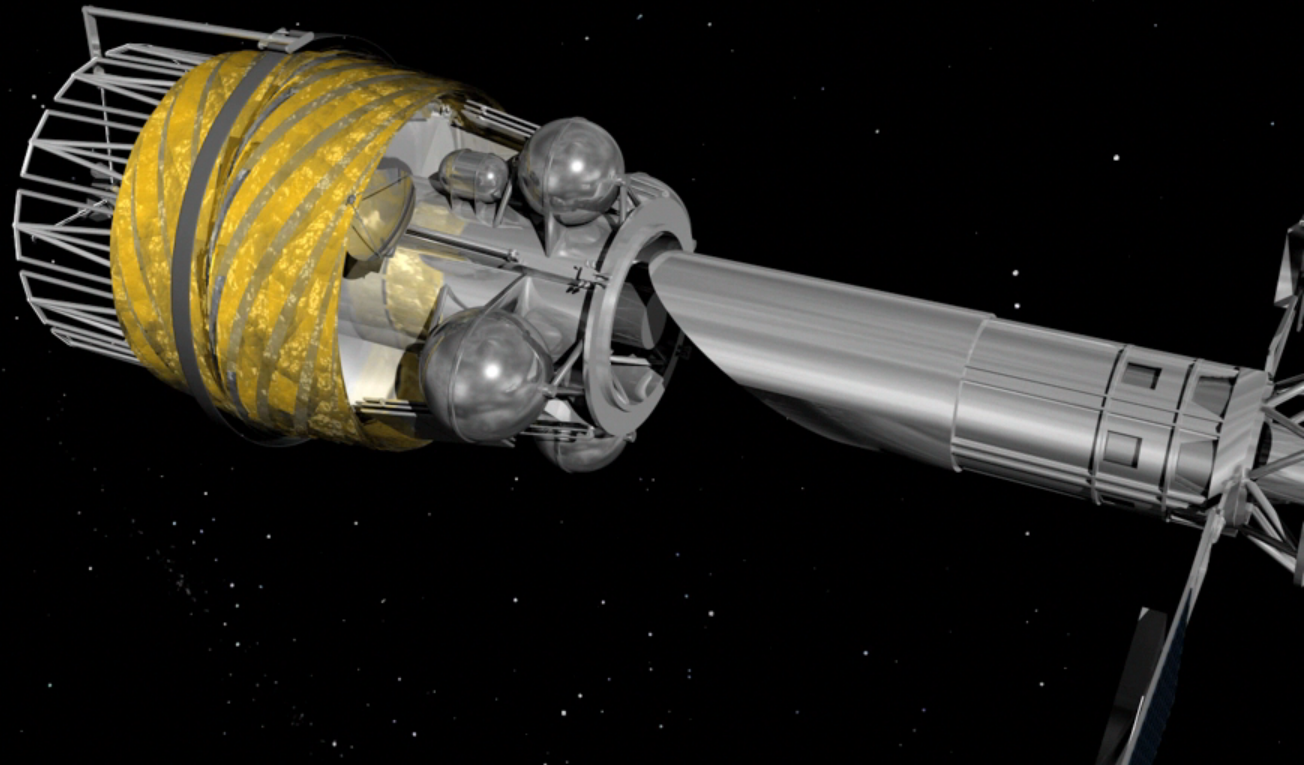




**Aki Roberge**  
**NASA Goddard Space Flight Center**

**THE THEORY AND DEVELOPMENT  
OF STARSHADES**



# Starshade strengths

- Contrast and inner working angle decoupled from telescope aperture size
  - IWA not proportional to  $\lambda / D$  anymore
- Broad bandpass, high total throughput
- No constraints on other astronomical instruments



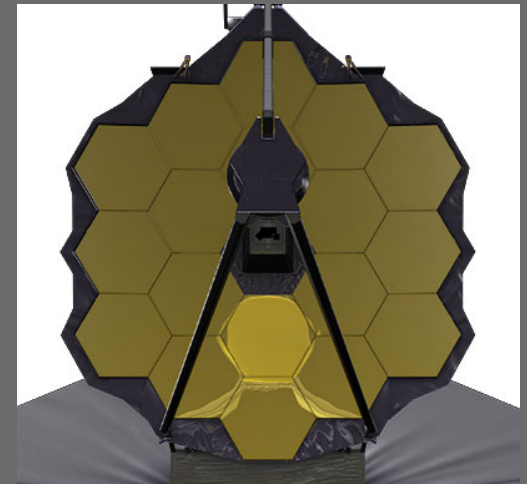
NASA / Swift

# Starshade strengths

- No outer working angle
- 360 degree suppressed field of view
- High quality telescope not required
  - Segments & obstructions not a problem
  - Wavefront correction unnecessary



