



Phase-Referencing and the Atmosphere

Francoise Delplancke

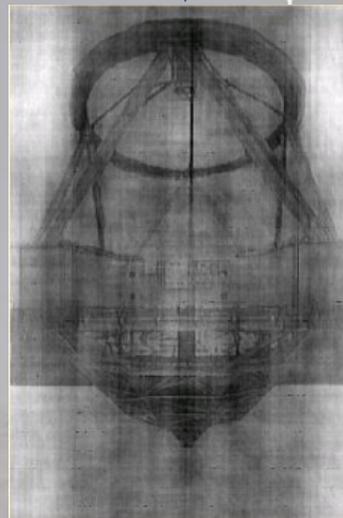
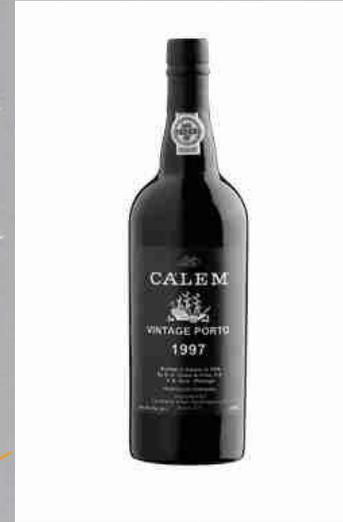
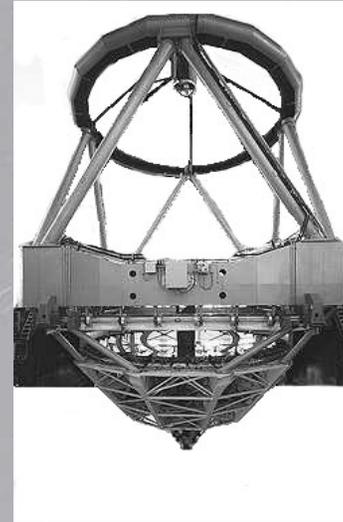
Outline:

- Basic principle of phase-referencing
- Atmospheric / astrophysical limitations
- Phase-referencing requirements:
- Practical problems:
 - dispersion problems and H₂O seeing
 - proper phase-reference stars
 - time aspect and evolving objects
 - injection stability and vibrations for fringe tracking
 - instrumental errors on dOPD measurements
- Conclusions

The importance of the phase

- Original images =>
- take their Fourier Transform
=> amplitude part (squared visibility)
and phase part
- cross the phase of one image
with the amplitude of the other
- reconstructed images =>

Conclusion: the phase of the image contains the most important part of the information on its shape !

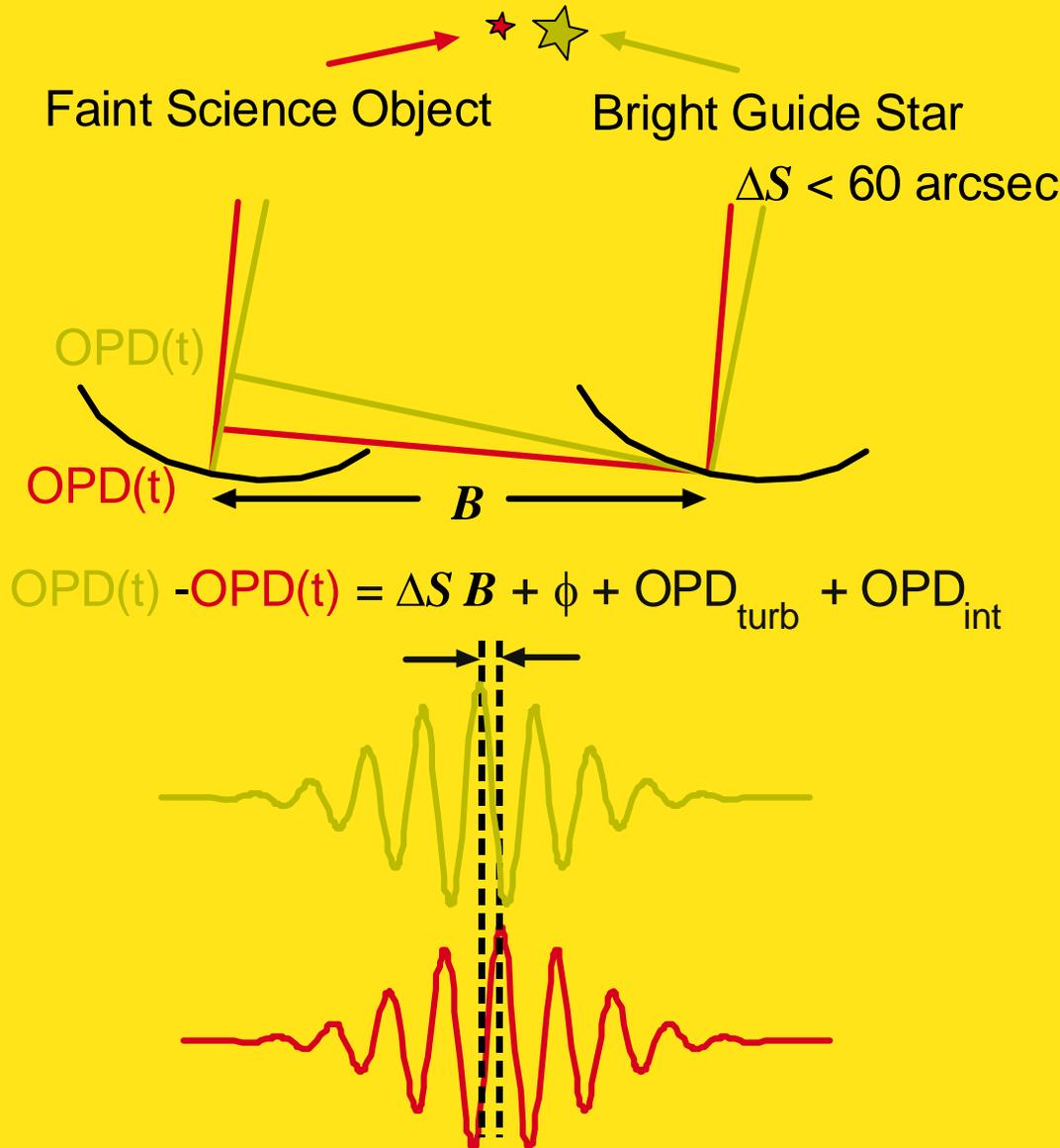


amplitude

phase

phase

Phase-referencing principle



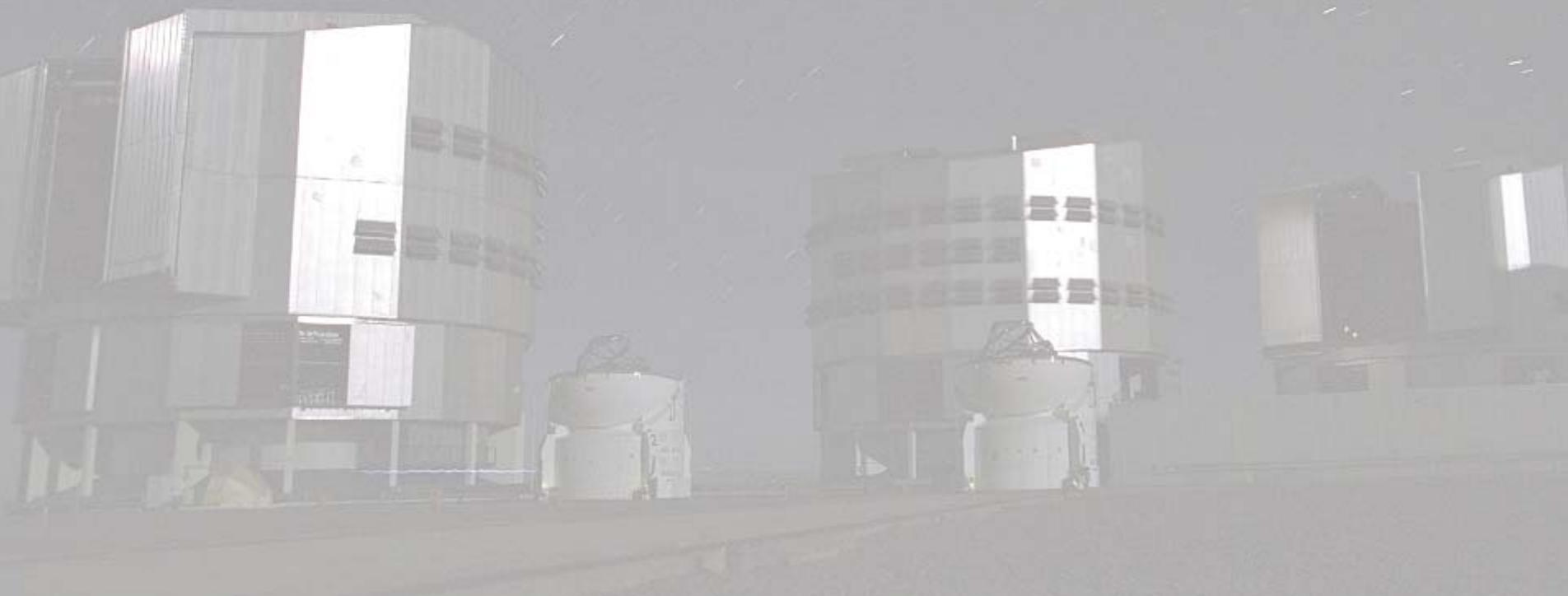
$\Delta s = \text{astrometry} \Rightarrow$ goal of $10 \mu\text{as}$ (planets...)

