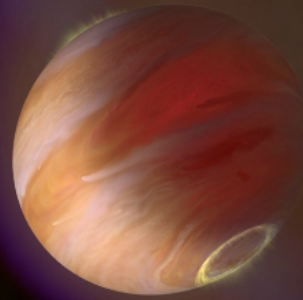
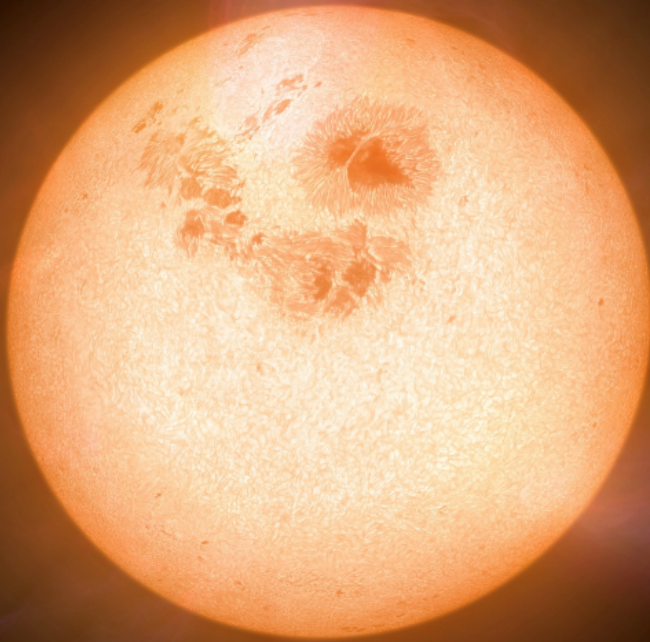


Development of multi-lens modelling codes

Nicholas James Rattenbury
The University of Auckland, New Zealand



@NJRattenbury

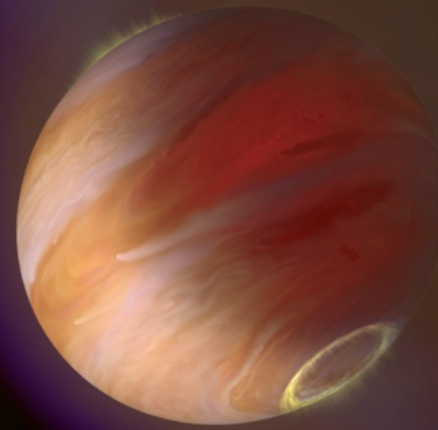
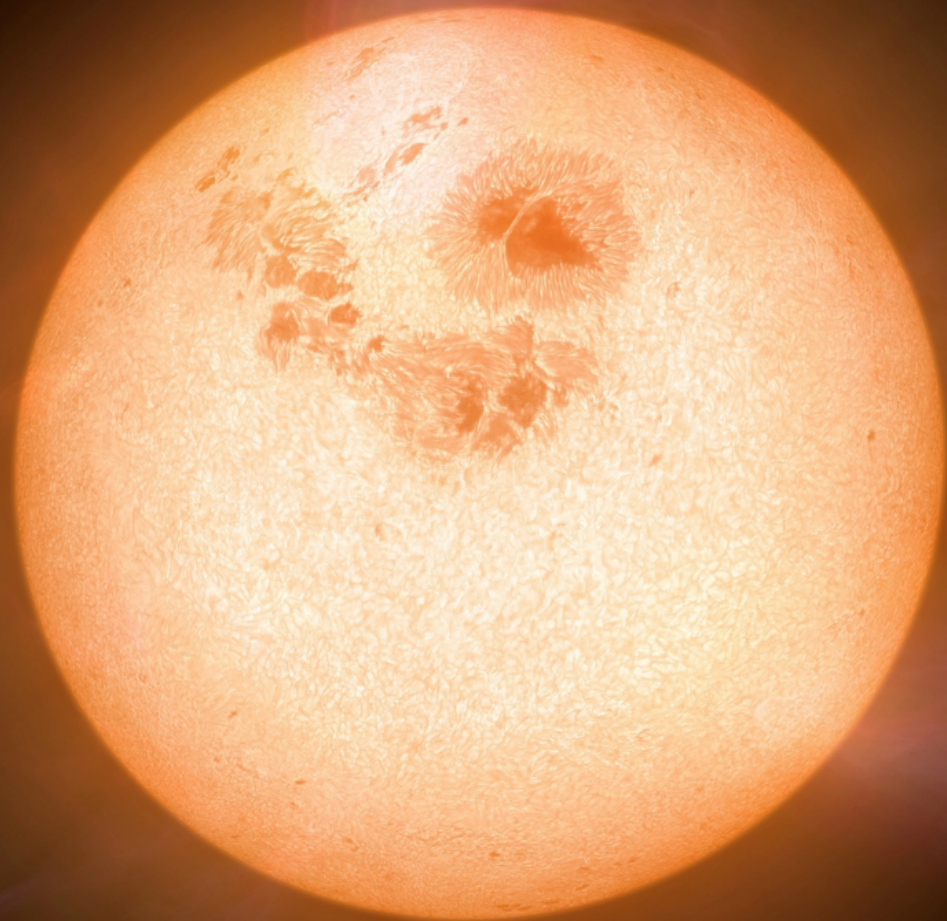
the ROYAL
SOCIETY of
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AUCKLAND
Te Whare Wānanga o Tamaki Makaurau
NEW ZEALAND

Development of multi-lens modelling codes

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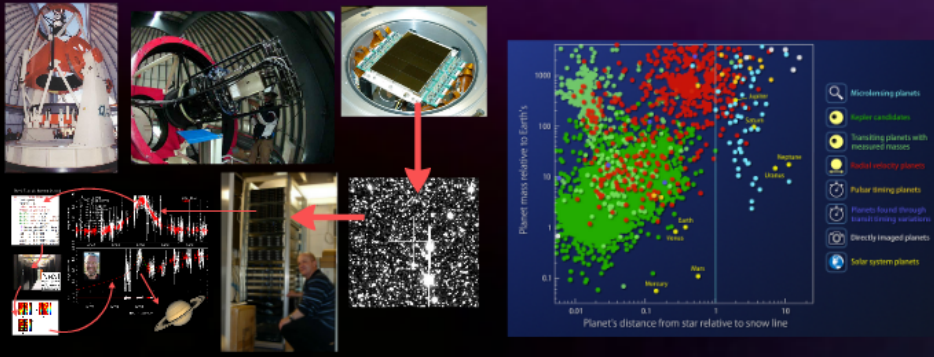


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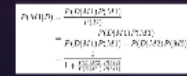
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AUCKLAND
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Efficient model exoplanet model discovery using GPU accelerated code and Nested Sampling.



