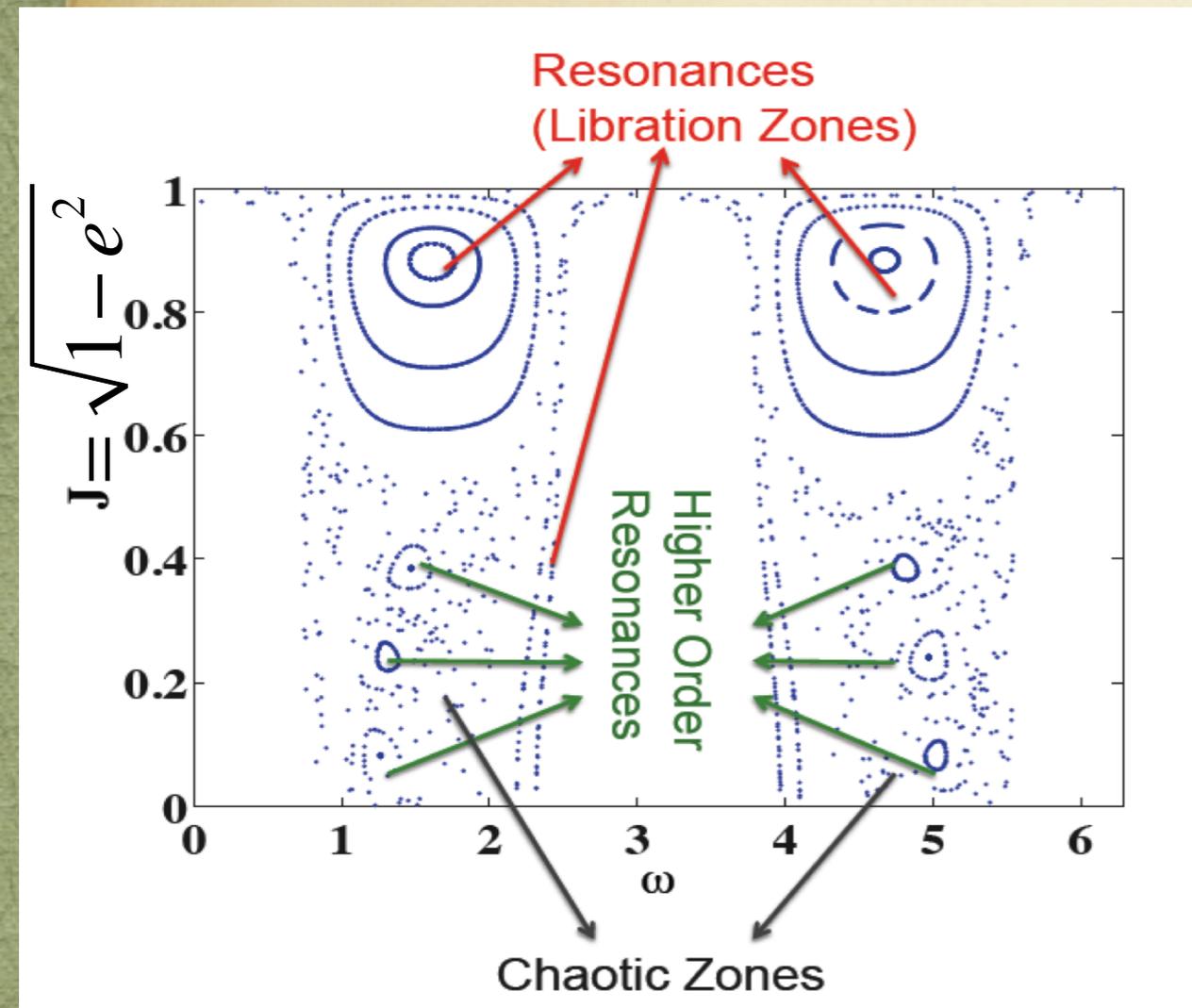
$$e_0 = 0, \cos i_0 = \sqrt{\frac{3}{5}}$$

Q: Is the 40 - 140 degrees limits hold?