W. Cash (Colorado)



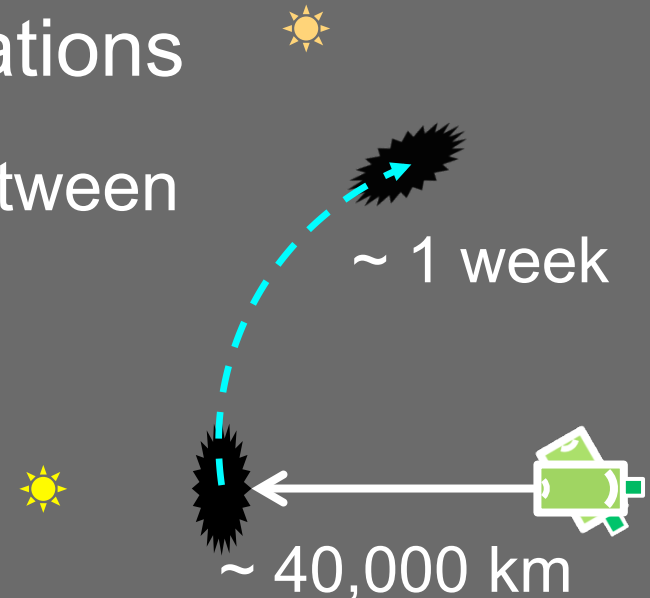
NASA / STScI

# Starshade drawbacks

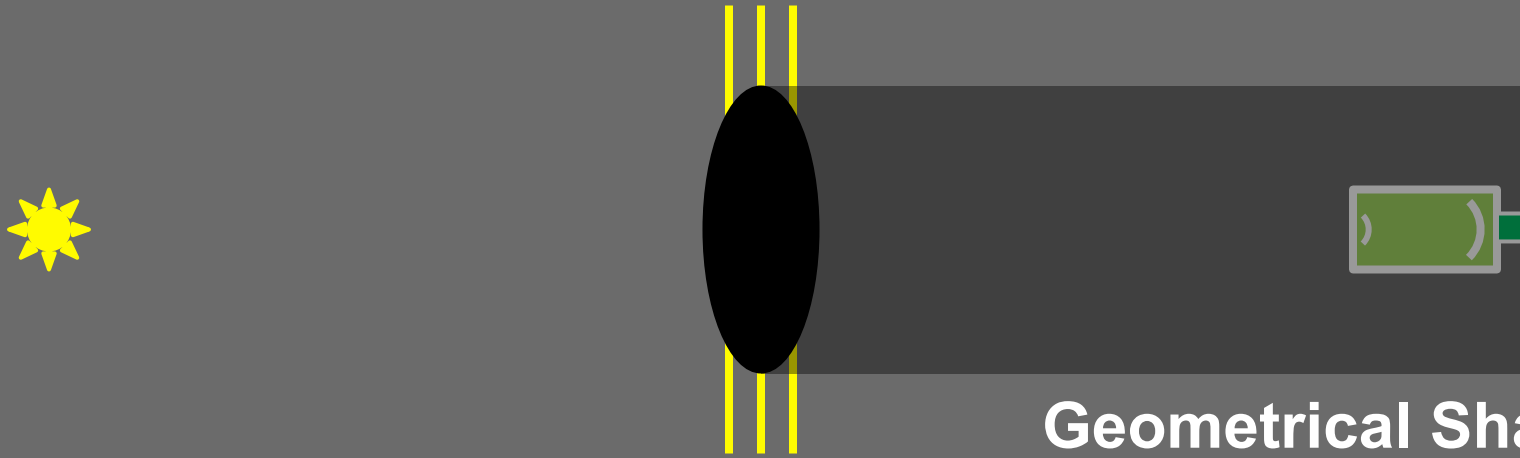
- Full-scale end-to-end system test on the ground not possible
  - Sub-scale lab and field tests possible (more later)
- Long times between observations
  - Need to slew the starshade between targets
- Limited number of starshade movements



T. Glassman / NGAS



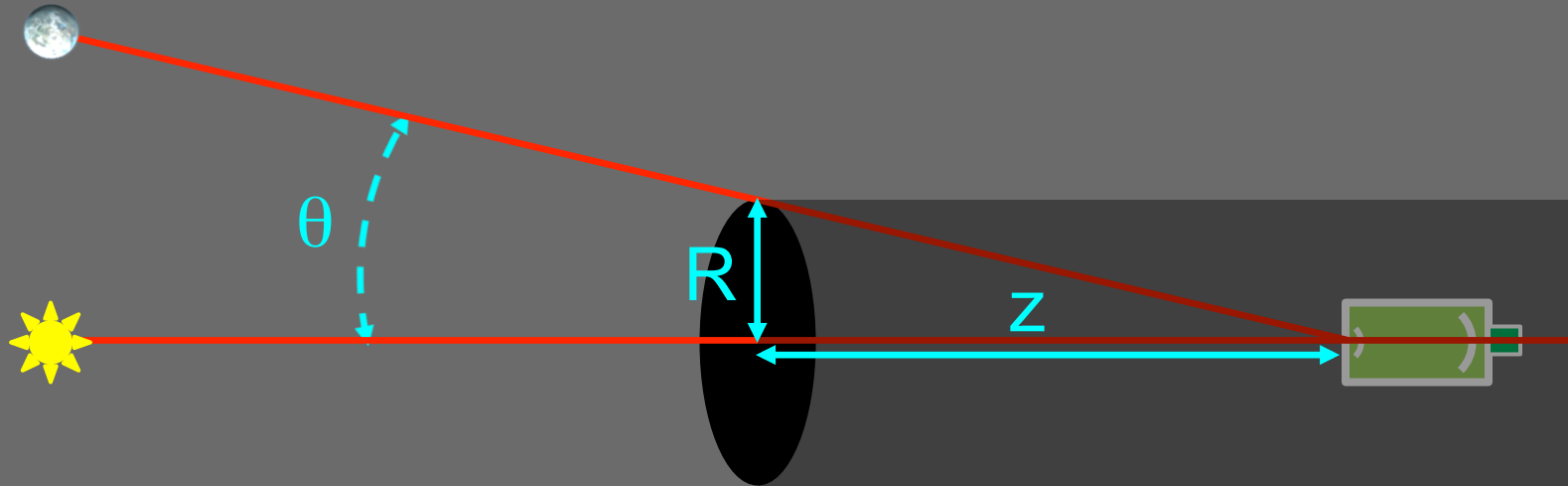
# Basics: shadow the telescope



- Starshade positioned to block the starlight
- Must be larger than the telescope to keep the starlight out