$\phi =$ imaging with high dynamic range (AGNs, star environment...)

\Rightarrow needs to know the $dOPD$ with nanometric accuracy



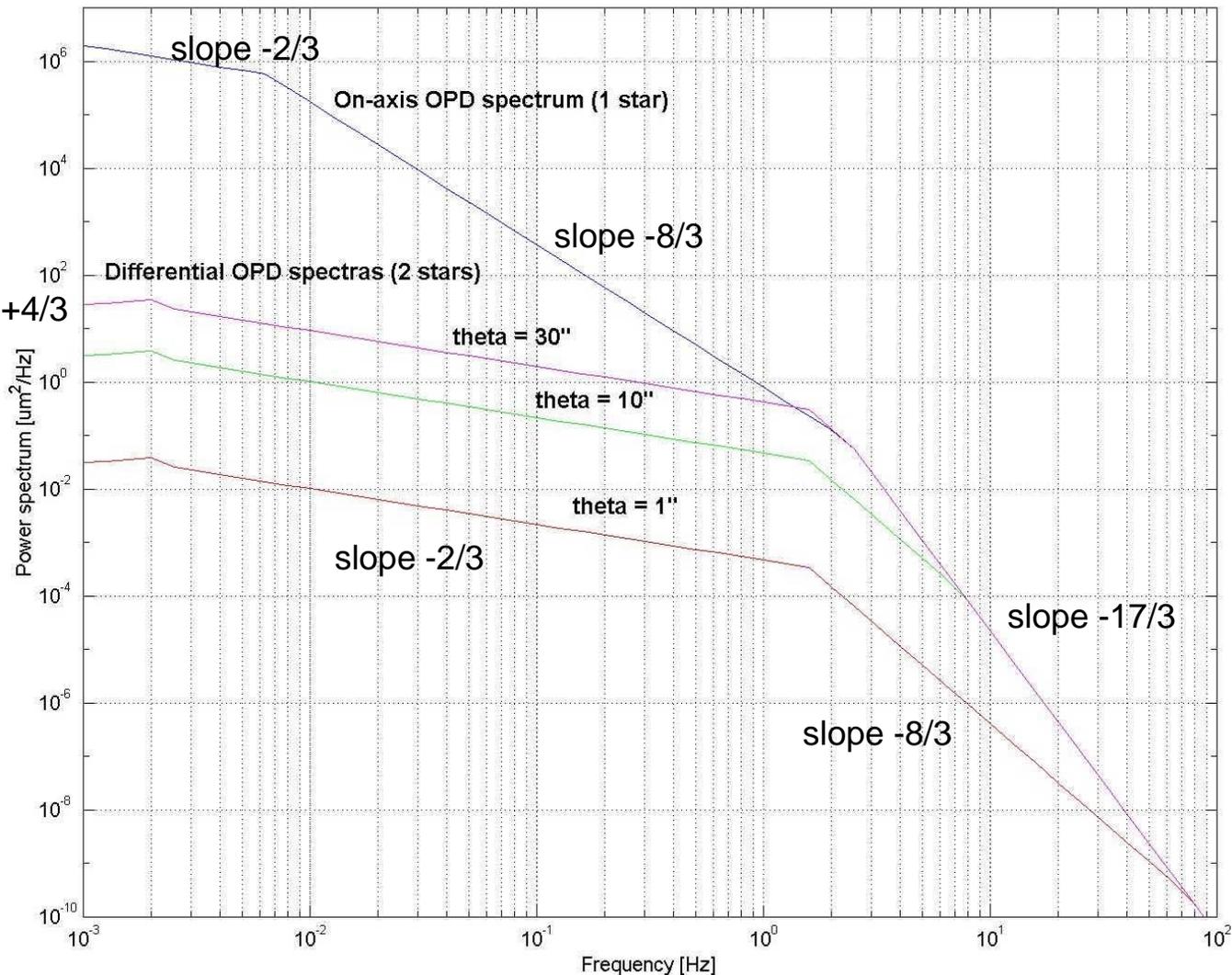
The limitations





Atmospheric anisoplanatism 1

Power Spectra of various OPD variations



Kolmogorov spectrum

Balloon measurements at Paranal

Seeing = $0.66''$ at $0.5 \mu\text{m}$

$\tau_0 = 10 \text{ ms}$ at $0.6 \mu\text{m}$

Atmospheric anisoplanatism 2

- Off-axis fringe tracking \Leftrightarrow anisoplanatic differential OPD

$$\sigma_{OPD_{measurement}} \cong 370 \cdot B^{-2/3} \cdot \frac{\theta}{\sqrt{T_{obs}}} \quad \text{for narrow angles } (\theta < 180'' \text{ UT or } 40'' \text{ AT})$$

and long total observation time $T_{obs} \gg \sim 100s$

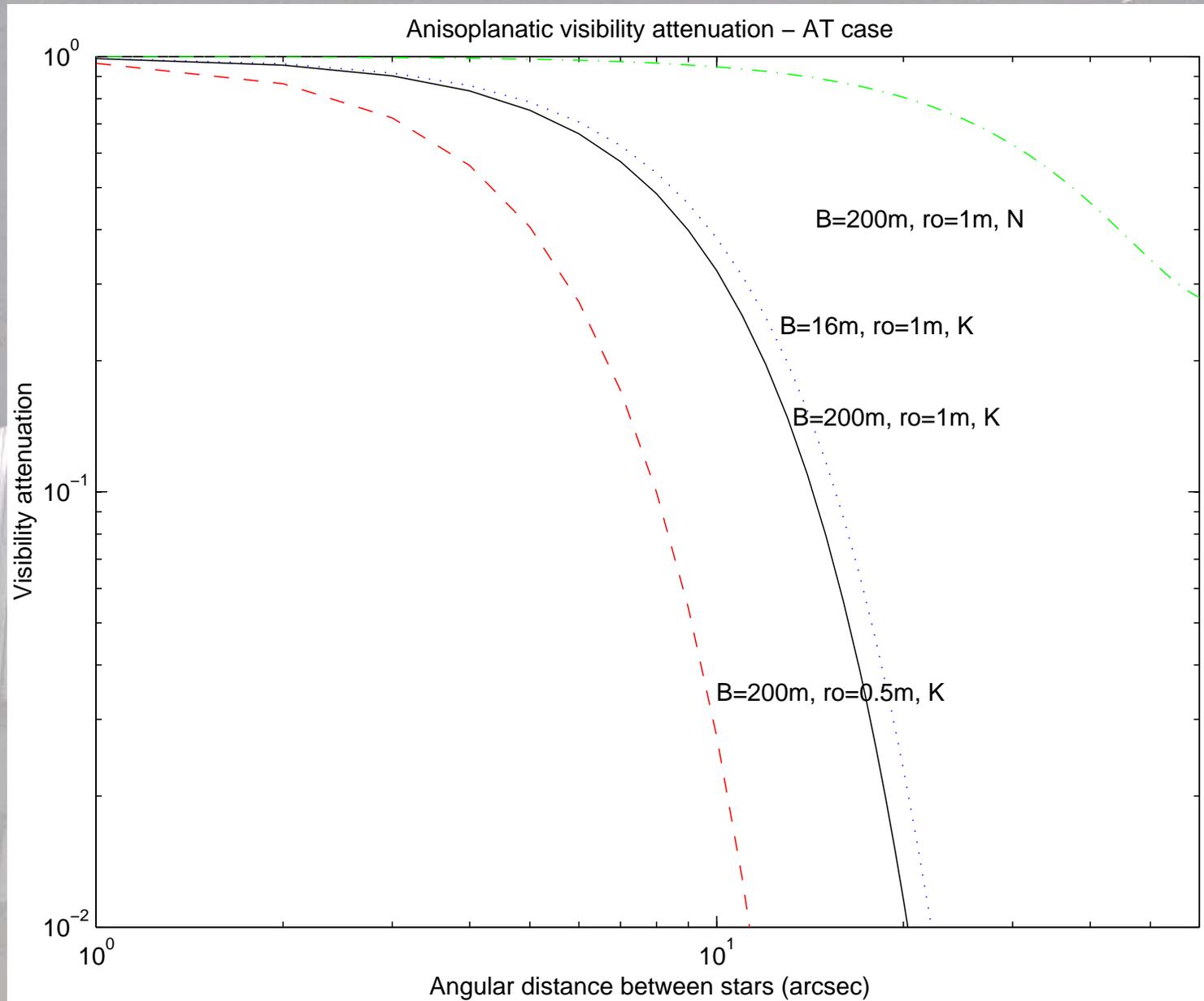
for Paranal seeing = 0.66" at 0.5 μ m, $\tau_0 = 10$ ms at 0.6 μ m (L. d'Arcio)
 Factor = 300 for Mauna Kea (Shao & Colavita, 1992 A&A 262)