A: No

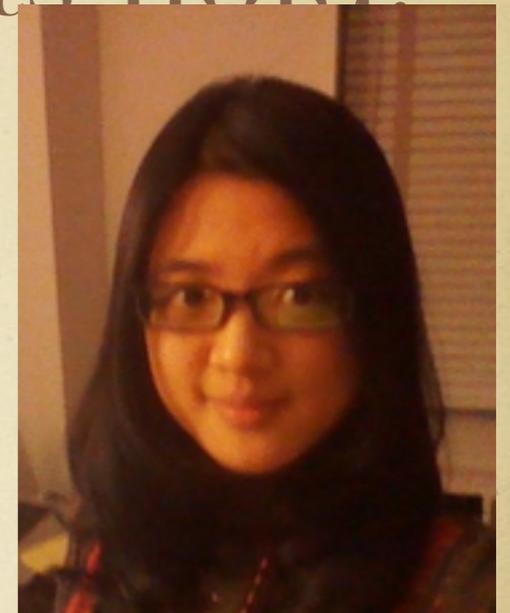


Gongjie Li

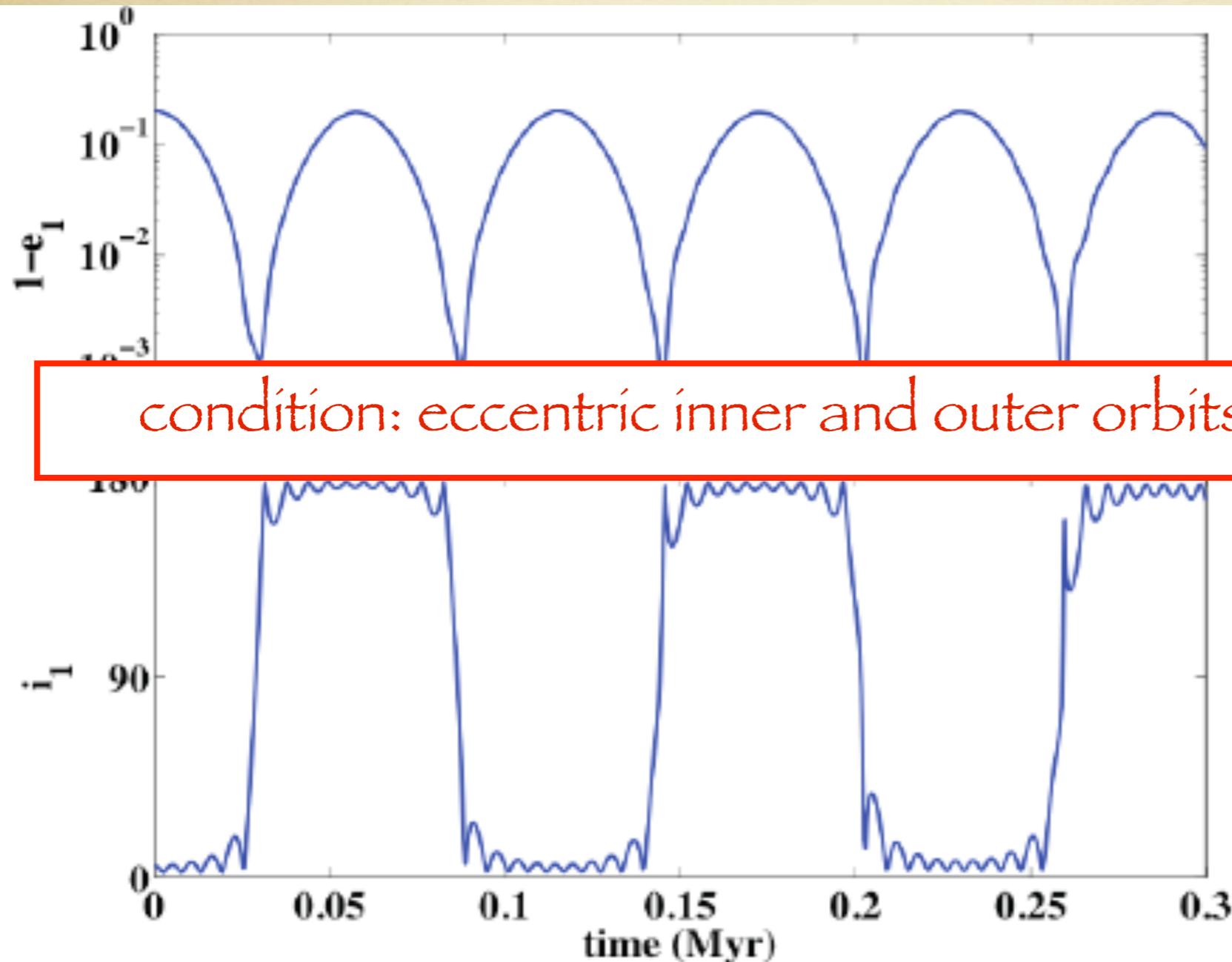


Q: Is the 40 - 140 degrees limits hold?

A: No



Gongjie Li



condition: eccentric inner and outer orbits