Credit: S. Shaklan

# Inner working angle

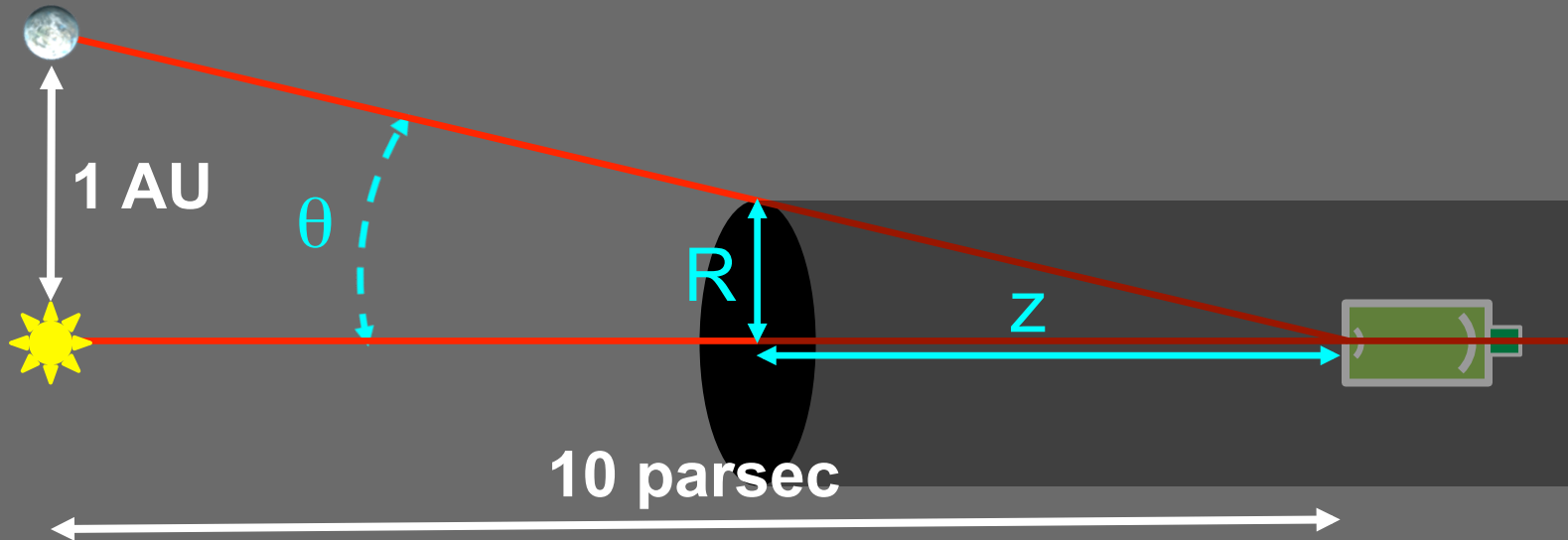


**Geometrical Shadow**

IWA  $\sim$  angle to edge of starshade

$$\theta \sim R / z$$

# Inner working angle



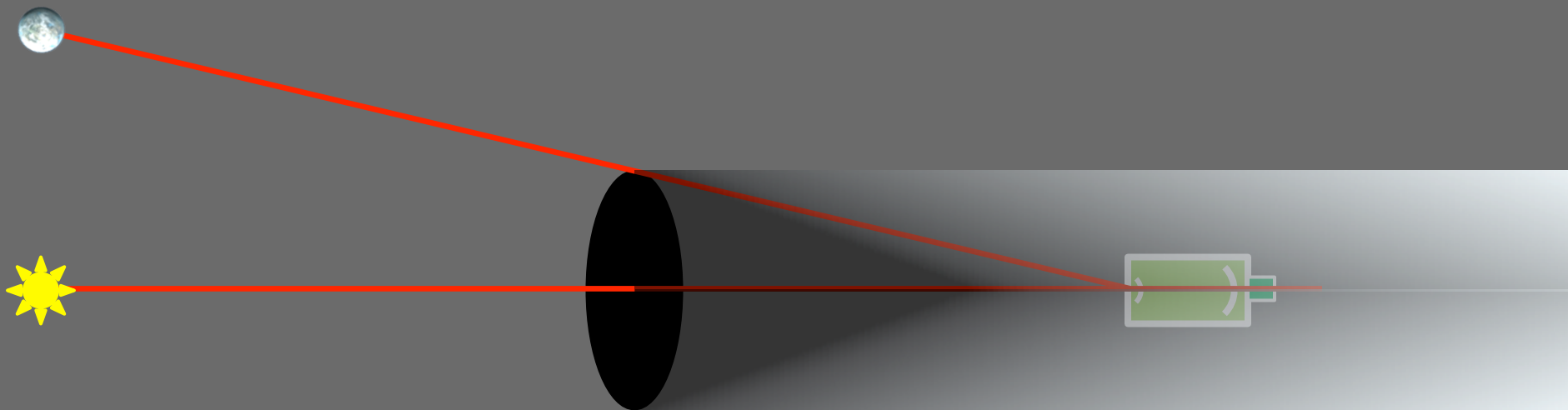
Earth at 10 pc: IWA = 100 mas

For  $D = 4$  m,  $2 \times R = 6$  m

$z \sim 6200$  km



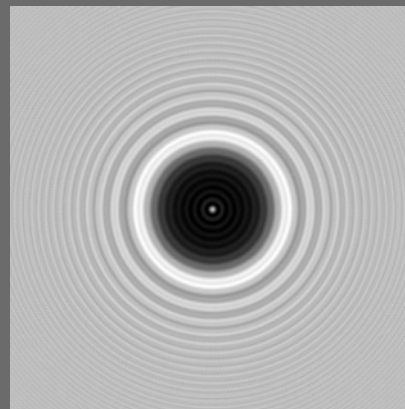
# Not so simple: diffraction



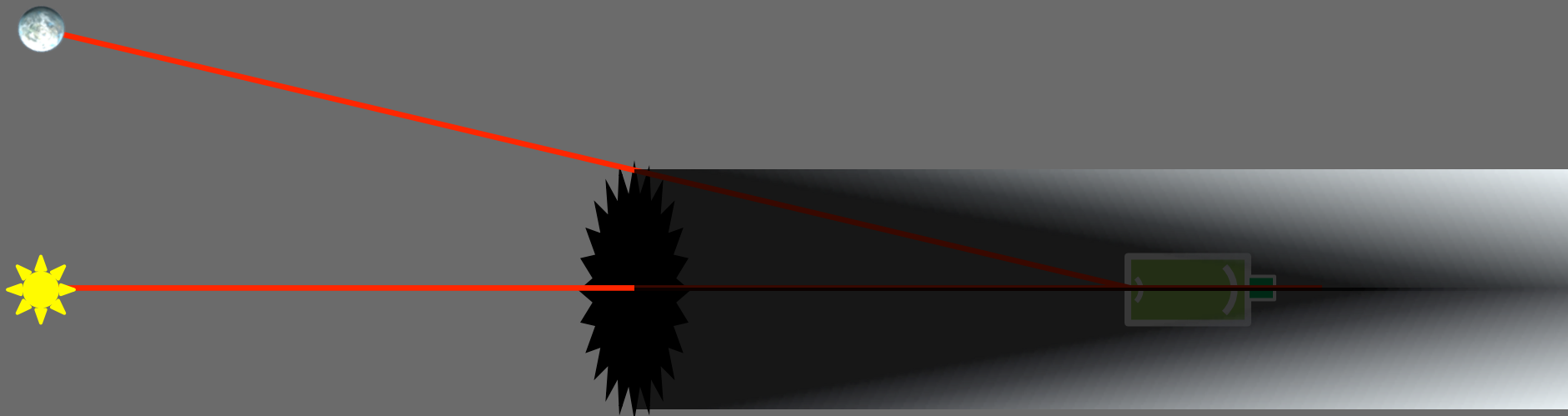
**Diffraction Shadow**

Circular disk makes diffraction  
pattern with Arago spot.

Shadow isn't dark enough.

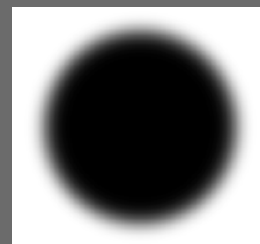


# Petals for high contrast

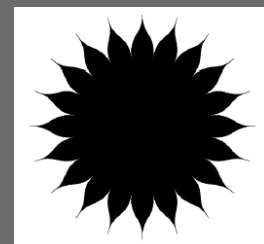


**Diffraction Shadow**

Approximate smooth radial apodization using petals.



~



Now can get better than  $10^{-10}$  contrast with reasonably sized starshade.