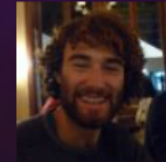
Wang, 2013, Bayesian astrophysics of planetary microlensing (MPE), using gpuaccelerated code, PhD thesis, doi: 10.1080/10447851.2013.812618



Sharma, 2014, "Nested Sampling" JML Conference Proceedings, 731, 308-312, doi:10.1007/978-3-319-01330-8_73



Ashna Sharan



Reversible Jump Markov Chain Metropolis Hastings Monte Carlo

$N = 1 | 2 | 3 | \dots$



LETTER
One or more faint planets per Milky Way star from microlensing observations

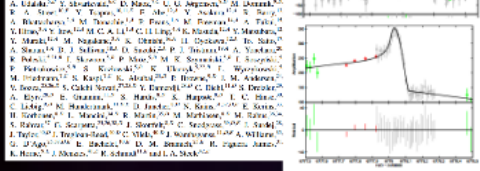
Cassan, A., et al., Nature 2012, 481, 167-169

LETTER
A bound on distant planetary mass population detected by gravitational microlensing

Sumi, T., et al., 2011, Nature, 473, 349-352

MOA-2010-BLG-303L is a possible Saturn revealed

N. J. Kashef, D. P. Bennett, E. Sarajedini, A. Torres, A. Udakis, F. Nie, A. Baranovska, M. Frezza, T. A. Pritzl, Y. Dong, M. C. A. Li, C. H. Ling, K. Muraki, Y. Murakami, Y. Murakami, K. Chakrabarti, T. Saito, A. Szymanski, D. L. Silliman, D. S. Brinkman, P. J. Tisserand, S. Kozlovski, P. Miglio, P. Piskunov, G. Pizunski, K. Poleski, D. Szymanski, J. Szymanski, I. Soszynski, M. A. Szymanski, E. Ulaczyk, and E. Wronski



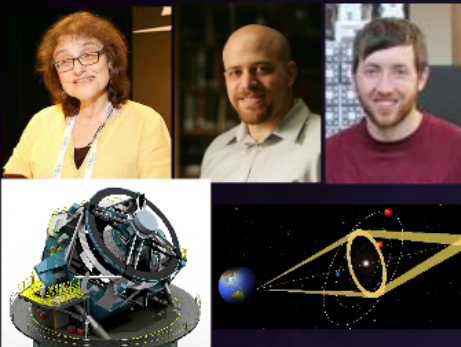
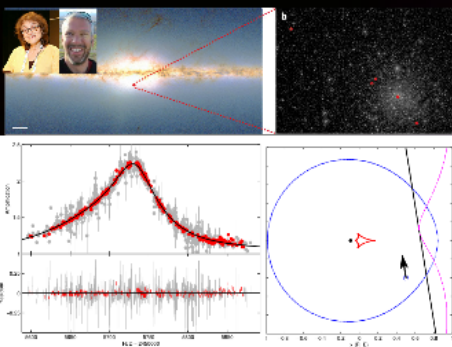
Microscopic images of a planet's surface, showing a rocky terrain with a small structure.



N. J. Kashef, D. P. Bennett, E. Sarajedini, A. Torres, A. Udakis, F. Nie, A. Baranovska, M. Frezza, T. A. Pritzl, Y. Dong, M. C. A. Li, C. H. Ling, K. Muraki, Y. Murakami, Y. Murakami, K. Chakrabarti, T. Saito, A. Szymanski, D. L. Silliman, D. S. Brinkman, P. J. Tisserand, S. Kozlovski, P. Miglio, P. Piskunov, G. Pizunski, K. Poleski, D. Szymanski, J. Szymanski, I. Soszynski, M. A. Szymanski, E. Ulaczyk, and E. Wronski



Transits

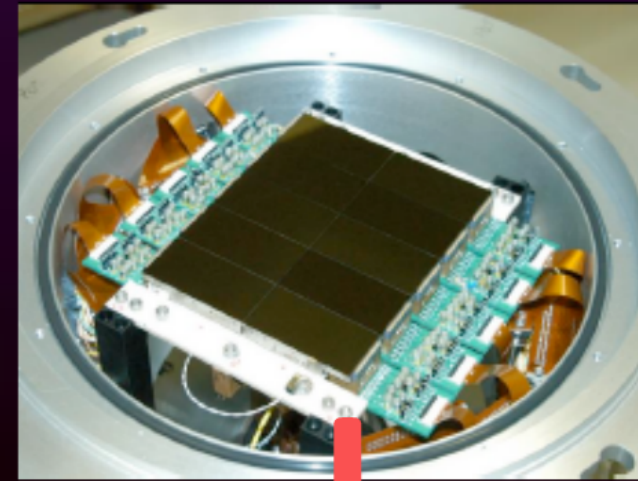
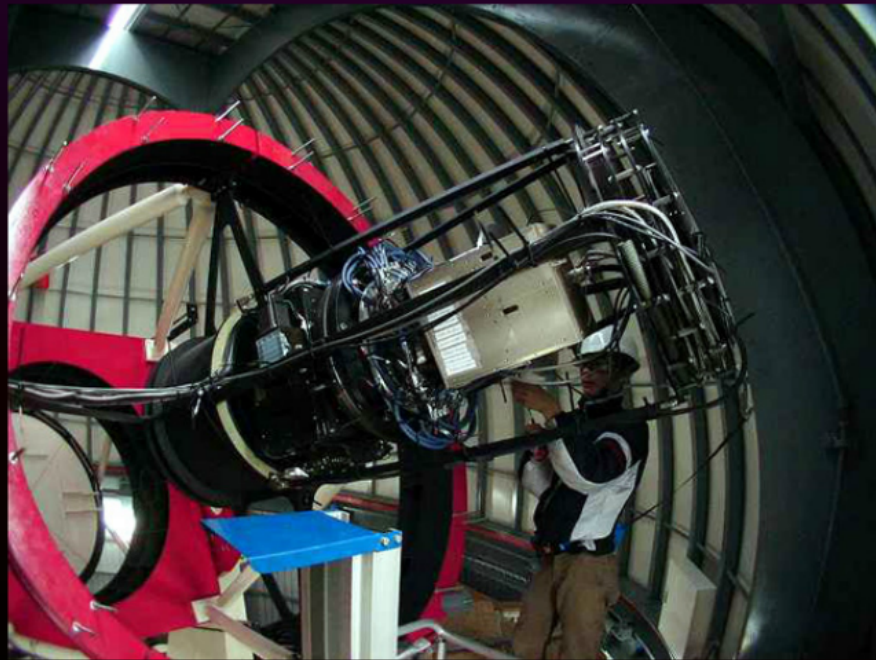


Exoplanet Microlensing Survey

Together, Kepler and WFIRST-AFTA complete the statistical census of planetary systems in the Galaxy.

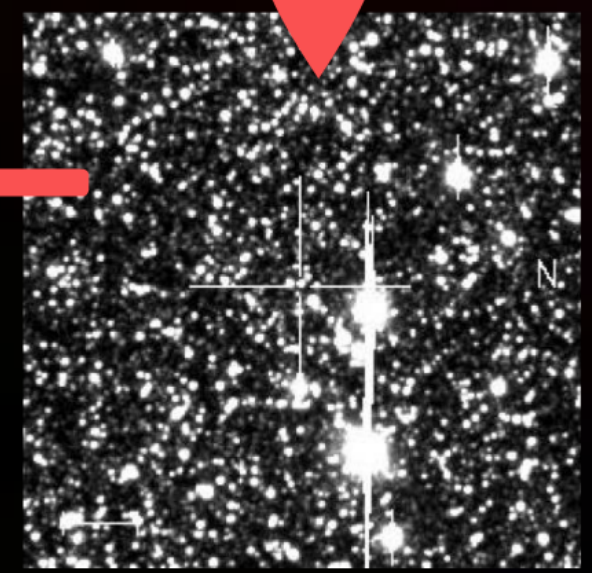
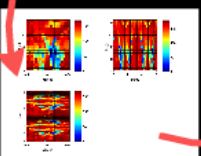
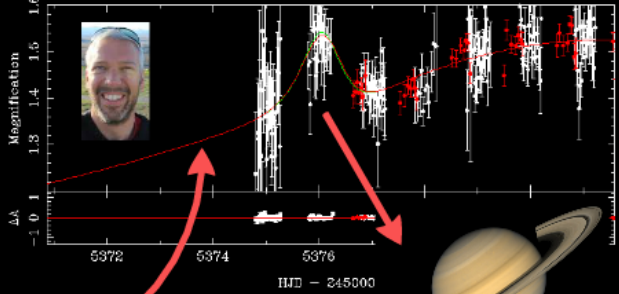
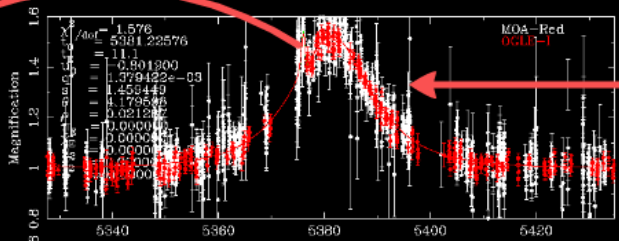
WFIRST-AFTA will:

- Detect 2800 planets, with orbits from the habitable zone outward, and masses closer to a few times the mass of the Moon.
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- Measure the abundance of non-transiting planets in the Galaxy with masses down to the mass of Mars.