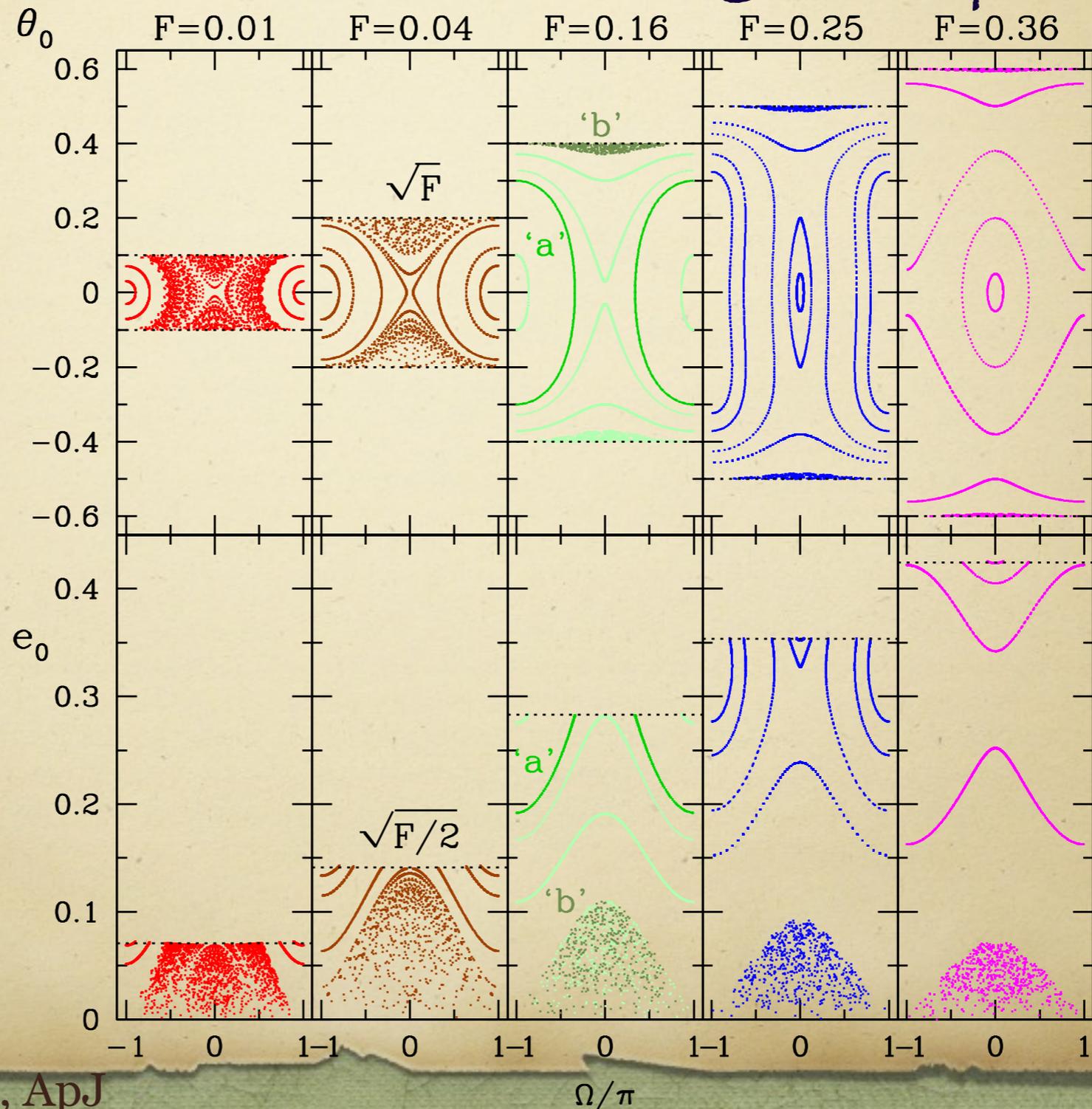
$\omega_1 = 0^\circ, \Omega_1 = 180^\circ,$
 $e_2 = 0.6, a_1 = 4AU, a_2 = 50AU$
 $e_1 = 0.8, i = 5^\circ$
 $m_1 = 1M_\odot, m_2 = 1M_J, m_3 = 0.3M_\odot$