# Calculating a starshade shape

Fresnel (near-field) diffraction with apodization function  $A(r)$

$$E(\rho) = E_0 e^{\frac{2\pi i z}{\lambda}} \left( 1 - \frac{2\pi}{i\lambda z} e^{\frac{i\pi}{\lambda z} \rho^2} \int_0^R A(r) e^{\frac{i\pi}{\lambda z} r^2} J_0 \left( \frac{2\pi r \rho}{\lambda z} \right) r dr \right)$$

$z$  = separation between starshade and telescope

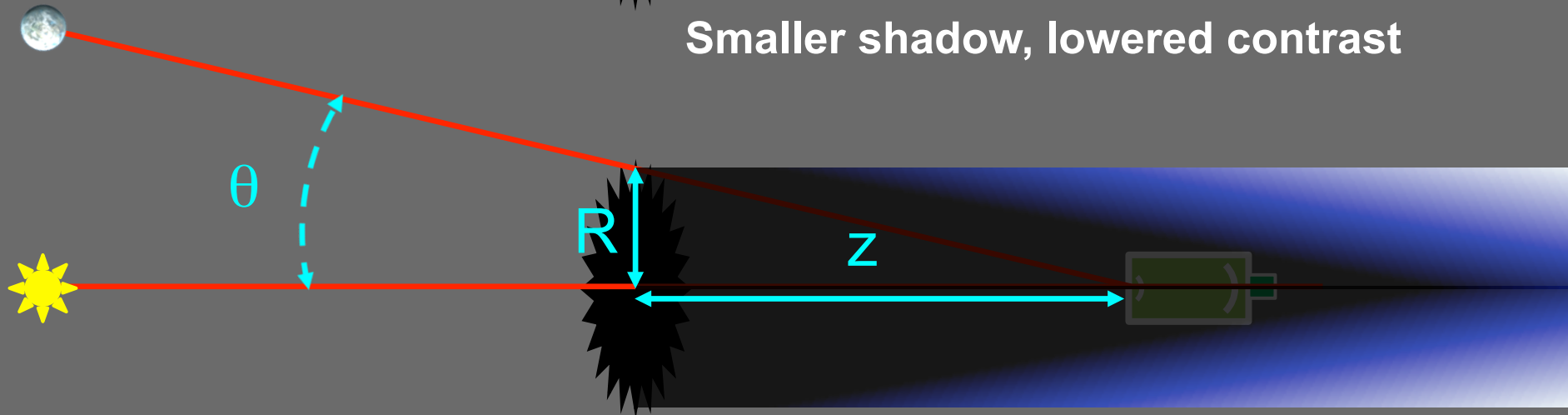
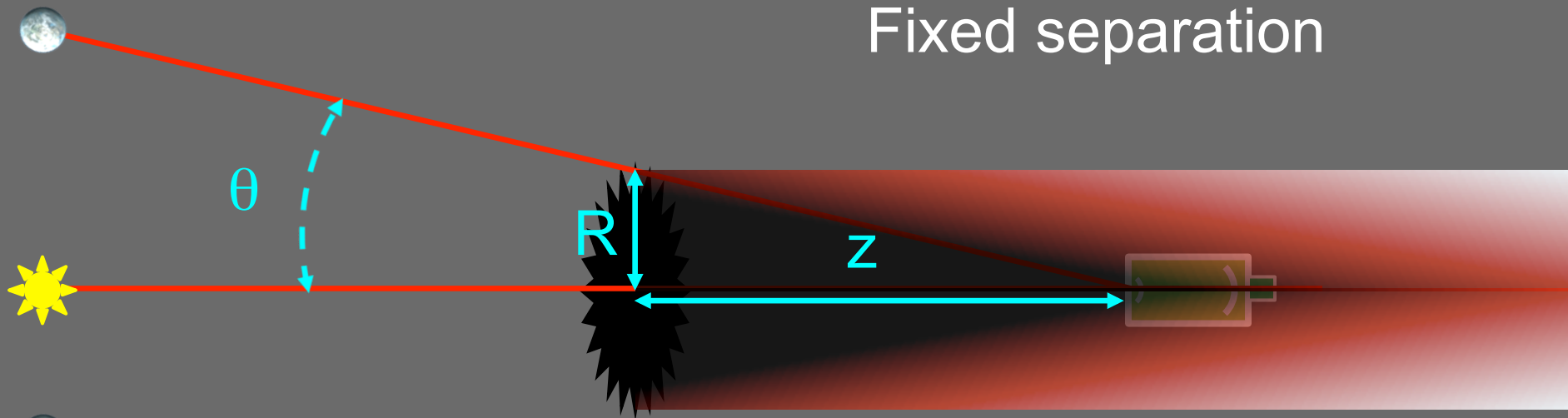
$R$  = radius of starshade

$\rho$  = radial position measured from center of shadow at telescope entrance

$r$  = radial position measured from center of shadow at the starshade

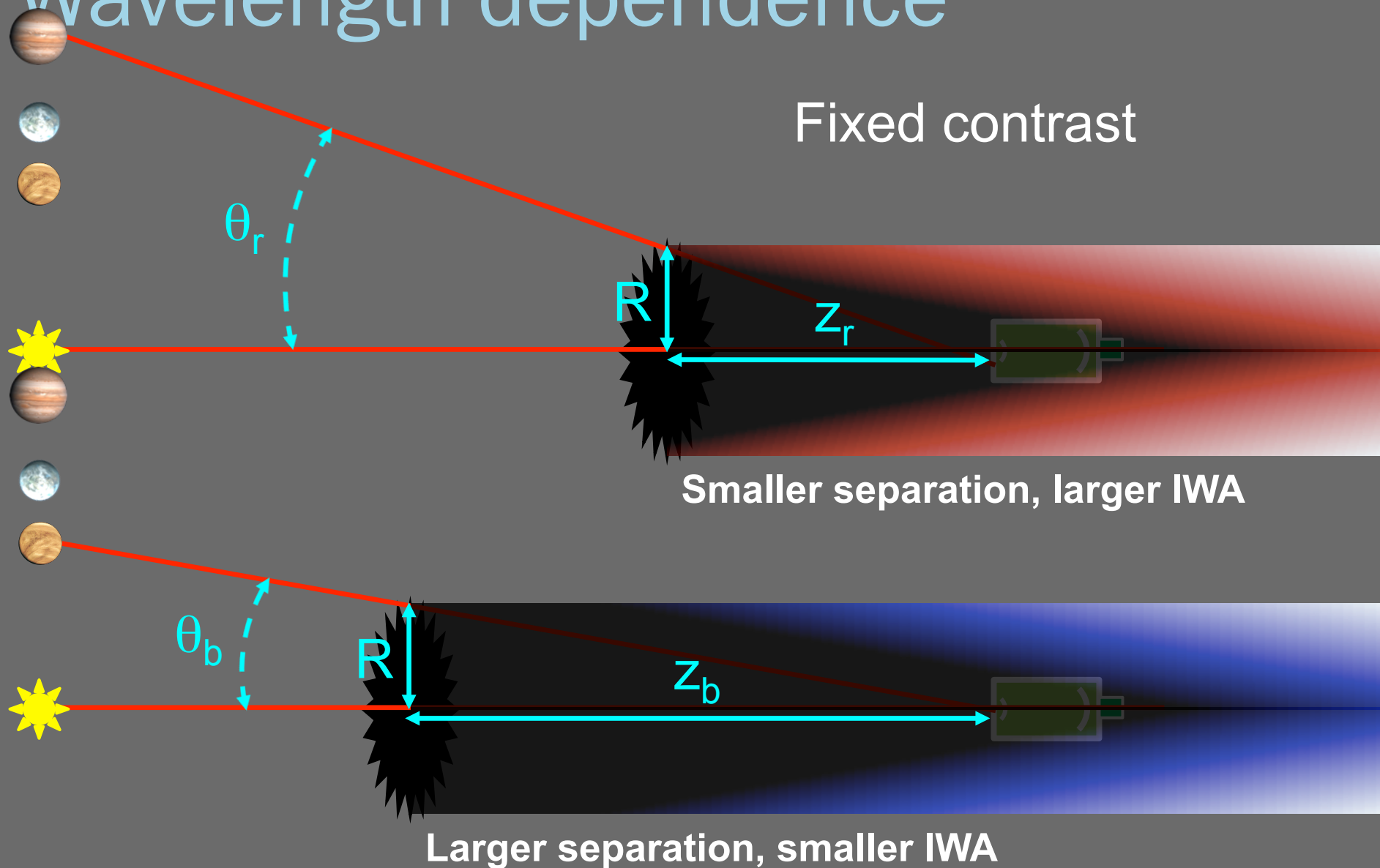
1. Exact solution for  $A(r)$  with  $\rho = 0$  : Hypergaussian (Cash 2006)
2. Numerically calculate optimal  $A(r)$  (Vanderbei, Cady, & Kasdin 2007)