- Increases with star separation
- Decreases with telescope aperture (averaging)
- High impact of seeing quality
- Translates into off-axis maximum angles to limit visibility losses (< 50 to 90%):
 - K-band imaging (2 μ m)
 - Bright fringe guiding star within **10-20"**
 - N-band imaging (10 μ m)
 - Bright fringe guiding star within **2'**

$$V = V_0 \cdot \exp \left[-2 \cdot \left(\frac{\pi}{\lambda} \cdot \sigma_{residual_OPD} \right)^2 \right]$$



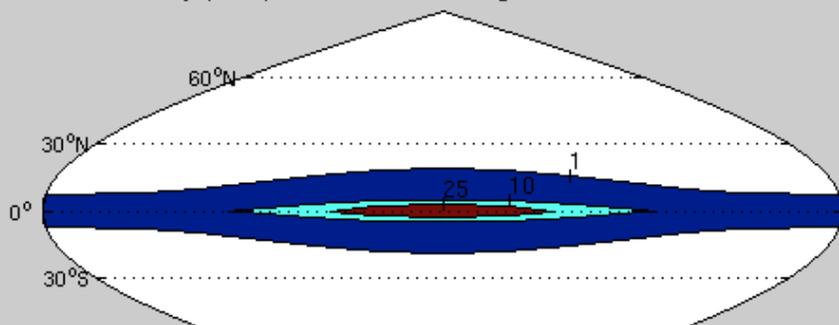
Anisoplanatism AT



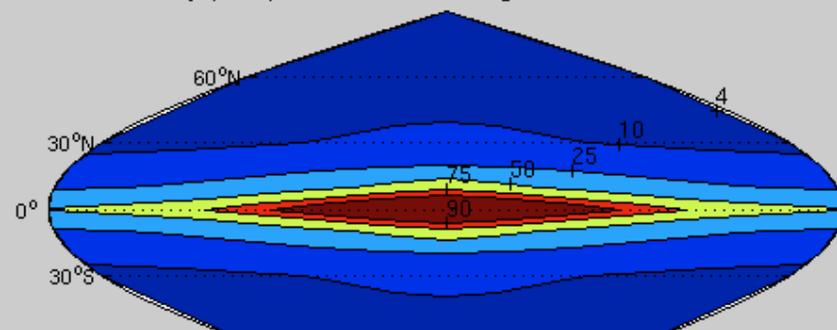
Sky coverage

- Sky coverage \Leftrightarrow limiting magnitude

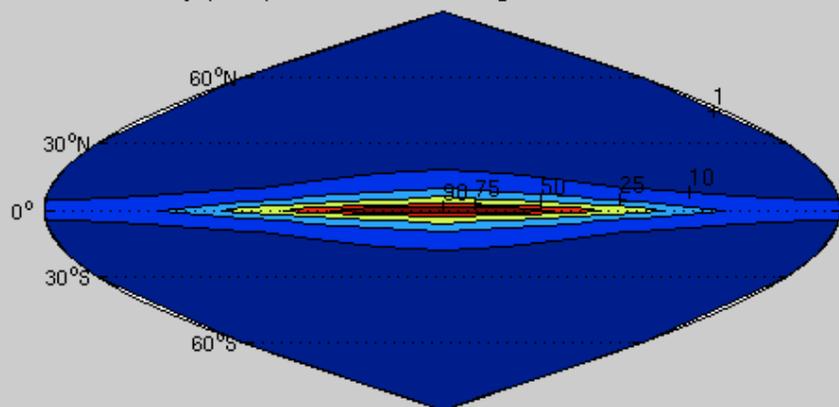
Probability (in %) to find one star brighter than $K=10$ within $10''$



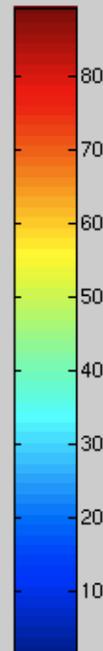
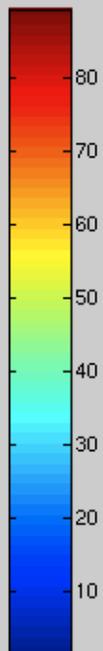
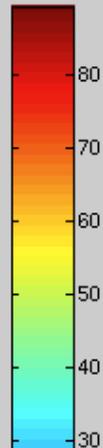
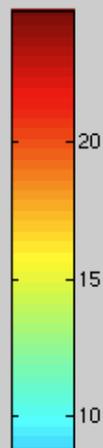
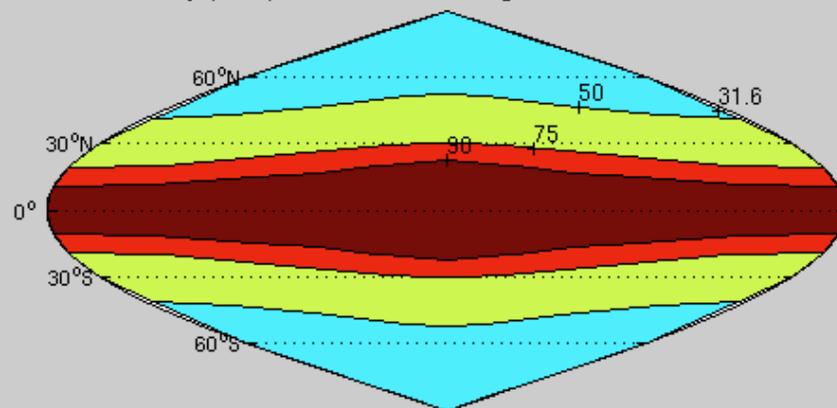
Probability (in %) to find one star brighter than $K=10$ within $60''$



Probability (in %) to find one star brighter than $K=13$ within $10''$



Probability (in %) to find one star brighter than $K=13$ within $60''$



The requirements

- Phase-referencing measurable: difference of group delay

$$\Delta\text{OPD} = \Delta\text{S.B} + \phi + \text{OPD}_{\text{turb}} + \text{OPD}_{\text{int}}$$

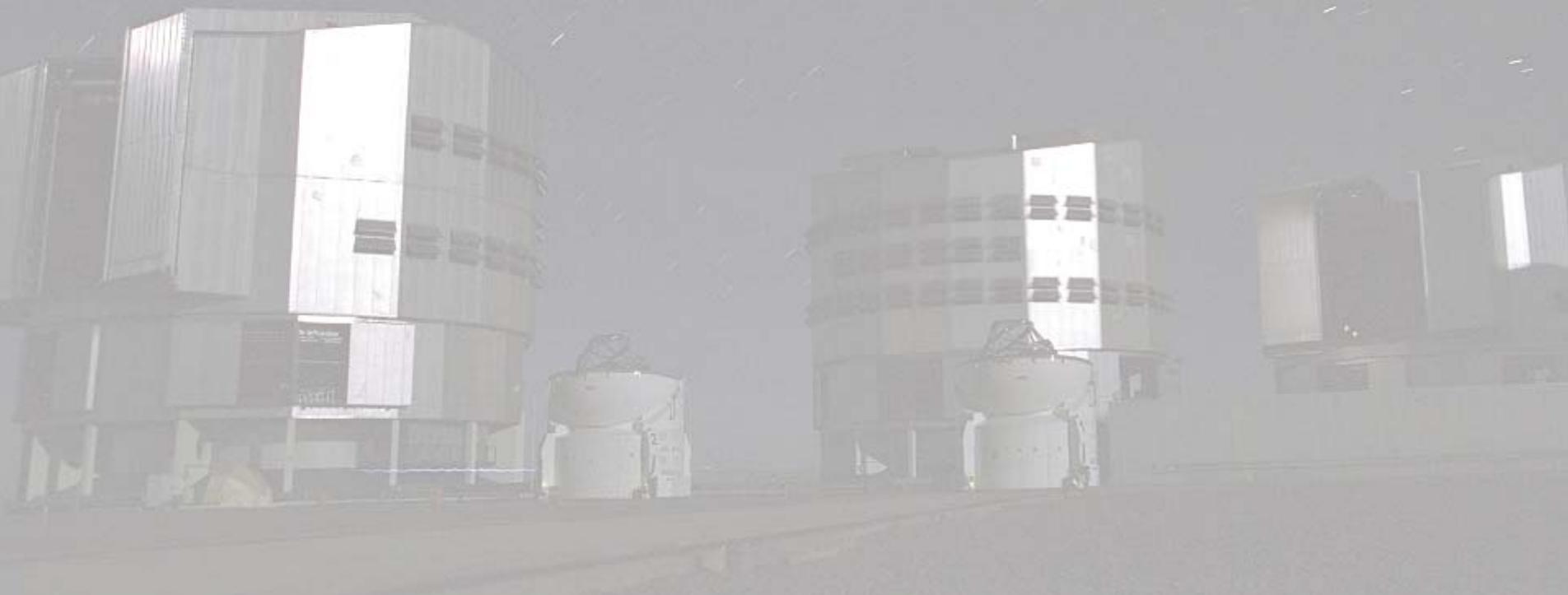
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Fringe sensor
astrometry
imaging
atmosphere
Internal metrology

