



resonance (MMR)

- of resonance?
- same formation pathway?



(TTVs)

**Distance from resonance**  $\Delta = \frac{P_2}{2} \frac{k-1}{k-1} - 1$ 

 $\psi = k\lambda_2 - (k-1)\lambda_1 - \widehat{\varpi}$ 



Among Kepler planets, when  $|\Delta| < 0.6\%$ ,  $\psi$  librates when  $|\Delta| > 0.6\%$ ,  $\psi$  circulates

This is a non-equilibrium state

# **Dynamics** and **Origins** of the **Near-Resonant** Kepler Planets

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### Aside:

Determining resonance from TTV data is tricky due to degeneracies! Make sure to use the generalized resonant angle  $\psi$  instead of standard resonant angles  $\phi_1, \phi_2$  (see paper for details).



**Conclusions:** Some dynamical excitation is required to

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## reproduce the near-resonant Kepler systems. Stochastic forces from turbulent eddies in the inner disk is a compelling solution to this problem.