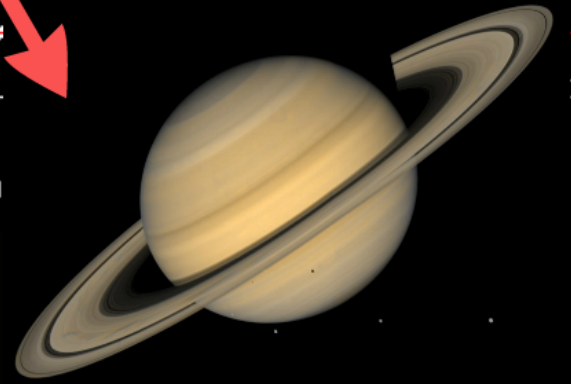
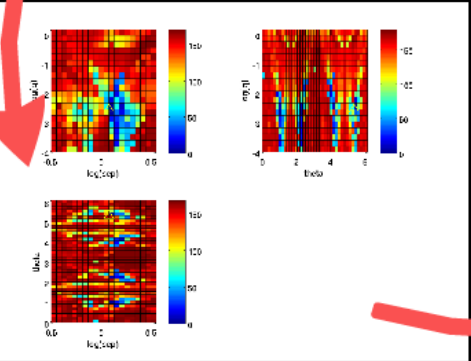
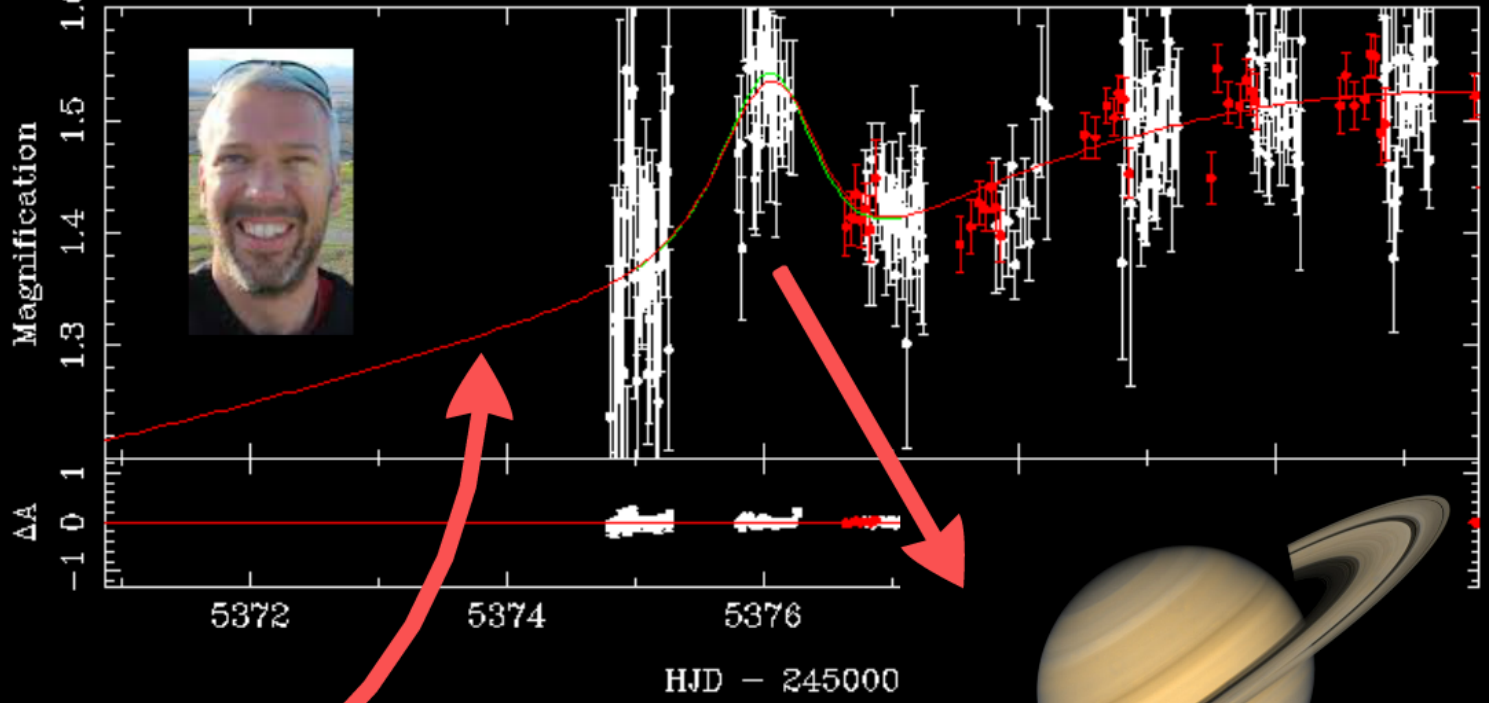
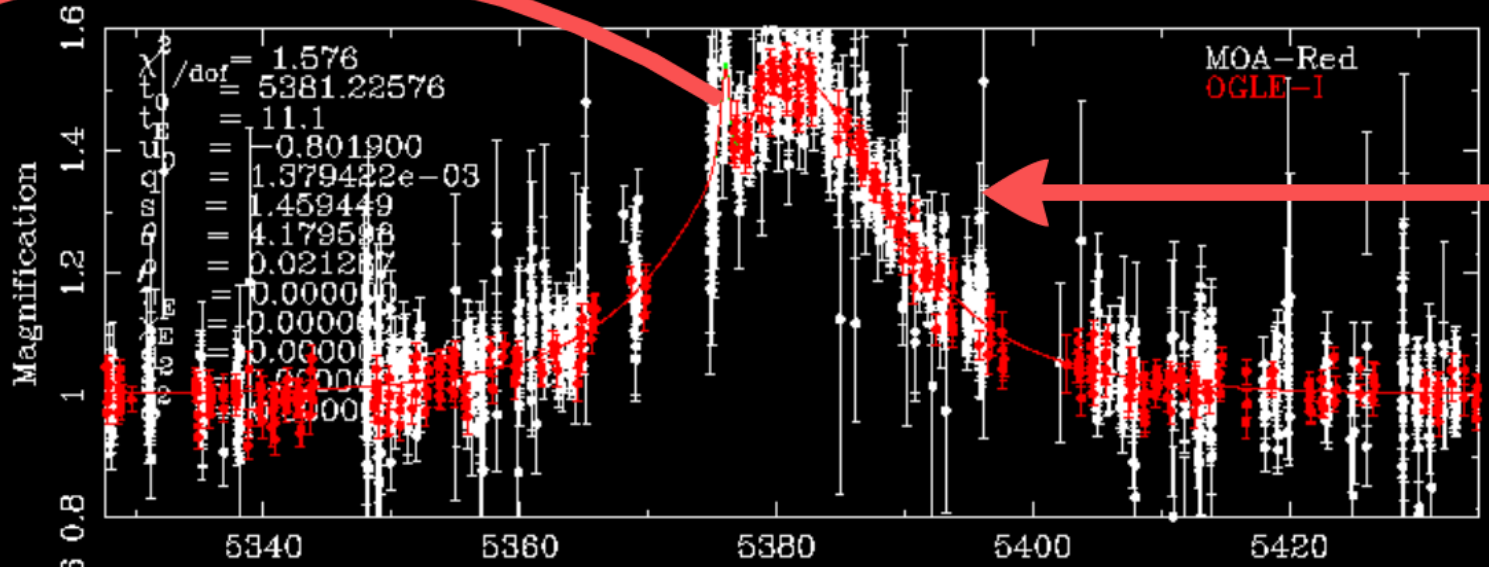
Sumi, T., et al.; Bennett D., et al