- Astrometric requirement
 - For 2 stars separated by $10'' - 0.8''$ seeing - $B=200\text{m} \Rightarrow$ Atmosphere averages to $10\mu\text{as rms}$ accuracy in 30 min
 - \Leftrightarrow 5nm rms measurement accuracy
- Imaging requirement \Rightarrow
 - dynamic range is important (ratio between typical peak power of a star in the reconstructed image and the reconstruction noise level)
 - $\text{DR} \sim \sqrt{M} \cdot \phi / \Delta\phi$ where M = number of independent observations
 - $\text{DR} > 100$ and $M=100 \Leftrightarrow \Delta\phi / \phi < 0.1 \Leftrightarrow 60\text{nm rms in K}$
- Ability to do off-axis fringe tracking



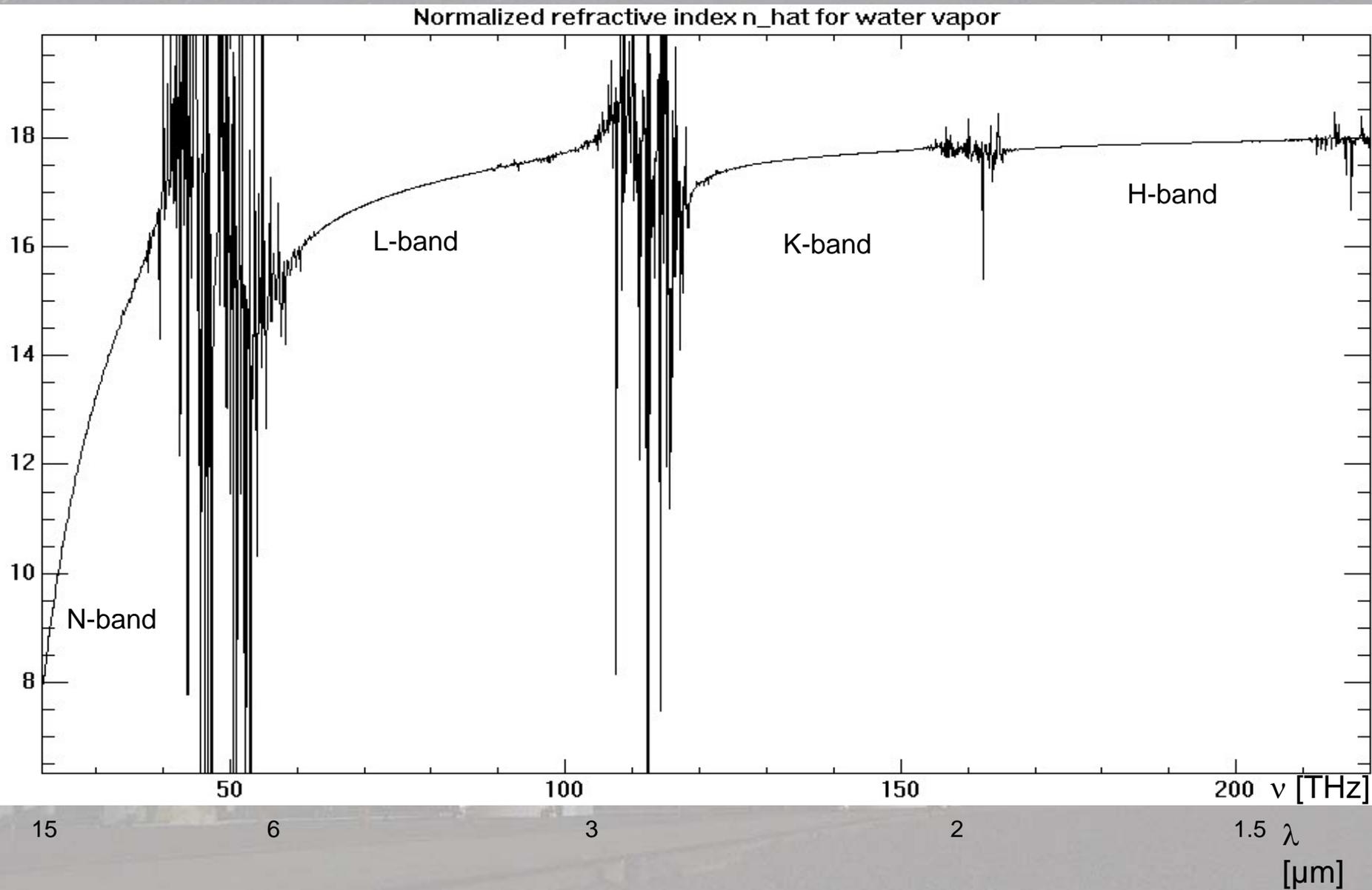
The problems



Dispersion and H₂O seeing

- Transversal & longitudinal dispersion
- Fringe tracking and observation at different λ
- Air index of refraction depends on wavelength =>
 - phase delay \neq group delay
 - group delay depends on the observation band
 - fringe tracking in K does not maintain the fringes stable in J / H / N bands
- Air index varies as well with air temperature, pressure & humidity
 - overall air index dominated by dry air
 - H₂O density varies somewhat independently
 - H₂O effect is very dispersive in IR (between K and N)
- Remedy: spectral resolution ▶

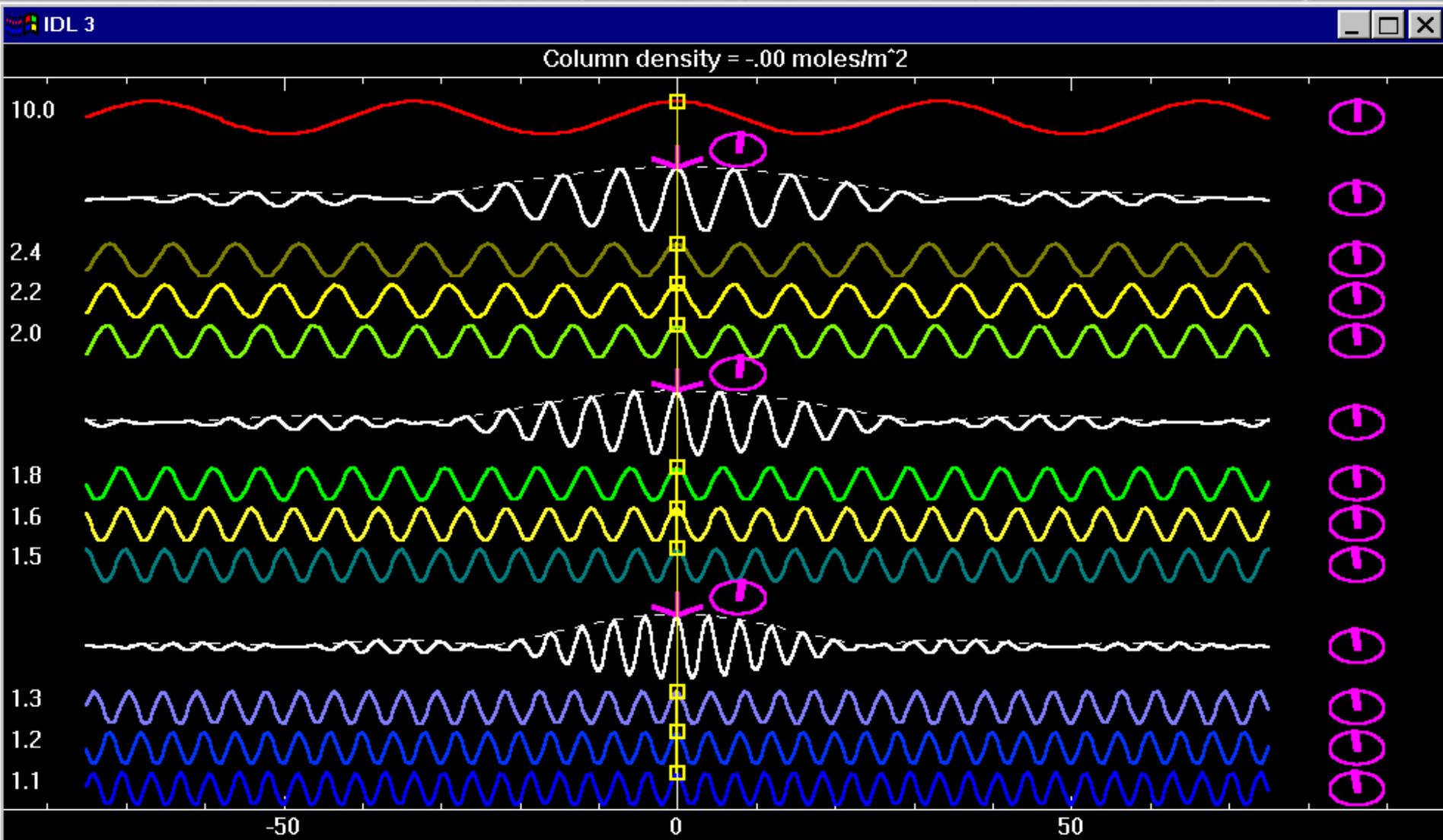
Refractive index of water vapor (©R. Mathar)





Dispersive effect between (and within) bands due to 0 – 600 mole/m² of additional dry air. (= 20 meter delay-line offset) (©J. Meisner)