# Wavelength dependence



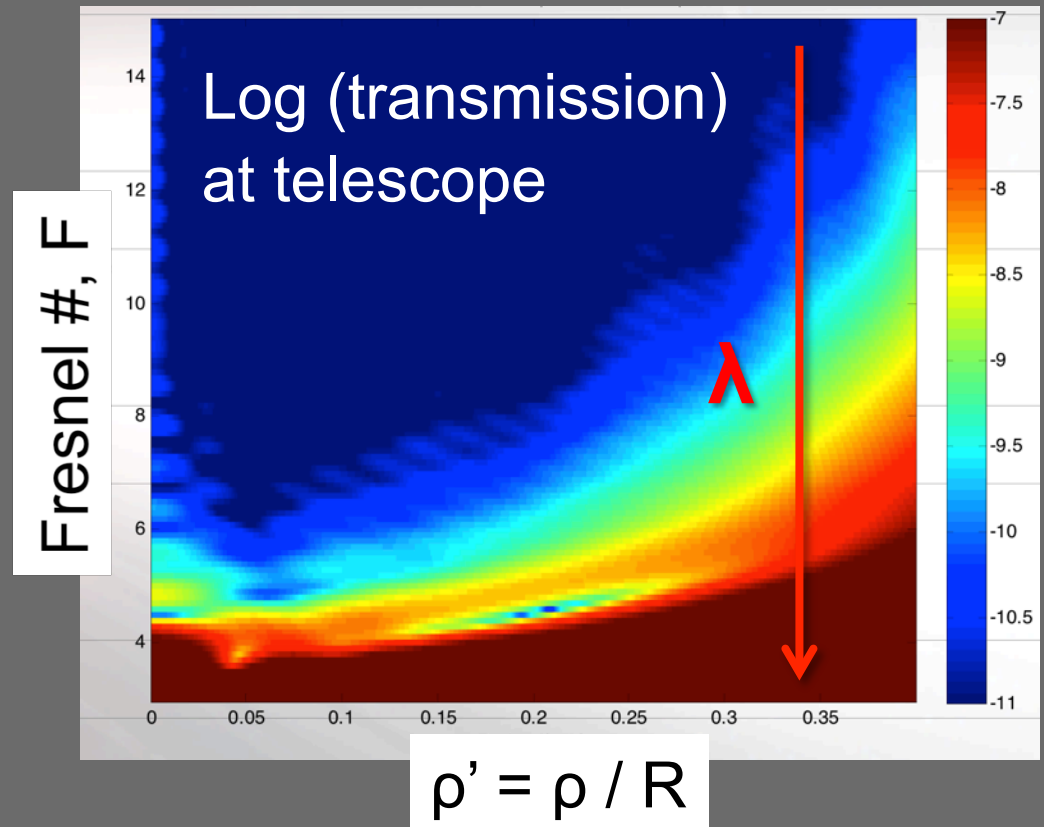
Larger shadow, deeper contrast

# Wavelength dependence



# Scaling a hypergaussian starshade

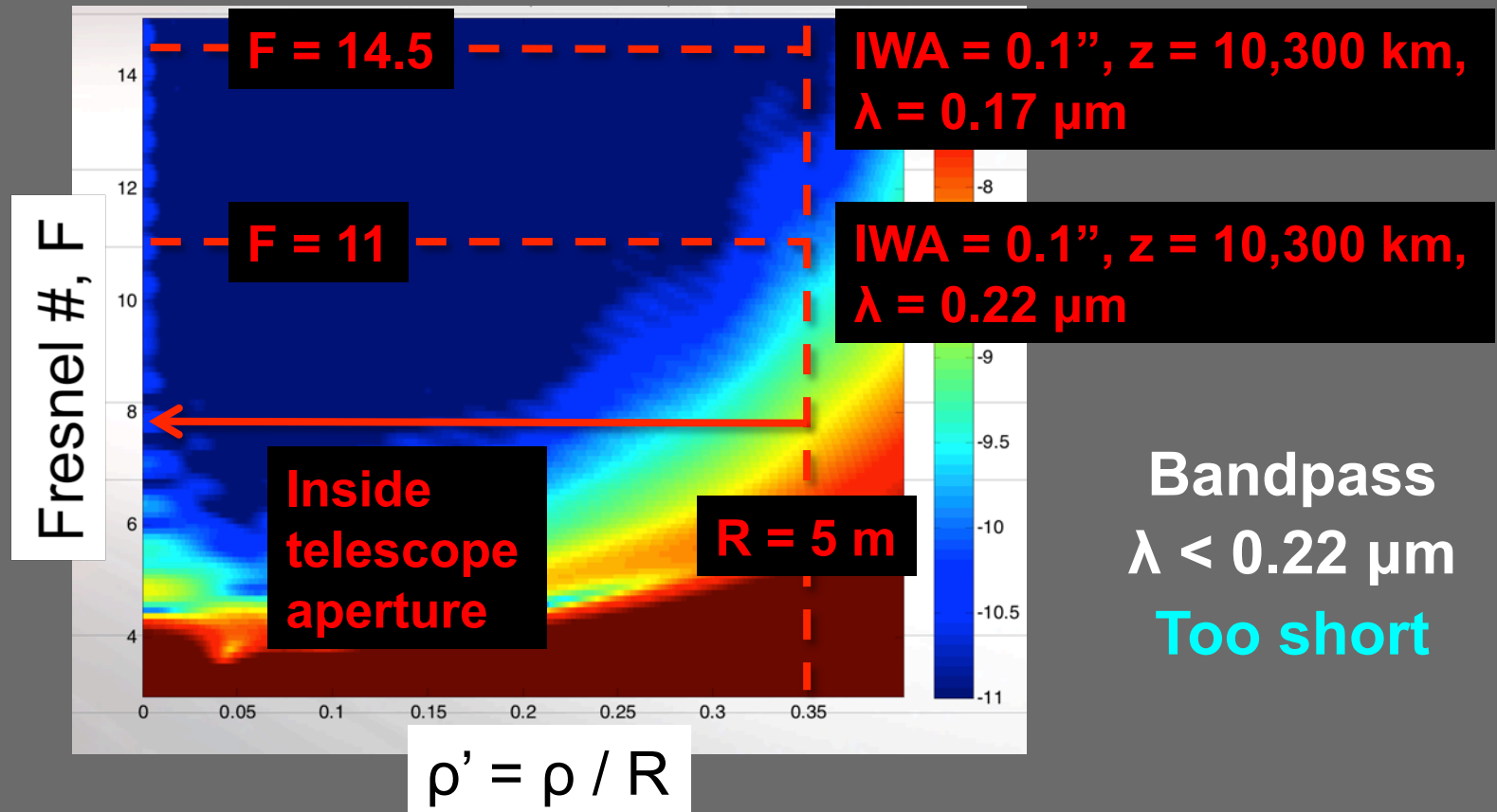
- Fresnel #: 
$$F = R^2 / (\lambda z)$$
- For a given  $\lambda$ , IWA: 
$$R = F \times \lambda / \text{IWA}$$
$$z = F \times \lambda / \text{IWA}^2$$
- For a given  $R$ , IWA: 
$$F = R \times \text{IWA} / \lambda$$