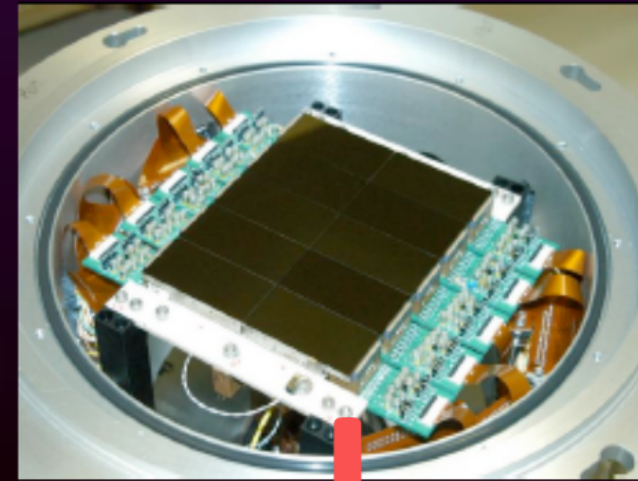
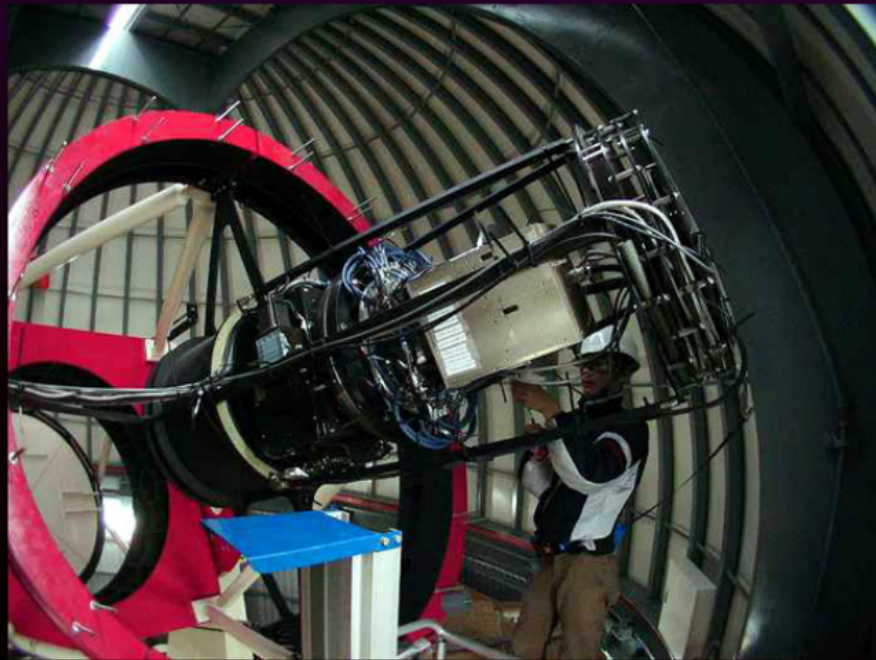
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//----- draw Anap-----
if (ANbins>0){
  FINITE = 0;
  //int ANbin = 1000;
  //double yratio=1.0;
  double theta = pi/6;
  double tN1 = -1.0, tN2 =
  double umin1=-1.0, umin2=
  double tN = dJO/TE;
  if (Anap_x0==999.9) Anap_x0 =
  if (Anap_y0==999.9) Anap_y0 =
  tN1 = -1.0*ROI +A
  tN2 = 1.0*ROI +A
  umin1 = -1.0*ROI+yratio+A
  umin2 = 1.0*ROI+yratio+A
```



Sumi, T., et al.; Bennett D., et al

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//-----draw Amap-----  
if (ANbin>0){  
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  if (Amap_y0==999.9) Amap_  
  tN1 = -1.0*ROI +A  
  tN2 = 1.0*ROI +A  
  umin1 = -1.0*ROI*yratio+A  
  umin2 = 1.0*ROI*yratio+A
```

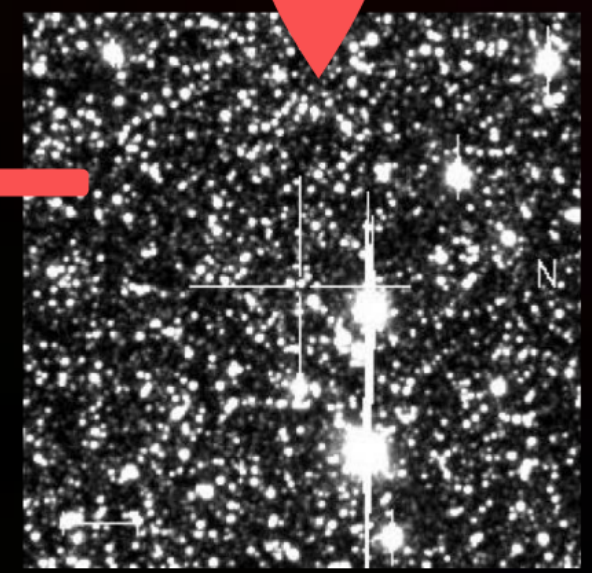
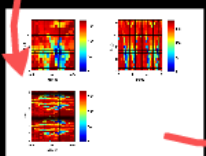
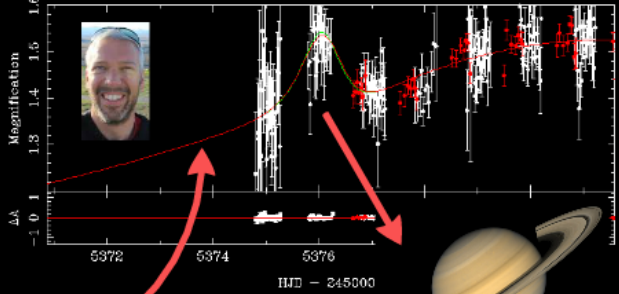
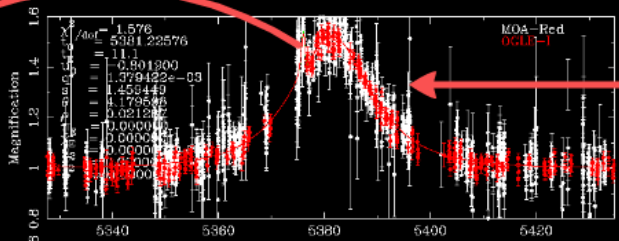




Sumi, T., et al.; Bennett D., et al

```

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  tN2 = 1.0*ROI +A
  umin1 = -1.0*ROI+yratio+A
  umin2 = 1.0*ROI+yratio+A
  }
  