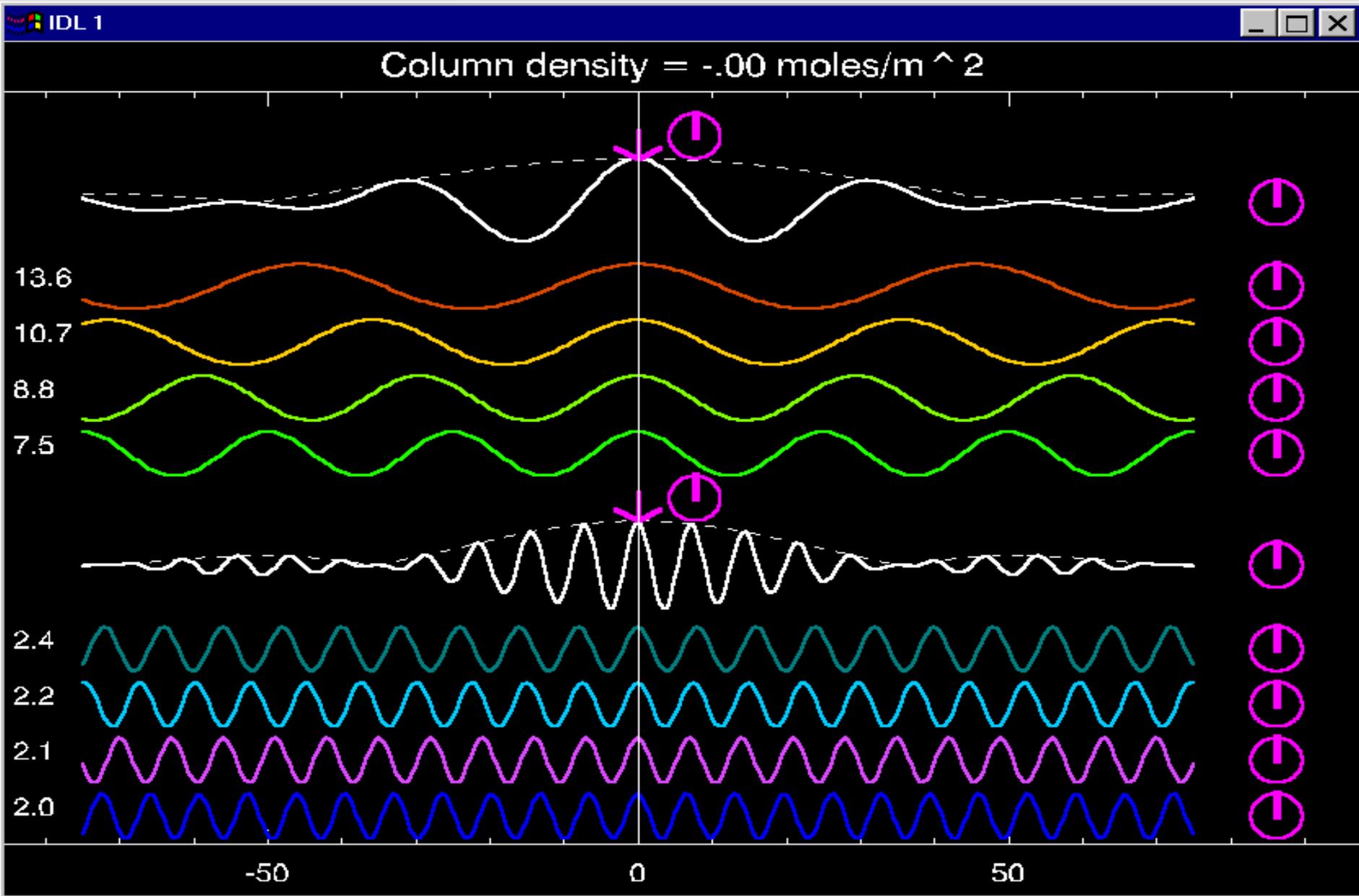
Note that dispersion from dry air increases rapidly at short wavelengths



(Tracking at the group-delay in K band)

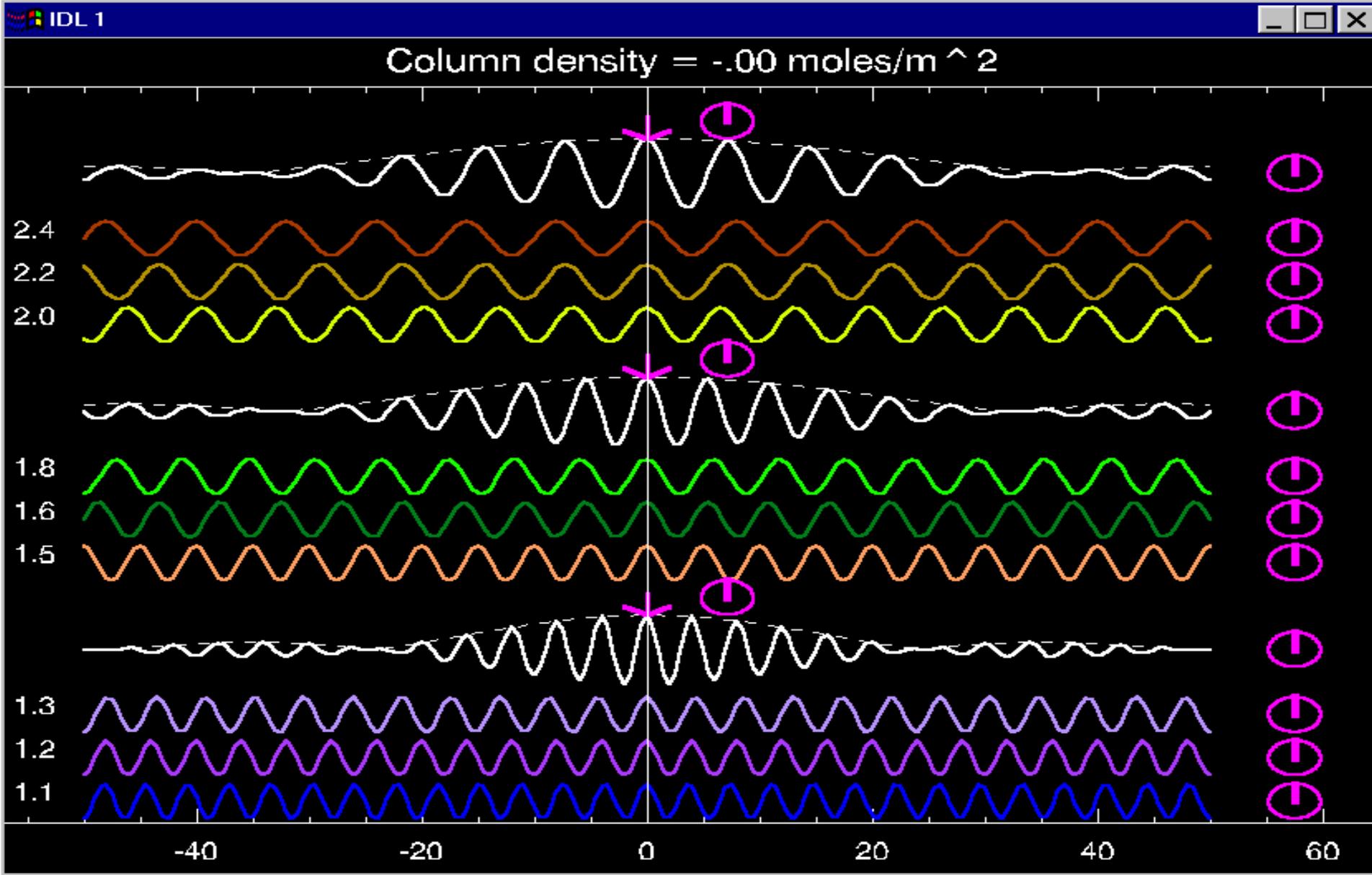


Water Vapor dispersion, with phase-tracking at K band
0 – 5 moles/m² (typical p-p value due to atmosphere) (©J. Meisner)





Water Vapor dispersion, with phase-tracking at K band
0 – 5 moles/m² (typical p-p value due to atmosphere) (©J. Meisner)



Proper phase references

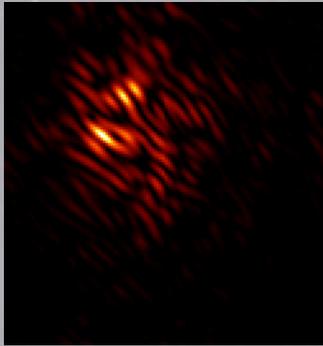
- We want to do imaging =>
 - usually the scientific target is faint =>
 - Reference star must be bright ($K < 10$ or 13)
 - Bright stars are close and big
 - need of long baselines
- => High probability that your guide star is:
 - resolved => low visibility
 - with resolved structures => non-zero phase
- Phase-referencing cannot disentangle between target phase and reference phase
- Remedies:
 - baseline bootstrapping
 - characterize your reference star (stellar type, spectrum, interferometry) as much as possible prior to observation
 - find a faint star close to the reference one to calibrate it