Credit: C. Noecker

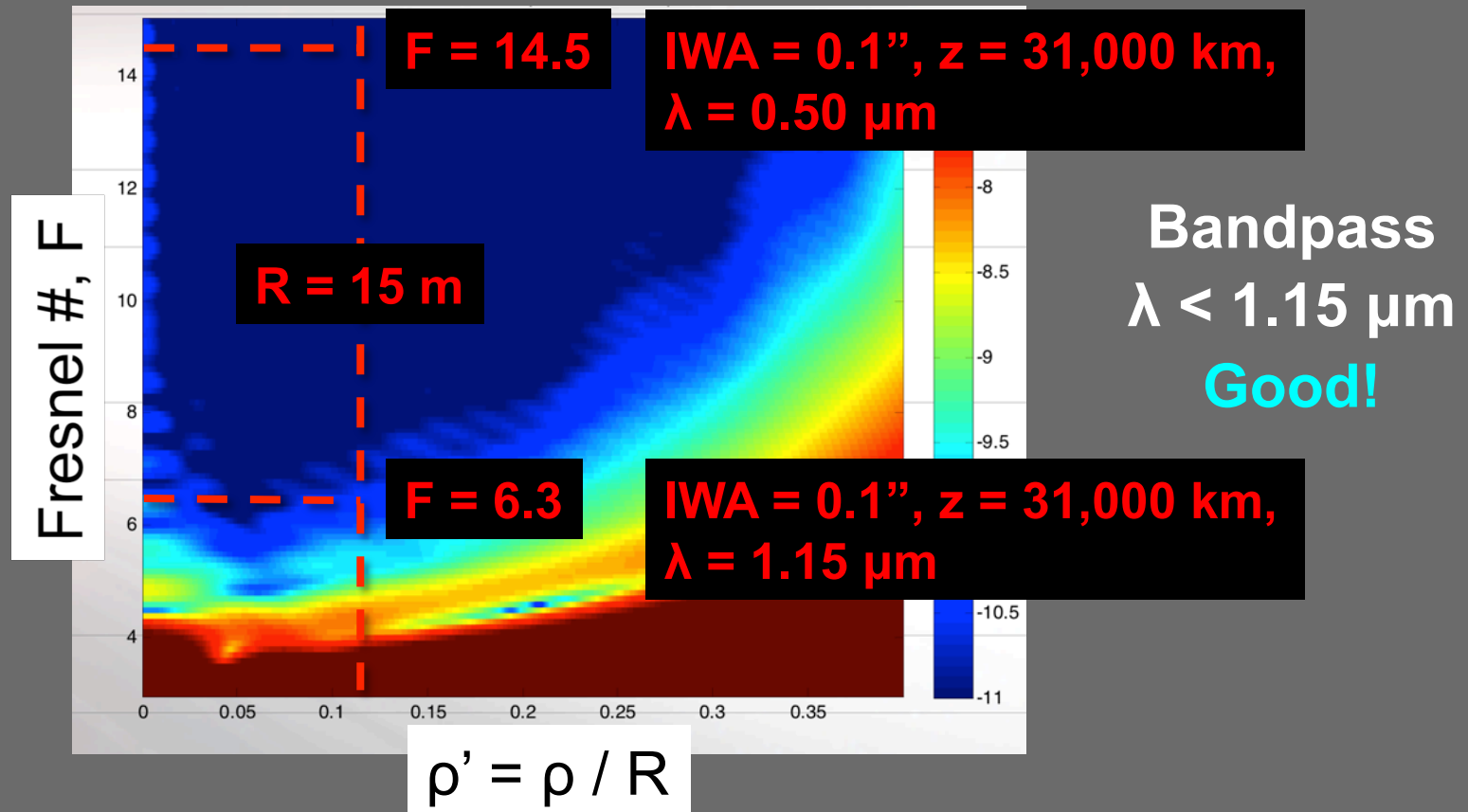
# Small starshade

- $D = 1.5 \text{ m}$ ,  $R = 5 \text{ m}$ ,  $\rho_{\max} = 1.75 \text{ m}$ ,  $\rho'_{\max} = 0.35$
- Want contrast =  $10^{-10}$  or better : blue region