```

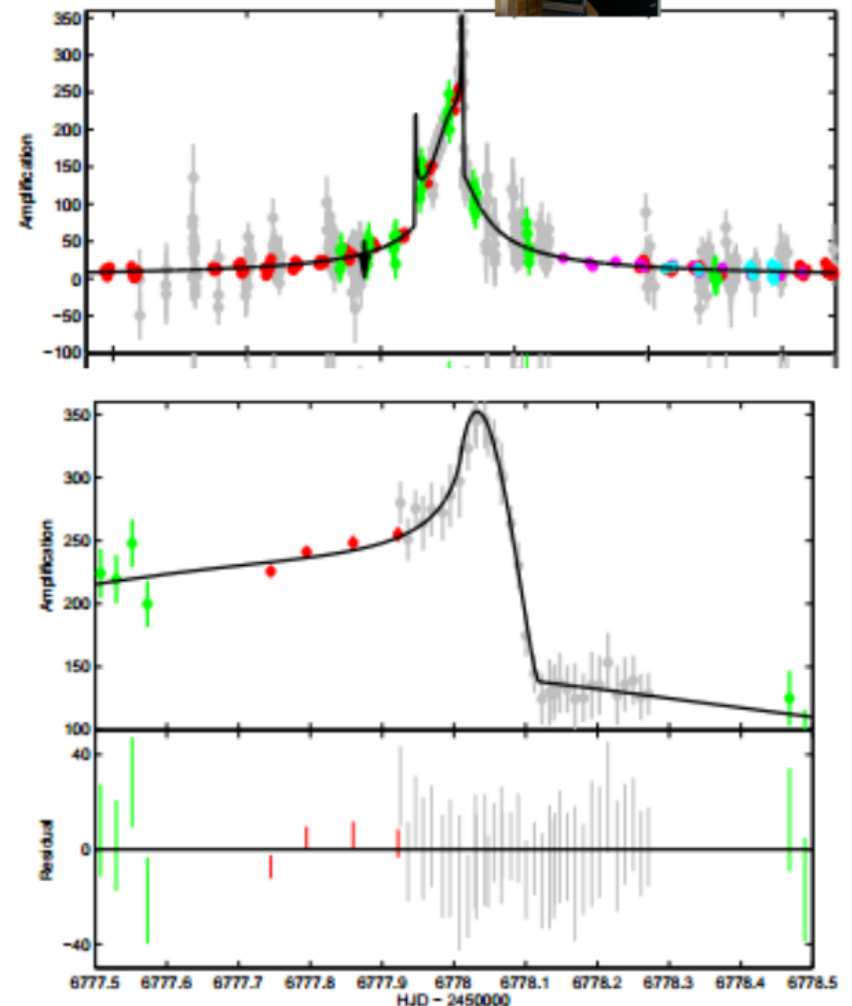
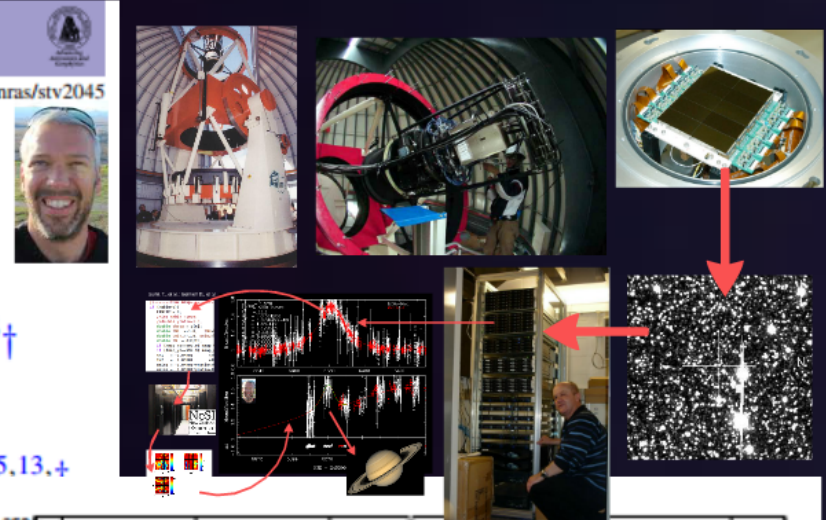


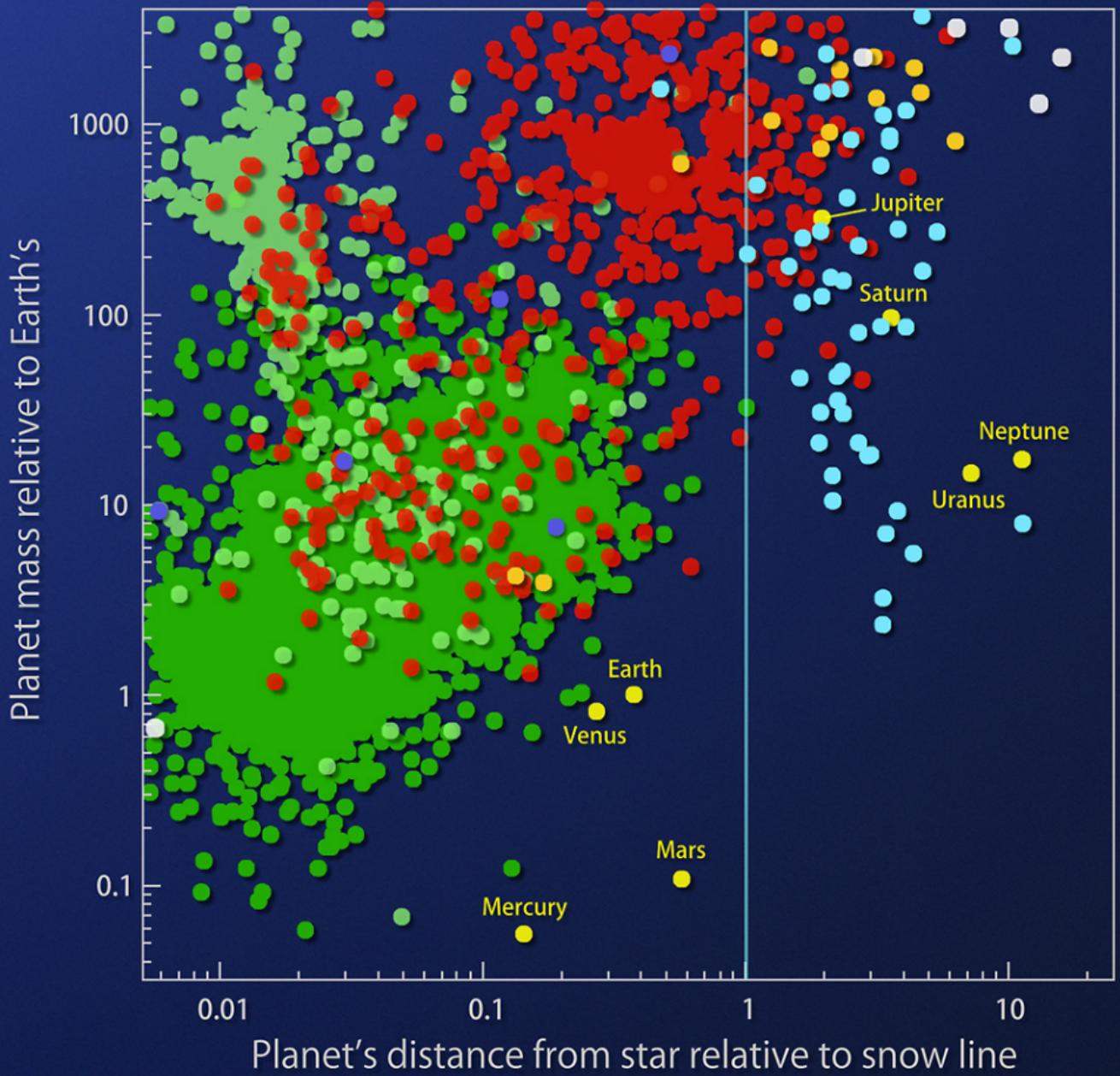
MOA-2010-BLG-353Lb: a possible Saturn revealed