Li, **Naoz**, Kocsis, Loeb 2014, ApJ arXiv:1310.6044

Li, **Naoz**, Holman, Loeb 2014, ApJ arXiv:1405.0494

Q: Why Chaos?

A: Octupole - chaotic behavior crossing the separatrix



chaos in these
systems: Holman, Touma
& Tremaine (1997)

Maximum eccentricity and initial conditions

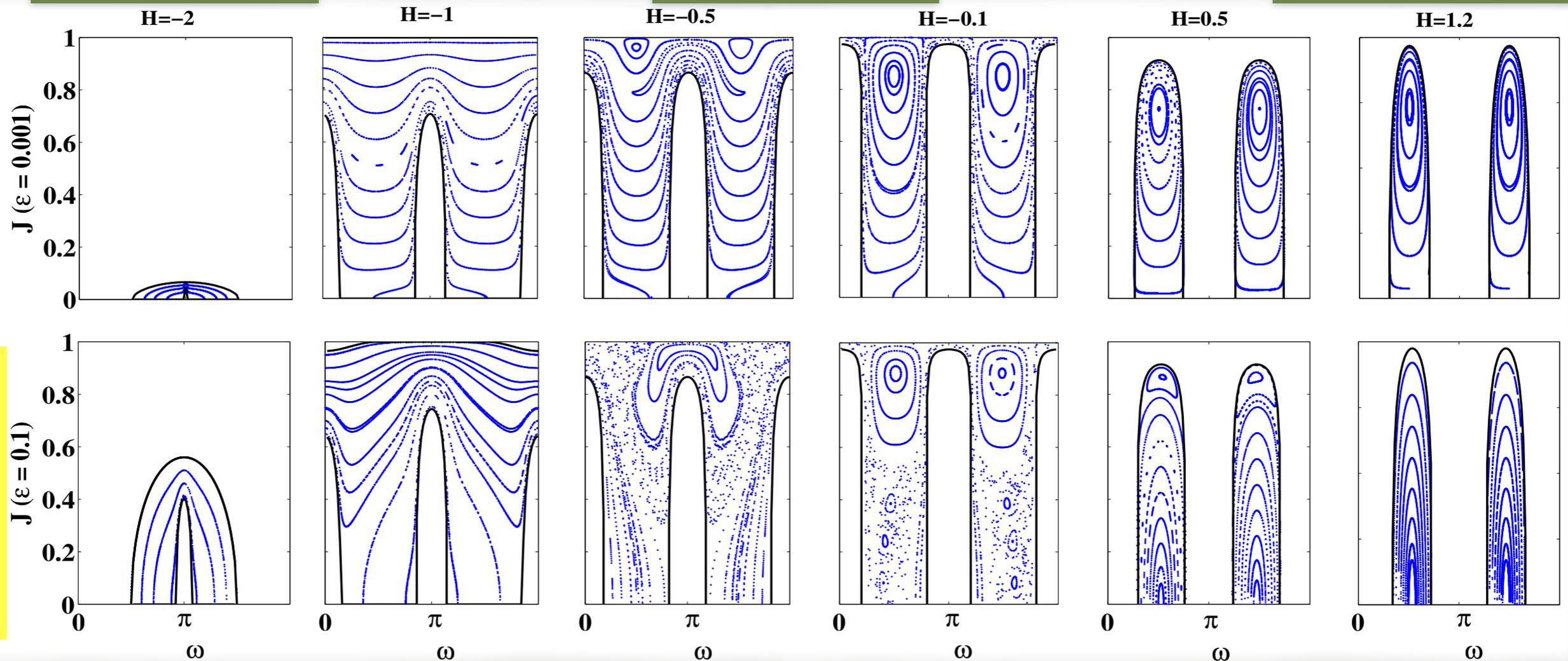


Gongjie Li

Low i High e

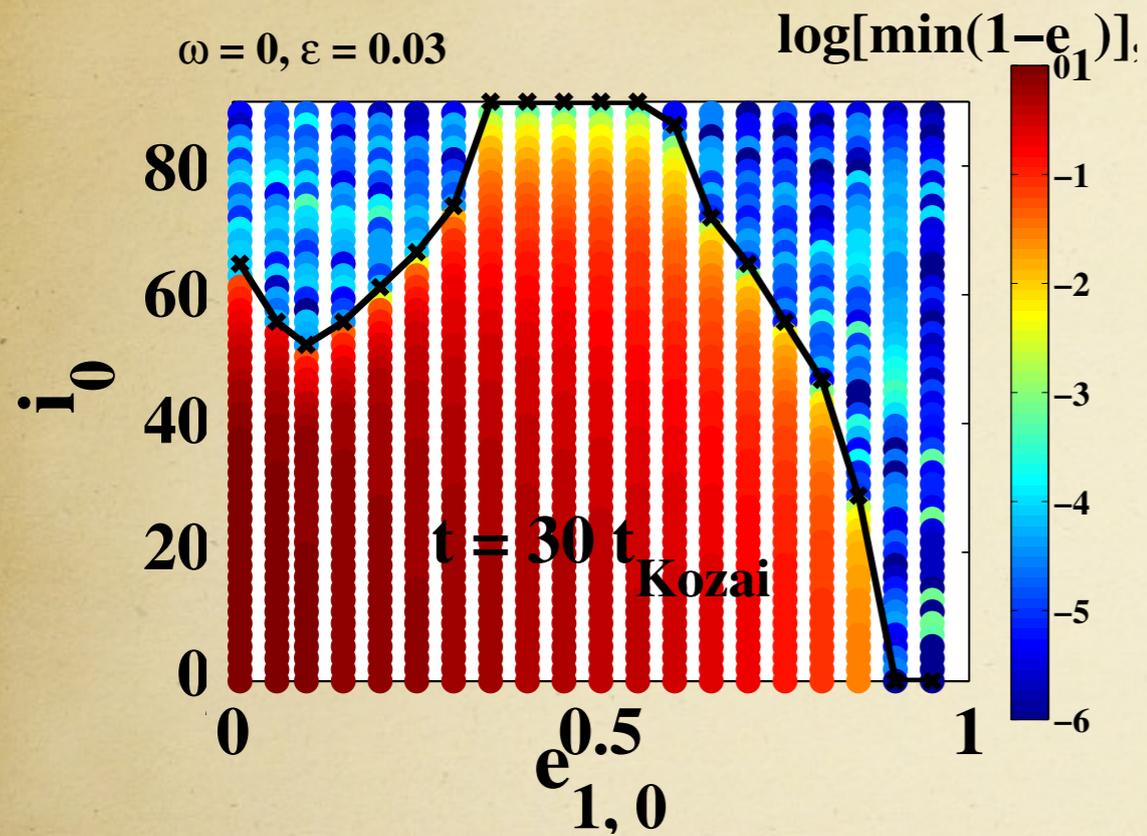
High i Low e

High i High e



octupole plays important role

Eccentricity spikes



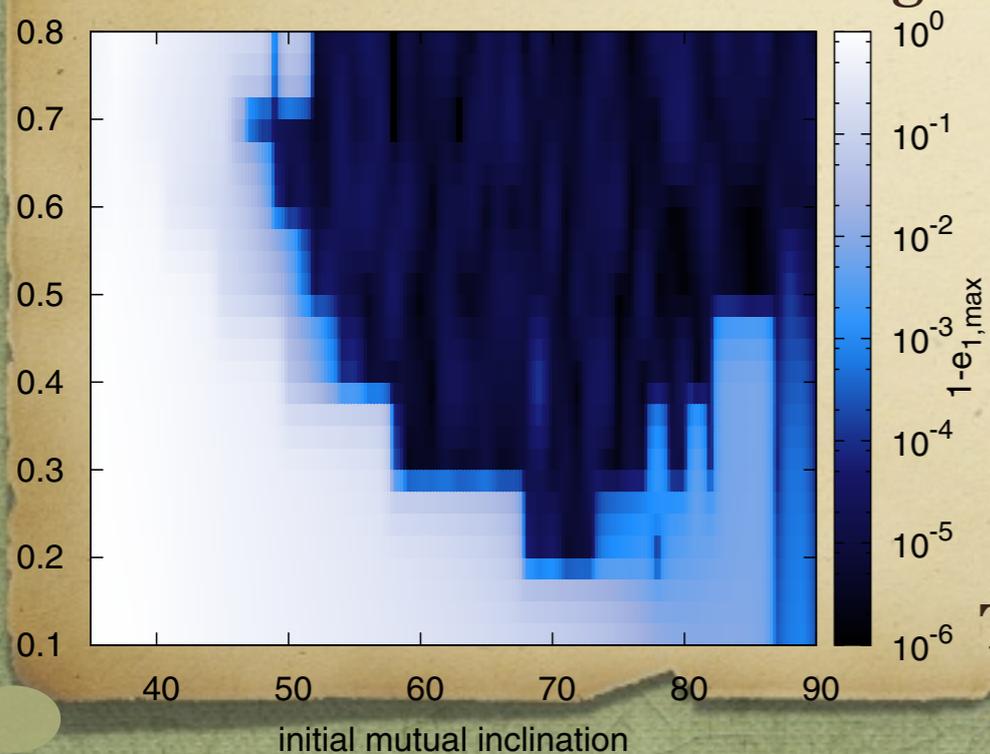
Maximum eccentricity at the **test particle** regime

Li, **Naoz** et al, (2014), ApJ 785, 116 + ApJ 791, 86



Gongjie Li

Maximum eccentricity **outside** the test particle regime



Teyssandier, **Naoz**, Lizarraga Rasio (2013), ApJ 779, 166



Ian Lizarraga



Jean Teyssandier

Astrodynamics is alive!