# Larger starshade

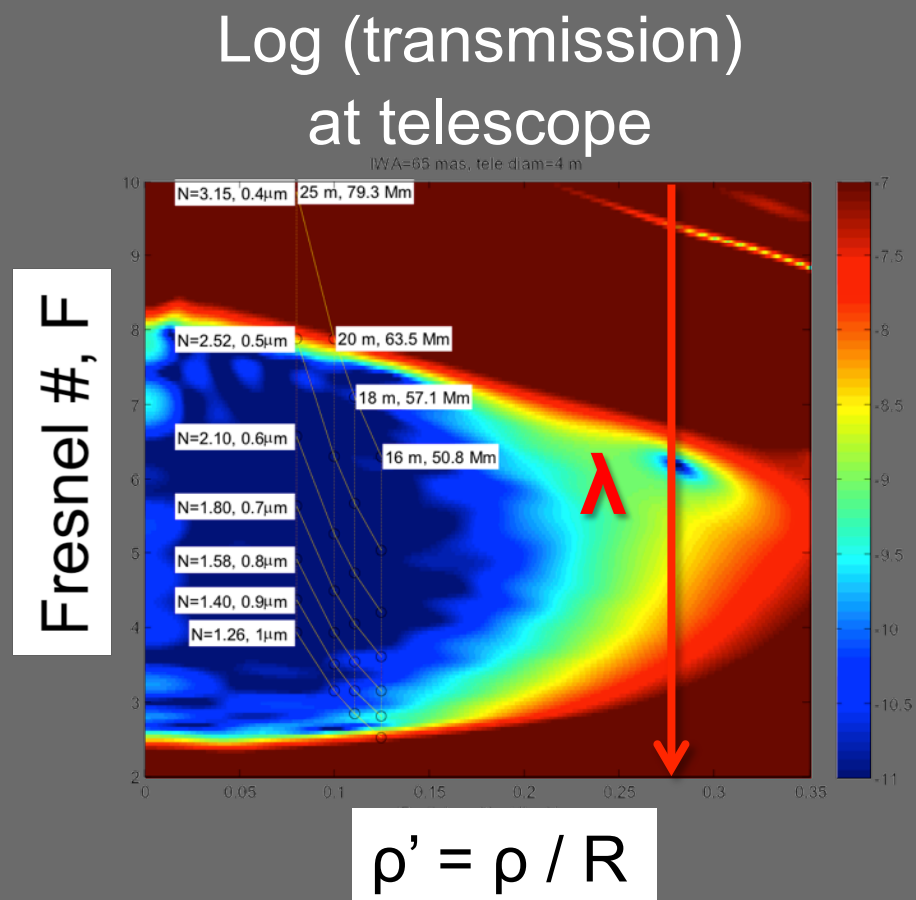
- $D = 1.5 \text{ m}$ ,  $R = 15 \text{ m}$ ,  $\rho_{\max} = 1.75 \text{ m}$ ,  $\rho'_{\max} = 0.12$
- Want contrast =  $10^{-10}$  or better : blue region





# Optimal starshade differences

- Numerically calculated optimal starshade is smaller for same contrast
- But it has a short-wavelength cutoff



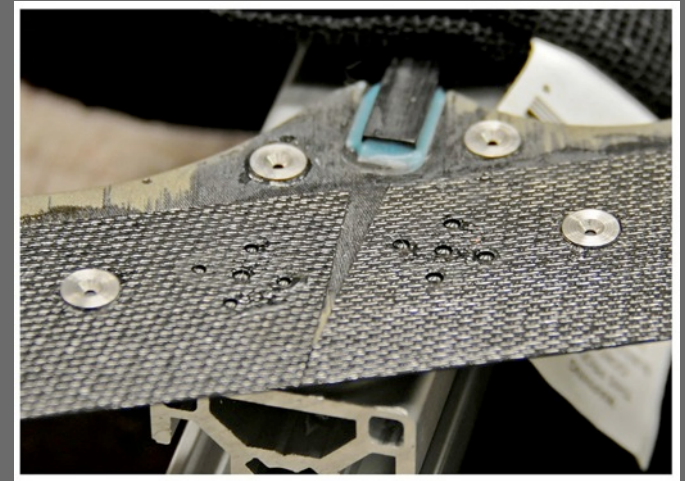
Credit: C. Noecker

# Starshade behavior summary

- Redder bandpass needs larger starshade
- Larger starshade has to be further away to get same IWA
- If starshade is further away, longer slew times for retargeting
- Hypergaussian starshade size set to achieve desired contrast at longest wavelength of interest
- Numerically calculated optimal starshade is smaller for same contrast but has a short wavelength cutoff

# Technical challenges

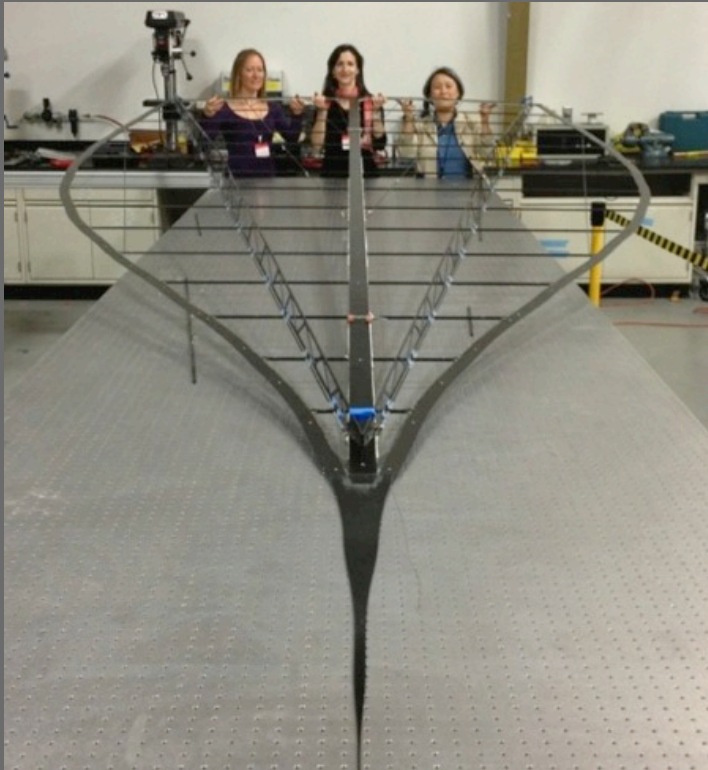
- Precise edge profile ( $\sim 50\text{ }\mu\text{m}$  tolerance) required over large structure
- Knife-edge to prevent sunlight scattering into telescope
- On-orbit deployment of large structure
- Precise alignment between starshade and telescope needed ( $\pm 1$  meter tolerance). Soft requirement