N. J. Rattenbury,^{1,★†} D. P. Bennett,^{2,†} T. Sumi,^{3,†} N. Koshimoto,^{3,†} I. A. Bond,^{4,†}
A. Udalski,^{5,‡} F. Abe,^{6,†} A. Bhattacharya,^{2,†} M. Freeman,^{7,†} A. Fukui,^{8,†} Y. Itow,^{6,†}
M. C. A. Li,^{1,†} C. H. Ling,^{4,†} K. Masuda,^{6,†} Y. Matsubara,^{6,†} Y. Muraki,^{6,†}
K. Ohnishi,^{9,†} To. Saito,^{10,†} A. Sharan,^{1,†} D. J. Sullivan,^{11,†} D. Suzuki,^{2,†}
P. J. Tristram,^{12,†} S. Kozłowski,^{5,‡} P. Mróz,^{5,‡} P. Pietrukowicz,^{5,‡} G. Pietrzyński,^{5,13,+}
R. Poleski,^{5,14,‡} D. Skowron,^{5,‡} J. Skowron,^{5,‡} I. Soszyński,^{5,‡} M. K. Szymański,^{5,‡}
K. Ulaczyk^{5,‡} and Ł. Wyrzykowski^{5,‡}

Faint source star planetary microlensing: the discovery of the cold gas giant planet OGLE-2014-BLG-0676Lb

N. J. Rattenbury,^{1,A★} D. P. Bennett,^{2,A} T. Sumi,^{3,A} N. Koshimoto,^{3,A} I. A. Bond,^{4,}
A. Udalski,^{5,B} Y. Shvartzvald,^{6,C} D. Maoz,^{7,C} U. G. Jørgensen,^{8,D} M. Dominik,^{9,D,}
R. A. Street,^{10,E} Y. Tsapras,^{10,11,E} F. Abe,^{12,A} Y. Asakura,^{12,A} R. Barry,^{13,}
A. Bhattacharya,^{2,A} M. Donachie,^{1,A} P. Evans,^{1,A} M. Freeman,^{14,A} A. Fukui,^{15,}
Y. Hirao,^{3,A} Y. Itow,^{12,A} M. C. A. Li,^{1,A} C. H. Ling,^{4,A} K. Masuda,^{12,A} Y. Matsubara,^{12,}
Y. Muraki,^{12,A} M. Nagakane,^{3,A} K. Ohnishi,^{16,A} H. Oyokawa,^{12,A} To. Saito,^{17,}
A. Sharan,^{1,A} D. J. Sullivan,^{18,A} D. Suzuki,^{2,A} P. J. Tristram,^{19,A} A. Yonehara,^{20,}
R. Poleski,^{5,21,B} J. Skowron,^{5,B} P. Mróz,^{5,B} M. K. Szymański,^{5,B} I. Soszyński,^{5,}
P. Pietrukowicz,^{5,B} S. Kozłowski,^{5,B} K. Ulaczyk,^{5,22,B} Ł. Wyrzykowski,^{5,}
M. Friedmann,^{7,C} S. Kaspi,^{7,C} K. Alsubai,^{23,D} P. Browne,^{9,D} J. M. Andersen,^{24,}
V. Bozza,^{25,26,D} S. Calchi Novati,^{27,25,D} Y. Damerdjji,^{28,D} C. Diehl,^{11,D} S. Dreizler,^{29,}
A. Elyiv,^{28,D} E. Giannini,^{11,D} S. Hardis,^{8,D} K. Harpsøe,^{8,D} T. C. Hinse,^{30,}
C. Liebig,^{9,D} M. Hundertmark,^{11,D,E} D. Juncher,^{8,D} N. Kains,^{31,32,D,E} E. Kerins,^{33,}
H. Korhonen,^{8,D} L. Mancini,^{34,D} R. Martin,^{35,D} M. Mathiasen,^{8,D} M. Rabus,^{36,34,}
S. Rahvar,³⁷ G. Scarpitta,^{25,26,38,D} J. Skottfelt,^{8,D} C. Snodgrass,^{39,D,E} J. Surdej,^{28,}
J. Taylor,^{40,D} J. Tregloan-Reed,^{40,D} C. Vilela,^{40,D} J. Wambsganss,^{11,D,E} A. Williams,^{35,}
G. D'Ago,^{25,38,D,E} E. Bachelet,^{10,E} D. M. Bramich,^{23,E} R. Figuera Jaimes,^{31,}
K. Horne,^{9,E} J. Menzies,^{41,E} R. Schmidt^{11,E} and I. A. Steele^{42,E}





-  Microlensing planets
-  Kepler candidates
-  Transiting planets with measured masses
-  Radial velocity planets
-  Pulsar timing planets
-  Planets found through transit timing variations
-  Directly imaged planets
-  Solar system planets

One or more bound planets per Milky Way star from microlensing observations

A. Cassan^{1,2,3}, D. Kúbas^{1,2,4}, J.-P. Beaulieu^{1,2,5}, M. Dominik^{1,5}, K. Horne^{1,5}, J. Greenhill^{1,6}, J. Wambsganss^{1,3}, J. Menzies^{1,7}, A. Williams^{1,8}, U. G. Jørgensen^{1,9}, A. Udalski^{10,11}, D. P. Bennett^{1,12}, M. D. Albrow^{1,13}, V. Batista^{1,2}, S. Brillant^{1,4}, J. A. R. Caldwell^{1,14}, A. Cole^{1,5}, Ch. Coutures^{1,2}, K. H. Cook^{1,15}, S. Dieters^{1,5}, D. Dominis Prester^{1,16}, J. Donatowicz^{1,17}, P. Fouqué^{1,18}, K. Hill^{1,6}, N. Kains^{1,19}, S. Kane^{1,20}, J.-B. Marquette^{1,2}, R. Martin^{1,5}, K. R. Pollard^{1,13}, K. C. Sahu^{1,14}, C. Vinter^{1,9}, D. Warren^{1,6}, B. Watson^{1,6}, M. Zub^{1,3}, T. Sumi^{21,22}, M. K. Szymański^{10,11}, M. Kubiak^{10,11}, R. Poleski^{10,11}, I. Soszynski^{10,11}, K. Ulaczyk^{10,11}, G. Pietrzyński^{10,11,23} & Ł. Wyrzykowski^{10,11,24}

Most known extrasolar planets (exoplanets) have been discovered using the radial velocity^{1,2} or transit³ methods. Both are biased towards planets that are relatively close to their parent stars, and studies find that around 17–30% (refs 4, 5) of solar-like stars host a planet. Gravitational microlensing^{6–9}, on the other hand, probes planets that are further away from their stars. Recently, a population of planets that are unbound or very far from their stars was discovered by microlensing¹⁰. These planets are at least as numerous as the stars in the Milky Way¹⁰. Here we report a statistical analysis of microlensing data (gathered in 2002–07) that reveals the fraction of bound planets 0.5–10 AU (Sun–Earth distance) from their stars. We find that $17^{+6}_{-9}\%$ of stars host Jupiter-mass planets ($0.3\text{--}10 M_J$, where $M_J = 318 M_\oplus$ and M_\oplus is Earth's mass). Cool Neptunes ($10\text{--}30 M_\oplus$) and super-Earths ($5\text{--}10 M_\oplus$) are even more common: their respective abundances per star are $52^{+22}_{-29}\%$ and $62^{+35}_{-37}\%$. We conclude that stars are orbited by planets as a rule, rather than the exception.