Time and evolving targets

- Phase-referencing works with 2 telescopes at a time
=> Measurements of different u-v points are taken at different epochs
- If a baseline change needs telescope relocation, it can take time (one day up to several months)
- If the object evolves, it is a problem
- Remedies:
 - have fast relocatable telescopes
 - if the “evolution” is periodic (Cepheid, planet), plan the observations at the same ephemeris time
 - have more telescopes and switch from one baseline to another within one night
 - no snap-shot image like with phase closure but better limiting magnitude

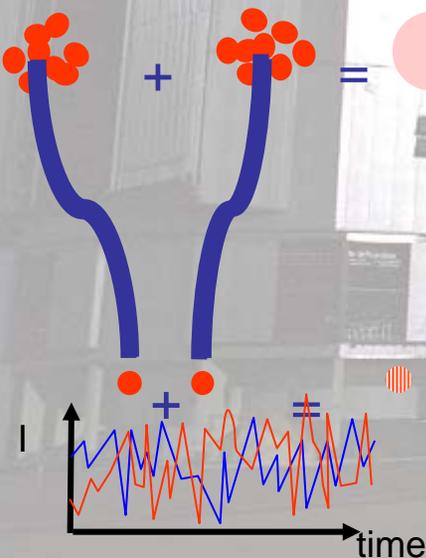
Fringe tracking problem nr 1: Injection stability



Spatial fringes for
2 UTs @ 2.2 μm
seeing = 0.5"

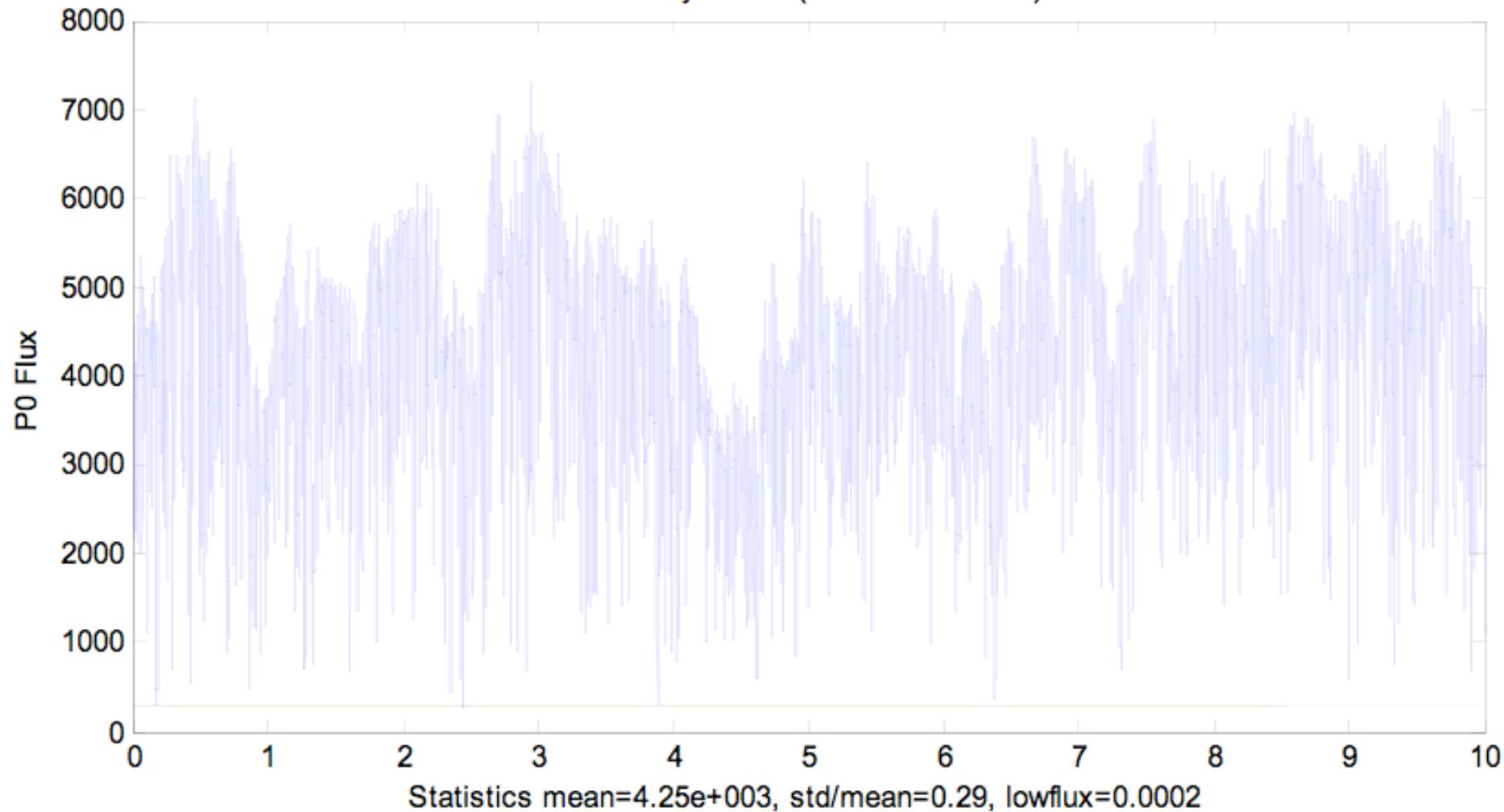
- Only the “flat” part of the wavefronts interfere coherently, all corrugations and tilts give noise
- Use of monomode optical fibers as spatial filter
- Strehl ratio is not stable at 10 ms timescales
- Too few photons ($< \sim 100$) \Rightarrow no fringe tracking
- Affects limiting magnitude & efficiency
- Remedies:

- tip-tilt sensing close to the instrument & correction in closed/open loop
- optimize the injection at the start
- check continuously at low rate if the injection is still optimum to compensate for drifts between tilt sensor and instrument



Injection stability

ADU-Sky-60.dat (2006-2-4T4:52:42)



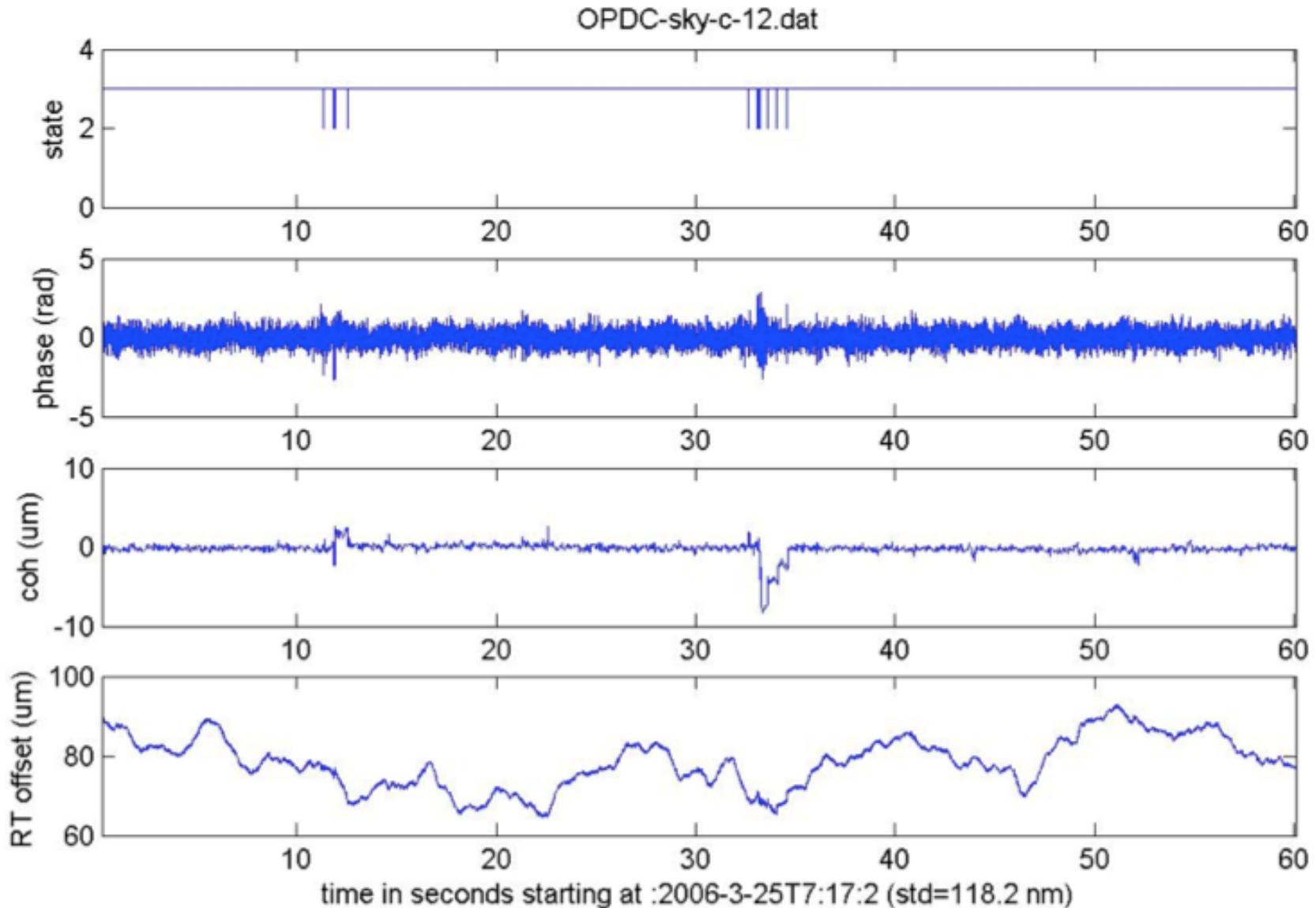


Fringe tracking problem nr 2: vibrations

- OPD instability due to vibrations affects
 - the capability to track fringes if too large / too fast
 - the accuracy of the fringe phase (if OPD scanning)
 - the fringe visibility (so the SNR) if fast and small
 - the OPD residuals
- Remedies:
 - Vibrations to be reduced at the source as much as possible:
 - passive damping,
 - active vibration control of well identified sources
 - Laser Metrology to measure fast ($> 1\text{kHz}$) the OPD between 2 telescopes from the telescope to the laboratory
 - Accelerometers and feed-forward for the mirrors not seen by the metrology