NASA / JPL / Princeton

# Precision petal manufacturing

Full-scale petal with edge profile for contrast  $< 10^{-10}$

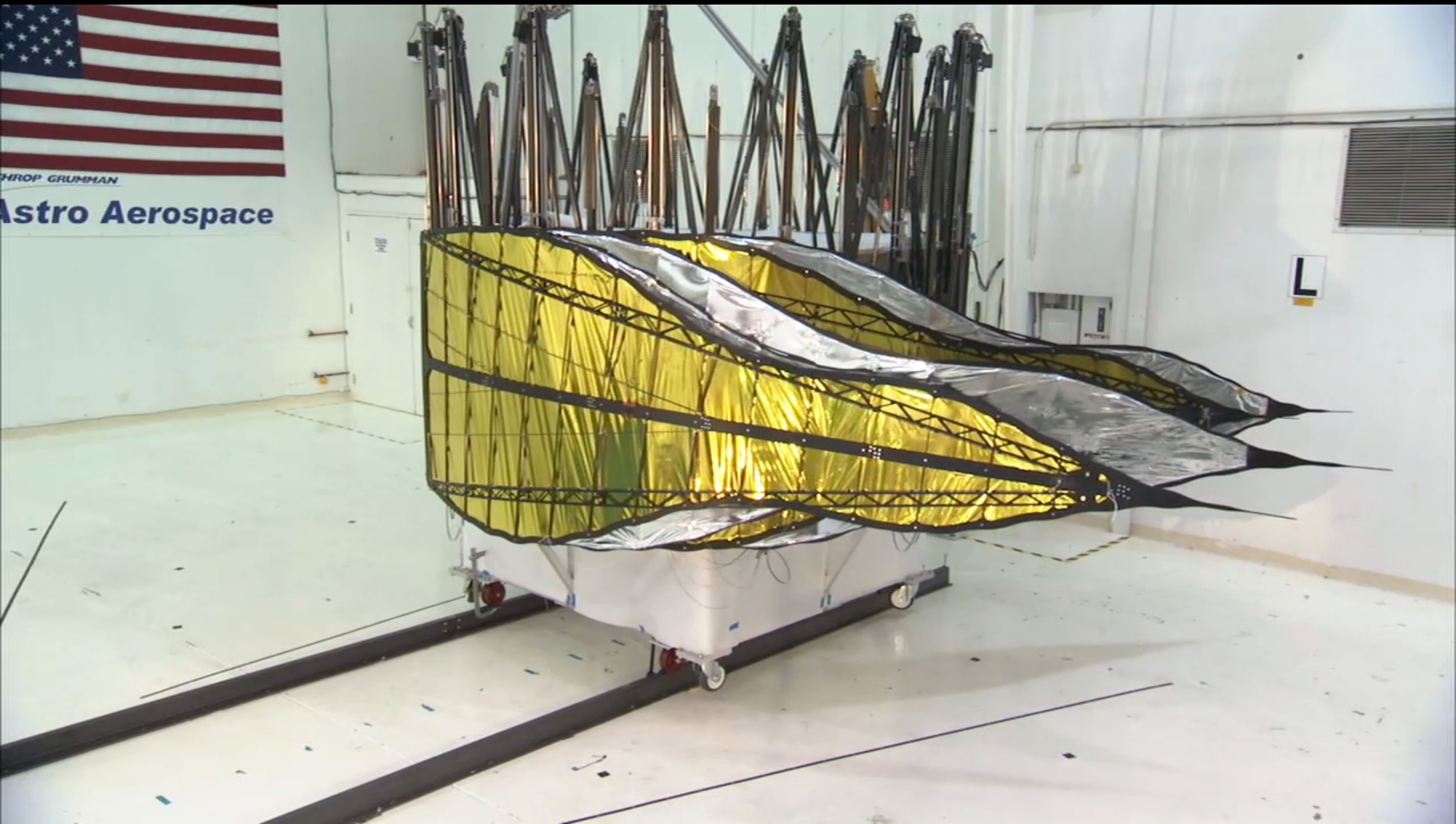


Credit: D. Lisman

Development of knife-edge to control edge scatter underway

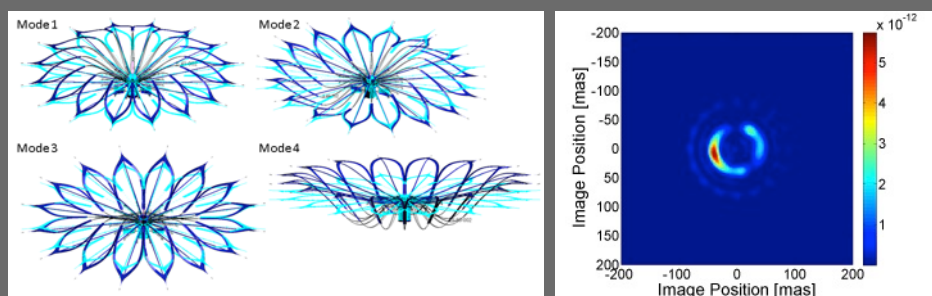


# Deployment demonstration

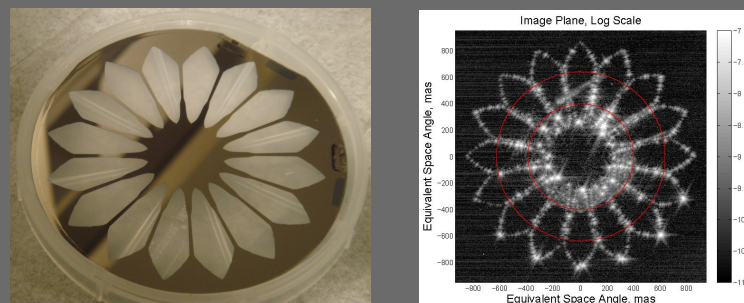


# Contrast demonstrations

Optical models with distortions  
monochromatic:  $10^{-12}$



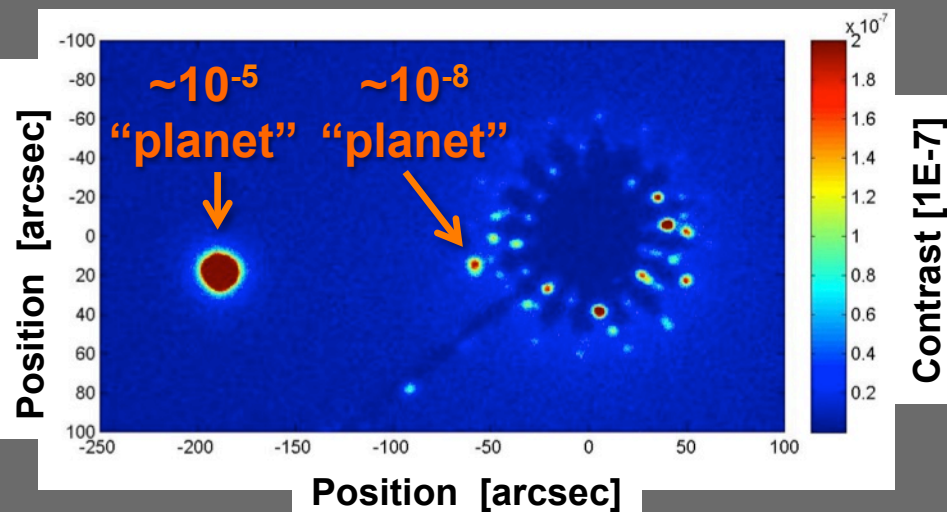
0.1% scale lab testing  
monochromatic:  $10^{-10}$



~ 1% scale field testing  
50% bandpass:  $10^{-8}$



T. Glassman / NGAS



# More info

Cash, W. (2006). "Detection of Earth-like planets around nearby stars using a petal-shaped occulter." *Nature*, 442, 51

Vanderbei, R., Cady, E., & Kasdin, N. J. (2007). "Optimal Occulter Design for Finding Extrasolar Planets." *ApJ*, 665, 794

Shaklan, S., et al. (2010). "Error budgeting and tolerancing of starshades for exoplanet detection", *SPIE*, 77312G

<http://proceedings.spiedigitallibrary.org/proceeding.aspx?articleid=749972>

Kasdin, N. J., et al. (2013). "Recent progress on external occulter technology for imaging exosolar planets."

<http://ieeexplore.ieee.org/xpl/articleDetails.jsp?arnumber=6497155>