"We conclude that stars are orbited by planets as a rule, rather than the exception"

Cassan, A., et al., Nature 2012, 481, 167–169

Unbound or distant planetary mass population detected by gravitational microlensing

The Microlensing Observations in Astrophysics (MOA) Collaboration & The Optical Gravitational Lensing Experiment (OGLE) Collaboration*

Since 1995, more than 500 exoplanets have been detected using different techniques^{1,2}, of which 12 were detected with gravitational microlensing^{3,4}. Most of these are gravitationally bound to their host stars. There is some evidence of free-floating planetary-mass objects in young star-forming regions^{5–7}, but these objects are limited to massive objects of 3 to 15 Jupiter masses with large uncertainties in photometric mass estimates and their abundance. Here, we report the discovery of a population of unbound or distant Jupiter-mass objects, which are almost twice ($1.8^{+1.7}_{-0.8}$) as common as main-sequence stars, based on two years of gravitational microlensing survey observations towards the Galactic Bulge. These planetary-mass objects have no host stars that can be detected within about ten astronomical units by gravitational microlensing. However, a comparison with constraints from direct imaging⁸ suggests that most of these planetary-mass objects are not bound to any host star. An abrupt change in the mass function at about one Jupiter mass favours the idea that their formation process is different from that of stars and brown dwarfs. They may have formed in proto-planetary disks and subsequently scattered into unbound or very distant orbits.

"Here, we report the discovery of a population of unbound or distant Jupiter-mass objects, which are almost twice as common as main-sequence stars..."

Sumi, T., et al., 2011, Nature, 473, 349–352



THE EXOPLANET MASS-RATIO FUNCTION FROM THE MOA-II SURVEY: DISCOVERY OF A BREAK AND LIKELY PEAK AT A NEPTUNE MASS

D. SUZUKI¹, D. P. BENNETT^{1,2}, T. SUMI³, I. A. BOND⁴, L. A. ROGERS^{5,14}, F. ABE⁶, Y. ASAKURA⁶, A. BHATTACHARYA^{1,2}, M. DONACHIE⁷, M. FREEMAN⁷, A. FUKUI⁸, Y. HIRAO⁹, Y. ITOW⁶, N. KOSHIMOTO⁹, M. C. A. LI⁷, C. H. LING⁴, K. MASUDA⁶, Y. MATSUBARA⁶, Y. MURAKI⁶, M. NAGAKANE³, K. ONISHI⁹, H. OYOKAWA⁶, N. RATTENBURY⁷, TO. SAITO¹⁰, A. SHARAN⁷, H. SHIBAI³, D. J. SULLIVAN¹¹, P. J. TRISTRAM¹², AND A. YONEHARA¹³
(THE MOA COLLABORATION)



Efficient model exoplanet model discovery using GPU accelerated code and Nested Sampling.



Ling, C., 2013, Simulation and modelling of gravitational microlensing events using graphical processing units, Ph.D. thesis, URL <http://muir.massey.ac.nz/handle/10179/5148>



$$\begin{aligned} P(M1|D) &= \frac{P(D|M1)P(M1)}{P(D)} \\ &= \frac{P(D|M1)P(M1)}{P(D|M1)P(M1) + P(D|M2)P(M2)} \\ &= \frac{1}{1 + \frac{P(D|M2)P(M2)}{P(D|M1)P(M1)}} \end{aligned}$$

Skilling, John (2004). "Nested Sampling". AIP Conference Proceedings 735: 395–405. doi:10.1063/1.1835238



Ashna Sharan

Reversible Jump

Markov Chain Metropolis

Hastings Monte Carlo

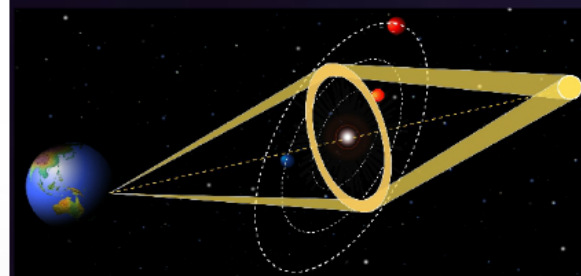
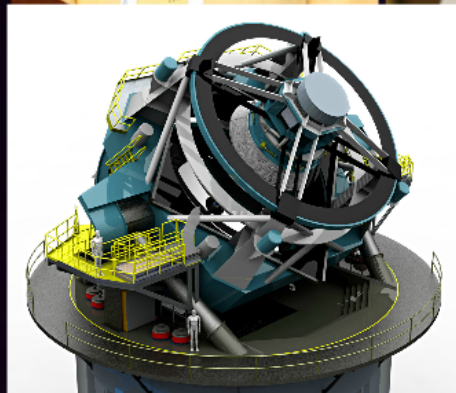
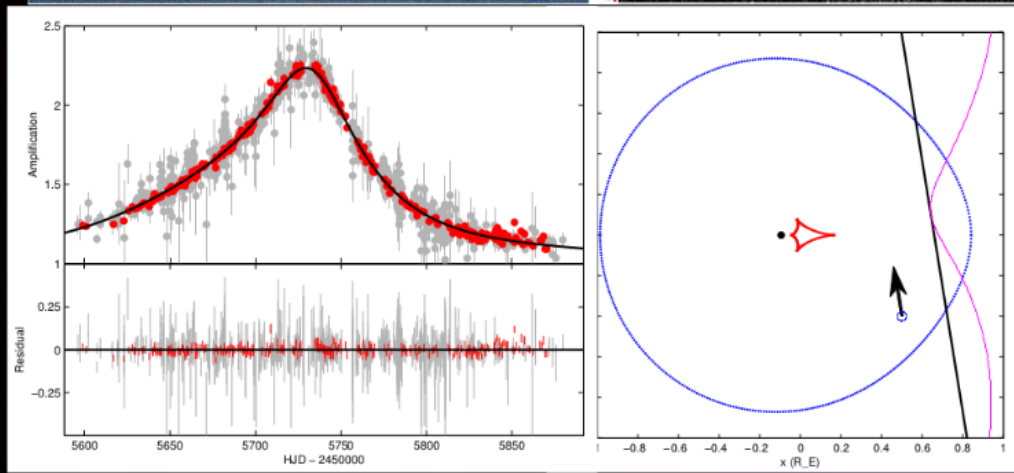
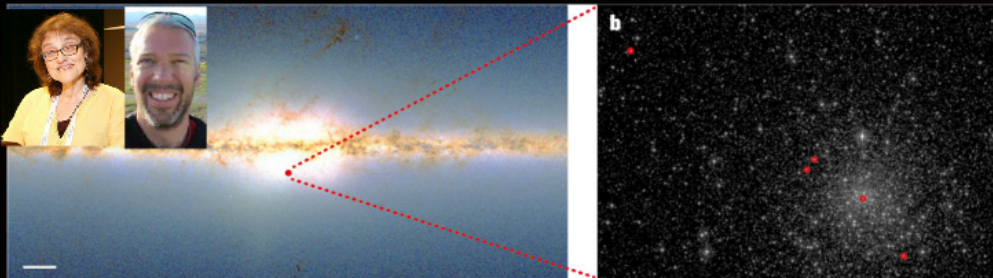
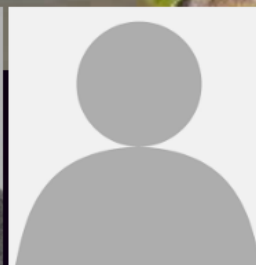
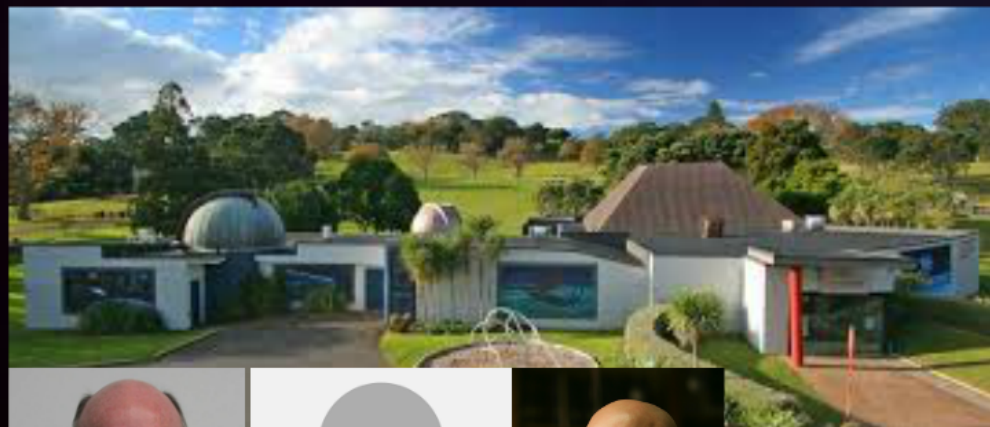
$N = 1 \mid 2 \mid 3 \mid \dots$