Fringe tracking can work: FINITO + MIDI + AT in March 2006

Seeing 0.99", $\tau_0 = 4.2$ ms, Hmag = 1.9



Other instrumental problems

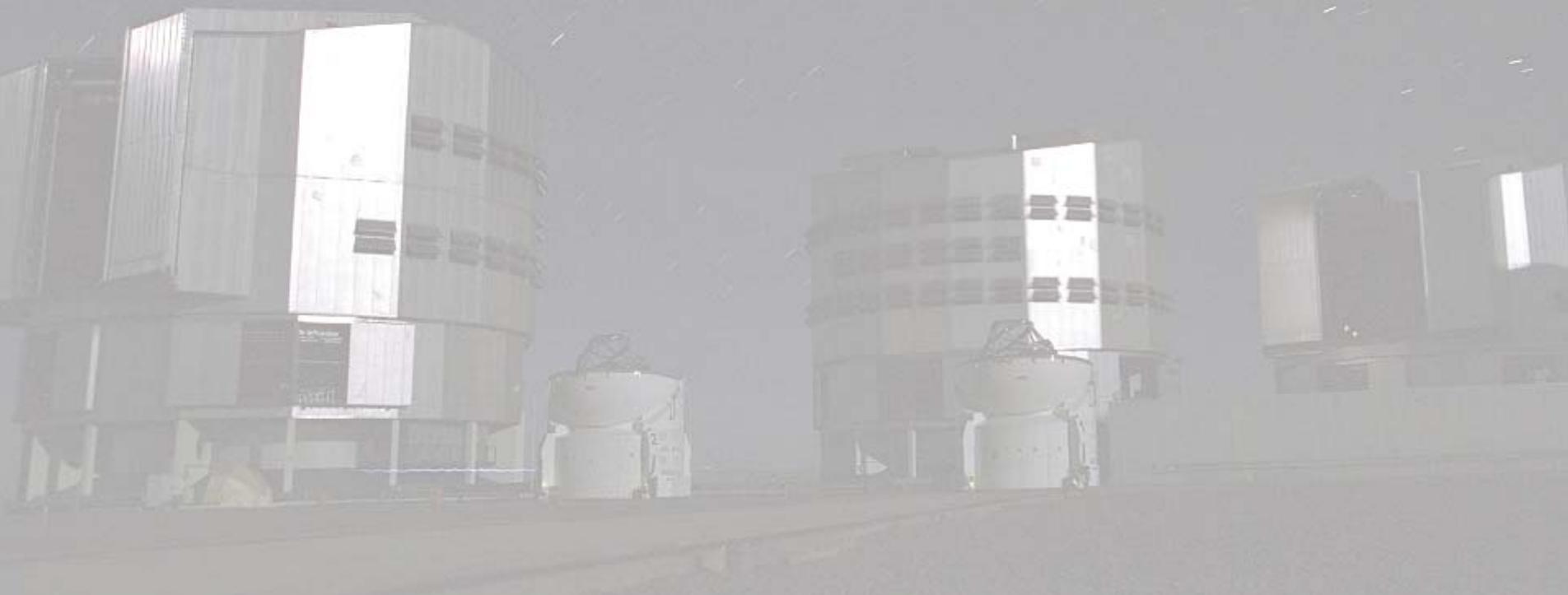
- **Baseline calibration:**
 - baseline should be known at better than $< 50\mu\text{m}$
 - dedicated calibrations are needed
 - stability with time and telescope relocation to be verified
 - VLTI auxiliary telescopes: baseline can be calibrated at better than $40\mu\text{m}$ (limited by reference star position knowledge) and is stable at better than $120\mu\text{m}$
- **Telescope differential flexures:**
 - everything that is not seen by the internal metrology must be very limited or modeled
 - second differential effect (2 telescopes - 2 stars)
- **Mirror irregularities & beam footprints**
 - non-common paths between internal metrology and stellar light should be minimized
 - bumps on mirrors should be avoided and mapped

Conclusions

- Phase-referenced imaging is complementary to the phase-closure technique
- Both are essential if one wants to get images and even for model constraint imaging (provides critical constraints on the model)
- Data reduction software developed for radio-astronomy can be adapted
- Performances are mainly limited by:
 - the number of available baselines
 - the sky-coverage
 - the instrumental degradations of fringe tracking
 - the choice of proper phase references
 - the correct design of the interferometer (metrology,...)
 - the variable humidity of the atmosphere / tunnels

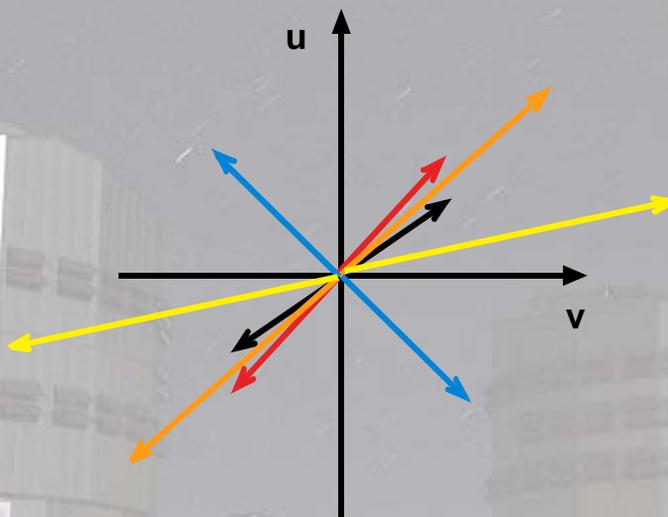
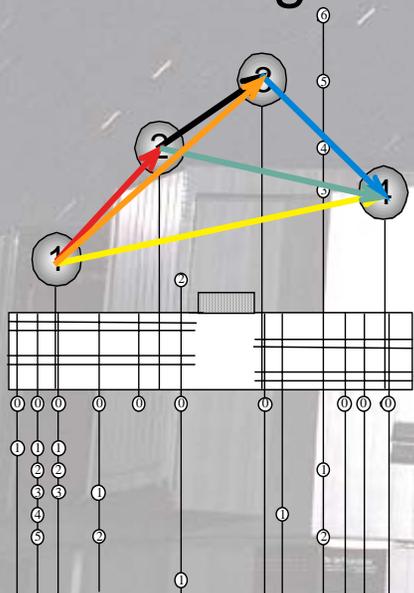


Additional slides



u-v plane and reconstructed PSF

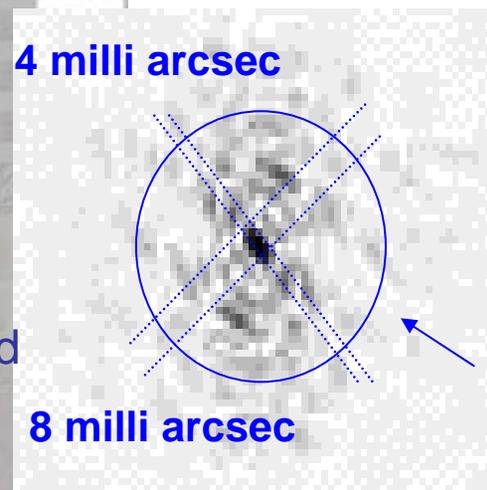
- Image intensity: $I_{im}(\alpha) = \text{IFT}(\Gamma(u_1 - u_2))$ (inverse the Fourier transform)
with $u_1 - u_2 =$ baseline vector and $\Gamma =$ complex visibility
- Good “synthetic aperture reconstruction” if good u-v coverage



u-v coverage
(UT 8 hours $\delta = -15^\circ$)