LSST



Transits



WFIRST

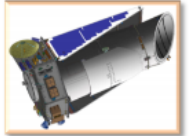


YouTube

Exoplanet Microlensing Survey

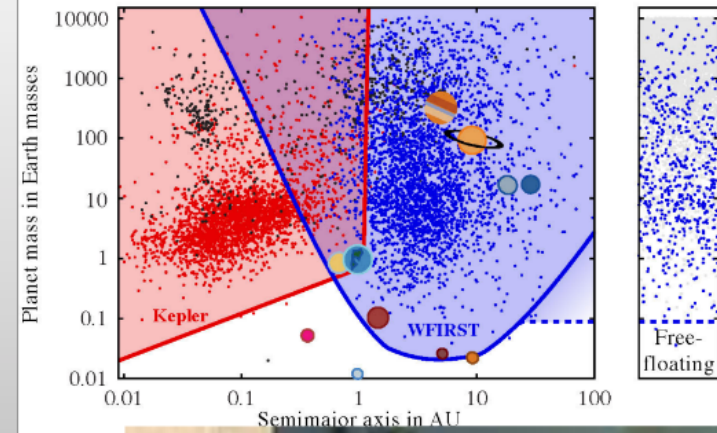


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- Be sensitive to analogs of all the solar system's planets except Mercury.
- Measure the abundance of free-floating planets in the Galaxy with masses down to the mass of Mars



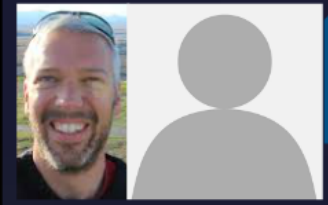


THE FIRST CIRCUMBINARY PLANET FOUND BY MICROLENSING: OGLE-2007-BLG-349L(AB)c

D. P. BENNETT^{1,2,48,49}, S. H. RHIE^{2,50}, A. UDALSKI^{3,51}, A. GOULD^{4,5,6,52}, Y. TSAPRAS^{7,8,53}, D. KUBAS^{9,49}, I. A. BOND^{10,48}, J. GREENHILL^{11,50,49}, A. CASSAN^{9,49}, N. J. RATTENBURY^{12,48}, T. S. BOYAJIAN¹³, J. LUHN¹⁴, M. T. PENNY⁴, J. ANDERSON¹⁵, F. ABE¹⁶, A. BHATTACHARYA², C. S. BOTZLER¹², M. DONACHIE¹², M. FREEMAN¹², A. FUKUI¹⁷, Y. HIRAO¹⁸, Y. ITOW¹⁶, N. KOSHIMOTO¹⁸, M. C. A. LI¹², C. H. LING⁹, K. MASUDA¹⁶, Y. MATSUBARA¹⁶, Y. MURAKI¹⁶, M. NAGAKANE¹⁸, K. OHNISHI¹⁹, H. OYOKAWA¹⁶, Y. C. PERROTT¹², TO. SAITO²⁰, A. SHARAN¹², D. J. SULLIVAN²¹, T. SUMI¹⁸, D. SUZUKI^{1,2}, P. J. TRISTRAM²², A. YONEHARA²³, P. C. M. YOCK¹²
(THE MOA COLLABORATION),
M. K. SZYMAŃSKI³, I. SOSZYŃSKI³, K. ULACZYK³, E. WYRZYKOWSKI³
(THE OGLE COLLABORATION),
W. ALLEN²⁴, D. DEPOY²⁵, A. GAL-YAM²⁶, B. S. GAUDI⁴, C. HAN²⁷, I. A. G. MONARD²⁸, E. OFEK²⁹, R. W. POGGE⁴
(THE μ FUN COLLABORATION),
R. A. STREET⁸, D. M. BRAMICH³⁰, M. DOMINIK³¹, K. HORNE³¹, C. SNODGRASS^{32,33}, I. A. STEELE³⁴
(THE ROBONET COLLABORATION),
AND
M. D. ALBROW³⁵, E. BACHELET⁸, V. BATISTA⁹, J.-P. BEAULIEU⁹, S. BRILLANT³⁶, J. A. R. CALDWELL³⁷, A. COLE¹¹, C. COUTURES⁹, S. DIETERS¹¹, D. DOMINIS PRESTER³⁸, J. DONATOWICZ³⁹, P. FOUQUÉ^{40,41}, M. HUNDERTMARK^{31,42}, U. G. JØRGENSEN⁴², N. KAINS¹⁵, S. R. KANE⁴³, J.-B. MARQUETTE⁹, J. MENZIES⁴⁴, K. R. POLLARD³⁵, C. RANC⁸, K. C. SAHU¹⁵, J. WAMBSGANSS⁴⁵, A. WILLIAMS^{46,47}, M. ZUB⁴⁵
(THE PLANET COLLABORATION)



Continuing the work of Denis Sullivan and students..



Continuing the work of Denis Sullivan and students..



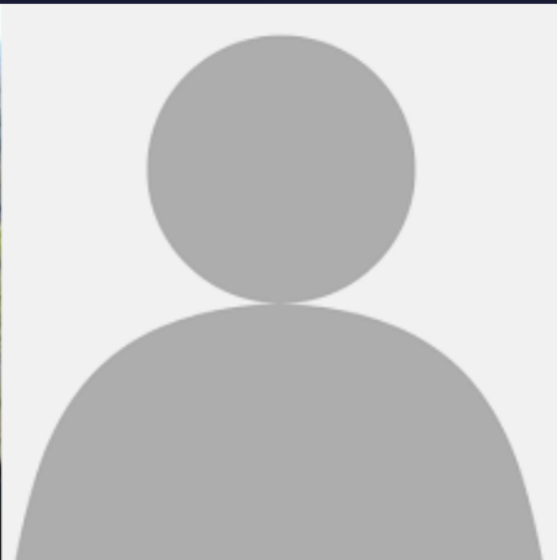
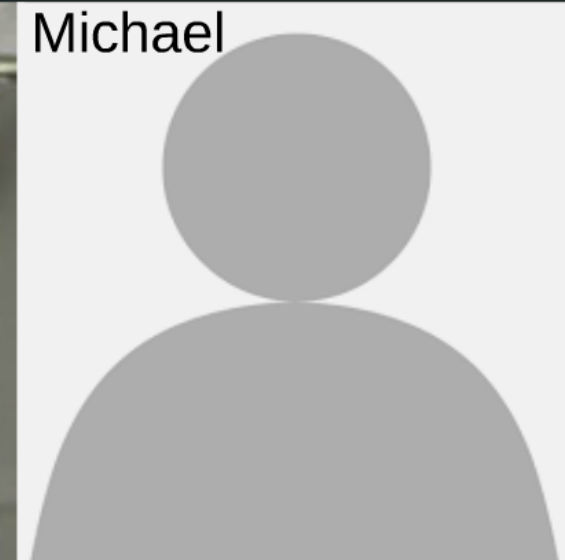
Aarno



Paul



Michael



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Auckland Microlensing Conference 2018



According to "Star Trek: First Contact" there are 1,199 notes



YouTube



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