4 milli arcsec



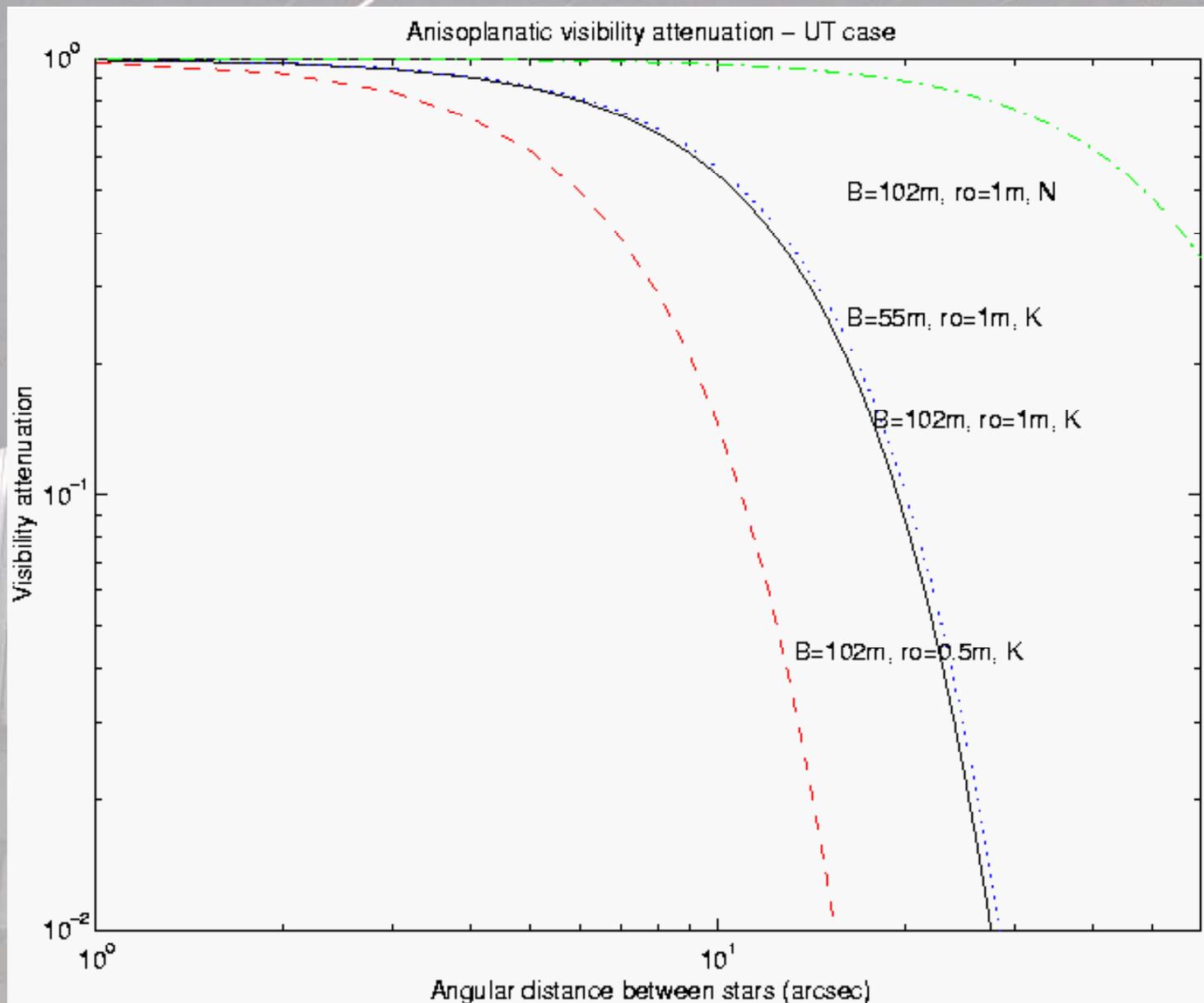
Airy disk
UT

This is NOT the u-v plane

This IS the u-v plane

Reconstructed
PSF
K-band

Anisoplanatism UT



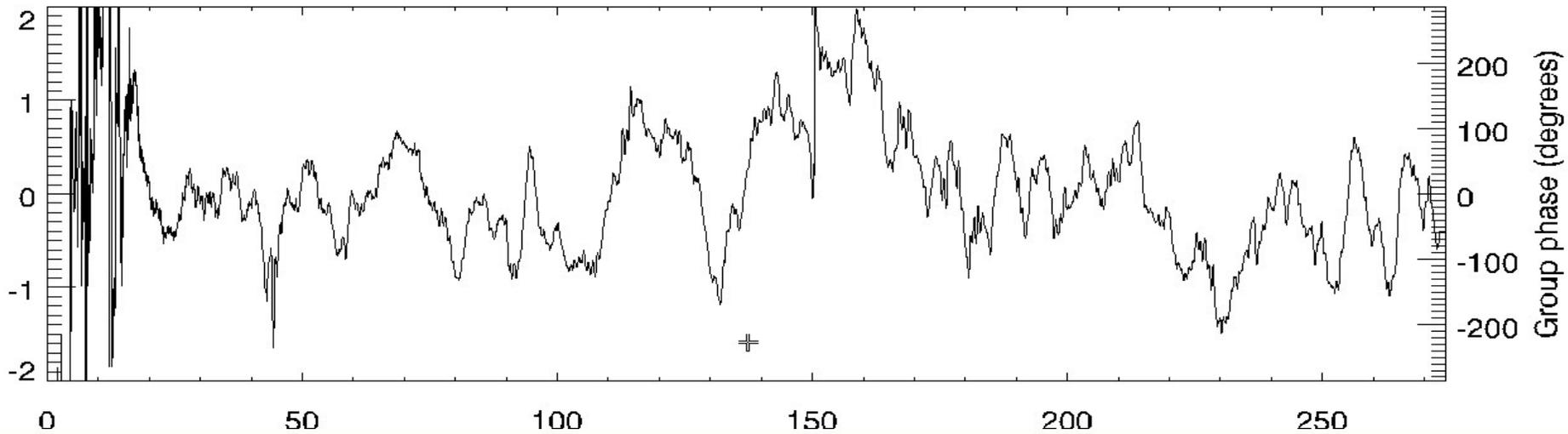
Fringe tracking requirements

- Fringe tracking performance is limited by atmosphere:
 - Total closed loop residuals should not introduce more fringe visibility loss (5-10%) than typical anisoplanatism => < 100 nm rms total OPD residuals
 - $$\sigma_{residual_OPD} \cong 2.54 \cdot 10^{-6} \cdot \frac{1}{D} \cdot T^{11/6}$$
 - Fringe tracking residuals depend on control loop transfer function:
 - low bandwidth (45 Hz) => 100 nm - improved bandwidth (100 Hz) => 70 nm
- In practice, it is very difficult to reach => what is needed ?
 - K-band:
 - Residual OPD < 300 nm rms =>
 - 0.1% probability of fringe jumps in K-band
 - loss of visibility on instrument < 30% but can be calibrated
 - Larger residuals => fringe jumps to be recovered by group delay tracking => loss of SNR accelerates =>
 - larger observation time to get the fringes out of the noise: $T \sim \text{noise}^2$
 - difficulty to calibrate the visibilities
 - N-band:
 - Relaxed coherencing requirements: residual closed-loop OPD <~ 10 μ m rms
 - Accurate fringe position measurement for post-processing: OPD noise < 1 μ m rms

oosterschelde:1 (meisner)

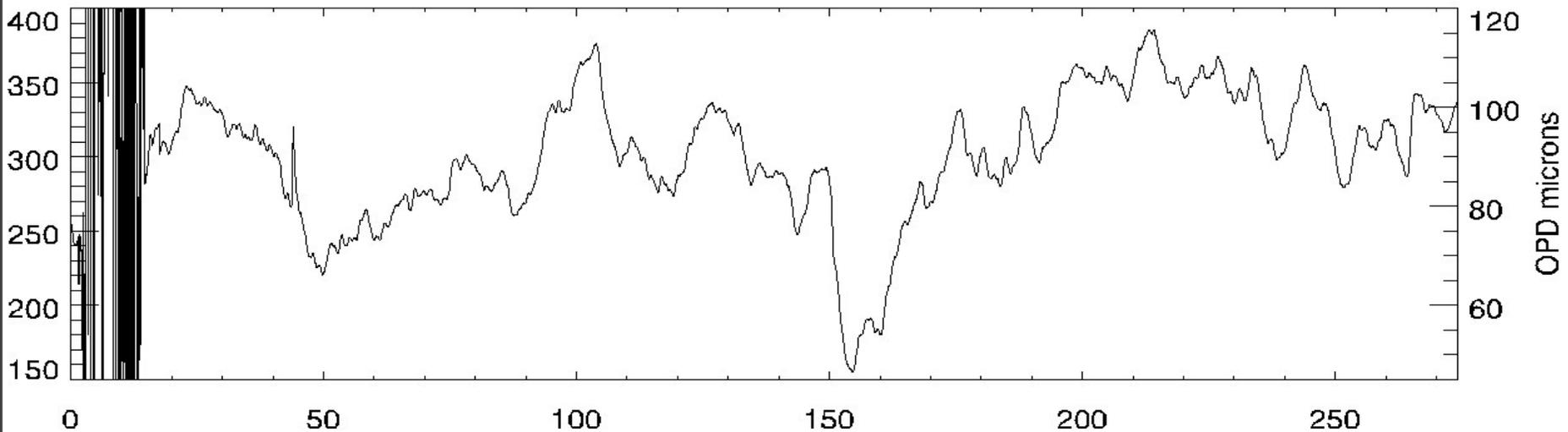
IDL 1

Water vapor column density variations (moles/m²) vs. time (seconds)



IDL 2

Atmospheric OPD (fs) vs. time (seconds)





Keck's results of dispersion extrapolation (©C. Koresko): estimated phase delay at 10 μ m vs. measured phase delay

